Thevenin's/Norton's theory (cont.)

Case 3 (Circuit with dependent source only)

Since the dependaent source depends on a independent source, $E_{\mathrm{TH}}=0$

Examples

1. Find Thevinin's equivalent between the terminals a-b.

$$E_{\mathrm{TH}} = 0$$

By connecting a current/voltage (1A/1V) supply between the two terminals a and b:

1. Calculate $V_{\rm ab}$ across the 1A current source.

$$\therefore R_{\rm ab} = \frac{V_{\rm ab}}{1A} = R_{\rm TH}$$

2. Using mesh analysis:

$$\begin{split} i_1 &= -3i_x \to 1 \\ 0 &= i_2(2+6+8) - i_2(2) - i_3(8) \to 2 \\ i_3 &= -1A \to 3 \\ i_x &= i_2 - i_3 \to 4 \\ & \div V_{\rm ab} = 8i_x = R_{\rm TH} \end{split}$$

The theory of the maximum power transfer

If a circuit containing either an independant source and a dependanent source or an independant source soley, is connected to a variable resistance between two terminals a-b, The value of the power (P_L) starts from 0 and ends at 0. If the circuit is substituted by a thevinin circuit, P_L can be considered a function with the variable R_L . Therefore, to find the maximum power generated by the circuit, the function can be diffrentiated and made equal to 0.

$$\begin{split} I_L &= \frac{E_{\mathrm{TH}}}{R_{\mathrm{TH}} + R_L} \\ P_L &= \left(I_L\right)^2 \times R_L \\ P_L &= \frac{\left(E_{\mathrm{TH}}\right)^2 \times R_L}{\left(R_{\mathrm{TH}} = R_L\right)^2} \end{split}$$

To find the maximum power:

$$\frac{dP_L}{dR_L} = 0$$

After diffrentiation:

$$\begin{split} R_L &= R_{\rm TH} \\ & \therefore P_{\rm max} = \frac{\left(E_{\rm TH}\right)^2 \times R_{\rm TH}}{4{\left(R_{\rm TH}\right)}^2} = \frac{\left(E_{\rm TH}\right)^2}{4R_{\rm TH}} W \end{split}$$

Examples

1. Find the maximum power.

By disconnecting all power sources:

$$R_{\rm TH}=9\Omega$$

$$E_{\rm TH} = V_{\rm ab}$$

Using nodal analysis at V_1 :

$$2 = \frac{V_1 - 0}{12} + \frac{V_1 - 12}{6}$$

(3 Ω resistance is ignored since it is connected in series with a current source)

By applying KVL on the first two loops from the right:

$$-V_1 - 6 - 0 + V_{\rm ab} = 0$$

$$E_{\mathrm{TH}} = V_{\mathrm{ab}}$$

$$\therefore P_L = \frac{\left(E_{\rm TH}\right)^2}{4R_{\rm TH}}$$