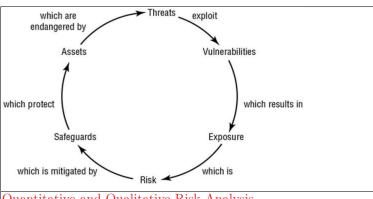
Asset	CIA triad
	The primary goal of Security infrastructure:
Information, Systems, Devices, Facilities, Personnel, Intellectual Property	- Confidentiality: prevention of unauthorized access to data
Confidentiality:	no matter if the data is in transit, in storage or in process
Military / Government confidentiality:	Usually done with encryption and access control
- Top Secret: drastic effects / grave damage to national security	- Integrity: prevention of unauthorized alteration of data
- Secret: significant effects / critical damage to national security	Data integrity: data is complete, consistent and accurate
- Confidential: noticeable effects / serious damage to national security	System integrity: System only does what it was intended to do
- Sensitive but unclassified: internal use	Usually done with hash verification, intrusion detection
- Unclassified: public data	- Availability: Systems should be accessible at all times
Commercial / private confidentiality	Usuall done with Redundancy, backups
, -	Nonrepudation & Accountability
	Nonrepudation ensures that every action can be traced to the actual source
	This prevents attackers from covering their actions. Accountability ensures that every being is responsible for their actions.
	E.G. Nonrepudation ensures Accountability.
· · · · · · · · · · · · · · · · · · ·	Usually done with certificates, session identifiers, logs, etc
- v	Data Classification
Simple tools can recover this data!	- Data in Use, Transit, Rest
- Clearing: Overwrites the data to delete it, usually with a single character	used by application, tranit via x, rest = storage, HDD, SSD
Can not be recovered using simple tools	- Personally Identifiable Information PII
- Purging: Clearing, but overwrites multiple times to make recovery harder	information to identify a person, name, social security number etc
This method might also include others such as degaussing. It is Irrecoverable	- Protected Health Information PHI
- Degaussing: Strong magnetic field that can wipe data from an HDD	Health Information recorded in any form.
(SSD, CD, etc not affected!)	- Proprietary(Trash) Data
- Destruction: Destroy the physical hardware of said data. Irrecoverable.	microtroll windoof, appul
Tracing and Hiding sensitive Data	Threats
- Steganography: Embedding a Message within a file	- Threat: A potential danger to an asset
- Watermarking: unique identifier, that usually can't copied, or mutated.	Threat intelligence: Knowledge about emerging or existing threats
Often used in Documents, movies, etc to stop counterfeits.	Thrat event: Accidental or malicious exploitation of a vulnerability
STRIDE Model	Vulnerability Common Vulnerabilities and Formance (CVF)
- Spoofing: Using a false identity to gain access to a system.	- Common Vulnerabilities and Exposures (CVE)
- Tampering: unauthorized changes/manipulation of data - Repudation: The ability to deny having performed an attack,	Industry wide standard identification number for Vulnerabilities - Common Vulnerability Scoring System (CVSS)
to others being blamed.	Uses the CIA triad to score vulnerabilities on severity
~	Risk
	Assessment of the possibility that a threat will exploit a vulnerability
	Realized Risk
	A threat actor has now taken advantage of a vulnerability
	The whole point of security is to stop exactly this.
Copyright	Risk Management
Protects these works: Literay, musical, dramatic, choreographic,	- Identifying vulnerabilities
graphical, sculptural, audiovisual, recordings, architectural works	- evaluating importance of data and countermeasure cost
Computer software is in the literary works category	- Implementing cost effective countermeasures
	Risk management is the balance of threat/risk and usability
	In other words, only implement measures that are necessary
	Some data is not worth protecting, and some systems can be replaced easily.
	Others are sensitive, or fundamental, these must be preserved at all costs.
	Risk Analysis Evaluation aggregation to aggregate to aggregate
Trademark Protects: Slogans, Logas, words used to identify something	- Evaluation, assessment, assignment of value to assets
Protects: Slogans, Logos, words used to identify something Implicit Trademark is automatically granted if you use the ™ symbol	- Examining environment for risks
Explicit Trademark is automatically granted if you use the "symbol Explicit Trademark has to be obtained from the government	 Evaluating the likelihood of a threat event occurring Assessing the cost of countermeasures
and lets you use the ® symbol.	- Assessing the cost of countermeasures - present cost/benefit report to upper management
	Asset Valuation
	The representation of an asset in currency
	This can include things such as repair costs, maintenance costs, etc
	Exposure
	Possibility of an asset loss due to a threat
	exposure factor (EF) checks how serious that loss would be
	Attack
	The intentional try to exploit a vulnerability
This means, while you are not protected by the law, as long as this information	Breach
stays within your company, it will be protected forever.	The circumvention of security measures by a threat actor.
Likely the "best way" to protect computer software, aka proprietary trash	A breach combined with an attack, can result in penetration



Quantitative and Qualitative Risk Analysis

-Quantitative Risk Analysis:

assignment of real dollar figures to loss of assets

-Qualitative Risk Analysis

The subjective / intangible worth value to the loss of assets

Both methodologies are necessary for complete risk analisys!

Quantitative Risk Analysis

Assign Asset Value (AV) what is this data/etc worth? how much would be lost in case of a breach? Calculate Exposure Factor (EF) how much data is affected? what happens in case of 1 breach Calculate single loss expectancy (SLE) breaches over the year? Derive the annualized loss expectancy (ALE) Perform cost/benefit analysis of countermeasures

Exposure Factor (EF): percentage of loss by realized risk

Single Loss Expectancy (SLE): Cost of single realized risk

SLE = EF * Asset Value (AV)

Annualized Rate of Occurrence (ARO):

expected frequency of a risk within a year

Annualized Loss Expectancy (ALE):

Expected yearly cost of Losses due to realized risks

ALE = SLE * ARO

If you implemented a safeguard, you have to recalculate the ARO.

The entire idea of of security is to reduce the ARO!!

The EF usually remains the same

Safeguard Costs

First, compile a list of safeguards against each threat.

Assign each safeguard a deployment value -> Annual Cost of Safeguard (ACS)

- Safeguard Cost/Benefit

ALE without safeguard - ALE with safeguard - ACS = Value of safeguard if the value of safeguard is below 0, then it is financially irresponsible

Note that this only takes in the financial damage since this is Quantitative!

Dealing with Risk

Risk Mitigation Implementation of safeguards in order to eliminate vulnerabilities or block threats

Risk Assignment / Risk Transferring

purchasing insurance or outsourcing. Transfer the cost of risk to other entity

Risk Acceptance Doing nothing as cost/benefit would be low

Risk Deterrence auditing, cameras, security guards, warnings, etc

Risk Avoidance Not using the system associated with the risk

Risk Rejection Simply ignore risk without cost/benefit analysis!

Residual Risk A countermeasure might not fully eliminate a risk

This is the remaining risk that we have decided to accept.

Privacy

GDPR

- Companies have inform authorities in case of serious data breaches
- Individuals have the right to demand their data from companies
- Individuals have the right to be forgotten (deletion of data)
- EU tries to enforce this globally
- enforces pseudonomization
- Patriot act
 - blanked authorization of surveillance of an individual with 1 warrant
 - ISP have to provide data
 - easier wiretapping

pseudonomization replacement of data with aliases

This makes it harder to identify a person from said data

anonymization Complete obfuscation of an identity

Access Control

Subject The Requesting party

Note, this can be a person, a program, a process, etc.

Object The requested "object"

Databases, programs, files, etc

Access Control The management of the relationship

Between Subject and Object

Preventive Access Control

Stops unwanted access to Objects

Detective Access Control

Detects unwanted access to Objects after it has occurred

Corrective Access Control

Restores the last "correct" state after unwanted access

Deterrent Access Control

discourages unwanted access to Objects

Directive Access Control

Directive issued by company. -> Don't click on links.

Compensating Access Control

Controls used in addition/ as a replacement. Can be any control measure

Recovery Access Control

More advanced version of corrective control

Physical Control

Control of items that one can physically touch

Technical / logical Control

Hardware or Software mechanism for access control

Administrative Control

Policies and Procedures created by a Company

Steps of Access Control

1. Identification

Providing an identity to enforce Nonrepudation.

is usually public information.

username, tokens, fingerprints, facial recognition

2. Authentication

Often used in combination with Identification.

Verifies the identity. Usually a password, or token.

3. Authorization

Controls what a user is allowed to do and what they aren't

There are different ways of controlling this. (Check next page)

4. Auditing

Record all actions by all Subjects in order to hold them accountable

5. Accounting (Accountability)

This would mean taking actions against a person,

that has acted in bad faith/maliciously

Keep in mind that you need a strong system of identification, and auditing

in order to actually win in a court of law against the bad actor!

Authentication Factors

- Type 1: Something you know
- Type 2: Something you have, ex. a Device, smartcard, etc
- Type 3: Something you are/do, ex. Fingerprint, face, etc.

Type 1 is the weakest form of authentication and type 3 the strongest!

- Location

This is a form that is used in combination with others.

Ex: A certain IP might be a requirement to log into one of your systems

Or your bank might block a transaction if it isn't from your country of residence

Multifactor Authentication

Multifactor Authentication simply uses more than one type to authenticate

This might be a password(Type1) and a token(Type2)

The strongest form of authentication if therefore all 3 types together!

Passwords

Passwords are never stored in plain text,

they might be stolen easily with 1 breach

Instead, they are saved with a hash-algorithm,

makes them nearly useless to threat actors

Unless they also have the access to said algorithm.

Types of passwords:

Plain Password

use numbers, characters and special symbols with a length of at least 10.

10 characters -> 928 years of cracking!!

Don't use personal information such as names etc.

PassPhrases

Passphrases are chained words that are easy to remember

It is important to have a longer passphrase than a regular password!

Still use special symbols. Also try to include random upper-lower case spelling

Or leadspeak s1nc3 that 1s qu1te 3ff3ct1v3!!

- Cognitive Passwords

A series of personal questions. -> what is the name of your first pet?

Best way to do this is letting users create both the question and the answer!

- SmartCards

Card used for identification / authentication. Often integrates key encryption Usually temper resistant

One downside, loss of card might give a threat a window of exploitation!

- Tokens

Generated by a special Device.

Regular password generators: any device can take that place. ex. smartphone

- Synchronous Dynamic Token

Time-based One-Time Password (TOTP)

Device generates Token every x seconds.

- Asynchronous Dynamic Token

HMAC-based One-Time Password (HOTP)

Device generates one time token based on algorithm. Stays until used!

Access Control Models (Authorization)

- Discretionary Access Control (DAC)

Every object has an owner, and that owner can to grant or deny permissions

NTFS from windoof uses this

- Role Based Access Control

Permissions are assigned to roles not users. Users are assigned to roles.

Users who are in a role with said privileges can use them.

- Rule Based Access Control

Global rules that are applied to all subjects

Good example is a firewall, which applies said rules equally to all subjects

– Attribute Based Access Control

Similar to Rule based Control but with additional attributes

This could give one subject more rights than another

- Mandatory Access Control

Use of labels applied to both subject and Object

If user has the same label as a file, then user has access to it.

Authorization Mechanism

- Implicit Deny

Deny everything that hasn't been specifically allowed

Most used!

- Constrained Interference

Applications might hide functionality based on the privileges of a user

Access Control Matrix

This writes Objects, Subjects and privileges into a table

If Subject tries to access an object the table for said object is checked

- Capability Table

This is the same as the Access Control Matrix but with a subject focus In this table the subject and all accessible Objects are written down

- Content-Dependent Control

Constrict Access to the data within an Object

In a database a user might be able to check table 1 but not table 2.

While the object is the entire database!

Context-Dependent Control

Give a subject access depending on what the subject does

Ex. The checkout button in an online shop only works, if you have something in the shopping cart.

Need to Know

Subjects should only have access to Objects they need to do their job.

– Least Privilege

Subjects should only have the privileges they need to do their job.

- Separation of Duties and Responsibilities

No single person should have total control over the entire System!

Common Access Control Attacks

- Access Aggregation Attacks (Passive Attacks)

This is the collection of nonsensitive data, that combined could give a threat actor the opportunity to launch a proper attack.

Ex. IP address, open ports, Operating System -> specific exploit

- Password Attacks (Brute Force)

Spam random sequences until you get the right one

- Dictionary Attacks (Brute Force)

Try passwords from a list of passwords, example leaked password list.

Can also be done with list of common passwords, or slightly changed previous passwords (One-Upped-Passwords -> 1 character changed)

- Birthday Attack (Brute Force)

Try to get the same hash as the password with a different sequence

Can be mitigated by using better hashing algorithms. SHA-3 instead of $\mathrm{md}5$

Note the attacker needs access to the hash in order for this to work!

- Rainbow Table Attacks

Combines the Birthday attack with a table of precomputed hashes.

This is then used to compare to a password hash list.

- Sniffer Attacks

Threat actor analyzes data sent over network with a sniffer tool.

A good example for this is wireshark

Can be mitigated by using encryption and One-Time passwords encryption makes the data useless and One-Time passwords are as well

- Spoofing Attacks

Pretending to be something/someone else. Ex. pretending to be router.

Social Engineering Attacks

Gaining and then misusing trust of someone.

Indian accent you get refund if you buy me 2 cards from target

- Shoulder Surfing (Social Engineering)

Reading information on a screen from a persons back.

- Phishing (Social Engineering)

Trick a Person to click on a fake link to log in, giving the attacker all the credentials to log-in

- Spear Phishing (Social Engineering)

Targeted Phishing at a group. Ex. Employees at company x.

- Whaling (Social Engineering)

"Phishing für grosse Fisch" -> CEOs etc

- Vishing (Social Engineering)

Phishing via VOIP or instant messaging

Protection Mechanism

- Layering (defense in depth)

Multiple Controls in Layers, if one fails, there are still the other ones

– Abstraction

Combining Objects into groups in order to simplify permission management

- Data Hiding	Manually set IP address (abando): edit /etc/network/interfaces	
Storing Objects in compartments that can't be seen / accessed	Configure SSH: edit /etc/ssh/sshd_config	
by an unauthorized subject	For birbs sake, use a nonstandard port for ssh :)	
– Security through Obscurity	Check current shells: ps	
Not informing a subject about an object, and hoping it will stay hidden	Check current processes: htop	
- Encryption	grep read lines	
Turning data into gibberish via algorithms.	grep 'Warning' /var/log/rkhunter.log	
Red-Team	Read Lines: awk 'sshd.*invalid user/ {print \$11}' auth.log	
Offensive Cyber-Security: simulate attacks – Think outside the box	bit-by-bit copy: dd if= <media partition=""> of<image_files></image_files></media>	
	mount - o ro,noexec,loop evidence_01 /mnt/investigation mount with read only and no execution	
Find new ways and tools and attack systems to show the flaws — Deep Knowledge of Systems	Check recently changed files ls -lasrt	
Deep Knowledge of Systems Deep Knowledge about systems, flaws, exploits, methodologies,etc	PID	
always up-to-date with technology	The unique identifier the kernel gives each process	
- Software Development	This shows both background and foreground applications	
Learn how to develop your own tools.	logs	
- Penetration testing	Logs capture every single action on linux, this can be used to detect bad actors.	
Identify vulnerabilities and potential threats	However, logs can also be spoofed, which means you always have to be sure, that	
– Social Engineering	everything is being logged, and that no logs have been tampered with.	
Blue-Team	notable logging systems/files: syslog, rsyslog, var/log ,auth.log	
Defensive Cyber-Security: prevent attacks	The shred command with -f and -n force deletes log files.	
- Organized and detail-oriented	Mainly used like this: shred -f -n 15 /var/log/auth.log*	
Prevent gaps by thinking about EVERYTHING — Cybersecurity Analysis and threat profile	This shreds 15 lines from every log file with the name auth.log(something)	
Assess the security of an organization. Create Risk/Threat Profiles.	other things to look out for: - set-UID Rogue Files	
- Hardening Techniques	- Directories with .something Hidden	
Reduce the attack surface hackers might exploit	- Regular files in the /dev directory	
– Knowledge about detection Software	- Recently modified files ls -lasrt	
Be familiar with software that recognizes unauthorized actions	Schedules Tasks	
low skill application would be rkhunter.	Schedules tasks can be written either in cron.d or with systemd	
- Security Information, Event Management (SIEM)	IP-Tables	
Software that allows real-time analysis of security events	name one reason not to use ufw	
Linux	Flush all rules: iptables -F	
Adding user: usermod -m username -s /path/to/shell	Block Input: iptables -P INPUT DROP	
Change shell: chsh -s /path/to/shell Change password: passwd username	Block Output: iptables -P OUTPUT DROP	
Change password: passwd username Add user to group: usermod -a -G groupname username	Block Forward: iptables -P FORWARD DROP	
Change file permission: chmod permission file	Allow Port: iptables -A INPUT/OUTPUT -p portother shit	
Change file owner: chown file user/group	Show rules: iptables -L -n -v - line-numbers	
Check IP address: ip addr / ip -c -brie a	Sticky Bit	
DNS query: dig domain (dig shitgaem.online)	This is a single bit in front of rwx> 1777 sticky set, 0777 sticky not set	
– File System Permissions	The interpretation of this bit depends on the file type For directories, it means that any files within that folder	
r = read, w = write, x = execute	May only be renamed or deleted by the owner.	
Every single file has these attributes.	For files this bit is deprecated!	
These attributes are also duplicated for 3 different types of users.	Security Enhanced Linux (SELinux)	
1. owner, 2. group of owner, 3. other This property the actual promission would lead like this.	This is a module created by the NSA that implements types,	
This means the actual permission would look like this:	which mark files based on the type of a subject.	
Read, write, and execute permissions	Ex. a top-secret process can create a file with chmod 777,	
"-": file for the group members owning the	but a confidential process still can't open it.	
"I'" : link file	This is called MLS in SELinux and is related to Multi Category Security (MCS)	
	Snort	
- r w - r w - r	Detection software like rkhunter	
	NetCat	
	This can be used for anything dealing with TCP and UDP.	
Read, write, and execute permissions execute permissions	You can also use it to control compromised systems	
for the owner of the file	Reverse Shell The idea is given the starting connection comes from the victim	
	The idea is, since the starting connection comes from the victim, Not only do we not have NAT and firewall problems, the connection	
- r w x 000=0 100=4	also looks more legit than when we connect.	
001=1 101=5	This gives a hacker some sort of legitimacy on that system.	
	Scapy	
1 1 1 010=2 110=6	Tool used to send, sniff, dissect and forge IP packets.	
011=3 111=7	You can probe, scan and attack networks	
	You can attack signature for IDS/IPS systems	

Encryption Terms

- Plain Text: unencrypted message

- Ciphertext: encrypted message

Cipher: Algorithm used to encrypt

Cryptographic key: Just a number to decrypt a message

The range is defined by the algorithm. 0 to $2^{n}\,$

A key with 128 bits would have a range of: 0 to 2^{128}

It is critical to keep the keys secret!

One-Way Function:

mathematical function that produces output in a way that input can't be retrieved.

There is no TRUE One-Way-Function

Cryptography works on the believe that it can't be broken RIGHT NOW

However, this does not mean it will stay so forever, see already broken ciphers

Reversability: The option of encryption....

Nonce: A Public, unique One-Time-Use Number

Makes sure a key is not re-used twice!

- Initialization Vector (IV): A random bit string

Same length as the block size and is 'XORed with the message'

IVs are used to create a unique ciphertext with the same key

- Confusion:

This is the case when encryption is so complicated,

that merely reforming the string doesn't reveal the message

Aka bruteforce doesn't work anymore.

Diffusion:

A change in the plaintext will result in multiple changes in the ciphertext.

The Kerckhoff's Principle

This means everything about the system is public but the key

It therefore requires the system to be secure even under these circumstances

The idea is that public algorithms may hasten the improvements on them

- Permutation Swapping Bytes around
- Byte Substitution Replacing bytes with others

SP-Networks algorithm that uses repeated Permutations and Substitutions

Permutations and Substitutions are combined to a round

Rounds are then repeated many times

Caesar Cipher or ROT3

One of the earliest encryption systems

Simply shifts a chracter by 3 A to D, B to E...

One-Time-Pad

Create a key with the same length as the message

XOR each message bit with each key bit

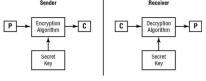
This Cipher is UNBREAKABLE!

However it is not practical.. 1GB file 1GB key...

No proper way to transmit, store a key

Using a key twice == Cipher broken

Symmetric Cryptography



- Same key for encrypting and decrypting

- Shared key for all parties involved!

If one leaks the key, the cipher is broken!

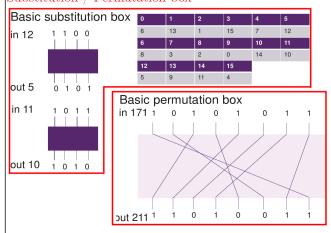
- Doesn't confirm identity!

Anyone who has the key can pretend do be another

Stream Ciphers Key Nonce $K_0, K_1, K_2, ...$ $M_0, M_1, M_2, ...$ $K_0, K_1, K_2, ...$ $K_0, K_1, K_2, ...$

- + Encryption of long continuous streams, of possible unknown length
- + Extremely fast with low memory footprint, ideal for low power devices
- + If designed well, it can seek to any location in the stream
- The keystream must appear statistically random
- You must never reuse a key + nonce
- Stream ciphers do not protect the ciphertext (no guaranteed integrity)

Substitution / Permutation box



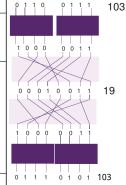
Block Cipher

Takes in an input of a fixed size and returns an output of the same size

- Diffusion and Confusion
- SP-Network

Advanced Ecryption Standard (AES) is a Block Cipher

Here is a Block Cipher works:



0	1	2	3	4	5
6	13	1	15	7	12
6	7	8	9	10	11
8	3	2	0	14	10
12	13	14	15		
5	9	11	4		

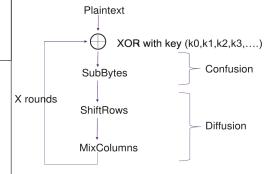
Basic SP- Decryption and Network encryption

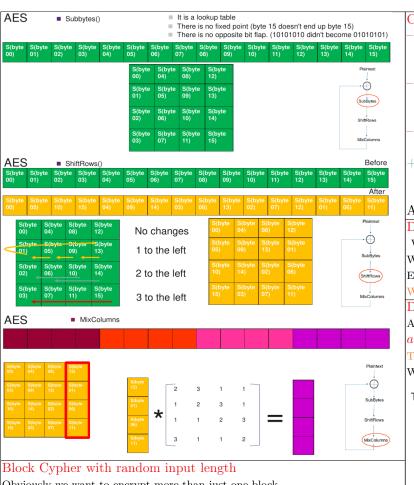
AES

Built around the Rijndael algorithm

Superceedes the DES as a standard

- SP-Network with 128-bit block size
 - » Key length 128,192,256 bit
 - » 10, 12 or 14 rounds
 - » Each Round: Substitute Bytes, ShiftRows, MixColumns, KeyAddition





Obviously we want to encrypt more than just one block

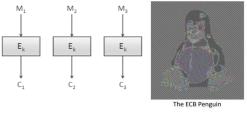
- How do we do that?
- Electronic Code Block (ECB)
- Cipher Block Chaining (CBC)
- Counter Mode (CTR)

Electronic Code Block (ECB)

Just encrypt block after block.

However, this might give away the bigger picture

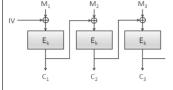
Aka the pattern of the data is still visible!!



Cipher Block Chaining (CBC)

XOR each output with the next block.

not parallelizable, but more secure than ECB



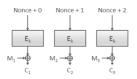
Counter Mode (CTR)

Encrypt a counter (Nonce) to produce a stream cypher

Encrypted Nonce is then XORed with the plain text

parallelizable!!

Standard for all AES ciphers!



Cons and Pros of symmetric Cryptography

Key distribution

Keys have to be shared securely, anyone who has the key can encrypt and decrypt all messages (sent by that key)

– No Nonrepudation

Because everyone who has the key can encrypt and decrypt, there is no guarantee that this message is from a trusted source.

– No message Integrity

If the message gets damaged, then there is no recovery inbuilt.

+ Speed

often 1000 to 10000 times faster than asymmetric algorithms

Lots of processors have an AES intruction set.

Alternatives: Chacha20 cipher

Diffie-Hellman

With this method the problem of sharing a key over the internet is solved. We can now do so without any worries of giving a malicious third party access. Every TLS handshake is in some way powered by this.

We are not actually exchanging a key, only some mathematical part of it!!

Discrete Logarithm

A logarithm that is implicit when using mod.

$$a^b (mod n) = c == b = \log_{a,n}(c)$$

These are harder to calculate than regular ones!

Which is why they are used in Diffie-Hellman!

■ 3× mod 7 = 1, what is x?

This leaves us having to brute force the answer

- Brute force:
 - $3^1 \pmod{7} = 3 \pmod{7} = 3$
 - $3^2 \pmod{7} = 9 \pmod{7} = 2$
 - $3^3 \pmod{7} = 27 \pmod{7} = 6$
 - $3^4 \pmod{7} = 81 \pmod{7} = 4$ = $3^5 \pmod{7} = 243 \pmod{7} = 5$
 - 36 (mod7) = 729 (mod 7) = 1

What if mod 7 was mod some 2000 bit number

Primitve Root

A number g is a primitive root of p when:

 $\bigvee_{k=0}^{p} g^{k} \mod p = \text{Distinct from each other}$

In other words, every single result from the modulo must be different!

Diffie-Hellman Example

1. Agree on Parameters

Alice and Bob agree on a large prime p and a second prime / primitive root g p is usually at least 2048 or 4096 bits

2. Select Private Numbers

Alice picks the random number a

Bob picks the random number b

- » private numbers are between 1 and p
- » If p is 2048 bits, then you are guessing a number with 2048 bits, have fun :)
- » They NEVER tell each other the private number
- 3. Alice and Bob each calculate a Public Key
- » Alice calculates key: $g^a \mod p$
- » Bob calculates key: $g^b \mod p$

Because we are using a discrete logarithm, it is mathematically infeasible to get the private numbers by calculation.

4. Alice and Bob exchange the Public Keys

These are simple the calculated versions of keys.

5. Alice and Bob calculate the shared key

for both this is: $q^{ab} \mod p$

The shared key is therefore the same for both parties

6. Calculate Master Secret

The shared key is also called the Pre-Master

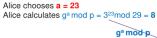
This is because the shared key is quite big and

not often used to encrypt directly

It is instead used to control sessions after it has been hashed

The hashed shared key is then called the Master Secret

Alice and Bob agree on g = 3 and p = 29



Bob chooses b = 12Alice calculates $g^b \mod p = 3^{12} \mod 29 = 16$

Alice calculates: (gb)amod 29 = 1623 mod 29 = 24 Bob calculates: (ga)b mod 29 = 812 mod 29 = 24 The shared secret is 24

Public Private

Eliptic Curve Cryptography

- Elliptic curves are a drop-in replacement for the mathematics underpinning regular Diffie-Hellman.
 - If you look into your browser, you see something like ECDHE
 - Elliptic curve Diffie Hellman is now becoming the standard
- Elliptic curve is a two dimension curve
 - y2=x3+ax+b
 - The private key is a number
 - The public key is composed of two numbers(X,Y) number
 - Elliptic curves are much stronger than traditional public-key schemes for the same key length.

Symmetric	Diffie-Hellman and RSA	Elliptic Curve
56	512	112
80	1024	160
112	2048	224
128	3072	256
192	7680	384
256	15360	512

Ephemeral Mode

For Diffie-Hellman this means calculating a new key for every session

This is also called Perfect Forwarding Secrecy

The reason for this is that calculating this key costs close to no power

So why not just create a new one for every session to increase security?

This is usually done every browser refresh etc.

It is also automatically done after a certain time, again to improve security

RSA Rivest-Shamir-Adleman

- Public Key cryptosystem
- widely used for secure data transmission
- Most common method for public cryptography
- Offers Nonrepudation!!
- Reverseable Keys

Both the public key and the private key can be used to encrypt or decrypt. It just has to be the inverse at the other end.

Encrypt pub-key -> decrypt priv-key | encrypt priv-key -> decrypt pub-key

- The reverseable keys lead to 2 operating Modes
- 1. Encrypt so only the receiver can read

If I want to send a message to the server that only said server can read, then I can encrypt my message with the servers public key.

The server then uses its private key to decrypt. Not even you can decrypt it:P

2. Nonrepudation Mode

By encrypting with the private key, everyone who has the public key can read.

However, it guarantees that said message is from you, and no one else!

Prime Factorization

Every non-prime number has a prime factorization

This means every non-prime number can be created by multiplying x primes

Prime factorization of 30 -> 5 * 3 * 2

Calculating the prime factorization is EXTREMELY HARD for big numbers

In other words, it is not feasible to calculate it with a current Computer

Which is why it is used by the RSA algorithm

RSA Functionality

Public keys: e n Prime factors: p1,p2

Private key: d

Message: m

e is almost always 3 or 65537 n is a random Prime factorization of 4096 bits

 $d = \frac{k * \phi(\mathbf{n}) + 1}{}$

where k is a random integer p1,p2,d must be private!!

- Encrypting: - Combined

 $c = m^e \mod n$ $m^{ed} \, mod \, n = m$

- Decrypting:

 $m = c^d \mod n$

The PHI Function

■ Euler has studied the distribution of prime numbers and invented the PHI function

It outputs how many integers are less than or equal to n that do not share any common factor with n. $\phi(7) = 6$ 1234567

12345678

In red, the numbers that are relatively prime with n.

where k is an integer

PHI = prime - 1 $\Phi(21377) = 21376$

counts for prime:

■ Euler theorem $m^{\phi(n)} = 1 \mod n$

 \Rightarrow ed = $(k^*\phi(n)+1)$ $m^{k^*\phi(n)} = 1 \mod n$ $d = (k*\phi(n)+1)/e$ $m^*m^{k^*\phi(n)} = m \mod n$ $m^{k^*\varphi(n)+1}=m \ mod \ n$

- It is computationally infeasible to calculate a private from a public key.
- This is achieved through intractable mathematical problems
- In order to calculate $\phi(n)$ easily, you have to know p1 and p2 where p1*p2=n

Using RSA

- 1. Choose two very large Primes
- Alice randomly generates a prime number p1
- then a second randomly generated number p2
- Alice calculates n

Alice hides p1 and p2 (p1 and p2 are secret)

- n is public
- 2. Calculate PHI

 $\phi(n) = \phi(a) * \phi(n)$

a and b are the prime factorization primes!

if number is prime, then: $\phi(a) = a - 1$

Ex. n = 77, a = 11, $b = 7 -> \phi(77) = \phi(11) * \phi(7) = 10 * 6 = 60$

3. Choose k and e to calculate d

 $d = \frac{k * \phi(n) + 1}{1}$ with k being an integer

Ex. n=55, e=7, k=4, $\phi(n) = 40$ $d = \frac{4 * \phi(55) + 1}{7} = 23$

RSA quirks

Very weak with short messages

To mitigate this, padding is added

Optimal assymetric Encryption Padding (OAEP) is used pseudo random padding that introduces an IV then hashes it Server has to create same padding to check if it matches up

Not common to encrypt with RSA!

TLS used RSA before but no longer.

RSA is used more for signing! Something that Diffe can't!!

RSA is 1000x slower than symmetric crypto systems!!