

# CS 663 Course Project

...

Exposing Image Splicing with Inconsistent Local Noise  
Variances

# Kurtosis Concentration

For a random variable  $x$ , we define its kurtosis as

$$\kappa = \frac{\tilde{\mu}_4}{(\sigma^2)^2} - 3$$

where  $\sigma^2 = \mathcal{E}_x[(x - \mathcal{E}_x(x))^2]$  ,  $\tilde{\mu}_4 = \mathcal{E}_x[(x - \mathcal{E}_x(x))^4]$

# CS 663 Course Project

...

## Global Noise Variance Estimation

# Global Noise Variance Estimation

$$\sqrt{\tilde{\kappa}} = \sqrt{\kappa} \left( \frac{\sigma_k^2 - \sigma^2}{\sigma_k^2} \right)$$

Objective function :

$$\min_{\sqrt{\kappa}, \sigma^2} \sum_{k=1}^K \left[ \sqrt{\tilde{\kappa}_k} - \sqrt{\kappa} \left( \frac{\sigma_k^2 - \sigma^2}{\sigma_k^2} \right) \right]^2$$

where

$\kappa$ : kurtosis of the original image in the k-th channel (constant)

$\tilde{\kappa}_k$ : kurtosis of the noisy image in the k-th channel

$\sigma_k$ : variance of the noisy image in the k-th channel

# Global Noise Variance Estimation

Closed form solution to the objective function:

$$\sqrt{\kappa} = \frac{\langle \sqrt{\tilde{\kappa}_k} \rangle_k \langle \frac{1}{(\tilde{\sigma}_k^2)^2} \rangle_k - \langle \frac{\sqrt{\tilde{\kappa}_k}}{\tilde{\sigma}_k^2} \rangle_k \langle \frac{1}{\tilde{\sigma}_k^2} \rangle_k}{\langle \frac{1}{(\tilde{\sigma}_k^2)^2} \rangle_k - \langle \frac{1}{\tilde{\sigma}_k^2} \rangle_k^2}$$

$$\sigma^2 = \langle \frac{1}{\tilde{\sigma}_k^2} \rangle_k - \frac{1}{\sqrt{\kappa}} \frac{\langle \sqrt{\tilde{\kappa}_k} \rangle_k}{\langle \frac{1}{\tilde{\sigma}_k^2} \rangle_k}$$

# CS 663 Course Project

...

## Local Noise Variance Estimation

# Local Noise Variance Estimation

The global noise variance estimator is then extended to a more general *local* noise variance estimator. Writing  $\sigma^2$  and  $\kappa$  in terms of the raw moments, we have (*per pixel location per channel*):

$$\sigma^2 = \mu_2 - \mu_1^2$$

$$\kappa = \frac{\mu_4 - 4\mu_3\mu_1 + 6\mu_2\mu_1^2 - 3\mu_1^4}{\mu_2^2 - 2\mu_2\mu_1^2 + \mu_1^4} - 3$$

# Local Noise Variance Estimation

The raw moment per window is estimated by spatial averaging:

$$\mu_m(\Omega_{(i,j)}^k) \approx \frac{1}{|\Omega_{(i,j)}^k|} \sum_{(i',j') \in \Omega_{(i,j)}^k} x(i',j',k)^m$$

To make the process more efficient, the raw moment  $\mu_m$  is computed using an *integrated image* as :

$$\frac{1}{IJ} [I(x^m)_{i+I,j+J} - I(x^m)_{i+I,j} - I(x^m)_{i,j+J} + I(x^m)_{i,j}]$$

with  $x^m$  being denoting pointwise multiplication  $m$  times



# CS 663 Course Project

...

## Results

# Different additive white Gaussian noise patterns

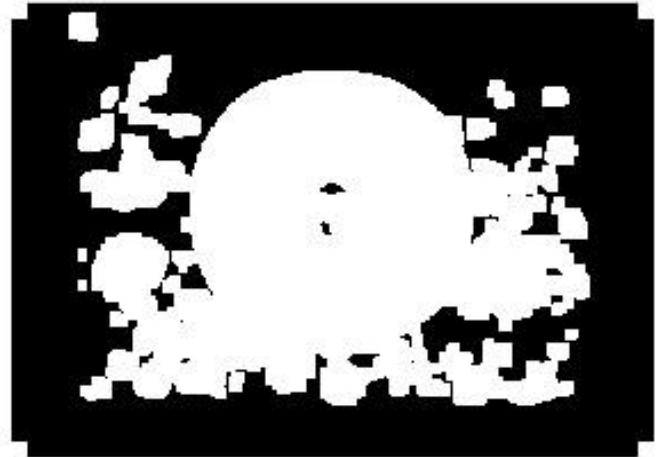


# Different additive white Gaussian noise patterns

Spliced image

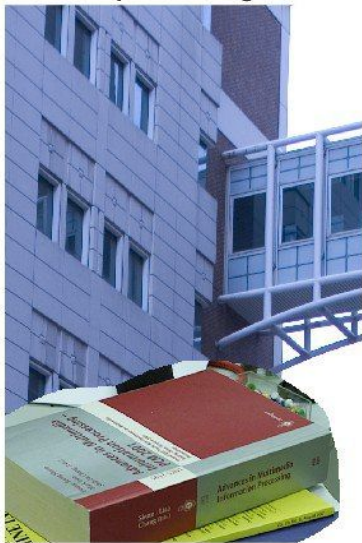


Detection



# Results on Columbia Dataset

Spliced image



Detection



Spliced image

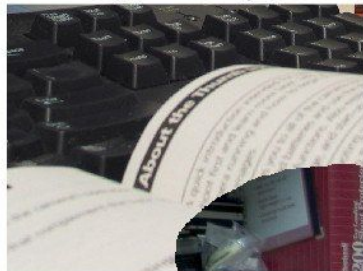


Detection



# Results on Columbia Dataset

Spliced image



Detection



Spliced image



Detection



# Results on Columbia Dataset

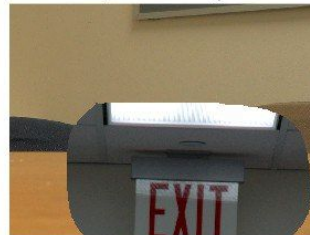
Spliced image



Detection



Spliced image

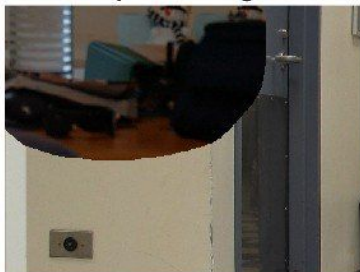


Detection

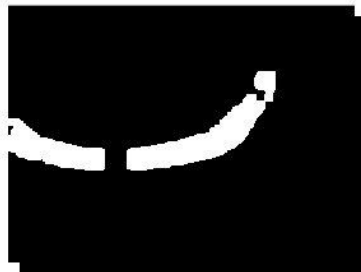


# Results on Columbia Dataset

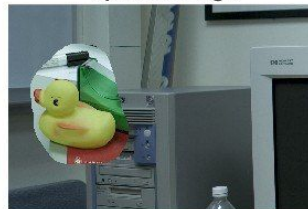
Spliced image



Detection



Spliced image

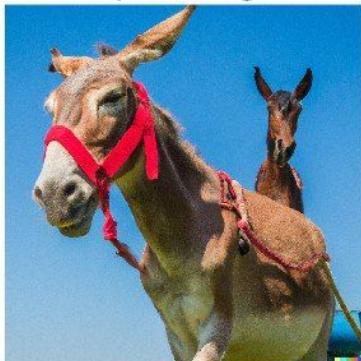


Detection

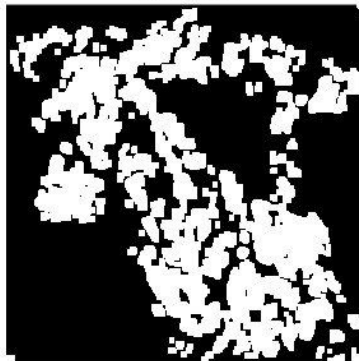


# Results on AI Generated Dataset

Spliced image



Detection



Spliced image



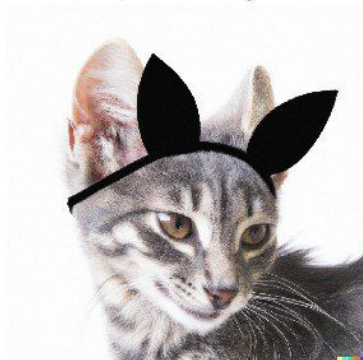
Detection





# Results on AI Generated Dataset

Spliced image



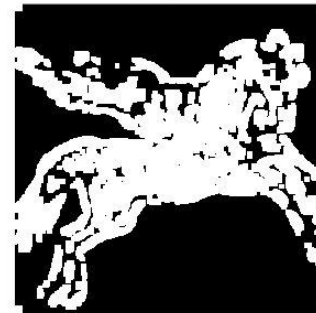
Detection



Spliced image



Detection



# Observations

1. The method is sensitive to the choice of the band-pass filter. A filter that is too narrow may not capture enough noise information, while a filter that is too wide may introduce too much noise from other parts of the image.
2. Size of the corrupted area doesn't have significant role in detection accuracy.

# Observations

1. The last image is screenshot extracted from the paper's pdf. We believe significant information about the noise variances is lost leading to a wrong result.
2. This method relies on the assumption that the spliced region and the original image have different intrinsic noise variances. For cases where tampered image underwent heavy JPEG compression, for example, information of the difference in noise variances is lost.
3. For images with distinct texture and smooth regions, inhomogeneous local noise variance can cause the method to make false detections. (As seen in the tree detected in the first limitation example)

# CS 663 Course Project

...

Project By

Darshan Kumar (210010023) Vedant Thakre (210010071)