

**Question:** The plane through the point  $(-1, 4, 2)$  that contains the line of intersection of the planes  $4x - y + z - 2 = 0$  and  $2x + y - 2z - 3 = 0$ .

Plane 1 has normal  $\vec{n}_1 = \langle 4, -1, 1 \rangle$ . Plane 2 has normal  $\vec{n}_2 = \langle 2, 1, -2 \rangle$ . The line that passes through both planes must have a directional vector perpendicular to both normals; that is,  $\vec{v} = \langle 1, 10, 6 \rangle$ .

The planes intersect at the points,  $\langle x, y, z \rangle = \langle \frac{t-5}{6}, \frac{5t+4}{3}, t \rangle$ . Let us choose  $t = 0$ : then an intersection is at  $\langle x, y, z \rangle = \langle -\frac{5}{6}, \frac{4}{3}, 0 \rangle$ .

The vector formed from  $(-1, 4, 2)$  to this point is given by  $u = \frac{1}{6}, -\frac{8}{3}, -2$ . Then, the normal vector is  $n = \langle 4, -3, 13/3 \rangle$ .

Then, the plane is:

$$4(x + 1) - 3(y - 4) + \frac{13}{3}(z - 2)$$
$$4x - 3y + \frac{13}{3}z = \frac{18}{3}$$