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CS 161 HW #6

1. (a)  $P(A, B, B)$ ,  $P(x, y, z)$ .  
 $\theta = \{x \mapsto A, y \mapsto B, z \mapsto B\}$

- (b)  $Q(y), G(A, B))$ ,  $Q(G(x), y)$ .

There is no possible unifier because  $x$  cannot have the values of both  $A$  and  $B$ .

- (c)  $R(x, A, z)$ ,  $R(B, y, z)$

- $\theta = \{x \mapsto B, y \mapsto A\}$

- (d)  $\text{older}(\text{Father}(y), y)$ ,  $\text{older}(\text{Father}(x), \text{John})$ .

- $\theta = \{x \mapsto \text{John}, y \mapsto \text{John}\}$

- (e)  $\text{knows}(\text{Father}(y), y)$ ,  $\text{knows}(x, x)$

There is no possible unifier because  $x$  cannot be both a constant and a function.

2. (a) There exists at most one  $x$  such that  $P(x)$   
 $\forall x \forall y ((P(x) \wedge P(y)) \rightarrow x = y)$

- (b) There exists exactly one such  $x$  such that  $P(x)$ .  
 $\exists x P(x) \wedge \forall x \forall y ((P(x) \wedge P(y)) \rightarrow x = y)$

- (c) There exists at least two  $x$  such that  $P(x)$ .  
 $\exists x \exists y ((P(x) \wedge P(y)) \wedge x \neq y)$

- (d) There exists at most two  $x$  such that  $P(x)$ .  
 $\forall x \forall y ((P(x) \wedge P(y)) \rightarrow x \neq y \wedge \forall z (P(z) \rightarrow (z = x \vee z = y)))$

- (e) There exists exactly two  $x$  such that  $P(x)$ .  
 $\exists x \exists y ((P(x) \wedge P(y)) \wedge x \neq y \wedge \forall z (P(z) \rightarrow (z = x \vee z = y)))$

3. (a)  $P(A), (\exists x)(\sim P(x))$ .

Satisfiable because we can have any  $x \neq ! \models A$  to satisfy the condition.

- (b)  $P(A), (A \neq) (\sim P(x))$ .

Unsatisfiable because if  $x = A$ ,  $P(A)$  and  $\sim P(A)$  is a contradiction.

- (c)  $(A \neq) (\exists y)(P(x, y))$ ,  $(A \neq) (\sim P(x, y))$ .

Satisfiable because we can find a  $y \neq x$  to satisfy the condition.

- (d)  $(A \neq) (P(x)) \Rightarrow (\exists x)(P(x))$ .

Satisfiable because for all  $x$ , if you have  $P(x)$ , this implies that at least one  $x$  will be in  $P(x)$ .

(e)  $(A \rightarrow P(x)) \Rightarrow (A \rightarrow (P(x)))$ .

Unatisfiable because for all  $\rightarrow$  you cannot guarantee that  $P(x)$  will imply that all of  $x$  will be in  $P(x)$

4. (a) 1. John likes all kind of food  
 $(\forall x) (\text{Food}(x) \rightarrow \text{Likes}(\text{John}, x))$

2. Apples are food

Food(Apples)

3. Chicken is food

Food(Chicken)

4. Anything anyone eats and isn't killed by is food  
 $(\exists x A(y)) (\text{Eat}(x, y) \wedge \neg \text{Kill}(y, x) \rightarrow \text{Food}(y))$

5. If you are killed by something, you are not alive.

$(A \times E(y)) (\text{Kill}(y, x) \rightarrow \neg \text{Alive}(x))$

6. Bill eats peanuts and is still alive.\*

$\text{Eat}(\text{Bill}, \text{Peanuts}) \wedge \text{Alive}(\text{Bill})$

7. Sue eats everything Bill eats.

$(A \times) (\text{Eat}(\text{Bill}, x) \rightarrow \text{Eat}(\text{Sue}, x))$

(b) 1.  $\neg \text{Food}(x) \vee \text{Likes}(\text{John}, x)$

2. Food(Apples)

3. Food(Chicken)

? 4.  $\neg \text{Eat}(\text{Fly}), y \vee \text{Kill}(y, \text{Fly}) \vee \text{Food}(y)$

5.  $\neg \text{Kill}(\text{Fly}, x) \vee \neg \text{Alive}(x)$

\* 6.  $\text{Eat}(\text{Bill}, \text{Peanuts}) \wedge \text{Alive}(\text{Bill})$  \* can break it

? 7.  $\neg \text{Eat}(\text{Bill}, x) \vee \text{Eat}(\text{Sue}, x)$

(c) 8.  $\neg \text{Eat}(\text{Fly}, y) \vee \text{Food}(y) \vee \neg \text{Alive}(\text{Fly})$  [4]

\* 9.  $\text{Eat}(\text{Bill}, \text{Peanuts})$  \* break up b

\* 10.  $\text{Alive}(\text{Bill})$  \* break up b

11.  $\text{Food}(\text{Peanuts}) \vee \neg \text{Alive}(\text{Bill})$  [8, 9]

$\Theta = \{y / \text{Peanuts}, \text{Fly} / \text{Bill}\}$

12.  $\text{Food}(\text{Peanuts})$  [10, 11]

13.  $\text{Likes}(\text{John}, \text{Peanuts})$  [11, 1]

$\Theta = \{x / \text{Peanuts}\}$

Hence, John likes peanuts.

3) (e)  $(A \times) P(x) \Rightarrow A$   
Universal

(d) "What food does Sue eat?"  
14. Eats(Sue, Peanuts) [9, 7]

$\Theta = \{x / \text{Peanuts}\}$   
Thus, Sue eats Peanuts.

(e) Use the following.

- 1) If you don't eat, you die.
- 2) If you die, you are not alive.
- 3) Bill is alive.

1)  $(A \times \exists y) (T \text{Eats}(x, y) \rightarrow \text{Die}(x))$   
CNF: Eat, ( $x, F(x)$ )  $\vee$  Die( $x$ )

2)  $(A \times) (\text{Die}(x) \rightarrow T \text{Alive}(x))$   
CNF:  $\neg \text{Die}(x) \vee T \text{Alive}(x)$

3)  $\text{Alive}(\text{Bill})$

CNF: Alive(Bill)

Our new knowledge base is as follows:

1.  $T \text{Food}(x) \vee \text{Likes}(\text{John}, x)$

2. Food(Apples)

3. Food(Chicken)

4.  $T \text{Eats}(F(y), y) \vee \text{Kills}(y, F(y)) \vee \text{Food}(y)$

5.  $T \text{Kills}(F(x), x) \vee T \text{Alive}(x)$

6.  $T \text{Eats}(\text{Bill}, x) \vee \text{Eats}(\text{Sue}, x)$

7.  $\text{Eats}(x, F(x)) \vee \text{Die}(x)$

8.  $T \text{Die}(x) \vee T \text{Alive}(x)$

9.  $\text{Alive}(\text{Bill})$

10.  $T \text{Die}(\text{Bill}) [8, 9]$

$\Theta = \{x / \text{Bill}\}$

11.  $\text{Eats}(\text{Bill}, F(\text{Bill})) [10, 7]$

$\Theta = \{x / \text{Bill}\}$

12.  $\text{Eats}(\text{Sue}, F(\text{Bill})) [11, 6]$

$\Theta = \{x / F(\text{Bill})\}$

This means Sue eats at least what Bill eats.

Since we do not know exactly what Bill eats, we cannot draw conclusions.