# Type Theorists HATE Him!

Learn this ONE WEIRD TRICK to fake dependent types in a language that doesn't support them

LEARN THE TRUTH NOW

#### Ryan Scott

⊠ rgscott@indiana.edu

→ github.com/RyanGlScott

September 1, 2017

#### Dependent types

#### Dependent types... in Idris

```
mkSingle
mkSingle
                                mkSingle
 False
            True
                     (x : Bool) ->
if x then Nat else List Nat
  II
             П
           ⊙
                               Bool) ->
```

### Dependent types... in Haskell?

```
mkSingle mkSingle
                                mkSingle
  False
            Irue
                                \stackrel{\textstyle \sim}{\times}
   П
                       x then Nat else
                               Bool) ->
0
                      [Nat]
```

### Dependent types... in Haskell?

```
mkSingle True = 0
mkSingle False = []
                                                mkSingle
                                                \sim
                                x then Nat else [Nat]
                                              :: Bool) ->
```

```
<interactive>:1:28: error: parse error on input 'if'
```



#### There's hope yet

- A Haskell can support dependent types, if you're willing to squint
- Ne'll need to enable a modest number of GHC extensions

#### There's hope yet

- A Haskell can support dependent types, if you're willing to squint
- Ne'll need to enable a modest number of GHC extensions

```
LANGUAGE
                                                                                                                                                                        LANGUAGE
                                                                                                                                                                                       LANGUAGE
                                                                                                                             LANGUAGE
LANGUAGE
                                                                                                                                                         LANGUAGE
                             LANGUAGE
                                          LANGUAGE
                                                        LANGUAGE
                                                                      LANGUAGE
                                                                                                   LANGUAGE
                                                                                                               LANGUAGE
                                                                                                                                             LANGUAGE
                                                                                   ANGUAGE
                                                                                                                                                                                      EmptyCase
                                                                                                                                                                                                  DefaultSignatures
                                                                    ScopedTypeVariables
                                                                                   RankNTypes
                                                                                                 KindSignatures
                                                                                                                                                          FlexibleContexts
UndecidableInstances
                                                                                                                                           FlexibleInstances
             lypeOperators
                           TypeInlype
                                                                                                                                                                        {\sf Existential} {\sf Quantification}
                                         「ypeFamilies
                                                       [emplateHaskell
                                                                                                               [nstanceSigs
                                                                                                                                                                                    #-}
                                                                                                                                                                         #-)
```

```
data family Sing
k -> Type
```

```
data instance Sing :: Bool -> Type where
   SFalse :: Sing False
   STrue :: Sing True
```

```
data instance Sing :: [
SFalse :: Sing False
STrue :: Sing True
                                         |Bool| -> Type where
```

```
data instance Sing ::
  STrue
                SFalse
: Sing True
              Sing False
                             Bool -> Type where
```

```
data instance Sing ::
SFalse :: Sing False
                         data instance Sing (z
                                                           STrue
(z ~ True)
                N
              ~ False)
                                                         Sing True
  => STrue
                SFalse
                            :: Bool
                                                                                    Bool -> Type where
```

```
data instance Sing ::
  STrue
                SFalse
Sing True
             Sing False
                            Bool -> Type where
```

```
data instance Sing (z
(Z
            N
~ |True)
           ~ |False)| =>
 => STrue
            SFalse
                      :: Bool)
```

```
data
                                                      data Nat = Z | S Nat
              SZ
                             instance Sing :: Nat -> Type where
              Sing
Sing (n
Nat) -> Sing (S n)
```

```
data
                                                        data Nat = Z | S Nat
               SZ
                               instance Sing :: Nat -> Type where
               Sing
Sing (n
Nat) -> Sing (S n)
```

```
data instance Sing (z :: Nat)
| forall (n :: Nat). (z ~ S n) => SS n
                                         (z \sim Z) \Rightarrow SZ
```

# Dependent types... in Idris (redux)

```
mkSingle
mkSingle
                            mkSingle
 False =
          Irue
                   if x then Nat else List Nat
                            ×
            П
                            Bool) ->
\odot
```

### Dependent types... in Haskell? (Heck yeah!)

```
type family
If (c :: Bool) (t
If True t f = t
If False t f = f
                          k) (f :: k)
                           :: k where
```

#### (Heck yeah!) Dependent types... in Haskell?

```
mkSingle STrue = ⊙
mkSingle SFalse = [
                                                      mkSingle ::
                                                                                                                                            type family
                                                                                           If (c :: Bool) (t
If True t f = t
If False t f = f
                                    Sing (x :: Bool) ->
If x Nat [Nat]
                                                                                                                          k) (f :: k) :: k where
```

### Dependent types... in Haskell? (Heck yeah!)

type II Sing

### Dependent types... in Haskell? (Heck yeah!)

```
type II
Sing
```

```
mkSingle STrue = 0
mkSingle SFalse = []
                                         mkSingle
                         If (x :: Bool) ->
```

Dependent pattern matching

Dependent pattern matching... in Idris

```
data Vect : Nat -> Type -> Type where
                                   Nil : Vect Z a
Cons : a -> Vect n a -> Vect (S n) a
```

Dependent pattern matching... in Idris

```
data Vect : Nat -> Type -> Type where
                                 Nil : Vect Z a
Cons : a -> Vect n a -> Vect (S n) a
```

```
len (Cons x \times s) = 1 + len xs
                           len Nil
                                                   len : Vect n a -> Nat
```

Dependent pattern matching... in Idris

```
data Vect : Nat -> Type -> Type where
                               Z
L
L
Cons : a -> Vect n a -> Vect (S n) a
                             : Vect Z a
```

```
len
                              len
len \{n=S k\} (Cons x xs) =
                \{n=Z\}
                             : {n : Nat} -> Vect n a -> Nat
                  Zi.
   1 + len xs
```

```
data Vect :: Nat -> Type -> Type where
                             Z
1
1
Cons :: a -> Vect n a -> Vect (S n) a
                           :: Vect Z a
```

```
data Vect :: Nat -> Type -> Type where
                               Z
1
1
Cons :: a -> Vect n a -> Vect (S n) a
                             :: Vect Z a
```

```
len
                     len SZ
len (SS k) (Cons x \times xs) = 1 + len xs
                                       :: Sing (n :: Nat) -> Vect n a -> Nat
                       Z
1:
1
                        ||
⊙
```

```
class SingI (a :: k) where
sing :: Sing (a :: k)
instance SingI n
sing = SS sing
                                                                               instance SingI Z where
                                                           sing = SZ
                   => SingI (S n) where
```

```
len
              len SZ
len (SS k) (Cons x xs)
                 :: Sing (n :: Nat) → Vect n a
SZ Nil = 0
  = 1 + 1en xs
                                 -> Nat
```

```
len
                                len'
                                                                           len SZ
len' = len (sing :: n)
                                                            len (SS k) (Cons x xs) = 1 + len xs
                                                                            forall (n :: Nat). SingI n =>
                Vect n a -> Nat
```

- $\lambda$  With enough elbow grease, one can simulate a great deal of dependently typed code
- A Impress your friends at the bar! Be the envy of your family!
- λhttp://hackage.haskell.org/package/singletons

# Any questions?