Homework 3 Solutions

Problem 1

A) Loss Function = $\sum_{i=1}^{11} (p(x_i; A_{12}, A_{21}) - p_i)^2$

OLS exists when:

- X^TX is invertible
- N < p
- $N \ge p$ but X*w=0
- Linear model

$$y = \exp(a_1 + a_2 x + a_0)$$

 $dy/da = \exp(a^T x) * [x1 x2 1]$

gradient is still a function of a and so is not linear meaning we can't use Least Squares for this model

B) Output:

```
Loss for current set is = tensor(0.6702, grad_fn=<SumBackward0>)
New set of A values = tensor([1.9584, 1.6892], requires_grad=True)

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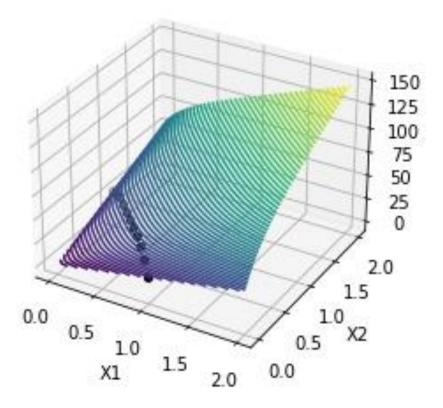
The final data sets for A = [1.958413  1.6891907]
The loss at this location = 0.6702072
The gradiant at this location = tensor([0., 0.])
```

Code is in the python file labeled Homework 3.py

C) The loss couldn't be reduced to zero, so some error still exists between the actual model and the optimized model. However, this loss is minimal and only depends on how accurate you need the model to be as the loss between each point is in the hundredths or thousandths

p_pred 36.8673 36.74983 36.39044 28.1 34.4 36.7 36.8 36.7 36.5 35.4 32.9 27.7 17.5 p_actual 36.9 0.52432 0.059678 0.061033 0.001069 0.005476 0.002483 0.012003 0.00023 0.002285 0.000902 0.000715 loss pred loss 0.670194

Plot of the model with the measured data points:



Problem 2

```
Output:
```

```
Using Bayesian Optimization on the function returns: X1 = 0.0918079780344101  
X2 = -0.7167301500347611  
Y = -1.0314847263331826  
With a gradient = [ 0.01124661 -0.06532344]  
Using gradient descent to refine values returns: X1 = 0.09077434518912046  
X2 = -0.7132673143955719  
Y = -1.0316225759431568  
With a gradient = [0. 0.]
```

Code is in the python file labeled Homework 3.py