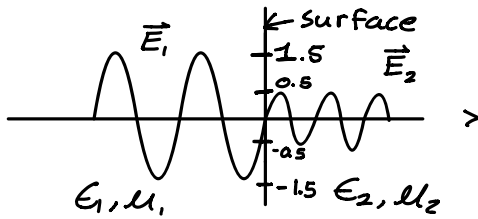


## 8.2

Given  $\epsilon_2 = 9\epsilon_0$ ,  $\epsilon_1 = \epsilon_0$ .



$$\vec{E}_1 = \vec{E}_{inc} + \vec{E}_{ref}, \quad \vec{E}_2 = \vec{E}_{trans}$$

Maxwell's Boundary Conditions state

$$E_1'' = E_2'' \quad , \quad E_1^+ = E_2^+ = 0 \quad * \text{ direction of propagation is } \perp \text{ to surface}$$

$$E_I + E_R = E_T \quad * \text{ Let } E_I = E_1^+, E_R = E_1^-, E_T = E_2^+ \text{ (no } E_2^- \text{ exists since wave is coming from left to right)}$$

$$E_1^- + E_1^+ = E_2^+$$

\* From Griffiths the Reflected & Transmitted amplitudes are solved in terms of the incident amplitude for normal incidence as:

$$\tilde{E}_R = \left( \frac{1-\beta}{1+\beta} \right) \tilde{E}_{OI} \quad , \quad \tilde{E}_T = \left( \frac{2}{1+\beta} \right) \tilde{E}_{OI}$$

where  $\beta = \frac{\mu_1 v_1}{\mu_2 v_2}$  &  $v_1$  &  $v_2$  can be defined in terms of  $\epsilon$  &  $\mu$

$$v = \frac{1}{\sqrt{\epsilon\mu}}$$

$$v_1 = c \quad \& \quad v_2 = \frac{c}{3} \quad * \mu_1 = \mu_2 = \mu_0 \quad \& \quad \epsilon_2 = 9\epsilon_1$$

$$\beta = \frac{\mu_0 c}{\mu_0 \frac{c}{3}} = 3$$

$$\therefore \tilde{E}_T = \left( \frac{2}{4} \right) E_{OI} = \frac{1}{2} \tilde{E}_{OI}$$

$$\tilde{E}_R = -\left( \frac{2}{4} \right) E_{OI} = -\frac{1}{2} \tilde{E}_{OI}$$

Analyzing the peak-to-peak amplitude of Transmitted wave:

$$1 = \frac{1}{2} E_{OI}$$

$$\therefore E_{OI} = 2 \frac{V_{pp}}{m} \quad * V_{pp} = \text{Voltage peak-to-peak amplitude}$$

$$\therefore E_{OR} = -1 \frac{V_{pp}}{m}, \quad E_{OT} = 1 \frac{V_{pp}}{m}$$