

## 1. Modification in Sequential Algorithm

- ✚ We can observe that during modified multiplication dependency is only on the loop k since we are taking minimum over that loop
- ✚ But, Two outer loops are independent with respect to each other
- ✚ Hence, we can give one outer loop and one middle loop to the different processors
- ✚ Hence simply we are giving N/P iterations to each processor
- ✚ We are only parallelizing the modified\_matrix\_multiplication function here
- ✚ We will not be parallelizing the While loop in All\_Pairs\_Distance function since it needs to be run sequentially, also its only takes  $\log(n)$  steps to complete

## 2. Pseudo Code

Modified\_Matrix\_Multiplication(A,B):

```
C ← inf // matrix of len(A) × len(B[0])

// This loop can run in parallel
LOOPS (i, 0, len(A)):
    LOOPS (j, 0, len(B)):
        LOOPS (k, 0, len(B[0])):
            C[i][j] ← min(C[i][j], A[i][k] + B[k][j])
        END
    END
END

RETURN C
```

## 3. Time Complexity

Time complexity for Modified Matrix multiplication  
=  $(N/p) * N * N$   
=  $(N^3) / p$

Time complexity for iterating till  $D(n) = \log(n)$

Overall time complexity :  $(N^3) * \log(n) / p$