

1) Linear Search (Pseudo Code)

```
int lin-search (int* arr, int n, int key)
{
    for (i = 0 to n-1)
        if (arr[i] == key)
            return i;
    return -1;
}
```

2) Iterative Insertion Sort

```
void insert-sort (int arr[], int n)
{
    int i, temp, j;
    for (i = 1 to n)
        temp = arr[i];
        j = i - 1;
        while (j >= 0 AND arr[j] > temp)
            arr[j + 1] = arr[j];
            j = j - 1;
        arr[j + 1] = temp;
}
```

Recursive Insertion Sort

```
void insert-sort (int arr[], int n)
```

```
if (n <= 1)
```

```
return
```

```
insert-sort (arr, n - 1)
```

```
last = arr[n - 1]
```

```
j = n - 2
```

```
while (j >= 0 & arr[j] > last)
```

```
arr[j + 1] = arr[j]
```

```
j --
```

```
arr[j + 1] = last
```

Why? - Online sorting Because it doesn't need to know anything about what values it will sort and the information is requested while the algorithm is running.

v) Selection Sort:

T.C. = Best Case = $O(n^2)$; Worst Case = $O(n^2)$
S.C. = $O(1)$

(i) Insertion Sort:

T.C. = Best Case = $O(n)$; Worst Case = $O(n^2)$
S.C. = $O(1)$

(ii) Merge Sort:

T.C. = Best case = $O(n \log n)$; worst case = $O(n \log n)$
S.C. = $O(n)$

(iv) Quick Sort:

T.C. = Best Case = $O(n \log n)$; Worst Case = $O(n^2)$
S.C. = $O(n)$

v) Heap Sort

T.C. = Best case = $O(n \log n)$, worst case = $O(n \log n)$
S.C. = $O(1)$

vi) Bubble Sort

T.C. = Best case = $O(n^2)$; Worst Case = $O(n^2)$
S.C. = $O(1)$

| Sorting | Inplace | stable | Online |
|-----------|---------|--------|--------|
| Selection | ✓ | | |
| Insertion | ✓ | ✓ | |
| Merge | | ✓ | |
| Quick | ✓ | | |
| Heap | ✓ | | |
| Bubble | ✓ | ✓ | |

1) Iterative Binary Search

```
int bin_search(int arr[], int l, int r, int x)
```

```
{ while(l <= r){
```

```
    int m = (l+r)/2;
```

```
    if(arr[m] == x)
```

```
        return m;
```

```
    if(arr[m] < x)
```

```
        else l = m+1;
```

```
        r = m-1;
```

```
}
```

```
return -1;
```

T.C.

Best case: $O(1)$

Avg. case: $O(\log_2 n)$

Worst case: $O(\log n)$

3

Recursive Binary Search

```
int bin_search(int arr[], int l, int r, int x)
```

```
{ if(r >= 1){
```

```
    int mid = (l+r)/2;
```

```
    if(arr[mid] == x)
```

```
        return mid;
```

```
    else if(arr[mid] > x)
```

```
        return bin_search(arr, l, mid-1, x);
```

```
    else
```

```
        return bin_search(arr, mid+1, r, x);
```

```
}
```

```
return -1;
```

T.C.

Best case = $O(1)$

Avg. case = $O(\log n)$

Worst case = $O(\log n)$

6) Recurrence Relation for binary recursive search

$$T(n) = T(n/2) + 1$$

QUICK SORT IS THE FASTEST GENERAL PURPOSE SORT. IN MOST PRACTICAL SITUATIONS, QUICK SORT IS THE METHOD OF CHOICE. IF STABILITY IS IMPORTANT AND SPACE IS AVAILABLE, MERGE SORT MIGHT BE BETTER.

Q7

How far does the array is from being sorted. If the array is already sorted, then the inversion count is 0. But if array is sorted in reverse order, the inversion count is max.

For following array arr[] = {7, 21, 31, 8, 10, 1, 20, 6, 9, 5}

```
#include <bits/stdc++.h>
```

```
using namespace std;
```

```
int mergeSort (int arr[], int temp[], int left, int right);
```

```
int merge (int arr[], int temp[], int left, int mid, int right);
```

```
int mergeSort (int arr[], int arrSize) {
```

```
    int temp[arrSize];
```

```
    return mergeSort (arr, temp, 0, arrSize - 1);
```

```
}
```

```
int mergeSort (int arr[], int temp[], int left, int right)
```

```
{ int mid, int count = 0;
```

```
    if (right > left) {
```

```
        mid = (right + left) / 2;
```

```
        invCount = mergeSort (arr, temp, left, mid);
```

```
        invCount += mergeSort (arr, temp, mid + 1, right);
```

```
        invCount += merge (arr, temp, mid + 1, right);
```

```
    }
```

```
    return invCount;
```

```
}
```

```
int merge (int arr[], int temp[], int left, int mid, int right)
```

```
{ int i, j, k;
```

```
    int invCount = 0;
```

```
    i = left;
```

```
    j = mid;
```

```
    k = left;
```

```

        while (i < mid - 1) && (j < right)
    } {
        if (arr[i] < arr[j])
            temp[i + 1] = arr[i + 1];
        else
    } {
        temp[k + 1] = arr[j + 1];
        inv_count = inv_count + (mid - i);
        j++;
    }
}

while (i <= mid - 1)
    temp[k + 1] = arr[i + 1];
arr[i] = temp[i];
return inv_count;
}

int main()
{
    int arr[] = {7, 21, 31, 8, 10, 1, 20, 6, 4, 5};
    int n = sizeof(arr) / sizeof(arr[0]);
    int ans = mergesort(arr, n);
    cout << "No. of inversion are" << ans;
    return 0;
}

```

\Rightarrow The worst case time complexity of quick sort $O(n^2)$ occurs when the picked pivot is always an extreme (smallest or largest) element. This happens when input array is sorted in reverse sorted & either first or last element is picked as pivot.
 The best case of quick sort is when we will select pivot as a mean element.

III relation of:

a) merge sort $\rightarrow T(n) = 2T(n/2) + n$

b) quick sort $\rightarrow T(n) = 2T(n/2) + n$

merge sort is more efficient and works faster than quick sort in case of larger array size or data sets.

worst case complexity for quick sort is $O(n^2)$ whereas $O(n \log n)$ for mergesort.

(2) → Stable Selection Sort:-

using namespace;

```
void stab-selectsort(int a[], int n) {
```

```
    for (int i=0; i<n-1; i++) {
```

```
        int min=i;
```

```
        for (int j=i+1; j<n; j++)
```

```
            if (a[min] > a[j])
```

```
                min=j;
```

```
        int key=a[min];
```

```
        while (min>i)
```

```
            a[min]=a[min-1];
```

```
            min-=1;
```

```
}
```

```
        a[i]=key;
```

```
}
```

```
}
```

```
int main () {
```

```
    int a[] = { 4, 5, 3, 2, 1 };
```

```
    int n = size(a) / size(a[0]);
```

```
    stab-selectsort(a, n);
```

```
    for (int i=0; i<n; i++)
```

```
        cout << a[i] << " ";
```

```
    cout << endl;
```

```
    return 0;
```

```
}
```

13] ^s

The easiest way to do this is to use external sorting we divide our source file into temporary files of size equal to the size of the RAM & first sort in files External sorting:- If the input data is such that it cannot adjust in the memory entirely at once, it needs to be stored in a hard disk, floppy disk or any other storage device this is external sorting.

Internal sorting:- If the input data is much that fit completely in the main memory at once, it is called internal sorting.