



**Министерство науки и высшего образования Российской Федерации
Федеральное государственное бюджетное образовательное учреждение
высшего образования
«Московский государственный технический университет
имени Н.Э. Баумана
(национальный исследовательский университет)»
(МГТУ им. Н.Э. Баумана)**

ФАКУЛЬТЕТ «Информатика и системы управления» (ИУ)

КАФЕДРА «Информационная безопасность» (ИУ8)

Отчёт

**по рубежному контролю № 3
по дисциплине «Методы оптимизации»**

Тема: « Исследование генетических алгоритмов в задачах поиска экстремумов »

Вариант 10

**Выполнил: Митрофанов Д.А.,
студент группы ИУ8-33**

**Проверил: Коннова Н. С.,
доцент каф. ИУ8**

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1.1. Цель работы

Изучить основные принципы действия генетических алгоритмов на примере решения задач оптимизации функций двух переменных.

1.2. Постановка задачи

Найти максимум функции $f(x,y)$ в области D с помощью простого (классического) генетического алгоритма. За исходную популяцию принять 4 случайных точки. Хромосома каждой особи состоит из двух генов: значений координат x, y . В качестве потомков следует выбирать результат скрещивания лучшего решения со вторым и третьим в порядке убывания значений функции приспособленности с последующей случайной мутацией обоих генов. В качестве критерия останова эволюционного процесса задаться номером конечной популяции ($N \sim 10^1 \dots 10^2$). Визуализировать результаты расчетов.

1.3. Условие варианта

Вид функции $f(x,y)$	Область допустимых значений D
$\frac{\sin^2(x)}{1+x^2+y^2}$	$(0,2) \times (-2,2)$

2. Расчёт с помощью программы

10 generations:

generation	prefix	X	Y	FIT	max element	average
0	p	0.4018	-0.0001607	0.1317		
0	p	0.9955	1.223	0.2019		
0	p	1.445	0.9934	0.2416		
0	p	1.283	-0.08465	0.3465	0.3465	0.2304
1	p	1.283	-0.08465	0.3465		
1	p	1.283	-0.0001607	0.3474		
1	p	0.9955	-0.08465	0.3523		
1	p	0.9955	-0.0001607	0.3536	0.3536	0.3499
1	ig	1.283	-0.08465	0.3465		
1	ig	1.283	-0.08465	0.3465		
1	ig	1.283	-0.08465	0.3465		
1	ig	1.283	-0.0001607	0.3474		
1	ig	1.283	-0.0001607	0.3474		
1	ig	1.283	-0.0001607	0.3474		
1	ig	0.9955	-0.08465	0.3523		
1	ig	0.9955	-0.08465	0.3523		
1	ig	0.9955	-0.08465	0.3523		
1	ig	0.9955	-0.0001607	0.3536		
1	ig	0.9955	-0.0001607	0.3536		
1	ig	0.9955	-0.0001607	0.3536	0.3536	0.3499
2	p	0.9955	-0.0001607	0.3536		
2	p	0.9955	-0.0001607	0.3536		
2	p	0.9955	-0.0001607	0.3536		
2	p	0.9955	-0.0001607	0.3536	0.3536	0.3536

9	p	0.9955	-0.0001607	0.3536			
9	p	0.9955	-0.0001607	0.3536			
9	p	0.9955	-0.0001607	0.3536			
9	p	0.9955	-0.0001607	0.3536	0.3536	0.3536	
9	ig	0.9955	-0.0001607	0.3536			
9	ig	0.9955	-0.0001607	0.3536			
9	ig	0.9955	-0.0001607	0.3536			
9	ig	0.9955	-0.0001607	0.3536			
9	ig	0.9955	-0.0001607	0.3536			
9	ig	0.9955	-0.0001607	0.3536			
9	ig	0.9955	-0.0001607	0.3536			
9	ig	0.9955	-0.0001607	0.3536			
9	ig	0.9955	-0.0001607	0.3536			
9	ig	0.9955	-0.0001607	0.3536			
9	ig	0.9955	-0.0001607	0.3536	0.3536	0.3536	
10	result	0.9955	-0.0001607	0.3536			
10	result	0.9955	-0.0001607	0.3536			
10	result	0.9955	-0.0001607	0.3536			
10	result	0.9955	-0.0001607	0.3536	0.3536	0.3536	

100 generations:

generation	prefix	X	Y	FIT	max element	average	
0	p	0.4897	-1.732	0.05218			
0	p	1.51	-1.321	0.1983			
0	p	0.9145	-0.5381	0.2953			
0	p	1.384	0.178	0.3276	0.3276	0.2183	
1	p	1.51	0.178	0.3009			
1	p	1.384	-0.5381	0.3013			
1	p	1.384	0.178	0.3276			
1	p	0.9145	0.178	0.336	0.336	0.3165	
1	ig	1.51	-0.5381	0.2792			
1	ig	0.9145	-0.5381	0.2953			
1	ig	1.51	0.178	0.3009			
1	ig	1.51	0.178	0.3009			
1	ig	1.384	-0.5381	0.3013			
1	ig	1.384	0.178	0.3276			
1	ig	1.384	0.178	0.3276			
1	ig	1.384	0.178	0.3276			
1	ig	1.384	0.178	0.3276			
1	ig	1.384	0.178	0.3276			
1	ig	0.9145	0.178	0.336			
1	ig	0.9145	0.178	0.336	0.336	0.3156	
2	p	1.384	0.178	0.3276			
2	p	0.9145	0.178	0.336			
2	p	0.9145	0.178	0.336			
2	p	0.9145	0.178	0.336	0.336	0.3339	
2	ig	1.384	0.178	0.3276			
2	ig	1.384	0.178	0.3276			

5	ig	0.9145	0.178	0.336		
5	ig	0.9145	0.178	0.336		
5	ig	0.9145	0.178	0.336	0.336	0.336

6	p	0.9145	0.178	0.336		
6	p	0.9145	0.178	0.336		
6	p	0.9145	0.178	0.336		
6	p	0.9145	0.178	0.336	0.336	0.336

6	ig	0.9145	0.178	0.336		
6	ig	0.9145	0.178	0.336		
6	ig	0.9145	0.178	0.336		
6	ig	0.9145	0.178	0.336		
6	ig	0.9145	0.178	0.336		
6	ig	0.9145	0.178	0.336		
6	ig	0.9145	0.178	0.336		
6	ig	0.9145	0.178	0.336		
6	ig	0.9145	0.178	0.336		
6	ig	0.9145	0.178	0.336		
6	ig	0.9145	0.178	0.336	0.336	0.336

7	p	0.9145	0.178	0.336		
7	p	0.9145	0.178	0.336		
7	p	0.9145	0.178	0.336		
7	p	0.9145	0.178	0.336	0.336	0.336

7	ig	0.9145	0.178	0.336		
7	ig	0.9145	0.178	0.336		
7	ig	0.9145	0.178	0.336		
7	ig	0.9145	0.178	0.336		
7	ig	0.9145	0.178	0.336		
7	ig	0.9145	0.178	0.336		
7	ig	0.9145	0.178	0.336		
7	ig	0.9145	0.178	0.336		
7	ig	0.9145	0.178	0.336		
7	ig	0.9145	0.178	0.336		
7	ig	0.9145	0.178	0.336	0.336	0.336

8	p	0.9145	0.178	0.336		
8	p	0.9145	0.178	0.336		
8	p	0.9145	0.178	0.336		
8	p	0.9145	0.178	0.336	0.336	0.336

8	ig	0.9145	0.178	0.336		
8	ig	0.9145	0.178	0.336		
8	ig	0.9145	0.178	0.336		
8	ig	0.9145	0.178	0.336		
8	ig	0.9145	0.178	0.336		
8	ig	0.9145	0.178	0.336		
8	ig	0.9145	0.178	0.336		
8	ig	0.9145	0.178	0.336		
8	ig	0.9145	0.178	0.336		
8	ig	0.9145	0.178	0.336		
8	ig	0.9145	0.178	0.336	0.336	0.336

9	p	0.9145	0.178	0.336		

9	p	0.9145	0.178	0.336		
9	p	0.9145	0.178	0.336		
9	p	0.9145	0.178	0.336	0.336	0.336

9	ig	0.9145	0.178	0.336		
9	ig	0.9145	0.178	0.336		
9	ig	0.9145	0.178	0.336		
9	ig	0.9145	0.178	0.336		
9	ig	0.9145	0.178	0.336		
9	ig	0.9145	0.178	0.336		
9	ig	0.9145	0.178	0.336		
9	ig	0.9145	0.178	0.336		
9	ig	0.9145	0.178	0.336		
9	ig	0.9145	0.178	0.336		
9	ig	0.9145	0.178	0.336	0.336	0.336

10	p	0.9145	0.178	0.336		
10	p	0.9145	0.178	0.336		
10	p	0.9145	0.178	0.336		
10	p	0.9145	0.178	0.336	0.336	0.336

10	ig	0.9145	0.178	0.336		
10	ig	0.9145	0.178	0.336		
10	ig	0.9145	0.178	0.336		
10	ig	0.9145	0.178	0.336		
10	ig	0.9145	0.178	0.336		
10	ig	0.9145	0.178	0.336		
10	ig	0.9145	0.178	0.336		
10	ig	0.9145	0.178	0.336		
10	ig	0.9145	0.178	0.336		
10	ig	0.9145	0.178	0.336		
10	ig	0.9145	0.178	0.336	0.336	0.336

11	p	0.9145	0.178	0.336		
11	p	0.9145	0.178	0.336		
11	p	0.9145	0.178	0.336		
11	p	0.9145	0.178	0.336	0.336	0.336

11	ig	0.9145	0.178	0.336		
11	ig	0.9145	0.178	0.336		
11	ig	0.9145	0.178	0.336		
11	ig	0.9145	0.178	0.336		
11	ig	0.9145	0.178	0.336		
11	ig	0.9145	0.178	0.336		
11	ig	0.9145	0.178	0.336		
11	ig	0.9145	0.178	0.336		
11	ig	0.9145	0.178	0.336		
11	ig	0.9145	0.178	0.336		
11	ig	0.9145	0.178	0.336	0.336	0.336

12	p	0.8731	0.3743	0.3087		
12	p	0.8499	0.2147	0.3191		
12	p	0.9721	0.2458	0.3403		
12	p	1.085	0.2404	0.3499	0.3499	0.3295

12	ig	0.6459	0.08588	0.2543		
12	ig	0.6916	0.3437	0.2548		

	12		ig		0.8682		0.1139		0.3297			
	12		ig		1.015		0.377		0.3322			
	12		ig		1.199		0.3364		0.3403			
	12		ig		0.9327		-0.01976		0.3449			
	12		ig		0.942		-0.05961		0.3459			
	12		ig		0.9686		0.00882		0.3504			
	12		ig		1.201		0.1403		0.3531			
	12		ig		1.14		0.1633		0.3549			
	12		ig		1.1		0.1489		0.3558			
	12		ig		1.146		0.02796		0.3587		0.3587	0.3312

	13		p		1.201		0.1403		0.3531			
	13		p		1.14		0.1633		0.3549			
	13		p		1.1		0.1489		0.3558			
	13		p		1.146		0.02796		0.3587		0.3587	0.3556

	13		ig		1.201		0.1633		0.3521			
	13		ig		1.201		0.1489		0.3527			
	13		ig		1.146		0.1633		0.3548			
	13		ig		1.1		0.1633		0.3551			
	13		ig		1.146		0.1489		0.3554			
	13		ig		1.14		0.1489		0.3556			
	13		ig		1.201		0.02796		0.3558			
	13		ig		1.146		0.1403		0.3558			
	13		ig		1.14		0.1403		0.356			
	13		ig		1.1		0.1403		0.3562			
	13		ig		1.14		0.02796		0.3589			
	13		ig		1.1		0.02796		0.3593		0.3593	0.3556

	14		p		1.1		0.1403		0.3562			
	14		p		1.146		0.02796		0.3587			
	14		p		1.14		0.02796		0.3589			
	14		p		1.1		0.02796		0.3593		0.3593	0.3583

	14		ig		1.146		0.1403		0.3558			
	14		ig		1.14		0.1403		0.356			
	14		ig		1.1		0.1403		0.3562			
	14		ig		1.146		0.02796		0.3587			
	14		ig		1.146		0.02796		0.3587			
	14		ig		1.14		0.02796		0.3589			
	14		ig		1.14		0.02796		0.3589			
	14		ig		1.1		0.02796		0.3593			
	14		ig		1.1		0.02796		0.3593			
	14		ig		1.1		0.02796		0.3593			
	14		ig		1.1		0.02796		0.3593			
	14		ig		1.1		0.02796		0.3593		0.3593	0.3583

	15		p		1.1		0.02796		0.3593			
	15		p		1.1		0.02796		0.3593			
	15		p		1.1		0.02796		0.3593			
	15		p		1.1		0.02796		0.3593		0.3593	0.3593

	15		ig		1.1		0.02796		0.3593			
	15		ig		1.1		0.02796		0.3593			
	15		ig		1.1		0.02796		0.3593			
	15		ig		1.1		0.02796		0.3593			
	15		ig		1.1		0.02796		0.3593			
	15		ig		1.1		0.02796		0.3593			
	15		ig		1.1		0.02796		0.3593			
	15		ig		1.1		0.02796		0.3593			
	15		ig		1.1		0.02796		0.3593			

19	p	1.1	0.02796	0.3593		
19	p	1.1	0.02796	0.3593		
19	p	1.1	0.02796	0.3593	0.3593	0.3593
19	ig	1.1	0.02796	0.3593		
19	ig	1.1	0.02796	0.3593		
19	ig	1.1	0.02796	0.3593		
19	ig	1.1	0.02796	0.3593		
19	ig	1.1	0.02796	0.3593		
19	ig	1.1	0.02796	0.3593		
19	ig	1.1	0.02796	0.3593		
19	ig	1.1	0.02796	0.3593		
19	ig	1.1	0.02796	0.3593		
19	ig	1.1	0.02796	0.3593		
19	ig	1.1	0.02796	0.3593	0.3593	0.3593
19	ig	1.1	0.02796	0.3593	0.3593	0.3593
20	p	1.1	0.02796	0.3593		
20	p	1.1	0.02796	0.3593		
20	p	1.1	0.02796	0.3593		
20	p	1.1	0.02796	0.3593	0.3593	0.3593
20	ig	1.1	0.02796	0.3593		
20	ig	1.1	0.02796	0.3593		
20	ig	1.1	0.02796	0.3593		
20	ig	1.1	0.02796	0.3593		
20	ig	1.1	0.02796	0.3593		
20	ig	1.1	0.02796	0.3593		
20	ig	1.1	0.02796	0.3593		
20	ig	1.1	0.02796	0.3593		
20	ig	1.1	0.02796	0.3593		
20	ig	1.1	0.02796	0.3593		
20	ig	1.1	0.02796	0.3593		
20	ig	1.1	0.02796	0.3593	0.3593	0.3593
20	ig	1.1	0.02796	0.3593	0.3593	0.3593
21	p	1.1	0.02796	0.3593		
21	p	1.1	0.02796	0.3593		
21	p	1.1	0.02796	0.3593		
21	p	1.1	0.02796	0.3593	0.3593	0.3593
21	ig	1.1	0.02796	0.3593		
21	ig	1.1	0.02796	0.3593		
21	ig	1.1	0.02796	0.3593		
21	ig	1.1	0.02796	0.3593		
21	ig	1.1	0.02796	0.3593		
21	ig	1.1	0.02796	0.3593		
21	ig	1.1	0.02796	0.3593		
21	ig	1.1	0.02796	0.3593		
21	ig	1.1	0.02796	0.3593		
21	ig	1.1	0.02796	0.3593		
21	ig	1.1	0.02796	0.3593		
21	ig	1.1	0.02796	0.3593	0.3593	0.3593
21	ig	1.1	0.02796	0.3593	0.3593	0.3593
22	p	0.9433	0.3001	0.331		
22	p	0.8888	-0.1718	0.3312		
22	p	0.9305	0.1513	0.3405		
22	p	1.203	0.09021	0.3546	0.3546	0.3393
22	ig	0.817	-0.2483	0.3074		
22	ig	1.37	0.3149	0.3227		

22	ig	0.8956	-0.2085	0.3301			
22	ig	1.301	0.2975	0.3341			
22	ig	0.9813	0.3238	0.3341			
22	ig	1.159	0.3108	0.3442			
22	ig	1.283	0.153	0.3444			
22	ig	1.047	-0.2175	0.3498			
22	ig	1.073	-0.1934	0.3527			
22	ig	1.169	0.1587	0.3541			
22	ig	1.11	0.1109	0.3575			
22	ig	1.153	-0.03746	0.3584	0.3584	0.3408	

23	p	1.169	0.1587	0.3541			
23	p	1.203	0.09021	0.3546			
23	p	1.11	0.1109	0.3575			
23	p	1.153	-0.03746	0.3584	0.3584	0.3562	

23	ig	1.203	0.1587	0.3522			
23	ig	1.203	0.1109	0.354			
23	ig	1.153	0.1587	0.3548			
23	ig	1.11	0.1587	0.3554			
23	ig	1.203	-0.03746	0.3556			
23	ig	1.169	0.1109	0.3561			
23	ig	1.169	0.09021	0.3567			
23	ig	1.153	0.1109	0.3567			
23	ig	1.153	0.09021	0.3574			
23	ig	1.169	-0.03746	0.3577			
23	ig	1.11	0.09021	0.3581			
23	ig	1.11	-0.03746	0.3592	0.3592	0.3562	

24	p	1.169	-0.03746	0.3577			
24	p	1.11	0.09021	0.3581			
24	p	1.153	-0.03746	0.3584			
24	p	1.11	-0.03746	0.3592	0.3592	0.3584	

24	ig	1.169	0.09021	0.3567			
24	ig	1.153	0.09021	0.3574			
24	ig	1.169	-0.03746	0.3577			
24	ig	1.169	-0.03746	0.3577			
24	ig	1.11	0.09021	0.3581			
24	ig	1.153	-0.03746	0.3584			
24	ig	1.153	-0.03746	0.3584			
24	ig	1.11	-0.03746	0.3592			
24	ig	1.11	-0.03746	0.3592			
24	ig	1.11	-0.03746	0.3592			
24	ig	1.11	-0.03746	0.3592			
24	ig	1.11	-0.03746	0.3592	0.3592	0.3584	

25	p	1.11	-0.03746	0.3592			
25	p	1.11	-0.03746	0.3592			
25	p	1.11	-0.03746	0.3592			
25	p	1.11	-0.03746	0.3592	0.3592	0.3592	

25	ig	1.11	-0.03746	0.3592			
25	ig	1.11	-0.03746	0.3592			
25	ig	1.11	-0.03746	0.3592			
25	ig	1.11	-0.03746	0.3592			
25	ig	1.11	-0.03746	0.3592			
25	ig	1.11	-0.03746	0.3592			
25	ig	1.11	-0.03746	0.3592			
25	ig	1.11	-0.03746	0.3592			
25	ig	1.11	-0.03746	0.3592			

25	ig	1.11	-0.03746	0.3592		
25	ig	1.11	-0.03746	0.3592		
25	ig	1.11	-0.03746	0.3592	0.3592	0.3592

26	p	1.11	-0.03746	0.3592		
26	p	1.11	-0.03746	0.3592		
26	p	1.11	-0.03746	0.3592		
26	p	1.11	-0.03746	0.3592	0.3592	0.3592

26	ig	1.11	-0.03746	0.3592		
26	ig	1.11	-0.03746	0.3592		
26	ig	1.11	-0.03746	0.3592		
26	ig	1.11	-0.03746	0.3592		
26	ig	1.11	-0.03746	0.3592		
26	ig	1.11	-0.03746	0.3592		
26	ig	1.11	-0.03746	0.3592		
26	ig	1.11	-0.03746	0.3592		
26	ig	1.11	-0.03746	0.3592		
26	ig	1.11	-0.03746	0.3592		
26	ig	1.11	-0.03746	0.3592	0.3592	0.3592

27	p	1.11	-0.03746	0.3592		
27	p	1.11	-0.03746	0.3592		
27	p	1.11	-0.03746	0.3592		
27	p	1.11	-0.03746	0.3592	0.3592	0.3592

27	ig	1.11	-0.03746	0.3592		
27	ig	1.11	-0.03746	0.3592		
27	ig	1.11	-0.03746	0.3592		
27	ig	1.11	-0.03746	0.3592		
27	ig	1.11	-0.03746	0.3592		
27	ig	1.11	-0.03746	0.3592		
27	ig	1.11	-0.03746	0.3592		
27	ig	1.11	-0.03746	0.3592		
27	ig	1.11	-0.03746	0.3592		
27	ig	1.11	-0.03746	0.3592		
27	ig	1.11	-0.03746	0.3592		
27	ig	1.11	-0.03746	0.3592	0.3592	0.3592

28	p	1.11	-0.03746	0.3592		
28	p	1.11	-0.03746	0.3592		
28	p	1.11	-0.03746	0.3592		
28	p	1.11	-0.03746	0.3592	0.3592	0.3592

28	ig	1.11	-0.03746	0.3592		
28	ig	1.11	-0.03746	0.3592		
28	ig	1.11	-0.03746	0.3592		
28	ig	1.11	-0.03746	0.3592		
28	ig	1.11	-0.03746	0.3592		
28	ig	1.11	-0.03746	0.3592		
28	ig	1.11	-0.03746	0.3592		
28	ig	1.11	-0.03746	0.3592		
28	ig	1.11	-0.03746	0.3592		
28	ig	1.11	-0.03746	0.3592		
28	ig	1.11	-0.03746	0.3592		
28	ig	1.11	-0.03746	0.3592	0.3592	0.3592

29	p	1.11	-0.03746	0.3592		

	29		p		1.11		-0.03746		0.3592					
	29		p		1.11		-0.03746		0.3592					
	29		p		1.11		-0.03746		0.3592		0.3592		0.3592	

	29		ig		1.11		-0.03746		0.3592					
	29		ig		1.11		-0.03746		0.3592					
	29		ig		1.11		-0.03746		0.3592					
	29		ig		1.11		-0.03746		0.3592					
	29		ig		1.11		-0.03746		0.3592					
	29		ig		1.11		-0.03746		0.3592					
	29		ig		1.11		-0.03746		0.3592					
	29		ig		1.11		-0.03746		0.3592					
	29		ig		1.11		-0.03746		0.3592					
	29		ig		1.11		-0.03746		0.3592					
	29		ig		1.11		-0.03746		0.3592		0.3592		0.3592	

	30		p		0.8837		-0.2737		0.322					
	30		p		0.8537		0.09882		0.3268					
	30		p		1.253		-0.08731		0.3501					
	30		p		1.206		-0.1019		0.3541		0.3541		0.3382	

	30		ig		0.8248		-0.07941		0.3198					
	30		ig		0.8459		0.07566		0.3256					
	30		ig		0.8962		0.2599		0.326					
	30		ig		1.401		-0.03646		0.3277					
	30		ig		0.9161		0.2483		0.331					
	30		ig		1.362		0.1316		0.3332					
	30		ig		1.328		-0.2447		0.3337					
	30		ig		1.19		-0.2904		0.3447					
	30		ig		1.29		-0.004256		0.3466					
	30		ig		1.257		0.1736		0.3466					
	30		ig		1.157		0.1034		0.3568					
	30		ig		1.174		-0.01883		0.3576		0.3576		0.3374	

	31		p		1.253		-0.08731		0.3501					
	31		p		1.206		-0.1019		0.3541					
	31		p		1.157		0.1034		0.3568					
	31		p		1.174		-0.01883		0.3576		0.3576		0.3547	

	31		ig		1.253		0.1034		0.3497					
	31		ig		1.253		-0.1019		0.3497					
	31		ig		1.253		-0.01883		0.3511					
	31		ig		1.206		0.1034		0.3541					
	31		ig		1.206		-0.08731		0.3545					
	31		ig		1.206		-0.01883		0.3556					
	31		ig		1.174		0.1034		0.3561					
	31		ig		1.174		-0.1019		0.3561					
	31		ig		1.174		-0.08731		0.3565					
	31		ig		1.157		-0.1019		0.3569					
	31		ig		1.157		-0.08731		0.3573					
	31		ig		1.157		-0.01883		0.3584		0.3584		0.3547	

	32		p		1.157		-0.1019		0.3569					
	32		p		1.157		-0.08731		0.3573					
	32		p		1.174		-0.01883		0.3576					
	32		p		1.157		-0.01883		0.3584		0.3584		0.3576	

	32		ig		1.174		-0.1019		0.3561					
	32		ig		1.174		-0.08731		0.3565					

35	ig	1.157	-0.01883	0.3584		
35	ig	1.157	-0.01883	0.3584		
35	ig	1.157	-0.01883	0.3584	0.3584	0.3584

36	p	1.157	-0.01883	0.3584		
36	p	1.157	-0.01883	0.3584		
36	p	1.157	-0.01883	0.3584		
36	p	1.157	-0.01883	0.3584	0.3584	0.3584

36	ig	1.157	-0.01883	0.3584		
36	ig	1.157	-0.01883	0.3584		
36	ig	1.157	-0.01883	0.3584		
36	ig	1.157	-0.01883	0.3584		
36	ig	1.157	-0.01883	0.3584		
36	ig	1.157	-0.01883	0.3584		
36	ig	1.157	-0.01883	0.3584		
36	ig	1.157	-0.01883	0.3584		
36	ig	1.157	-0.01883	0.3584		
36	ig	1.157	-0.01883	0.3584		
36	ig	1.157	-0.01883	0.3584		
36	ig	1.157	-0.01883	0.3584	0.3584	0.3584

37	p	1.157	-0.01883	0.3584		
37	p	1.157	-0.01883	0.3584		
37	p	1.157	-0.01883	0.3584		
37	p	1.157	-0.01883	0.3584	0.3584	0.3584

37	ig	1.157	-0.01883	0.3584		
37	ig	1.157	-0.01883	0.3584		
37	ig	1.157	-0.01883	0.3584		
37	ig	1.157	-0.01883	0.3584		
37	ig	1.157	-0.01883	0.3584		
37	ig	1.157	-0.01883	0.3584		
37	ig	1.157	-0.01883	0.3584		
37	ig	1.157	-0.01883	0.3584		
37	ig	1.157	-0.01883	0.3584		
37	ig	1.157	-0.01883	0.3584		
37	ig	1.157	-0.01883	0.3584		
37	ig	1.157	-0.01883	0.3584	0.3584	0.3584

38	p	1.157	-0.01883	0.3584		
38	p	1.157	-0.01883	0.3584		
38	p	1.157	-0.01883	0.3584		
38	p	1.157	-0.01883	0.3584	0.3584	0.3584

38	ig	1.157	-0.01883	0.3584		
38	ig	1.157	-0.01883	0.3584		
38	ig	1.157	-0.01883	0.3584		
38	ig	1.157	-0.01883	0.3584		
38	ig	1.157	-0.01883	0.3584		
38	ig	1.157	-0.01883	0.3584		
38	ig	1.157	-0.01883	0.3584		
38	ig	1.157	-0.01883	0.3584		
38	ig	1.157	-0.01883	0.3584		
38	ig	1.157	-0.01883	0.3584		
38	ig	1.157	-0.01883	0.3584		
38	ig	1.157	-0.01883	0.3584	0.3584	0.3584

39	p	1.157	-0.01883	0.3584		

	39		p		1.157		-0.01883		0.3584				
	39		p		1.157		-0.01883		0.3584				
	39		p		1.157		-0.01883		0.3584		0.3584		0.3584

	39		ig		1.157		-0.01883		0.3584				
	39		ig		1.157		-0.01883		0.3584				
	39		ig		1.157		-0.01883		0.3584				
	39		ig		1.157		-0.01883		0.3584				
	39		ig		1.157		-0.01883		0.3584				
	39		ig		1.157		-0.01883		0.3584				
	39		ig		1.157		-0.01883		0.3584				
	39		ig		1.157		-0.01883		0.3584				
	39		ig		1.157		-0.01883		0.3584				
	39		ig		1.157		-0.01883		0.3584				
	39		ig		1.157		-0.01883		0.3584		0.3584		0.3584

	40		p		1.327		-0.115		0.3394				
	40		p		1.23		0.1582		0.35				
	40		p		1.121		0.2042		0.3528				
	40		p		1.191		-0.04289		0.3564		0.3564		0.3497

	40		ig		1.402		-0.2806		0.3191				
	40		ig		1.41		0.08513		0.3252				
	40		ig		0.8953		0.2481		0.3269				
	40		ig		0.8597		0.03431		0.3299				
	40		ig		1.357		-0.08288		0.3354				
	40		ig		0.9937		0.2356		0.3438				
	40		ig		0.9722		0.06636		0.3501				
	40		ig		1.134		-0.2435		0.3501				
	40		ig		0.9857		0.1141		0.3502				
	40		ig		1.247		-0.1055		0.3502				
	40		ig		1.003		0.01384		0.3543				
	40		ig		1.207		-0.03463		0.3553		0.3553		0.3409

	41		p		1.121		0.2042		0.3528				
	41		p		1.003		0.01384		0.3543				
	41		p		1.207		-0.03463		0.3553				
	41		p		1.191		-0.04289		0.3564		0.3564		0.3547

	41		ig		1.003		0.2042		0.3471				
	41		ig		1.207		0.2042		0.3495				
	41		ig		1.191		0.2042		0.3506				
	41		ig		1.003		-0.04289		0.354				
	41		ig		1.003		-0.03463		0.3541				
	41		ig		1.207		-0.04289		0.3552				
	41		ig		1.207		0.01384		0.3554				
	41		ig		1.191		-0.03463		0.3565				
	41		ig		1.191		0.01384		0.3566				
	41		ig		1.121		-0.04289		0.3591				
	41		ig		1.121		-0.03463		0.3592				
	41		ig		1.121		0.01384		0.3593		0.3593		0.3547

	42		p		1.191		0.01384		0.3566				
	42		p		1.121		-0.04289		0.3591				
	42		p		1.121		-0.03463		0.3592				
	42		p		1.121		0.01384		0.3593		0.3593		0.3586

	42		ig		1.191		-0.04289		0.3564				
	42		ig		1.191		-0.03463		0.3565				

[illegible]

49	p	1.121	0.01384	0.3593		
49	p	1.121	0.01384	0.3593		
49	p	1.121	0.01384	0.3593	0.3593	0.3593
49	ig	1.121	0.01384	0.3593		
49	ig	1.121	0.01384	0.3593		
49	ig	1.121	0.01384	0.3593		
49	ig	1.121	0.01384	0.3593		
49	ig	1.121	0.01384	0.3593		
49	ig	1.121	0.01384	0.3593		
49	ig	1.121	0.01384	0.3593		
49	ig	1.121	0.01384	0.3593		
49	ig	1.121	0.01384	0.3593		
49	ig	1.121	0.01384	0.3593		
49	ig	1.121	0.01384	0.3593	0.3593	0.3593
50	p	1.121	0.01384	0.3593		
50	p	1.121	0.01384	0.3593		
50	p	1.121	0.01384	0.3593		
50	p	1.121	0.01384	0.3593	0.3593	0.3593
50	ig	1.121	0.01384	0.3593		
50	ig	1.121	0.01384	0.3593		
50	ig	1.121	0.01384	0.3593		
50	ig	1.121	0.01384	0.3593		
50	ig	1.121	0.01384	0.3593		
50	ig	1.121	0.01384	0.3593		
50	ig	1.121	0.01384	0.3593		
50	ig	1.121	0.01384	0.3593		
50	ig	1.121	0.01384	0.3593		
50	ig	1.121	0.01384	0.3593		
50	ig	1.121	0.01384	0.3593	0.3593	0.3593
51	p	0.8859	0.2745	0.3225		
51	p	1.348	-0.1815	0.3338		
51	p	0.8975	-0.126	0.3356		
51	p	1.17	0.07722	0.357	0.357	0.3372
51	ig	1.378	0.2998	0.3223		
51	ig	1.395	-0.137	0.327		
51	ig	0.9798	0.2878	0.3375		
51	ig	1.22	-0.2815	0.3435		
51	ig	1.306	-0.03513	0.3441		
51	ig	1.296	0.08919	0.3446		
51	ig	1.242	0.2213	0.3456		
51	ig	1.01	-0.2201	0.3466		
51	ig	1.24	0.1364	0.35		
51	ig	1.212	-0.04924	0.3548		
51	ig	1.049	-0.1271	0.3551		
51	ig	1.094	-0.124	0.3568	0.3568	0.344
52	p	1.212	-0.04924	0.3548		
52	p	1.049	-0.1271	0.3551		
52	p	1.094	-0.124	0.3568		
52	p	1.17	0.07722	0.357	0.357	0.3559
52	ig	1.212	-0.1271	0.3528		
52	ig	1.212	-0.124	0.3529		

	52		ig		1.212		0.07722		0.3543			
	52		ig		1.049		-0.124		0.3552			
	52		ig		1.17		-0.1271		0.3554			
	52		ig		1.17		-0.124		0.3556			
	52		ig		1.094		-0.1271		0.3567			
	52		ig		1.049		0.07722		0.3568			
	52		ig		1.049		-0.04924		0.3574			
	52		ig		1.17		-0.04924		0.3575			
	52		ig		1.094		0.07722		0.3584			
	52		ig		1.094		-0.04924		0.3589		0.3589	0.356

	53		p		1.049		-0.04924		0.3574			
	53		p		1.17		-0.04924		0.3575			
	53		p		1.094		0.07722		0.3584			
	53		p		1.094		-0.04924		0.3589		0.3589	0.358

	53		ig		1.049		0.07722		0.3568			
	53		ig		1.17		0.07722		0.357			
	53		ig		1.049		-0.04924		0.3574			
	53		ig		1.049		-0.04924		0.3574			
	53		ig		1.17		-0.04924		0.3575			
	53		ig		1.17		-0.04924		0.3575			
	53		ig		1.094		0.07722		0.3584			
	53		ig		1.094		-0.04924		0.3589			
	53		ig		1.094		-0.04924		0.3589			
	53		ig		1.094		-0.04924		0.3589			
	53		ig		1.094		-0.04924		0.3589		0.3589	0.358

	54		p		1.094		-0.04924		0.3589			
	54		p		1.094		-0.04924		0.3589			
	54		p		1.094		-0.04924		0.3589			
	54		p		1.094		-0.04924		0.3589		0.3589	0.3589

	54		ig		1.094		-0.04924		0.3589			
	54		ig		1.094		-0.04924		0.3589			
	54		ig		1.094		-0.04924		0.3589			
	54		ig		1.094		-0.04924		0.3589			
	54		ig		1.094		-0.04924		0.3589			
	54		ig		1.094		-0.04924		0.3589			
	54		ig		1.094		-0.04924		0.3589			
	54		ig		1.094		-0.04924		0.3589			
	54		ig		1.094		-0.04924		0.3589			
	54		ig		1.094		-0.04924		0.3589		0.3589	0.3589

	55		p		1.094		-0.04924		0.3589			
	55		p		1.094		-0.04924		0.3589			
	55		p		1.094		-0.04924		0.3589			
	55		p		1.094		-0.04924		0.3589		0.3589	0.3589

	55		ig		1.094		-0.04924		0.3589			
	55		ig		1.094		-0.04924		0.3589			
	55		ig		1.094		-0.04924		0.3589			
	55		ig		1.094		-0.04924		0.3589			
	55		ig		1.094		-0.04924		0.3589			
	55		ig		1.094		-0.04924		0.3589			
	55		ig		1.094		-0.04924		0.3589			
	55		ig		1.094		-0.04924		0.3589			
	55		ig		1.094		-0.04924		0.3589			

55	ig	1.094	-0.04924	0.3589		
55	ig	1.094	-0.04924	0.3589		
55	ig	1.094	-0.04924	0.3589	0.3589	0.3589
56	p	1.094	-0.04924	0.3589		
56	p	1.094	-0.04924	0.3589		
56	p	1.094	-0.04924	0.3589		
56	p	1.094	-0.04924	0.3589	0.3589	0.3589
56	ig	1.094	-0.04924	0.3589		
56	ig	1.094	-0.04924	0.3589		
56	ig	1.094	-0.04924	0.3589		
56	ig	1.094	-0.04924	0.3589		
56	ig	1.094	-0.04924	0.3589		
56	ig	1.094	-0.04924	0.3589		
56	ig	1.094	-0.04924	0.3589		
56	ig	1.094	-0.04924	0.3589		
56	ig	1.094	-0.04924	0.3589		
56	ig	1.094	-0.04924	0.3589		
56	ig	1.094	-0.04924	0.3589	0.3589	0.3589
57	p	1.094	-0.04924	0.3589		
57	p	1.094	-0.04924	0.3589		
57	p	1.094	-0.04924	0.3589		
57	p	1.094	-0.04924	0.3589	0.3589	0.3589
57	ig	1.094	-0.04924	0.3589		
57	ig	1.094	-0.04924	0.3589		
57	ig	1.094	-0.04924	0.3589		
57	ig	1.094	-0.04924	0.3589		
57	ig	1.094	-0.04924	0.3589		
57	ig	1.094	-0.04924	0.3589		
57	ig	1.094	-0.04924	0.3589		
57	ig	1.094	-0.04924	0.3589		
57	ig	1.094	-0.04924	0.3589		
57	ig	1.094	-0.04924	0.3589		
57	ig	1.094	-0.04924	0.3589		
57	ig	1.094	-0.04924	0.3589	0.3589	0.3589
58	p	1.094	-0.04924	0.3589		
58	p	1.094	-0.04924	0.3589		
58	p	1.094	-0.04924	0.3589		
58	p	1.094	-0.04924	0.3589	0.3589	0.3589
58	ig	1.094	-0.04924	0.3589		
58	ig	1.094	-0.04924	0.3589		
58	ig	1.094	-0.04924	0.3589		
58	ig	1.094	-0.04924	0.3589		
58	ig	1.094	-0.04924	0.3589		
58	ig	1.094	-0.04924	0.3589		
58	ig	1.094	-0.04924	0.3589		
58	ig	1.094	-0.04924	0.3589		
58	ig	1.094	-0.04924	0.3589		
58	ig	1.094	-0.04924	0.3589		
58	ig	1.094	-0.04924	0.3589		
58	ig	1.094	-0.04924	0.3589	0.3589	0.3589
59	p	1.094	-0.04924	0.3589		

59	p	1.094	-0.04924	0.3589		
59	p	1.094	-0.04924	0.3589		
59	p	1.094	-0.04924	0.3589	0.3589	0.3589
59	ig	1.094	-0.04924	0.3589		
59	ig	1.094	-0.04924	0.3589		
59	ig	1.094	-0.04924	0.3589		
59	ig	1.094	-0.04924	0.3589		
59	ig	1.094	-0.04924	0.3589		
59	ig	1.094	-0.04924	0.3589		
59	ig	1.094	-0.04924	0.3589		
59	ig	1.094	-0.04924	0.3589		
59	ig	1.094	-0.04924	0.3589		
59	ig	1.094	-0.04924	0.3589		
59	ig	1.094	-0.04924	0.3589	0.3589	0.3589
60	p	1.094	-0.04924	0.3589		
60	p	1.094	-0.04924	0.3589		
60	p	1.094	-0.04924	0.3589		
60	p	1.094	-0.04924	0.3589	0.3589	0.3589
60	ig	1.094	-0.04924	0.3589		
60	ig	1.094	-0.04924	0.3589		
60	ig	1.094	-0.04924	0.3589		
60	ig	1.094	-0.04924	0.3589		
60	ig	1.094	-0.04924	0.3589		
60	ig	1.094	-0.04924	0.3589		
60	ig	1.094	-0.04924	0.3589		
60	ig	1.094	-0.04924	0.3589		
60	ig	1.094	-0.04924	0.3589		
60	ig	1.094	-0.04924	0.3589		
60	ig	1.094	-0.04924	0.3589		
60	ig	1.094	-0.04924	0.3589	0.3589	0.3589
61	p	1.094	-0.04924	0.3589		
61	p	1.094	-0.04924	0.3589		
61	p	1.094	-0.04924	0.3589		
61	p	1.094	-0.04924	0.3589	0.3589	0.3589
61	ig	1.094	-0.04924	0.3589		
61	ig	1.094	-0.04924	0.3589		
61	ig	1.094	-0.04924	0.3589		
61	ig	1.094	-0.04924	0.3589		
61	ig	1.094	-0.04924	0.3589		
61	ig	1.094	-0.04924	0.3589		
61	ig	1.094	-0.04924	0.3589		
61	ig	1.094	-0.04924	0.3589		
61	ig	1.094	-0.04924	0.3589		
61	ig	1.094	-0.04924	0.3589		
61	ig	1.094	-0.04924	0.3589		
61	ig	1.094	-0.04924	0.3589	0.3589	0.3589
62	p	1.094	-0.04924	0.3589		
62	p	1.094	-0.04924	0.3589		
62	p	1.094	-0.04924	0.3589		
62	p	1.094	-0.04924	0.3589	0.3589	0.3589
62	ig	1.094	-0.04924	0.3589		
62	ig	1.094	-0.04924	0.3589		

	62		ig		1.094		-0.04924		0.3589			
	62		ig		1.094		-0.04924		0.3589			
	62		ig		1.094		-0.04924		0.3589			
	62		ig		1.094		-0.04924		0.3589			
	62		ig		1.094		-0.04924		0.3589			
	62		ig		1.094		-0.04924		0.3589			
	62		ig		1.094		-0.04924		0.3589			
	62		ig		1.094		-0.04924		0.3589			
	62		ig		1.094		-0.04924		0.3589			
	62		ig		1.094		-0.04924		0.3589		0.3589	0.3589

	63		p		0.8117		-0.1273		0.3142			
	63		p		0.8567		-0.0657		0.3285			
	63		p		1.014		-0.3378		0.3365			
	63		p		1.045		-0.268		0.3457		0.3457	0.3312

	63		ig		0.8726		-0.2805		0.3189			
	63		ig		1.381		-0.2719		0.3235			
	63		ig		0.8909		-0.1626		0.3322			
	63		ig		1.282		-0.3409		0.3329			
	63		ig		1.285		-0.2988		0.3359			
	63		ig		0.9557		-0.1749		0.3431			
	63		ig		1.244		0.164		0.3484			
	63		ig		1.258		-0.04802		0.3502			
	63		ig		1.236		0.07917		0.352			
	63		ig		1.061		-0.1902		0.3524			
	63		ig		1.207		-0.1033		0.3539			
	63		ig		1.125		0.08361		0.3582		0.3582	0.3418

	64		p		1.236		0.07917		0.352			
	64		p		1.061		-0.1902		0.3524			
	64		p		1.207		-0.1033		0.3539			
	64		p		1.125		0.08361		0.3582		0.3582	0.3541

	64		ig		1.236		-0.1902		0.3479			
	64		ig		1.207		-0.1902		0.3503			
	64		ig		1.236		-0.1033		0.3514			
	64		ig		1.236		0.08361		0.3519			
	64		ig		1.125		-0.1902		0.3537			
	64		ig		1.207		0.08361		0.3545			
	64		ig		1.207		0.07917		0.3546			
	64		ig		1.061		-0.1033		0.3566			
	64		ig		1.061		0.08361		0.3572			
	64		ig		1.061		0.07917		0.3574			
	64		ig		1.125		-0.1033		0.3576			
	64		ig		1.125		0.07917		0.3583		0.3583	0.3543

	65		p		1.061		0.07917		0.3574			
	65		p		1.125		-0.1033		0.3576			
	65		p		1.125		0.08361		0.3582			
	65		p		1.125		0.07917		0.3583		0.3583	0.3579

	65		ig		1.061		-0.1033		0.3566			
	65		ig		1.061		0.08361		0.3572			
	65		ig		1.061		0.07917		0.3574			
	65		ig		1.125		-0.1033		0.3576			
	65		ig		1.125		-0.1033		0.3576			
	65		ig		1.125		0.08361		0.3582			
	65		ig		1.125		0.08361		0.3582			
	65		ig		1.125		0.07917		0.3583			
	65		ig		1.125		0.07917		0.3583			

65	ig	1.125	0.07917	0.3583		
65	ig	1.125	0.07917	0.3583		
65	ig	1.125	0.07917	0.3583	0.3583	0.3579
66	p	1.125	0.07917	0.3583		
66	p	1.125	0.07917	0.3583		
66	p	1.125	0.07917	0.3583		
66	p	1.125	0.07917	0.3583	0.3583	0.3583
66	ig	1.125	0.07917	0.3583		
66	ig	1.125	0.07917	0.3583		
66	ig	1.125	0.07917	0.3583		
66	ig	1.125	0.07917	0.3583		
66	ig	1.125	0.07917	0.3583		
66	ig	1.125	0.07917	0.3583		
66	ig	1.125	0.07917	0.3583		
66	ig	1.125	0.07917	0.3583		
66	ig	1.125	0.07917	0.3583		
66	ig	1.125	0.07917	0.3583		
66	ig	1.125	0.07917	0.3583	0.3583	0.3583
67	p	1.125	0.07917	0.3583		
67	p	1.125	0.07917	0.3583		
67	p	1.125	0.07917	0.3583		
67	p	1.125	0.07917	0.3583	0.3583	0.3583
67	ig	1.125	0.07917	0.3583		
67	ig	1.125	0.07917	0.3583		
67	ig	1.125	0.07917	0.3583		
67	ig	1.125	0.07917	0.3583		
67	ig	1.125	0.07917	0.3583		
67	ig	1.125	0.07917	0.3583		
67	ig	1.125	0.07917	0.3583		
67	ig	1.125	0.07917	0.3583		
67	ig	1.125	0.07917	0.3583		
67	ig	1.125	0.07917	0.3583		
67	ig	1.125	0.07917	0.3583		
67	ig	1.125	0.07917	0.3583	0.3583	0.3583
68	p	1.125	0.07917	0.3583		
68	p	1.125	0.07917	0.3583		
68	p	1.125	0.07917	0.3583		
68	p	1.125	0.07917	0.3583	0.3583	0.3583
68	ig	1.125	0.07917	0.3583		
68	ig	1.125	0.07917	0.3583		
68	ig	1.125	0.07917	0.3583		
68	ig	1.125	0.07917	0.3583		
68	ig	1.125	0.07917	0.3583		
68	ig	1.125	0.07917	0.3583		
68	ig	1.125	0.07917	0.3583		
68	ig	1.125	0.07917	0.3583		
68	ig	1.125	0.07917	0.3583		
68	ig	1.125	0.07917	0.3583		
68	ig	1.125	0.07917	0.3583		
68	ig	1.125	0.07917	0.3583	0.3583	0.3583
69	p	1.125	0.07917	0.3583		

69	p	1.125	0.07917	0.3583		
69	p	1.125	0.07917	0.3583		
69	p	1.125	0.07917	0.3583	0.3583	0.3583
69	ig	1.125	0.07917	0.3583		
69	ig	1.125	0.07917	0.3583		
69	ig	1.125	0.07917	0.3583		
69	ig	1.125	0.07917	0.3583		
69	ig	1.125	0.07917	0.3583		
69	ig	1.125	0.07917	0.3583		
69	ig	1.125	0.07917	0.3583		
69	ig	1.125	0.07917	0.3583		
69	ig	1.125	0.07917	0.3583		
69	ig	1.125	0.07917	0.3583		
69	ig	1.125	0.07917	0.3583	0.3583	0.3583
69	ig	1.125	0.07917	0.3583		
70	p	1.125	0.07917	0.3583		
70	p	1.125	0.07917	0.3583		
70	p	1.125	0.07917	0.3583		
70	p	1.125	0.07917	0.3583	0.3583	0.3583
70	ig	1.125	0.07917	0.3583		
70	ig	1.125	0.07917	0.3583		
70	ig	1.125	0.07917	0.3583		
70	ig	1.125	0.07917	0.3583		
70	ig	1.125	0.07917	0.3583		
70	ig	1.125	0.07917	0.3583		
70	ig	1.125	0.07917	0.3583		
70	ig	1.125	0.07917	0.3583		
70	ig	1.125	0.07917	0.3583		
70	ig	1.125	0.07917	0.3583		
70	ig	1.125	0.07917	0.3583		
70	ig	1.125	0.07917	0.3583	0.3583	0.3583
70	ig	1.125	0.07917	0.3583		
71	p	1.125	0.07917	0.3583		
71	p	1.125	0.07917	0.3583		
71	p	1.125	0.07917	0.3583		
71	p	1.125	0.07917	0.3583	0.3583	0.3583
71	ig	1.125	0.07917	0.3583		
71	ig	1.125	0.07917	0.3583		
71	ig	1.125	0.07917	0.3583		
71	ig	1.125	0.07917	0.3583		
71	ig	1.125	0.07917	0.3583		
71	ig	1.125	0.07917	0.3583		
71	ig	1.125	0.07917	0.3583		
71	ig	1.125	0.07917	0.3583		
71	ig	1.125	0.07917	0.3583		
71	ig	1.125	0.07917	0.3583		
71	ig	1.125	0.07917	0.3583		
71	ig	1.125	0.07917	0.3583	0.3583	0.3583
71	ig	1.125	0.07917	0.3583		
72	p	0.8414	0.267	0.3124		
72	p	0.9691	-0.08189	0.3493		
72	p	1.229	-0.08949	0.3524		
72	p	1.181	-0.118	0.3552	0.3552	0.3423
72	ig	0.833	-0.1129	0.3208		
72	ig	0.8533	-0.04678	0.3281		

	72		ig		1.375		-0.159		0.33			
	72		ig		1.334		-0.1768		0.3362			
	72		ig		0.9594		0.183		0.3432			
	72		ig		0.9897		-0.2185		0.3446			
	72		ig		0.9549		-0.1358		0.3452			
	72		ig		1.129		0.2178		0.3519			
	72		ig		1.023		0.09588		0.3545			
	72		ig		1.181		-0.135		0.3546			
	72		ig		1.026		-0.03101		0.3561			
	72		ig		1.114		-0.01244		0.3594		0.3594	0.3437

	73		p		1.181		-0.135		0.3546			
	73		p		1.181		-0.118		0.3552			
	73		p		1.026		-0.03101		0.3561			
	73		p		1.114		-0.01244		0.3594		0.3594	0.3563

	73		ig		1.026		-0.135		0.3532			
	73		ig		1.026		-0.118		0.3539			
	73		ig		1.181		-0.135		0.3546			
	73		ig		1.181		-0.118		0.3552			
	73		ig		1.026		-0.01244		0.3563			
	73		ig		1.114		-0.135		0.3565			
	73		ig		1.181		-0.03101		0.3571			
	73		ig		1.181		-0.03101		0.3571			
	73		ig		1.114		-0.118		0.3572			
	73		ig		1.181		-0.01244		0.3572			
	73		ig		1.181		-0.01244		0.3572			
	73		ig		1.114		-0.03101		0.3593		0.3593	0.3562

	74		p		1.181		-0.01244		0.3572			
	74		p		1.181		-0.01244		0.3572			
	74		p		1.114		-0.03101		0.3593			
	74		p		1.114		-0.01244		0.3594		0.3594	0.3583

	74		ig		1.181		-0.03101		0.3571			
	74		ig		1.181		-0.03101		0.3571			
	74		ig		1.181		-0.01244		0.3572			
	74		ig		1.181		-0.01244		0.3572			
	74		ig		1.181		-0.01244		0.3572			
	74		ig		1.181		-0.01244		0.3572			
	74		ig		1.114		-0.03101		0.3593			
	74		ig		1.114		-0.01244		0.3594			
	74		ig		1.114		-0.01244		0.3594			
	74		ig		1.114		-0.01244		0.3594			
	74		ig		1.114		-0.01244		0.3594			
	74		ig		1.114		-0.01244		0.3594		0.3594	0.3583

	75		p		1.114		-0.01244		0.3594			
	75		p		1.114		-0.01244		0.3594			
	75		p		1.114		-0.01244		0.3594			
	75		p		1.114		-0.01244		0.3594		0.3594	0.3594

	75		ig		1.114		-0.01244		0.3594			
	75		ig		1.114		-0.01244		0.3594			
	75		ig		1.114		-0.01244		0.3594			
	75		ig		1.114		-0.01244		0.3594			
	75		ig		1.114		-0.01244		0.3594			
	75		ig		1.114		-0.01244		0.3594			
	75		ig		1.114		-0.01244		0.3594			
	75		ig		1.114		-0.01244		0.3594			
	75		ig		1.114		-0.01244		0.3594			

	79		p		1.114		-0.01244		0.3594					
	79		p		1.114		-0.01244		0.3594					
	79		p		1.114		-0.01244		0.3594		0.3594		0.3594	

	79		ig		1.114		-0.01244		0.3594					
	79		ig		1.114		-0.01244		0.3594					
	79		ig		1.114		-0.01244		0.3594					
	79		ig		1.114		-0.01244		0.3594					
	79		ig		1.114		-0.01244		0.3594					
	79		ig		1.114		-0.01244		0.3594					
	79		ig		1.114		-0.01244		0.3594					
	79		ig		1.114		-0.01244		0.3594					
	79		ig		1.114		-0.01244		0.3594					
	79		ig		1.114		-0.01244		0.3594					
	79		ig		1.114		-0.01244		0.3594		0.3594		0.3594	

	80		p		1.114		-0.01244		0.3594					
	80		p		1.114		-0.01244		0.3594					
	80		p		1.114		-0.01244		0.3594					
	80		p		1.114		-0.01244		0.3594		0.3594		0.3594	

	80		ig		1.114		-0.01244		0.3594					
	80		ig		1.114		-0.01244		0.3594					
	80		ig		1.114		-0.01244		0.3594					
	80		ig		1.114		-0.01244		0.3594					
	80		ig		1.114		-0.01244		0.3594					
	80		ig		1.114		-0.01244		0.3594					
	80		ig		1.114		-0.01244		0.3594					
	80		ig		1.114		-0.01244		0.3594					
	80		ig		1.114		-0.01244		0.3594					
	80		ig		1.114		-0.01244		0.3594					
	80		ig		1.114		-0.01244		0.3594		0.3594		0.3594	

	81		p		1.329		-0.2285		0.3345					
	81		p		0.9956		-0.2684		0.3412					
	81		p		1.296		0.01628		0.3457					
	81		p		1.016		0.147		0.3518		0.3518		0.3433	

	81		ig		0.8289		0.1804		0.316					
	81		ig		0.8173		0.06417		0.3181					
	81		ig		0.9072		0.09116		0.3389					
	81		ig		0.9131		0.05738		0.3409					
	81		ig		0.9269		0.107		0.3419					
	81		ig		1.208		0.2332		0.3477					
	81		ig		1.261		-0.1137		0.3485					
	81		ig		0.9701		-0.03846		0.3503					
	81		ig		0.9886		-0.08807		0.3514					
	81		ig		1.198		-0.1319		0.3537					
	81		ig		1.124		0.09032		0.358					
	81		ig		1.094		-0.003841		0.3593		0.3593		0.3437	

	82		p		1.016		0.147		0.3518					
	82		p		1.198		-0.1319		0.3537					
	82		p		1.124		0.09032		0.358					
	82		p		1.094		-0.003841		0.3593		0.3593		0.3557	

	82		ig		1.016		-0.1319		0.3525					
	82		ig		1.198		0.147		0.3531					

82	ig	1.016	0.09032	0.3541			
82	ig	1.198	0.09032	0.355			
82	ig	1.016	-0.003841	0.3555			
82	ig	1.094	0.147	0.3558			
82	ig	1.124	0.147	0.3559			
82	ig	1.198	-0.003841	0.3562			
82	ig	1.094	-0.1319	0.3565			
82	ig	1.124	-0.1319	0.3566			
82	ig	1.094	0.09032	0.358			
82	ig	1.124	-0.003841	0.3593	0.3593	0.3557	

83	p	1.094	0.09032	0.358			
83	p	1.124	0.09032	0.358			
83	p	1.094	-0.003841	0.3593			
83	p	1.124	-0.003841	0.3593	0.3593	0.3587	

83	ig	1.094	0.09032	0.358			
83	ig	1.094	0.09032	0.358			
83	ig	1.094	0.09032	0.358			
83	ig	1.124	0.09032	0.358			
83	ig	1.124	0.09032	0.358			
83	ig	1.124	0.09032	0.358			
83	ig	1.094	-0.003841	0.3593			
83	ig	1.094	-0.003841	0.3593			
83	ig	1.094	-0.003841	0.3593			
83	ig	1.124	-0.003841	0.3593			
83	ig	1.124	-0.003841	0.3593			
83	ig	1.124	-0.003841	0.3593	0.3593	0.3587	

84	p	1.124	-0.003841	0.3593			
84	p	1.124	-0.003841	0.3593			
84	p	1.124	-0.003841	0.3593			
84	p	1.124	-0.003841	0.3593	0.3593	0.3593	

84	ig	1.124	-0.003841	0.3593			
84	ig	1.124	-0.003841	0.3593			
84	ig	1.124	-0.003841	0.3593			
84	ig	1.124	-0.003841	0.3593			
84	ig	1.124	-0.003841	0.3593			
84	ig	1.124	-0.003841	0.3593			
84	ig	1.124	-0.003841	0.3593			
84	ig	1.124	-0.003841	0.3593			
84	ig	1.124	-0.003841	0.3593			
84	ig	1.124	-0.003841	0.3593			
84	ig	1.124	-0.003841	0.3593	0.3593	0.3593	

85	p	1.124	-0.003841	0.3593			
85	p	1.124	-0.003841	0.3593			
85	p	1.124	-0.003841	0.3593			
85	p	1.124	-0.003841	0.3593	0.3593	0.3593	

85	ig	1.124	-0.003841	0.3593			
85	ig	1.124	-0.003841	0.3593			
85	ig	1.124	-0.003841	0.3593			
85	ig	1.124	-0.003841	0.3593			
85	ig	1.124	-0.003841	0.3593			
85	ig	1.124	-0.003841	0.3593			
85	ig	1.124	-0.003841	0.3593			
85	ig	1.124	-0.003841	0.3593			
85	ig	1.124	-0.003841	0.3593			

	89		p		1.124		-0.003841		0.3593				
	89		p		1.124		-0.003841		0.3593				
	89		p		1.124		-0.003841		0.3593		0.3593		0.3593

	89		ig		1.124		-0.003841		0.3593				
	89		ig		1.124		-0.003841		0.3593				
	89		ig		1.124		-0.003841		0.3593				
	89		ig		1.124		-0.003841		0.3593				
	89		ig		1.124		-0.003841		0.3593				
	89		ig		1.124		-0.003841		0.3593				
	89		ig		1.124		-0.003841		0.3593				
	89		ig		1.124		-0.003841		0.3593				
	89		ig		1.124		-0.003841		0.3593				
	89		ig		1.124		-0.003841		0.3593				
	89		ig		1.124		-0.003841		0.3593		0.3593		0.3593

	90		p		1.124		-0.003841		0.3593				
	90		p		1.124		-0.003841		0.3593				
	90		p		1.124		-0.003841		0.3593				
	90		p		1.124		-0.003841		0.3593		0.3593		0.3593

	90		ig		1.124		-0.003841		0.3593				
	90		ig		1.124		-0.003841		0.3593				
	90		ig		1.124		-0.003841		0.3593				
	90		ig		1.124		-0.003841		0.3593				
	90		ig		1.124		-0.003841		0.3593				
	90		ig		1.124		-0.003841		0.3593				
	90		ig		1.124		-0.003841		0.3593				
	90		ig		1.124		-0.003841		0.3593				
	90		ig		1.124		-0.003841		0.3593				
	90		ig		1.124		-0.003841		0.3593				
	90		ig		1.124		-0.003841		0.3593				
	90		ig		1.124		-0.003841		0.3593		0.3593		0.3593

	91		p		1.124		-0.003841		0.3593				
	91		p		1.124		-0.003841		0.3593				
	91		p		1.124		-0.003841		0.3593				
	91		p		1.124		-0.003841		0.3593		0.3593		0.3593

	91		ig		1.124		-0.003841		0.3593				
	91		ig		1.124		-0.003841		0.3593				
	91		ig		1.124		-0.003841		0.3593				
	91		ig		1.124		-0.003841		0.3593				
	91		ig		1.124		-0.003841		0.3593				
	91		ig		1.124		-0.003841		0.3593				
	91		ig		1.124		-0.003841		0.3593				
	91		ig		1.124		-0.003841		0.3593				
	91		ig		1.124		-0.003841		0.3593				
	91		ig		1.124		-0.003841		0.3593				
	91		ig		1.124		-0.003841		0.3593				
	91		ig		1.124		-0.003841		0.3593		0.3593		0.3593

	92		p		1.397		0.1751		0.3254				
	92		p		1.383		0.06953		0.3307				
	92		p		1.179		-0.2905		0.3452				
	92		p		0.9736		-0.03464		0.3508		0.3508		0.338

	92		ig		1.416		-0.08996		0.3241				
	92		ig		1.385		-0.2114		0.326				

92	ig	0.8539	0.06848	0.3278			
92	ig	1.34	0.2622	0.3308			
92	ig	1.328	-0.2039	0.3359			
92	ig	1.296	0.1955	0.3408			
92	ig	0.9441	-0.107	0.3448			
92	ig	1.236	-0.223	0.3461			
92	ig	0.9681	0.1196	0.3478			
92	ig	1.262	-0.07811	0.3492			
92	ig	1.105	-0.1809	0.3542			
92	ig	1.181	-0.09039	0.3561	0.3561	0.3403	

93	p	1.262	-0.07811	0.3492			
93	p	0.9736	-0.03464	0.3508			
93	p	1.105	-0.1809	0.3542			
93	p	1.181	-0.09039	0.3561	0.3561	0.3526	

93	ig	0.9736	-0.1809	0.3452			
93	ig	1.262	-0.1809	0.3457			
93	ig	1.262	-0.09039	0.3489			
93	ig	0.9736	-0.09039	0.3496			
93	ig	1.262	-0.03464	0.3499			
93	ig	0.9736	-0.07811	0.3499			
93	ig	1.181	-0.1809	0.3525			
93	ig	1.181	-0.07811	0.3564			
93	ig	1.181	-0.03464	0.3571			
93	ig	1.105	-0.09039	0.3581			
93	ig	1.105	-0.07811	0.3584			
93	ig	1.105	-0.03464	0.3592	0.3592	0.3526	

94	p	1.181	-0.03464	0.3571			
94	p	1.105	-0.09039	0.3581			
94	p	1.105	-0.07811	0.3584			
94	p	1.105	-0.03464	0.3592	0.3592	0.3582	

94	ig	1.181	-0.09039	0.3561			
94	ig	1.181	-0.07811	0.3564			
94	ig	1.181	-0.03464	0.3571			
94	ig	1.105	-0.09039	0.3581			
94	ig	1.105	-0.09039	0.3581			
94	ig	1.105	-0.07811	0.3584			
94	ig	1.105	-0.07811	0.3584			
94	ig	1.105	-0.03464	0.3592			
94	ig	1.105	-0.03464	0.3592			
94	ig	1.105	-0.03464	0.3592			
94	ig	1.105	-0.03464	0.3592			
94	ig	1.105	-0.03464	0.3592	0.3592	0.3582	

95	p	1.105	-0.03464	0.3592			
95	p	1.105	-0.03464	0.3592			
95	p	1.105	-0.03464	0.3592			
95	p	1.105	-0.03464	0.3592	0.3592	0.3592	

95	ig	1.105	-0.03464	0.3592			
95	ig	1.105	-0.03464	0.3592			
95	ig	1.105	-0.03464	0.3592			
95	ig	1.105	-0.03464	0.3592			
95	ig	1.105	-0.03464	0.3592			
95	ig	1.105	-0.03464	0.3592			
95	ig	1.105	-0.03464	0.3592			
95	ig	1.105	-0.03464	0.3592			
95	ig	1.105	-0.03464	0.3592			

	99		p		1.105		-0.03464		0.3592					
	99		p		1.105		-0.03464		0.3592					
	99		p		1.105		-0.03464		0.3592		0.3592		0.3592	

	99		ig		1.105		-0.03464		0.3592					
	99		ig		1.105		-0.03464		0.3592					
	99		ig		1.105		-0.03464		0.3592					
	99		ig		1.105		-0.03464		0.3592					
	99		ig		1.105		-0.03464		0.3592					
	99		ig		1.105		-0.03464		0.3592					
	99		ig		1.105		-0.03464		0.3592					
	99		ig		1.105		-0.03464		0.3592					
	99		ig		1.105		-0.03464		0.3592					
	99		ig		1.105		-0.03464		0.3592					
	99		ig		1.105		-0.03464		0.3592					
	99		ig		1.105		-0.03464		0.3592		0.3592		0.3592	

	100		result		1.105		-0.03464		0.3592					
	100		result		1.105		-0.03464		0.3592					
	100		result		1.105		-0.03464		0.3592					
	100		result		1.105		-0.03464		0.3592		0.3592		0.3592	

Значение префиксов:

- 1) p – parent
- 2) ig – intermediate generation
- 3) result – результат

Код программы приведён в Приложении.

3. Графическая часть

1) Для 10 поколений

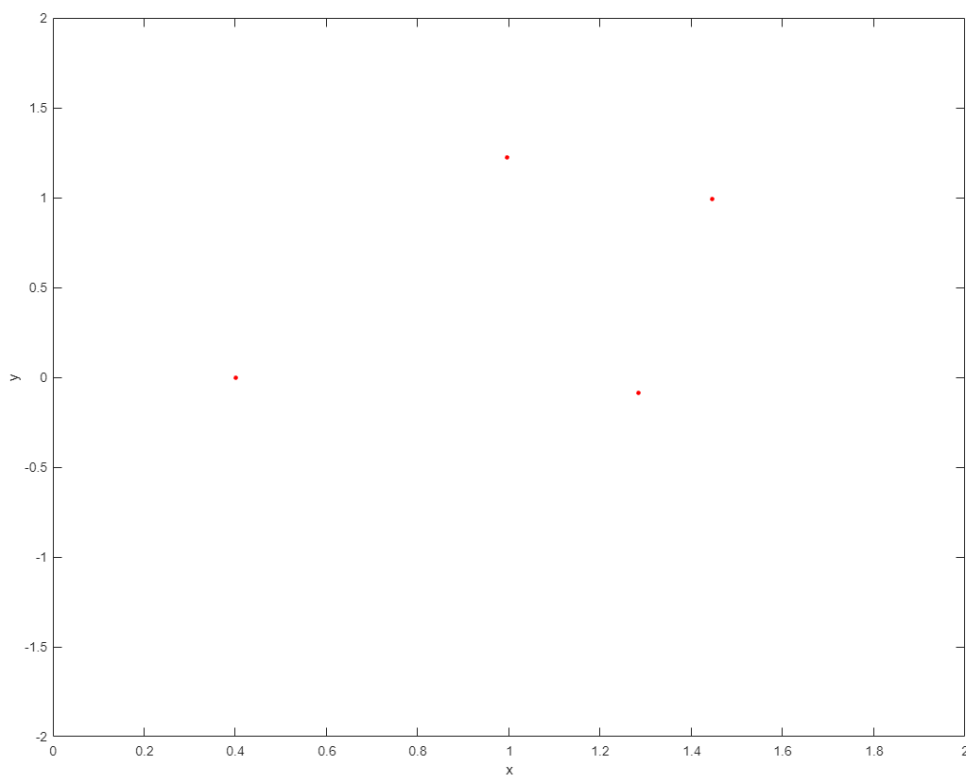


Рисунок 1 – поколение 0

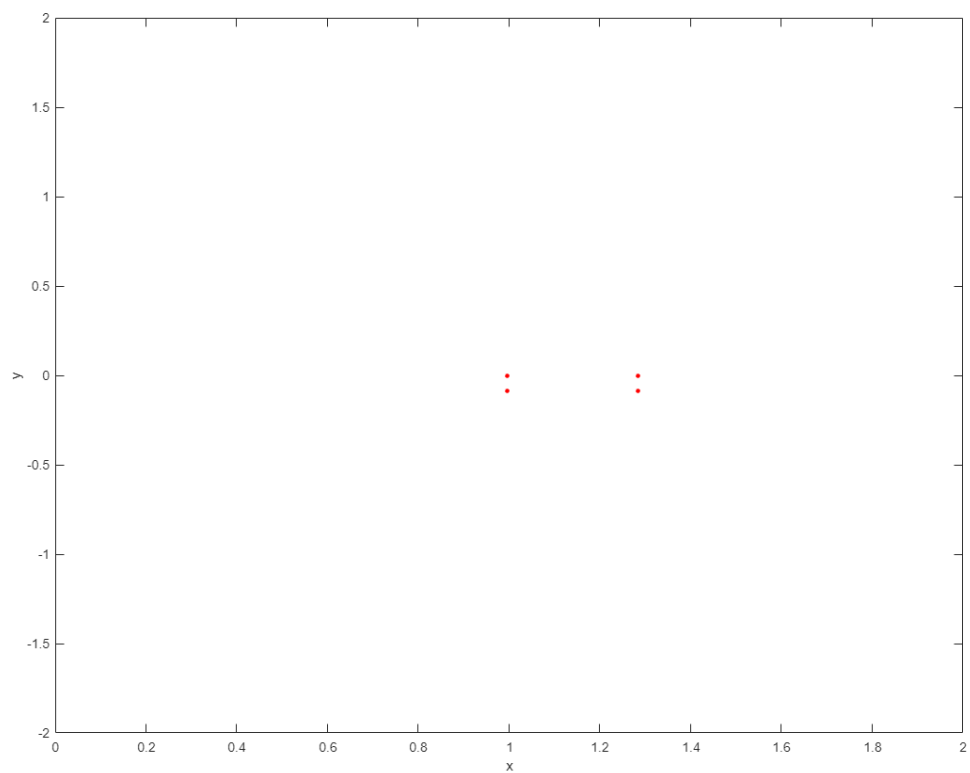


Рисунок 2 – поколение 1

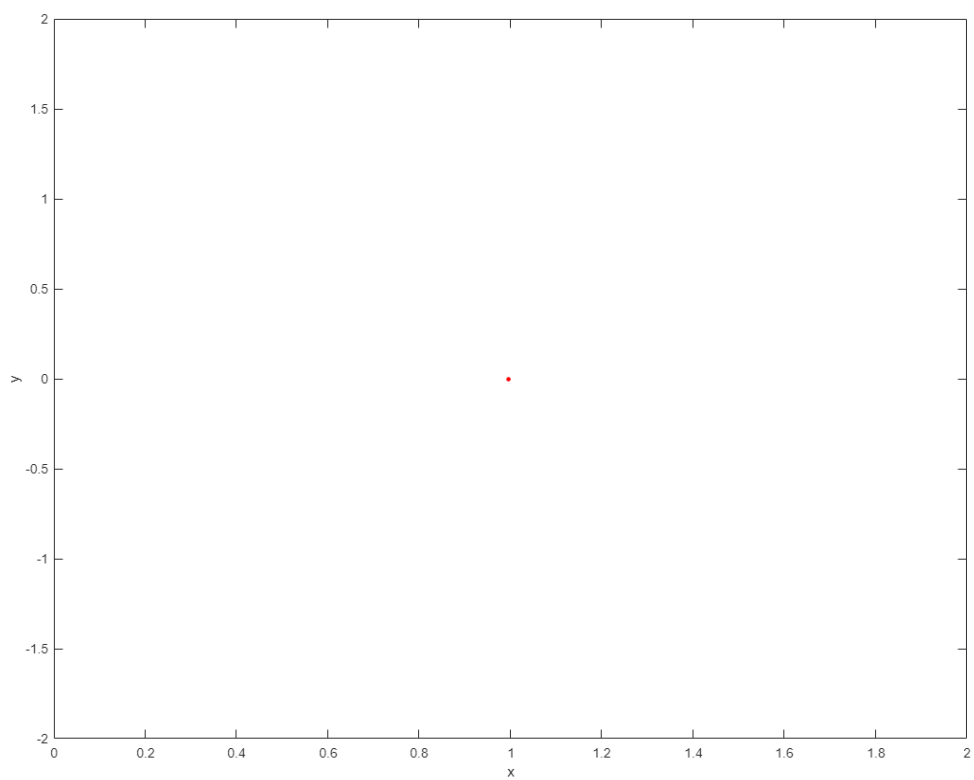


Рисунок 3 - поколения 2-10

2) Для 100 поколений

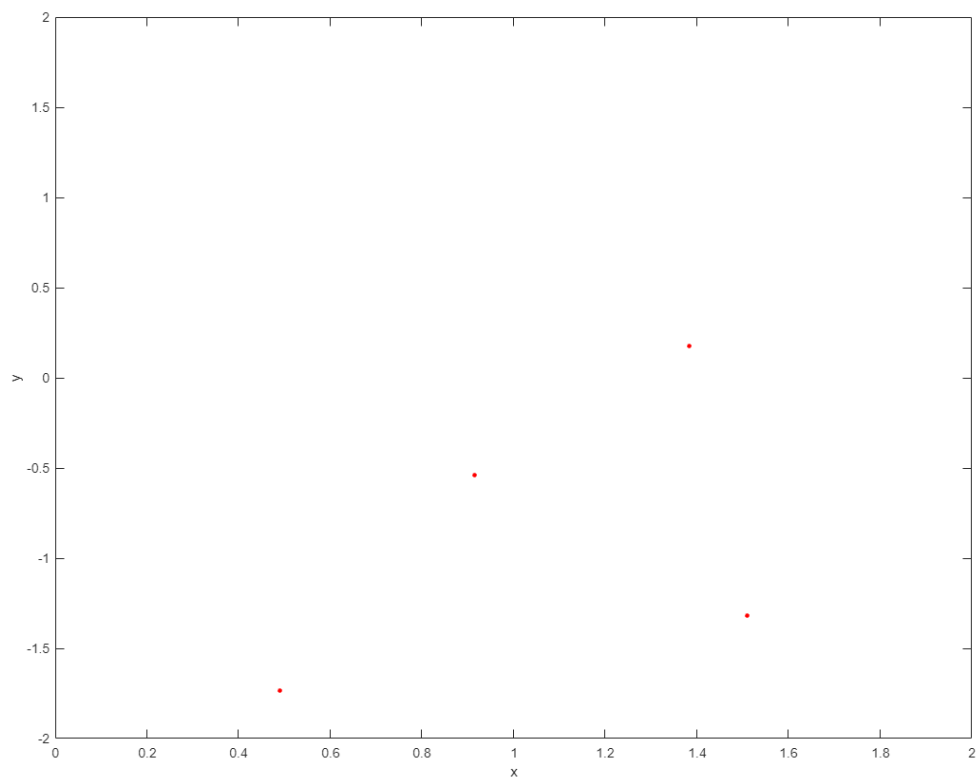


Рисунок 4 – поколение №0

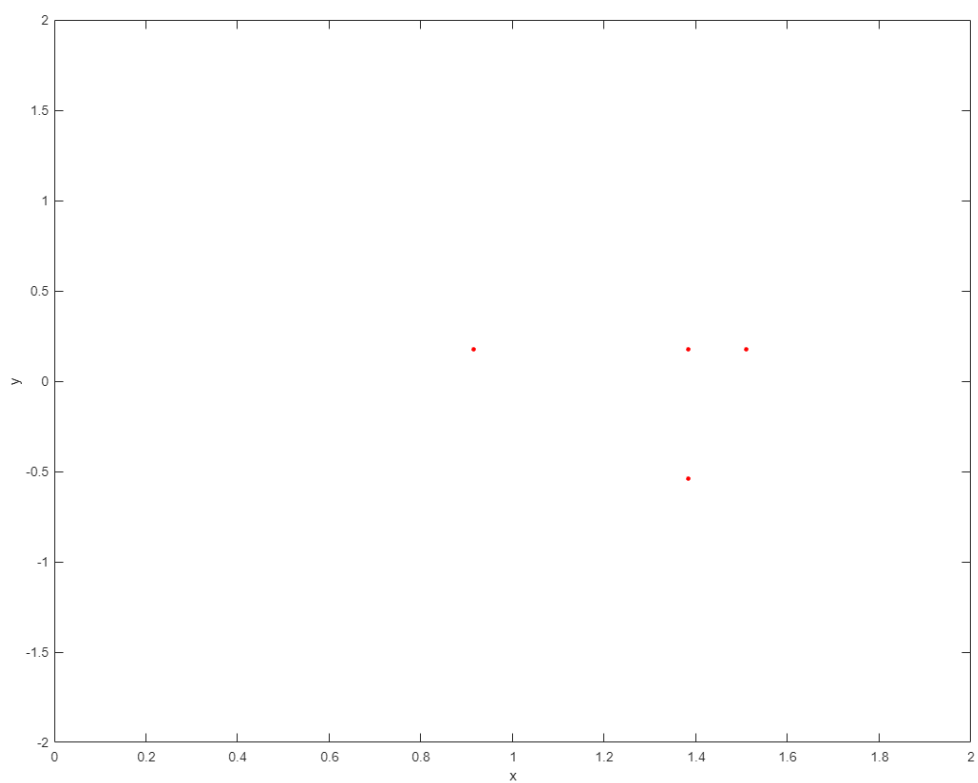


Рисунок 5 - поколение №1

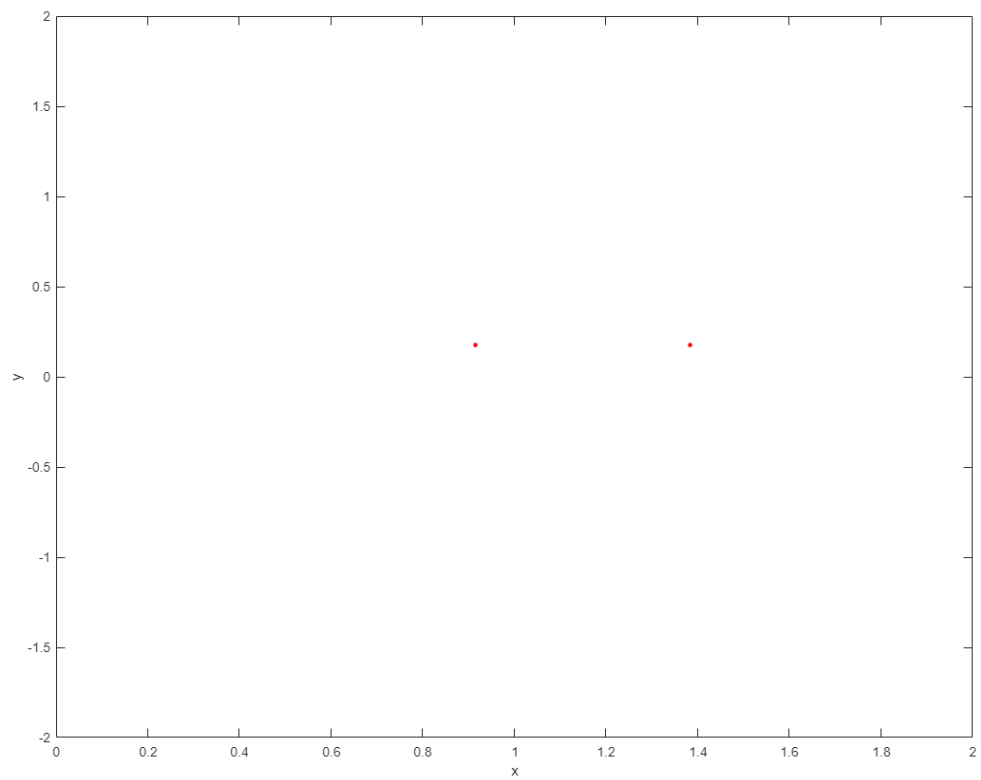


Рисунок 6 - поколение №2

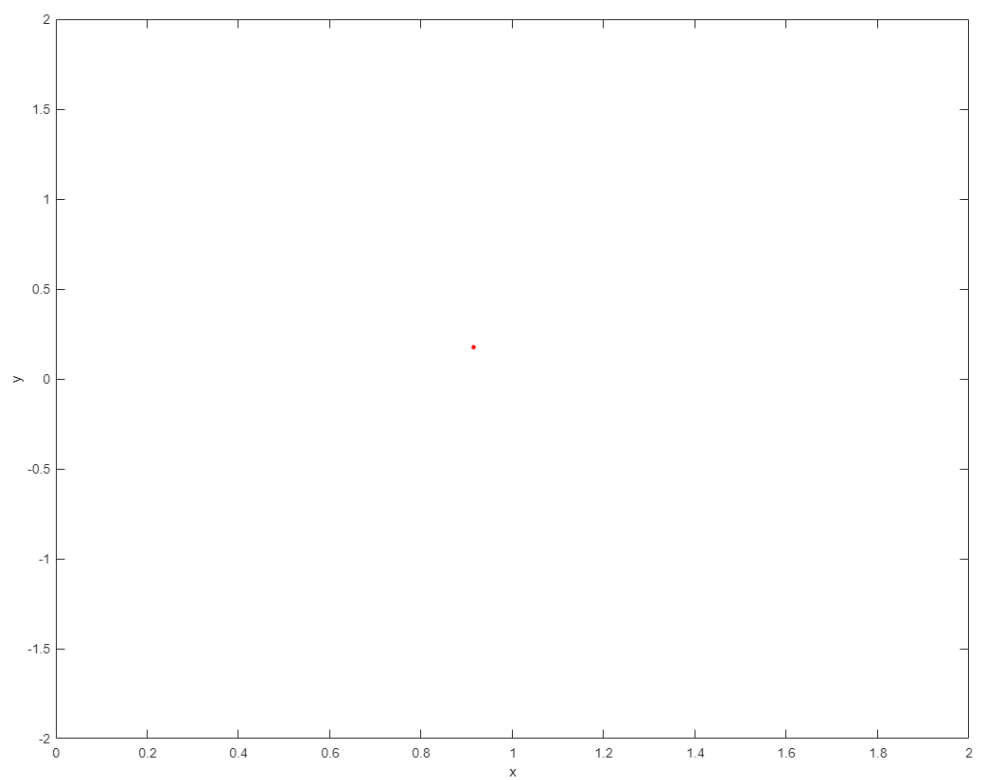


Рисунок 7 поколения №3-11

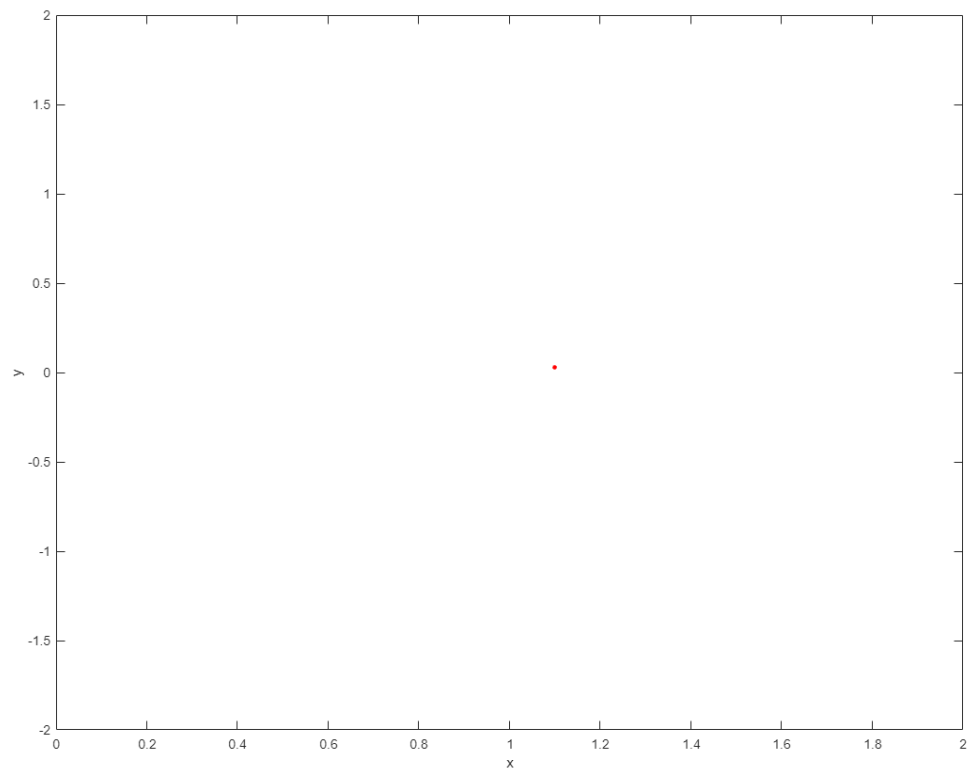


Рисунок 8 - поколение №15

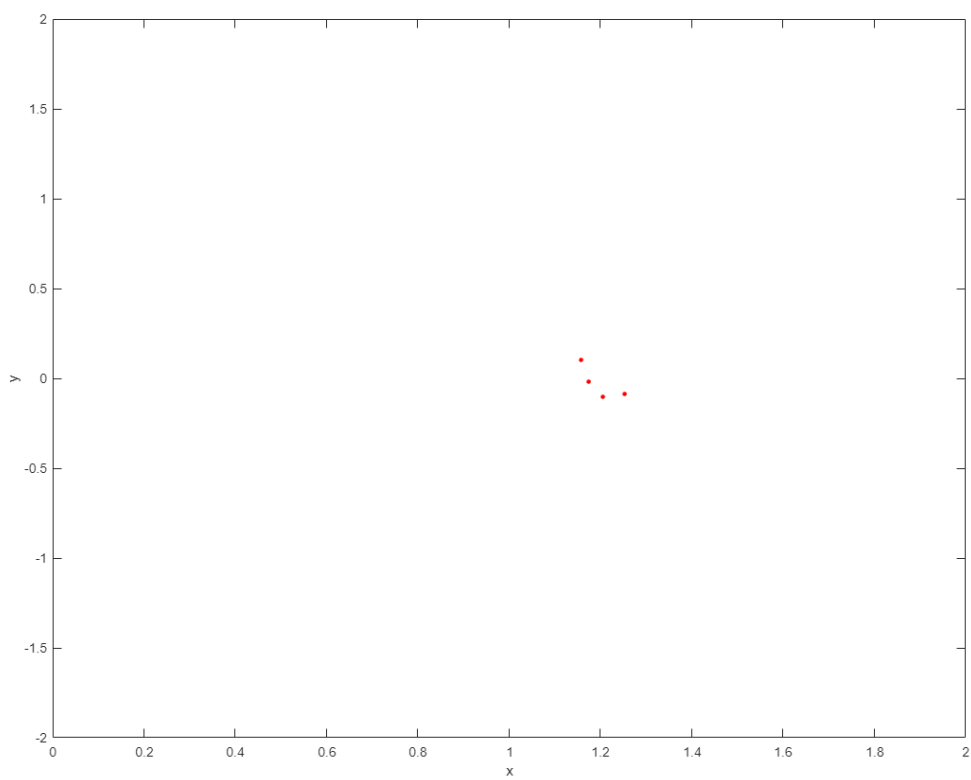


Рисунок 9 - поколение №31

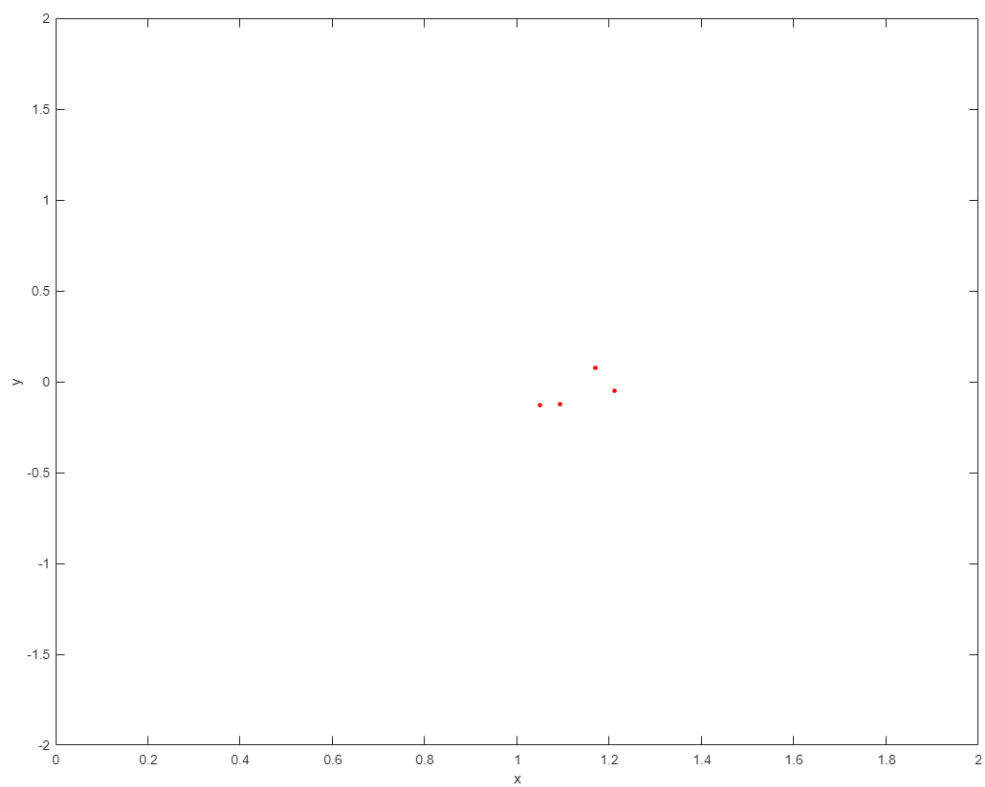


Рисунок 10 - поколение №52

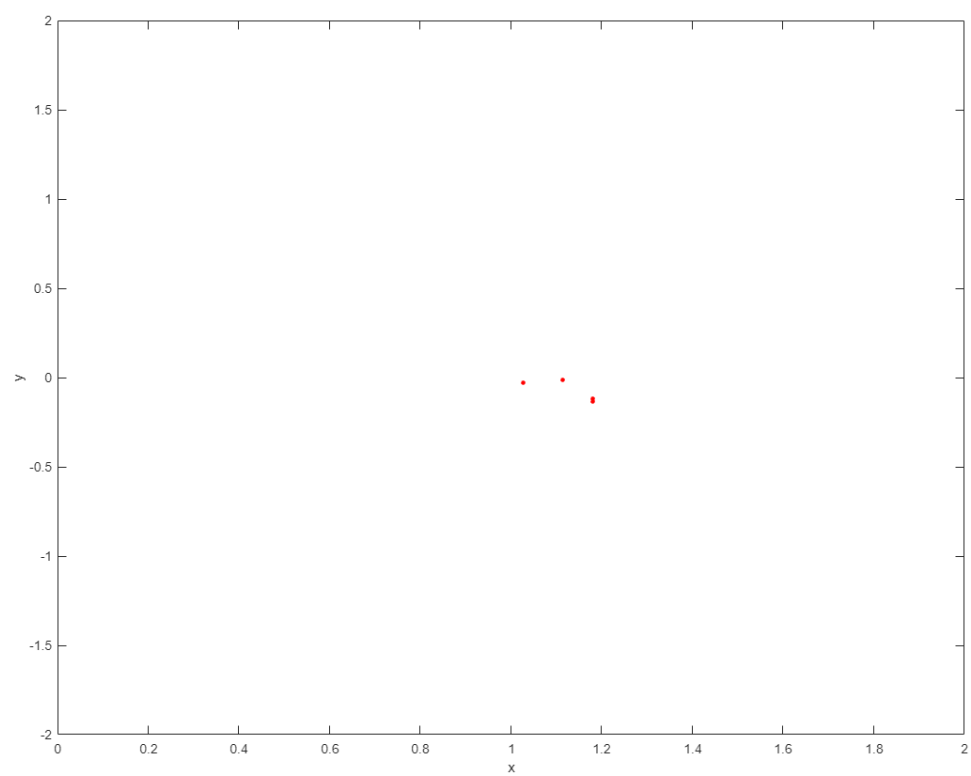


Рисунок 11 - поколение №73

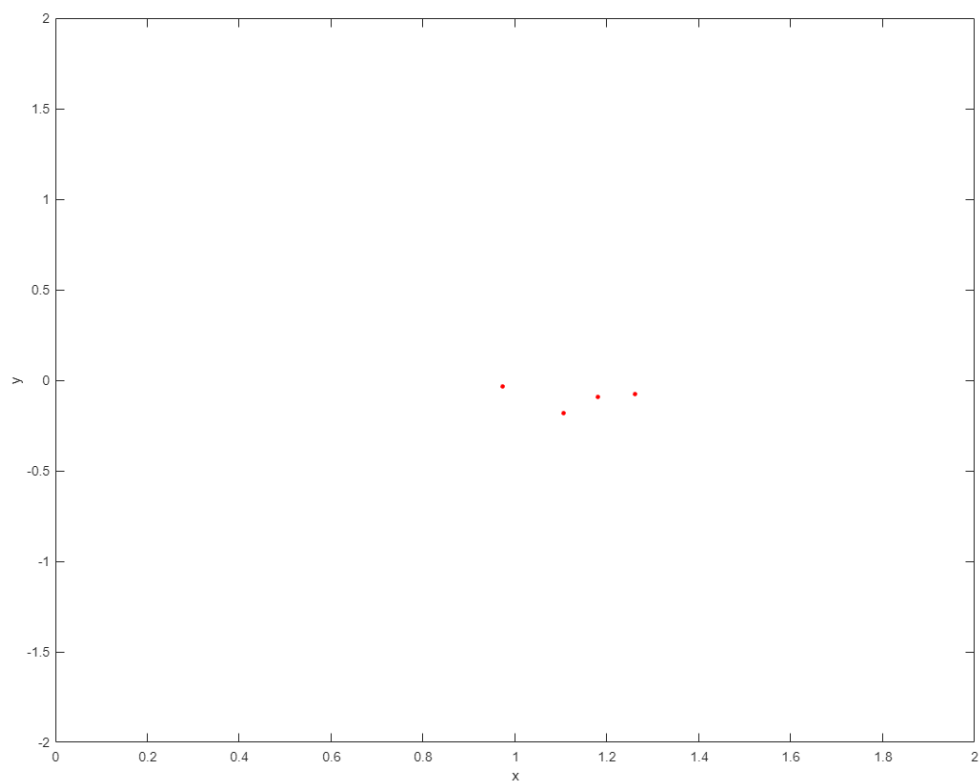


Рисунок 12 - поколение №93

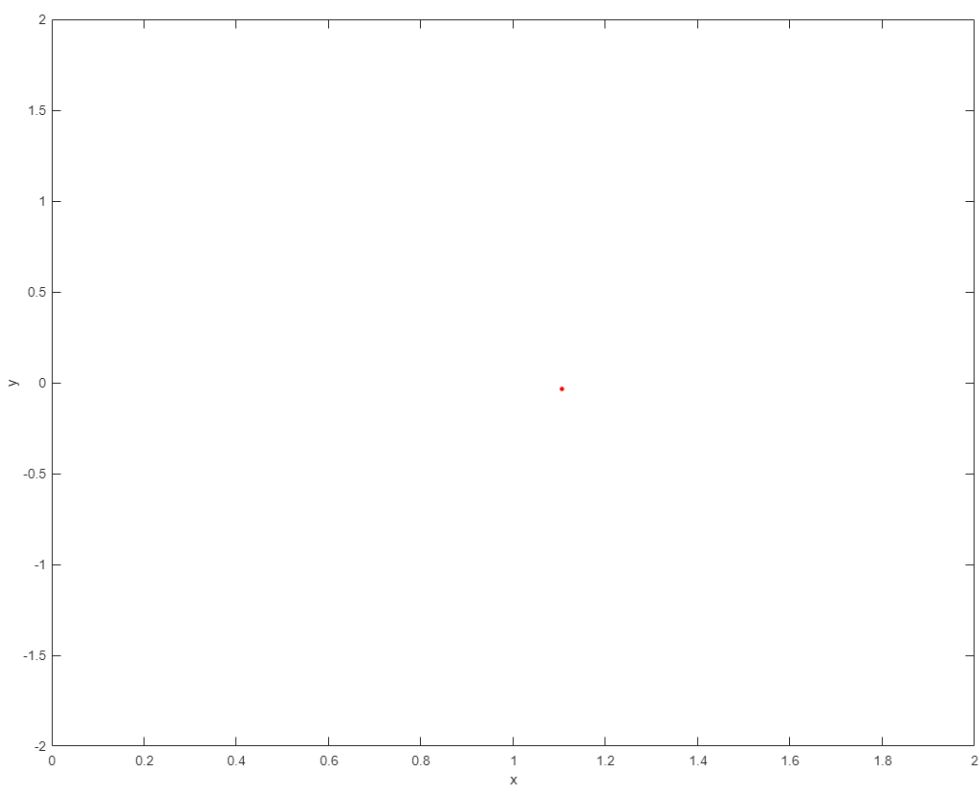


Рисунок 13 - поколение №100

4. Выводы

В процессе выполнения рубежного контроля я изучил метод поиска экстремума функции с помощью генетического алгоритма. В ходе работы мною был использован

алгоритм генерации промежуточной популяции, опирающийся на генетику, рулеточной селекции и мутации, в основе которой лежит случайное изменение генов. Значения полученные в ходе выполнения программы совпадают с графическими, что говорит о корректном ходе её работы.

Приложение

Файл main.cpp

```
#include "GeneticAlg.h"

using namespace std;

int main()
{
    std::cout<<"\t\t\t\t10 generations:\n\n";
    GeneticAlgorithm A(10);
    A.pass();
    std::cout<<"\n\t\t\t\t100 generations:\n\n";
    GeneticAlgorithm B(100);
    B.pass();
    system("pause");
    return 0;
}
```

Файл GeneticAlg.h

```
#pragma once
#include <map>
#include <random>
#include <iostream>
#include <iomanip>
#include <string>

struct point
{
    double x; // Координата x
    double y; // Координата y
    double z; // Координата z

    point()
    {
        x = 0.0;
        y = 0.0;
        z = 0.0;
    }
    point(double xval,double yval,double zval = 0.0)
    {
        x = xval;y = yval;z=zval;
    }
    bool operator!=( point point_2 )
    {
        if ((x != point_2.x) && (y != point_2.y))
        {
            return true;
        }
        return false;
    }
    bool operator==( point point_2 )
    {
        if ((x == point_2.x) && (y == point_2.y))
        {
            return true;
        }
    }
}
```

```

        }
        return false;
    }
};

struct borders
{
    double a;    // Нижняя граница
    double b;    // Верхняя граница

    borders()
    {
        a = 0.0;
        b = 0.0;
    }
    borders(double a2, double b2)
    {
        a=a2;
        b=b2;
    }
};

class GeneticAlgorithm
{
protected:
    /**
     *    Область поиска для координат x и y
     */
    std::pair<borders, borders> border{{0.0, 2.0}, {-2.0, 2.0}};
    /**
     *    Родители
     */
    std::multimap<double, point> parents;
    /**
     *    Промежуточная популяция
     */
    std::multimap<double, point> intermediate_generation;
    /**
     *    Максимальное количество поколений
     */
    size_t max_generations;

public:
    GeneticAlgorithm(size_t generations = 100u, std::pair<borders, borders>
input_border = {{0.0, 2.0}, {-2.0, 2.0}})
    {
        max_generations = generations;
        border = input_border;
    }

    /**
     * @brief Функция используется для полного прохождения генетического алгоритма
     */
    void pass();
    /**
     * @brief Функция используется для создания 0 генерации
     */
    /**
     * @param[in] count_of_parents Количество родителей
     */
    void init_gen(size_t count_of_parents = 4u);
    /**
     * @brief Функция, описывающая селекцию

```

```

*
*/
void selection();

/**
* @brief Функция, описывающая мутацию
*
*/
void mutation();

/**
* @brief Функция, описывающая селекцию
*
*/
void reduction();

/**
* @brief Функция для печати multimap
*
* @param[in] multimap Контейнер std::multimap<double,point>
* @param[in] prefix Префикс перед строкой
* @param[in] up_border Рисует границу сверху и снизу, если значение true
*
*/
void print(size_t generation, std::multimap<double,point> multimap,
std::string prefix = "", bool border = true);
};

```

Файл GeneticAlg.cpp

```

#include "GeneticAlg.h"
#include "Function.h"
#include <iterator>
#include <algorithm>

std::random_device rd;
std::mt19937 gen(rd());

void draw_hat()
{
    std::cout<<std::left<<std::setprecision(4)<<"|"<<std::setw(9)<<"generation"<<"|"<<std::
d::setw(6)<<"prefix"<<"|"<<std::setw(10)<<"X"<<"|"<<std::setw(10)<<"Y"<<"|"<<std::
"<<std::setw(10)<<"FIT"<<"|"<<std::setw(10)<<"max element"<<"|"<<std::
"<<std::setw(9)<<"average"<<"|\n";
}

void GeneticAlgorithm::init_gen(size_t count_of_parents)
{
    std::uniform_real_distribution<double> x_border
(border.first.a, border.first.b);
    std::uniform_real_distribution<double> y_border
(border.second.a, border.second.b);

    parents.clear();

    point temp_point;

    for (size_t count = 0; count < count_of_parents; ++count)
    {
        temp_point.x = x_border(gen);
        temp_point.y = y_border(gen);
        temp_point.z = F(temp_point.x, temp_point.y);
    }
}

```

```

        parents.insert({temp_point.z,temp_point});
    }
}

void GeneticAlgorithm::selection()
{
    intermediate_generation.clear();

    point temp_point;

    for(auto index = parents.begin();index != parents.end();++index)
    {
        /*
        Так как потомок может иметь что-то от каждого из
        родителей, то я сделал следующее:
        у 2 родителей могут быть 2 потомка с координатами
        (x1,y2,f(x1,y2)) и (x2,y1,f(x2,y1)),
        где (x1,y1) - координаты 1 родителя, (x2,y2) - координаты
        2 родителя.
        */
        for(auto index_2 = std::next(index);index_2 !=
parents.end();++index_2)
        {
            // 1)
            temp_point.x = index->second.x;
            temp_point.y = index_2->second.y;
            temp_point.z = F(temp_point.x,temp_point.y);

            intermediate_generation.insert({temp_point.z,temp_point});
            // 2)
            temp_point.x = index_2->second.x;
            temp_point.y = index->second.y;
            temp_point.z = F(temp_point.x,temp_point.y);

            intermediate_generation.insert({temp_point.z,temp_point});
        }
    }
}

void GeneticAlgorithm::reduction()
{
    for (auto temp : intermediate_generation)
    {
        parents.insert(temp);
    }
    intermediate_generation.clear();

    size_t temp = parents.size() - 4;
    for (size_t index = 0u;index < temp;++index)
    {
        parents.erase(parents.begin());
    }
    std::cout<<" ";
}

void GeneticAlgorithm::mutation()
{
    /*
    Заметка:
    Мутация в данной реализации генного алгоритма выглядит следующим
    образом:

```

```

        берется координата точки x и случайно сдвигается и также с y
        координатой.
    */
    std::uniform_real_distribution<double> delta(-0.3,0.3);

    std::multimap<double, point> temp_multimap;

    for (auto parent = parents.begin();parent != parents.end();++parent)
    {
        parent->second.x += delta(gen);
        parent->second.y += delta(gen);

        if (parent->second.x < border.first.a)
        {
            parent->second.x = border.first.a;
        }
        else if (parent->second.x > border.first.b)
        {
            parent->second.x = border.first.b;
        }
        if (parent->second.y < border.second.a)
        {
            parent->second.y = border.second.a;
        }
        else if (parent->second.y > border.second.b)
        {
            parent->second.y = border.second.b;
        }
        parent->second.z = F(parent->second.x,parent->second.y);
        temp_multimap.insert({parent->second.z,parent->second});
    }
    parents = temp_multimap;
    temp_multimap.clear();

    for (auto child = intermediate_generation.begin();child !=
intermediate_generation.end();++child)
    {
        child->second.x += delta(gen);
        child->second.y += delta(gen);
        if (child->second.x < border.first.a)
        {
            child->second.x = border.first.a;
        }
        else if (child->second.x > border.first.b)
        {
            child->second.x = border.first.b;
        }
        if (child->second.y < border.second.a)
        {
            child->second.y = border.second.a;
        }
        else if (child->second.y > border.second.b)
        {
            child->second.y = border.second.b;
        }
        child->second.z = F(child->second.x,child->second.y);
        temp_multimap.insert({child->second.z,child->second});
    }
    intermediate_generation = temp_multimap;
    temp_multimap.clear();
}

void GeneticAlgorithm::pass()
{

```

```

double P = 0.0;
std::uniform_real_distribution<double> Probability(0.0,0.1);

draw_hat();
init_gen();
print(0u,parents,"p");
selection();
reduction();
std::cout<<"\n";

for (size_t iteration = 1u;iteration <= max_generations - 1u ;++iteration)
{
    P += Probability(gen);
    // std::cout<<P<<"\n"; // Debug
    selection();
    if (P > 0.5)
    {
        mutation();
        P = 0.0;
    }
    print(iteration, parents,"p");
    print(iteration, intermidiate_generation, "ig",true);
    reduction();
    std::cout<<"\n";
}
print(max_generations,parents,"result");
}

void GeneticAlgorithm::print(size_t generation,std::multimap<double,point> multimap,
std::string prefix,bool border)
{
    if (border)
    {
        std::cout<<" ";
        for (int index = 1;index < 85;++index)
        {
            std::cout<<"-";
        }
        std::cout<<"\n";
    }

    double average = 0.0;

    for (auto tochka: multimap)
    {
        average +=tochka.second.z;
    }

    average=average/multimap.size();

    auto max_element = std::max_element(multimap.begin(),multimap.end(),

[](std::pair<double,point> var1,std::pair<double,point> var2)

{

    return var1.first < var2.first;

})

);

    for (auto tochka = multimap.begin();tochka != multimap.end();++tochka)
    {
        std::cout<<std::left<<std::setprecision(4)<<"|
"<<std::setw(9)<<generation<<"|"<<std::setw(6)<<' '+prefix<<" | "<<std::setw(10)<<tochka-
>second.x<<" | "<<std::setw(10)<<tochka->second.y<<" | "<<std::setw(10)<<tochka->second.z;

```



```

        if (tochka == std::prev(multimap.end()))
        {
            std::cout<<" | "<<std::setw(10)<<max_element-
>first<<" | "<<std::setw(10)<<average<<" |";
        }
        else
        {
            std::cout<<" | "<<std::setw(10)<<"          "<<" |
"<<std::setw(10)<<"          "<<" |";
        }
        std::cout<<"\n";
    }

    if (border)
    {
        std::cout<<" ";
        for (int index = 1;index < 85;++index)
        {
            std::cout<<"-";
        }
        std::cout<<"\n";
    }
}

```