

Variadic Templates

“Look Ma, no recursion!”

Disclaimer

- Opinions expressed are solely my own and do not express the views or opinions of my employer.
- All mistakes are mine, please point them out.
- When taking a note for a question, please write down the slide number!

Rationale

- Variadic templates and template meta programming are used everywhere.
- `std::tuple` is the most obvious example.
- Using `std::tuple` can increase compile-time significantly.
- Used behind the scenes of other APIs, e.g., a database framework.

C++11

- This talk is C++11 or newer.
- Tested with GCC/Clang.
- I omitted `std::` qualifications.
- No error detection/handling, real-world code is slightly longer due to `static_assert()`, etc.

C++14

- Some C++14 helpers are used, implementations for C++11 are available.
- `something_t<...>` is short for **typename** `something<...>::type`.
- <http://cppreference.com>

Type Traits

```
#include <type_traits>
```

Most important for this talk:

```
integral_constant<T, N>
```

```
true_type
```

```
false_type
```

```
is_same<T, U>
```


Type Traits

```
template<typename T, T V>  
struct integral_constant  
{  
    static constexpr T value = V;  
};
```

The above skips some standardized members.

Type Traits

```
template<typename T, T V>  
struct integral_constant  
{  
    static constexpr T value = V;  
};
```

```
// Standardized in C++17  
template<bool B>  
using bool_constant =  
    integral_constant<bool, B>;
```


Type Traits

```
using true_type =  
    bool_constant<true>;
```

```
using false_type =  
    bool_constant<false>;
```

```
true_type::value → true
```

```
false_type::value → false
```


Type Traits

```
template<typename, typename>  
struct is_same : false_type {};
```

```
template<typename T>  
struct is_same<T, T> : true_type {};
```

```
is_same<int, int>::value → true
```

```
is_same<int, double>::value → false
```


Variadic Templates

```
template<typename...>  
struct typelist {};
```

```
typelist<int, double, long>
```


Variadic Templates

```
template<typename...>  
struct typelist {};
```

```
typelist<int, double, long>
```

```
typelist<>
```

```
typelist<int>
```


Variadic Templates

```
template<int...>  
struct intlist {};
```

```
intlist<1, -3, 42, 1701>
```


Variadic Templates

```
template<bool...>  
struct boollist {};
```

```
boollist<true, false, false>
```


Logical And

```
template<bool...>  
struct is_all;
```

```
template<bool B, bool... Bs>  
struct is_all<B, Bs...>  
    : bool_constant<  
        B && is_all<Bs...>::value>  
{};
```

```
template<>  
struct is_all<> : true_type {};
```


Logical And

```
template<int... Is>  
using is_all_even =  
    is_all<(Is % 2 == 0) ...>;
```

is_all_even<0, 2, 42>::value → **true**

is_all_even<4, 5, 6>::value → **false**

Logical And

```
template<int... Is>  
using is_all_even =  
    is_all<(Is % 2 == 0) ...>;
```

is_all_even<0, 2, 42>::value → **true**

is_all_even<4, 5, 6>::value → **false**

Logical And

```
template<int... Is>  
using is_all_even =  
    is_all<(Is % 2 == 0) ...>;
```

is_all_even<0, 2, 42>::value → **true**

is_all_even<4, 5, 6>::value → **false**

Logical And

```
template<bool...>
struct is_all : true_type {};

template<bool B, bool... Bs>
struct is_all<B, Bs...>
    : bool_constant<
        B && is_all<Bs...>::value>
    {};
```


Logical And

```
// Recursive solution
template<bool...>
struct is_all : true_type {};

template<bool B, bool... Bs>
struct is_all<B, Bs...>
    : bool_constant<
        B && is_all<Bs...>::value>
    {};
```


Logical And

```
// The idea  
template<bool... Bs>  
using is_all =  
    is_same<boollist<Bs...>,  
            boollist<true...>>;
```


Logical And

```
// The idea  
template<bool... Bs>  
using is_all =  
    is_same<boollist<Bs...>,  
            boollist<true...>>;
```

Nope, does not work! :(

Logical And

```
// Solution 1  
template<bool... Bs>  
using is_all =  
    is_same<boollist<Bs...>,  
            boollist<(Bs || true)...>>;
```


Logical And

```
// Solution 2  
template<bool... Bs>  
using is_all =  
    is_same<boollist<true, Bs...>,  
            boollist<Bs..., true>>;
```


C++17

```
// C++17 fold expression  
template<bool... Bs>  
using is_all =  
    bool_constant<(Bs && ...) >;
```


C++17

```
// C++17 fold expression  
template<bool... Bs>  
using is_all =  
    bool_constant<(Bs && ...) >;
```


C++17

```
// C++14 variable template  
// C++17 fold expression  
template<int... Is>  
constexpr bool is_all_even =  
    ((Is % 2 == 0) && ...);
```

is_all_even<0, 2, 42> → **true**

is_all_even<4, 5, 6> → **false**

is_all_same

```
template<typename T, typename... Ts>  
using is_all_same =  
    is_all<is_same<T, Ts>::value...>;
```

```
is_all_same<int, int, int>::value  
→ true
```

```
is_all_same<int, int, void>::value  
→ false
```


is_all_same

```
template<typename T, typename... Ts>  
using is_all_same =  
    is_all<is_same<T, Ts>::value...>;
```

- Requires at least one type.
- No recursion, all the way down.
- Often you build new traits with `using` and smaller building blocks.

Logical Or

```
template<bool... Bs>
using is_any =
    bool_constant<
        !is_all<!Bs...>::value>;
```


enable_if_any/all

// C++11 / C++14

```
template<typename R, bool... Bs>  
using enable_if_any =  
    enable_if<is_any<Bs>::value..., R>;
```

```
template<typename R, bool... Bs>  
using enable_if_all =  
    enable_if<is_all<Bs>::value..., R>;
```


enable_if_any/all

// C++17 fold expression

```
template<typename R, bool... Bs>
```

```
using enable_if_any =
```

```
    enable_if<(Bs || ...), R>;
```

```
template<typename R, bool... Bs>
```

```
using enable_if_all =
```

```
    enable_if<(Bs && ...), R>;
```


Tuple

```
template<typename...>  
struct tuple { ... };
```

- Very useful as a real object.
- Can also be used as a `typelist`.
- When used as such, do not instantiate it!

Replace Type

```
template<
    typename T, typename U,
    typename... Ts>
using replace_t =
    tuple<
        conditional_t<
            is_same<Ts, T>::value, U, Ts
        >...
    >;
```


Replace Type

```
template<
    typename T, typename U,
    typename... Ts>
using replace_t =
    tuple<
        conditional_t<
            is_same<Ts, T>::value, U, Ts
        >...
    >;
```


Replace Type

```
template<  
    typename T, typename U,  
    typename... Ts>  
using replace_t = ...;
```

```
replace_t<int, double,  
    void, int, long, int>  
→ tuple<void, double, long, double>
```


Tuple Size

```
template<typename>  
struct tuple_size;
```

```
template<typename... Ts>  
struct tuple_size<tuple<Ts...>>  
    : integral_constant<size_t,  
        sizeof...(Ts)>  
{};
```


Tuple 🐱

```
template<typename... Ts>  
constexpr tuple<CTypes...>  
    tuple_cat(Ts&&... args) { ... }
```


Tuple 🐱

```
template<typename... Ts>  
constexpr tuple<CTypes...>  
    tuple_cat(Ts&&... args) { ... }
```

- Each element of Ts is itself a tuple<Us...>.
- CTypes is the concatenation of all Us... from all Ts.

Tuple 🐱

```
auto t = tuple_cat(  
    make_tuple(1, true),  
    make_tuple(1.0),  
    make_tuple(1UL, nullptr);
```

```
decltype(t)  
→ tuple<int, bool,  
    double,  
    unsigned long, nullptr_t>
```


Tuple 🐱

```
template<typename... Ts>
using tuple_cat_t =
    decltype(
        tuple_cat(declval<Ts>()...)
    );
```


Tuple 🐱

```
template<typename... Ts>
using tuple_cat_t =
    decltype(
        tuple_cat(declval<Ts>()...)
    );
```

- The above does not always work...
- ...but it is easy to fix. (see appendix A)

Remove Type

```
template<typename T, typename... Ts>
using remove_t =
    tuple_cat_t<
        conditional_t<
            is_same<Ts, T>::value,
            tuple<>,
            tuple<Ts>
        >...
    >;
```


Remove Type

```
template<typename T, typename... Ts>  
using remove_t = ...;
```

```
remove_t<int, void, int, long, int>  
→ tuple<void, long>
```

```
remove_t<void, void, int, void>  
→ tuple<int>
```


Indices

```
template<typename T, T...>  
struct integer_sequence { ... };
```

- Standardized in C++14.
- Extremely useful!

Indices

```
template<typename T, T...>  
struct integer_sequence { ... };
```

```
integer_sequence<long>
```

```
integer_sequence<unsigned, 0, 42, 1>
```

```
integer_sequence<int, -2, 5, -1, 9>
```


Indices

```
template<size_t... Ns>  
using index_sequence =  
    integer_sequence<size_t, Ns...>;
```

```
index_sequence<>
```

```
index_sequence<2, 5, 11, 3, 7, 13>
```

```
index_sequence<0, 1, 2, 3, 4, 5, 6>
```


Indices

```
template<typename T, T N>  
using make_integer_sequence =  
    integer_sequence<T,  
        /* a sequence 0, ..., N-1 */>;
```

```
template<size_t N>  
using make_index_sequence =  
    make_integer_sequence<size_t, N>;
```


Indices

`make_index_sequence<3>`

→ `index_sequence<0, 1, 2>`

`make_index_sequence<0>`

→ `index_sequence<>`

`make_index_sequence<7>`

→ `index_sequence<0, 1, 2, 3, 4, 5, 6>`

Indices

```
template<typename... Ts>  
using index_sequence_for =  
    make_index_sequence<sizeof...(Ts)>;
```

```
index_sequence_for<int, void, int>  
→ index_sequence<0, 1, 2>
```


Replace Index

```
template<
    typename T,
    size_t N, typename U,
    typename = make_index_sequence<
        tuple_size<T>::value
    >
>
struct replace_n;
```


Replace Index

```
template<typename... Ts,  
        size_t N, typename U,  
        size_t... Ns>  
struct replace_n<tuple<Ts...>,  
                N, U,  
                index_sequence<Ns...>>  
{  
    using type = tuple<  
        conditional_t<Ns==N, U, Ts>...  
    >;  
};
```


Replace Index

```
template<typename... Ts,  
        size_t N, typename U,  
        size_t... Ns>  
struct replace_n<tuple<Ts...>,  
                N, U,  
                index_sequence<Ns...>>  
{  
    using type = tuple<  
        conditional_t<Ns==N, U, Ts>...  
    >;  
};
```


Replace Index

```
template<typename T,  
        size_t N, typename U>  
using replace_n_t =  
    typename replace_n<T, N, U>::type;
```

```
using T1 = tuple<int, void, long>;
```

```
replace_n_t<T1, 1, double>  
→ tuple<int, double, long>
```


Replace Index

```
using T1 = tuple<int, double, long>;  
  
using T2 = replace_n_t<T1, 1, void>;  
using T3 = replace_n_t<T2, 0, T1>;  
using T4 = replace_n_t<T3, 2, int>;
```


Replace Index

```
using T1 = tuple<int, double, long>;
```

```
using T2 = replace_n_t<T1, 1, void>;
```

```
using T3 = replace_n_t<T2, 0, T1>;
```

```
using T4 = replace_n_t<T3, 2, int>;
```

```
T4 → tuple<  
    tuple<int, double, long>, void, int  
>
```


Benchmark

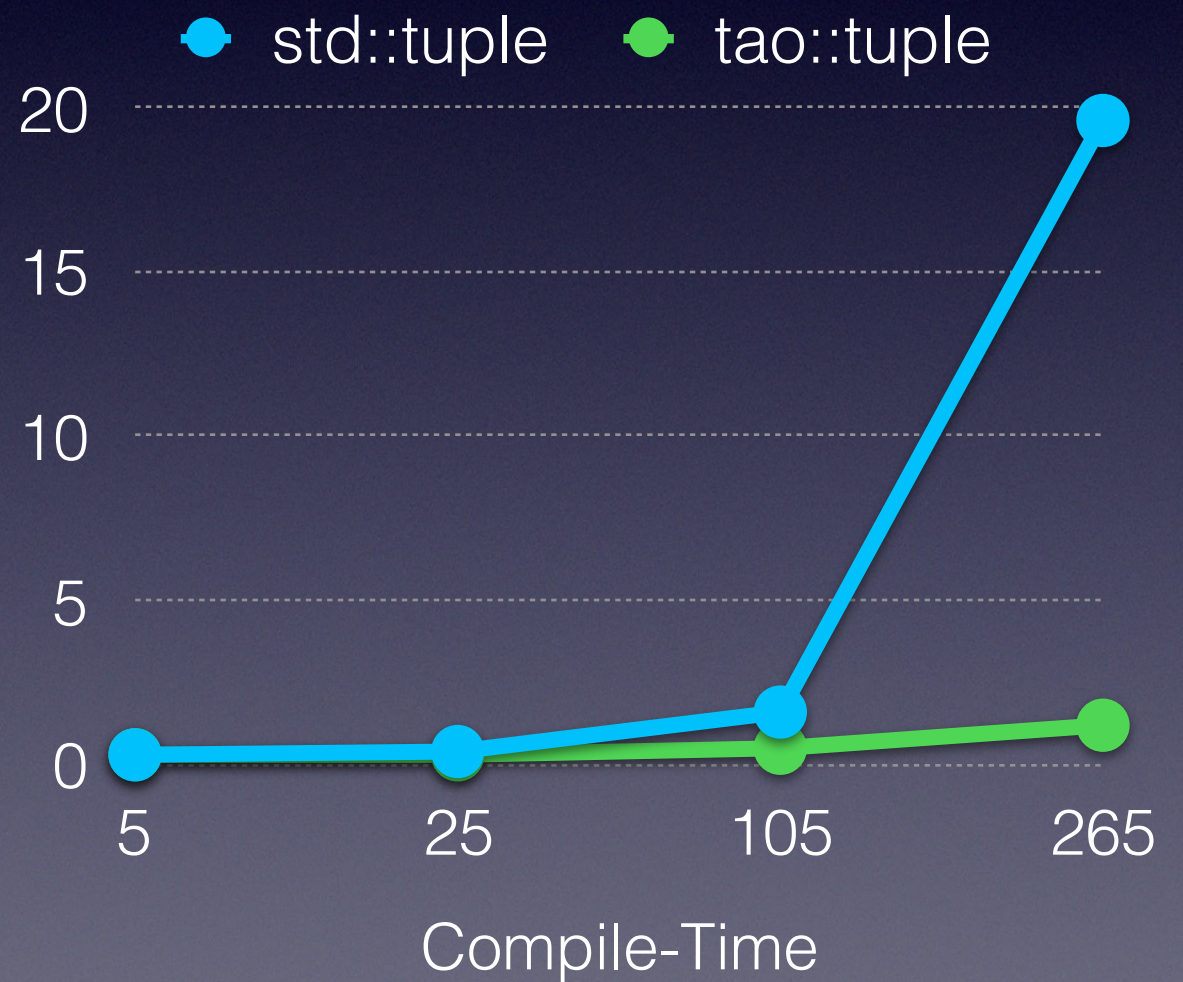
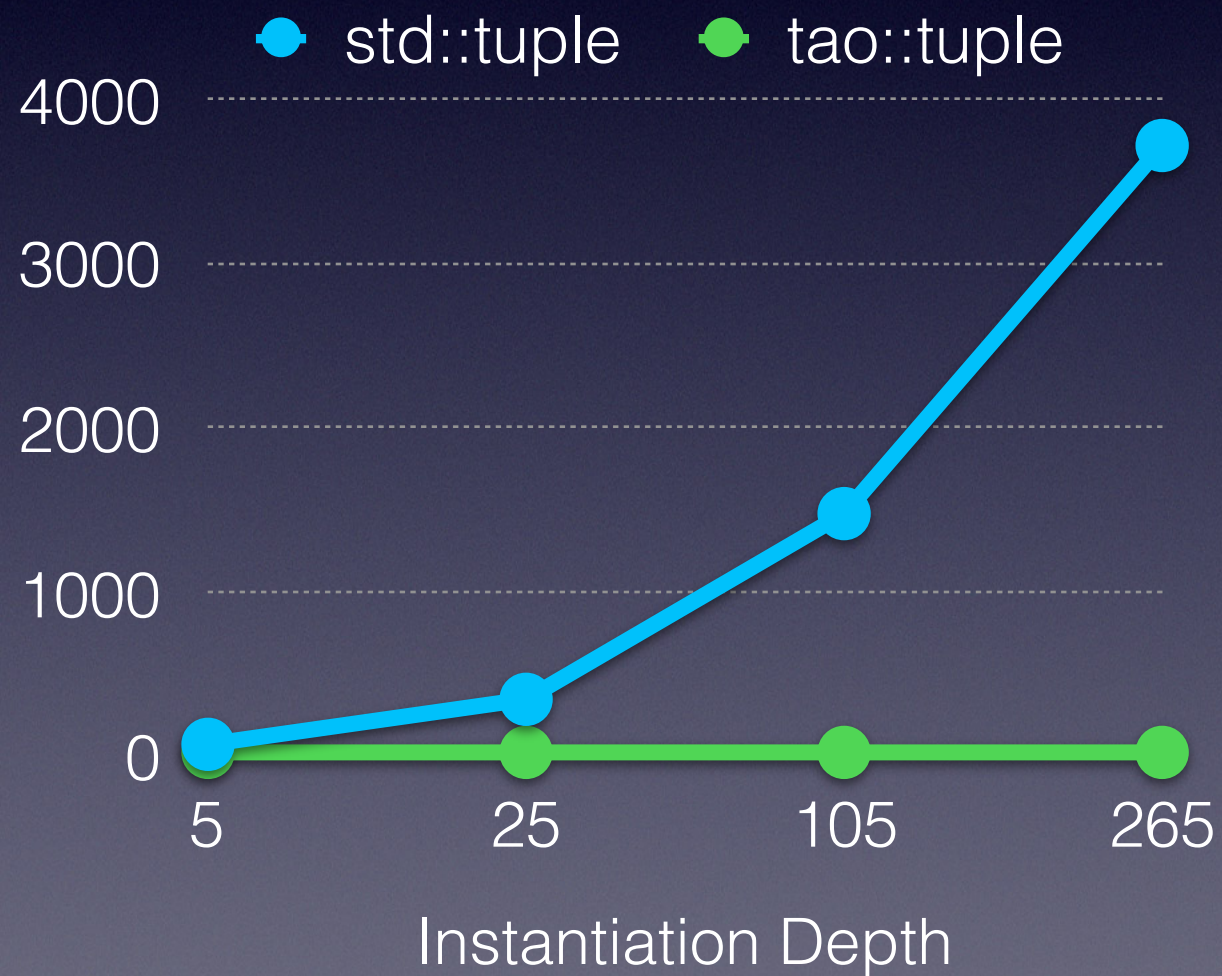
- Create a tuple, with `tuple_cat()`, 5 elements
- Join this tuple with itself and some other elements. Result tuple is 25 elements.
- Repeat, result tuple is 105 elements.
- Repeat, final result tuple is 265 elements.
- Measure instantiation depth and compile time.

Benchmark

System	Compiler	Tuple	Instantiation Depth	Compile Time
Linux	GCC 5	libstdc++ std::tuple	3719	19.6s
Linux	GCC 5	libstdc++ tao::tuple	26	1.2s
Mac OS X	Apple LLVM 7.0	libc++ std::tuple	514	>70.0s
Mac OS X	Apple LLVM 7.0	libc++ tao::tuple	15	1.7s

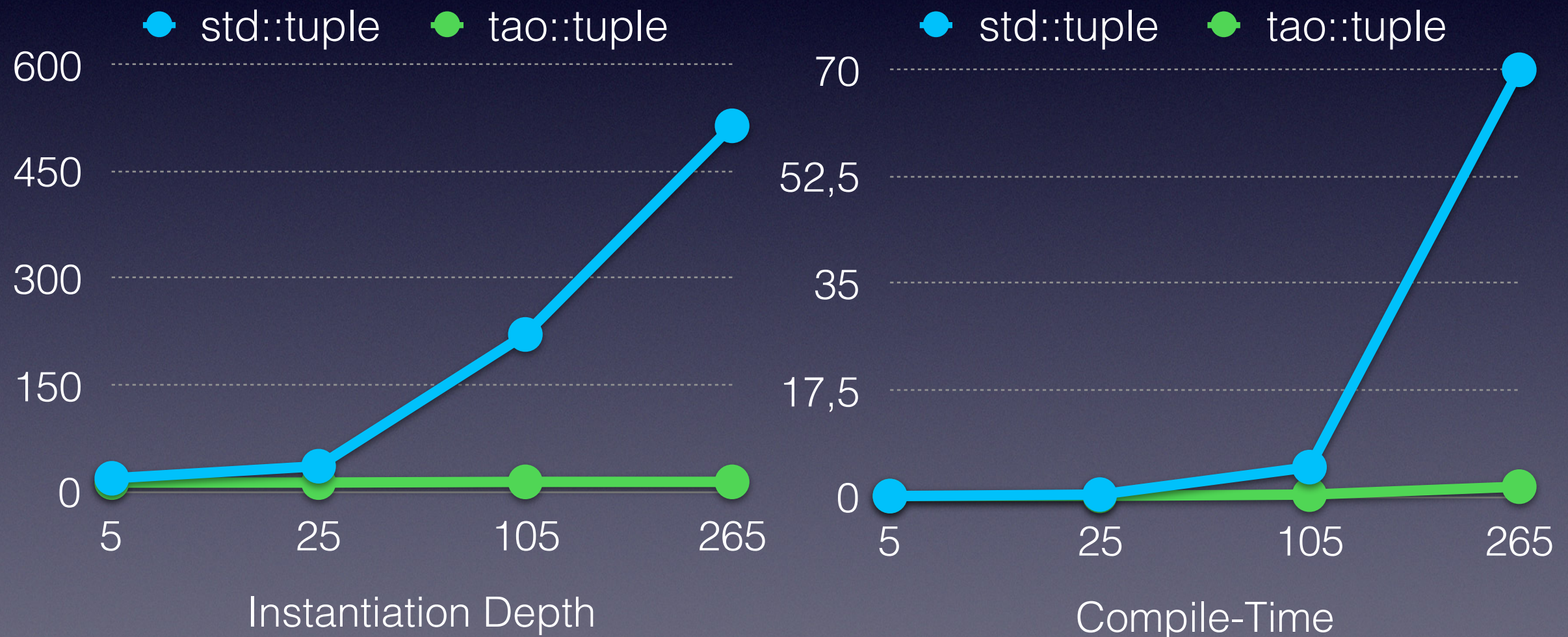
Benchmark

GCC 5 with libstdc++



Benchmark

Apple LLVM 7.0 (~Clang 3.7) with libc++



**YEAH, IF YOU COULD JUST GO AHEAD
AND STOP USING RECURSION FROM NOW ON...**

THAT WOULD BE GREEEAT, M'KAY?

Questions?

Thank you!

<https://github.com/taocpp/>

Appendix A

Fixing tuple_cat_t

Tuple 🐱 (fixed)

```
template<typename... Ts>
using tuple_cat_t =
    decltype(
        tuple_cat(declval<Ts>()...)
    );
```

- Does not work with **void**.
- Solution: Temporarily wrap the types.

Tuple 🐱 (fixed)

```
template<typename>  
struct wrapper {};
```


Tuple 🐱 (fixed)

```
template<typename>  
struct wrap;
```

```
template<typename... Ts>  
struct wrap<tuple<Ts...>>  
{  
    using type = tuple<wrapper<Ts>...>;  
};
```


Tuple 🐱 (fixed)

```
template<typename>  
struct unwrap;
```

```
template<typename... Ts>  
struct unwrap<tuple<wrapper<Ts>...>>  
{  
    using type = tuple<Ts...>;  
};
```


Tuple 🐱 (fixed)

```
template<typename T>  
using wrap_t =  
    typename wrap<T>::type;
```

```
template<typename T>  
using unwrap_t =  
    typename unwrap<T>::type;
```


Tuple 🐱 (fixed)

```
template<typename... Ts>
using tuple_cat_t =
    unwrap_t<
        decltype(
            tuple_cat(
                declval<wrap_t<Ts>>() ...
            )
        )
    >;
```


Appendix B

A better `make_integer_sequence`

Make Indices

```
template<typename T, T N>  
using make_integer_sequence =  
    integer_sequence<T,  
        /* a sequence 0, ..., N-1 */>;
```

- Naive implementation recurses for each step.
- `libstdc++` currently implements it that way.

Make Indices

```
template<typename T, T N>  
using make_integer_sequence =  
    integer_sequence<T,  
        /* a sequence 0, ..., N-1 */>;
```

- A better implementation has $O(\log N)$.
- Based on <http://stackoverflow.com/a/13073076>

Make Indices

```
template<typename, size_t, bool>  
struct _double;
```


Make Indices

```
template<typename T, T... Ns,  
        size_t N>  
struct _double<  
    integer_sequence<T, Ns...>,  
    N, false>  
{  
    using type = integer_sequence<T,  
        Ns..., (N + Ns) ...>;  
};
```


Make Indices

```
template<typename T, T... Ns,  
        size_t N>  
struct _double<  
    integer_sequence<T, Ns...>,  
    N, true>  
{  
    using type = integer_sequence<T,  
        Ns..., (N + Ns) ..., 2 * N>;  
};
```


Make Indices

```
template<typename T, T N,  
        typename = void>  
struct _generate;
```

```
template<typename T, T N>  
using _generate_t =  
    typename _generate<T, N>::type;
```


Make Indices

```
template<typename T, T N>
struct _generate
: _double<
    _generate_t<T, N / 2>,
    N / 2,
    N % 2 == 1>
>
{};
```


Make Indices

```
template<typename T, T N>
struct _generate<T, N,
    enable_if_t<(N == 0)>
>
{
    using type =
        integer_sequence<T>;
};
```


Make Indices

```
template<typename T, T N>
struct _generate<T, N,
    enable_if_t<(N == 1)>
>
{
    using type =
        integer_sequence<T, 0>;
};
```


Make Indices

```
template<typename T, T N>  
using make_integer_sequence =  
    _generate_t<T, N>;
```

- Timing for `make_index_sequence<10000>`
- GCC 5: ~2.5s (~0.15s with a small change)
- Clang 3.6: ~0.15s

Make Indices

- libc++ has a very efficient library-based solution, better than the one I've shown.
- Best solution is a compiler intrinsic.
- Visual C++ will get one soon:

```
template<typename T, T N>  
using make_integer_sequence =  
    __make_integer_seq<T, N>;
```


Appendix C

More non-recursive goodies

Plus

```
template<typename, typename>  
struct plus;
```

```
template<typename A, typename B>  
using plus_t =  
    typename plus<A, B>::type;
```


Plus

```
template<typename A, A... As,  
        typename B, B... Bs>  
struct plus<  
    integer_sequence<A, As...>,  
    integer_sequence<B, Bs...>>  
{  
    using type =  
        integer_sequence<  
            common_type_t<A, B>,  
            (As + Bs) ...>;  
};
```


Minus

```
template<typename, typename>  
struct minus;
```

```
template<typename A, typename B>  
using minus_t =  
    typename minus<A, B>::type;
```


Minus

```
template<typename A, A... As,  
        typename B, B... Bs>  
struct minus<  
    integer_sequence<A, As...>,  
    integer_sequence<B, Bs...>>  
{  
    using type =  
        integer_sequence<  
            common_type_t<A, B>,  
            (As - Bs) ...>;  
};
```


Sum

```
template<typename T, T... Ns>
struct sum
    : integral_constant<T, (Ns + ...) >
{ };
```

- Simple with C++17's fold expressions.
- But what about C++11/C++14?

Sum

```
// Helper  
template<size_t, size_t N>  
struct _chars  
{  
    char _dummy[N + 1];  
};
```


Sum

// Helper

```
template<typename, size_t...>  
struct _collector;
```

```
template<size_t... Is, size_t... Ns>  
struct _collector<  
    index_sequence<Is...>, Ns...  
>  
    : _chars<Is, Ns>...  
{ };
```


Sum

```
// Helper  
template<size_t N, size_t... Ns>  
using _sum =  
    integral_constant<size_t,  
        sizeof(  
            _collector<  
                make_index_sequence<N>,  
                Ns...  
            >  
        > - N  
    >;
```


Sum

```
template<size_t... Ns>
struct sum
    : _sum<sizeof... (Ns) + 1, Ns..., 0>
{};
```

- Works with C++14 (C++11).
- This version is `size_t` only, can be extended for integer types.

Sum

```
template<typename T, T... Ns>
struct sum<
    integer_sequence<T, Ns...>
>
    : sum<T, Ns...>
{};
```


Partial Sum

```
template<size_t,  
        typename S,  
        typename =  
            make_index_sequence<S::size()>>  
struct _partial_sum;
```


Partial Sum

```
template<size_t I,  
        typename T, T... Ns,  
        size_t... Is>  
struct _partial_sum<I,  
    integer_sequence<T, Ns...>,  
    index_sequence<Is...>  
>  
    : sum<T, ((Is < I) ? Ns : 0) ...>  
{ };
```


Partial Sum

```
template<size_t I,  
        typename T, T... Ns>  
struct partial_sum  
    : _partial_sum<I,  
        integer_sequence<T, Ns...>>  
{};
```


Partial Sum

```
template<size_t I,  
        typename T, T... Ns>  
struct partial_sum<I,  
    integer_sequence<T, Ns...>  
>  
    : _partial_sum<I,  
        integer_sequence<T, Ns...>>  
{};
```


Exclusive Scan

```
template<typename S,  
        typename =  
            make_index_sequence<S::size()>>  
struct _exclusive_scan;
```


Exclusive Scan

```
template<typename S, size_t... Is>
struct _exclusive_scan<S,
    index_sequence<Is...>>
{
    using type =
        integer_sequence<
            typename S::value_type,
            partial_sum<Is, S>::value...>;
};
```


Exclusive Scan

```
template<typename T, T... Ns>
struct exclusive_scan
    : _exclusive_scan<
        integer_sequence<T, Ns...>>
{};
```


Exclusive Scan

```
template<typename T, T... Ns>
struct exclusive_scan<
    integer_sequence<T, Ns...>
>
    : exclusive_scan<T, Ns...>
{};
```


Exclusive Scan

```
template<typename T, T... Ns>  
using exclusive_scan_t =  
    typename  
        exclusive_scan<T, Ns...>::type;
```


Inclusive Scan

```
template<typename T, T... Ns>
struct inclusive_scan
    : plus<
        exclusive_scan_t<T, Ns...>,
        integer_sequence<T, Ns...>
    >
{};
```


Inclusive Scan

```
template<typename T, T... Ns>
struct inclusive_scan<
    integer_sequence<T, Ns...>
>
    : inclusive_scan<T, Ns...>
{};
```


Inclusive Scan

```
template<typename T, T... Ns>  
using inclusive_scan_t =  
    typename  
        inclusive_scan<T, Ns...>::type;
```


Select

```
template<typename T, T... Ns>
struct _select
{
    static constexpr T arr[] = {Ns...};
};
```


Select

```
template<size_t I,  
        typename T, T... Ns>  
struct select  
    : integral_constant<T,  
        _select<T, Ns...>::arr[I]>  
{};
```


Select

```
template<size_t I,  
        typename T, T... Ns>  
struct select<  
    I, integer_sequence<T, Ns...>  
>  
    : select<I, T, Ns...>  
{};
```


Map

```
template<typename, typename>  
struct map;
```


Map

```
template<size_t... Ns, typename M>
struct map<index_sequence<Ns...>, M>
{
    using type =
        integer_sequence<
            typename M::value_type,
            integer_select<Ns, M>::value...
        >;
};
```


Map

```
template<typename S, typename M>  
using map_t =  
    typename map<S, M>::type;
```


Appendix D

type_select

Type By Index

```
template<size_t>  
struct any  
{  
    any(...);  
};
```

The above ellipsis does not denote a variadic template, it is a C-style variadic parameter.

Type By Index

```
template<typename>
struct get_nth;

template<size_t... Is>
struct get_nth<index_sequence<Is...>>
{
    template<typename T>
    static T deduce(
        any<Is & 0>..., T*, ...);
};
```


Type By Index

```
template<typename>  
struct wrapper;
```

```
template<typename>  
struct unwrap;
```

```
template<typename T>  
struct unwrap<wrapper<T>>  
{  
    using type = T;  
};
```


Type By Index

```
template<size_t I, typename... Ts>
using type_select =
    unwrap<
        decltype (
            get_nth<
                make_index_sequence<I>
            >::deduce (
                declval<wrapper<Ts>*>() ...
            )
        )
    >;
```


Type By Index

```
template<size_t I, typename... Ts>  
using type_select_t =  
    typename  
        type_select<I, Ts...>::type;
```


Appendix E

A better tuple_cat

Tuple 🐱

```
template<size_t M, size_t... Ns>
struct count_less_or_equal
    : sum<size_t, ((Ns <= M) ? 1 : 0) ...>
{};
```

The above should be implemented as a type-alias, but that triggers a bug in GCC 4.x.

Tuple

```
template<typename, typename>  
struct expand;
```

```
template<typename I, typename S>  
using expand_t =  
    typename expand<I, S>::type;
```


Tuple

```
template<size_t... Is, size_t... Ns>
struct expand<
    index_sequence<Is...>,
    index_sequence<Ns...>>
{
    using type =
        index_sequence<
            count_less_or_equal<Is, Ns...>
            ::value...>;
};
```


Tuple 🐱

```
template<size_t, typename>  
struct tuple_select;
```

```
template<size_t I, typename... Ts>  
struct tuple_select<I, tuple<Ts...>>  
    : type_select<I, Ts...>  
{};
```

```
template<size_t I, typename T>  
using tuple_select_t =  
    typename tuple_select<I, T>::type;
```


Tuple 🐱

```
template<typename...>
struct tuple_cat_result;

template<typename... Ts>
using tuple_cat_result_t =
    typename
        tuple_cat_result<Ts...>::type;
```


Tuple 🐱

```
template<
    size_t... Os, size_t... Is,
    typename... Ts>
struct tuple_cat_result<
    index_sequence<Os...>,
    index_sequence<Is...>, Ts...>
{
    using type = tuple<
        tuple_select_t<Is,
            type_select_t<Os, Ts...>>...>;
};
```


Tuple

```
template<typename... Ts>
struct tuple_cat_h
{
    using S =
        index_sequence<
            tuple_size<Ts>::value...>;
    // ...
};
```


Tuple 🐱

```
template<typename... Ts>
struct tuple_cat_h
{
    // ...
    using R =
        make_index_sequence<
            sum<S>::value>;
    // ...
};
```


Tuple 🐱

```
template<typename... Ts>
struct tuple_cat_h
{
    // ...
    using O =
        expand_t<R, inclusive_scan_t<S>>>;
    // ...
};
```


Tuple

```
template<typename... Ts>
struct tuple_cat_h
{
    // ...
    using I =
        minus_t<R,
            map_t<0, exclusive_scan_t<S>>>>;
    // ...
};
```


Tuple 🐱

```
template<typename... Ts>
struct tuple_cat_h
{
    // ...
    using type =
        tuple_cat_result_t<0, I, Ts...>;
};
```


Tuple

```
template<typename R,  
        size_t... Os, size_t... Is,  
        typename Tuples>  
R _tuple_cat(  
    index_sequence<Os...>,  
    index_sequence<Is...>,  
    Tuples t)  
{  
    return R(get<Is>(get<Os>(t))...);  
}
```


Tuple 🐱

```
template<typename... Ts,  
        typename H = tuple_cat_h<Ts...>,  
        typename R = typename H::type>  
R tuple_cat(Ts&&... ts)  
{  
    return _tuple_cat<R>(  
        typename H::O(),  
        typename H::I(),  
        forward_as_tuple(  
            forward<Ts>(ts)...));  
}
```