Number Base Case	information flow
$N = d_n R^n + d_1 R^1 + d_0 R^0$ the d specifies the Number system -> $d_2 ==$ binary	essentially information content over time
can also be written as R_2 This can also be used to expand numbers:	$H_0^* = \frac{\log_2(N)}{\tau} \left[\frac{bit}{\varepsilon} \right]$
	information quantity
Quantities:	$I(x_k) = -log_2(P(x_k))[bit]$
$N \rightarrow \text{natural numbers} \mid \mathbf{Z} \rightarrow \text{full numbers} $ $\mathbf{Q} \rightarrow \text{rational numbers} \mid \mathbf{R} \rightarrow \text{real numbers} $	Entropy
Common number systems: Decimal: $N_{10} = n * 10^n 0 * 10^0$	Probability * information content
Binary: $N_2 = n * 2^n 0 * 2^0$ $2^{10} = 1024, 2^9 = 512, 2^8 = 256, 2^7 = 128, 2^6 = 64,$	$H(X) = \sum_{k=1}^{N} P(x_k) * I(x_k) \left[\frac{bit}{sumbol} \right]$
$2^5 = 32, 2^4 = 16, 2^3 = 8, 2^2 = 4, 2^1 = 2, 2^0 = 1$ Hexadecimal: $N_1 6 = n * n^{16} 0 * 16^0$	nerfect match
notation: 0 1 2 3 4 5 6 7 8 9 A B C D E F $16^5 = 1048576, 16^4 = 65536, 16^3 = 4096, 16^2 = 256,$	where X is the list of symbols Sink Redundance / Code Redunca
$16^1 = 16, 16^0 = 1$	D = H = H(Y) bit
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	
if $x < y$ in x mod y then the result will always be x! any negative numbers can be considered as NOTnegative	$R_c = L - H(X) \left[\frac{bit}{symbol} \right]$
aka only absolute values! modulo deals with x many programming languages actually do not follow this!	$symoot$ $_{0}$ $_{PeX=1}^{a,b,b}$ $_{1}$ Code Word Length
they have their own implementation of modulo. $5 \equiv 3 \mod 2$ -> as $5 \mod 2 = 1$ and $3 \mod 2 = 1$	Code Word Length $L(x_k) = \text{rounded}(I(x_k))[bit]$
Codeword length Byte = 8 bit Word = 16 or 32 bit	$E(x_k) = \text{Founded}(Y(x_k))[ott]$ Median Code Word Length
TCP packet = 1024 bit Cyclic group	• • • • • • • • • • • • • • • • • • • •
Es sei $F(a) = a^3 + a + 1 = 0$,	$L = \sum_{k=1}^{N} P(x_k) * L(x_k) \left[\frac{bit}{symbol} \right]$
Dann können wir zunächst festhalten	Entropy of the entire Code
■ a = a ■ a ² = a ² aber	
$\mathbf{a}^3 = \mathbf{a} + 1$	$H_c(X) = \sum_{k=1}^{N} P(x_k) * L(x_k) \left[\frac{bit}{symbol} \right]$
$a^4 = a(a + 1) = a^2 + a$ $a^5 = a(a^2 + a) = a^3 + a^2 = a^2 + a + 1$	H_c can be a real number -> $H_c \in \mathbb{R}$
$ a^3 = a(a^2 + a) = a^3 + a^2 = a^2 + a + 1 $ $ a^6 = a(a^2 + a + 1) = a^3 + a^2 + a = a + 1 + a^2 + a = a^2 + 1 $	Für jede beliebige zugehörige Für jede beliebige Quelle kann eine Binärcodierung mit Binärcodierung gefunden werden so
$a^7 = a(a^2 + 1) = a^3 + a = a + 1 + a = 1$	Binarcodierung mit Präfixeigenschaft ist die mittlere Codewortlänge nicht kleiner als die
a ⁸ = a : der Zyklus beginnt von vorne!	Entropie $H(X)$:
$= \{0, 1, a, a^2, a+1, a^2+a, a^2+a+1, a^2+1\}$ = $\{000, 001, 010, 100, 011, 110, 111, 101\}$	$H(X) \le L \qquad \qquad H(X) \le L \le H(X) + 1$
WHAT THE FUCK	Sink without memory
Result Quantity the result of all possible outcomes it is denoted with: Ω	$P(x_k, y_k) = P(x_k) + P(y_i)$
A single element of the result list is: ω -> $\omega \in \Omega$ The list of results is $ \Omega $	Sink with memory
Example Dice roll: $\Omega = \{1, 2, 3, 4, 5, 6\}$	$P(x_k, y_i) = P(x_k) + P(x_k y_i)$
Probability: $P(A) = \frac{\text{best results}}{\text{all results}} = \frac{ A }{ \Omega } = \frac{ A }{n}$	Entropy without memory
So what is the probability of rolling a 6? only 1 good result! 1	$H(H,Y) = \sum_{x_k}^{N} \sum_{y_i}^{N} P(x_k, y_i) * (-log_2(P(x_k, y_i)))$
$P(\text{desired number to roll}) = {6 \text{ possible results}} = -$	Entropy with memory
hence the chance is 1 in 6 Why this complicated method? You can modify desired results!	$H(H,Y) = \sum_{x_k}^{N} \sum_{y_i}^{N} P(x_k) *$
just change the A in P(A)! Inverse Probability: P(inverse) = 1 - P(A)	$P(x_k, y_i) * (-log_2(P(x_k) * P(x_k y_i))$
dice -> $1 - \frac{1}{6} = \frac{5}{6}$	Encoding of Symbols Ordne die Zeichen gemäss ihrer Auftrittswahrscheinlichkeit
Addition rule:	* Die beiden Zeichen mit der kleinsten Auftrittswahrscheinlichkeit haben die gleiche CW-Länge L_N * Sei L_N die mittlere CW-Länge für eine Quelle mit N Zeichen und L_{N-1}
$P(A \cup B) = P(A) + P(B) - P(A \cap B)$	die mittlere CW-Länge für den Fall, dass die beiden letzten zu einem einzigen Zeichen zusammengefasst werden, dann gilt:
!!The last part is needed, as otherwise the number would exceed the possible states!!	$\begin{split} L_N - \left(p(x_{N-1}) + p(x_N) \right) \cdot L(x_N) &= L_{N-1} - \left(p(x_{N-1}) + p(x_N) \right) \cdot \left(L(X_N) - 1 \right) \\ \Rightarrow L_N &= L_{N-1} + p(x_{N-1}) + p(x_N) \end{split}$
$P(A \cup B \cup C) = P(A) + P(B) + P(C) - P(A \cap B) - P(A \cap C)$	1 2 3 4 5 6 7 8 9 0.22 0.19 0.15 0.12 0.08 0.07 0.07 0.06 0.04
$\frac{-P(B \cap C) + P(A \cap B \cap C)}{\text{Amount of possibilities:}}$	1 2 3 4 8 9 5 6 7
ordered probes with replication: 2 coins, head and tail, possibilities? k=head/tail=2 n=coins=2	0 1 0.22 0.19 0.15 0.12 0.1 0.08 0.07 0.07
$\Omega = n^k = 2^2$	1 2 3 6 7 4 8 9 5
ordered probes without replication:	0.22 0.19 0.15 0.14 0.12 0.1 0.08 1 2 8 9 5 3 6 7 4
5 dices. How many combinations? dice numbers = $\mathbf{n} = 6$ (1-6), dice amount = $\mathbf{k} = 5$	00 01 1 0 1 0.22 0.19 0.18 0.15 0.14 0.12
dice numbers = $\mathbf{n} = 6$ (1-6), dice amount = $\mathbf{k} = 5$ possibilities = $\Omega = \frac{n!}{(n-k)!} = \Omega = \frac{6!}{(6-5)!} = 720$	continue this pattern until every symbol has a code note the extra 0 on every step
Or this:	Run Length Encoding RLE/RLC
$\Omega = \Pi_n^{n-k+1} n = \Pi_6^{6-5+1} 6 = 2 * 35 * 6 = 720$	Quelltext w: Agggbbehfffgggg => w =15 shortening of length
unordered probes wihout replication: 25 players, each should only play once with the other.	Codiert w _g : A3g2beh3f4g => w _g = 11 by compressing repetition.
$\Omega = \frac{n!}{k!(n-k)!} -> \frac{25!}{2!(25-2)!} -> \frac{\text{too big}}{\text{too big}} = 300$ as you can see the bottom is a BIG calculation, so	A+3xg+2xb+e+h+3xf+4xg
	Encoder and Decoder You need to either choose 1 or 0 as the starting
$\Omega = \frac{\Pi_n^{n-k+1}n}{k!} - \frac{\Pi_{25}^{25-2+1}25}{2!} - \frac{24 * 25}{2} = 300$	bit. After that the decoder can print out the correct code. Chiffre text
$\frac{k!}{N}$ 2! 2	You can "encrypt" your data by shifting the codes by a certain amount.
length of the tuple we want to receive> (Player,Player) - > 2	In the caesar chiffre this is done with the number 4. a -> e Please do not use this, use RSA or other algorithms.
Source to Sink Information	Errors
Nachricht (Darstellung & Bedeutung) redundant nicht-redundant	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
irrelevant Zeichenvorrat bei Quelle und Senke verschieden	
relevant vorhersagbar Information	$p(Y X) = \begin{bmatrix} p & 1-p \\ 1-q & q \end{bmatrix} \mapsto \begin{bmatrix} \sum_{i=1}^{n-1} \\ \sum_{i=1}^{n-1} \end{bmatrix}$ 1-p and 1-q are the chance for error. Which we of course have to
Entropy information content	take into account. $p(x)=0.5 x 0.95$
information content this essentially just us how many bits are needed	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
k is base state count -> bit = 2 and N is the full number of states example: list True, False, True, False 4 states total, base 2.	$p(x_3) = 0.25 \qquad x_3 \qquad y_3 \qquad [\rho(y_3)] [\rho(x_1) \cdot \rho(y_3 x_1) + \rho(x_2) \cdot \rho(y_3 x_2) + \rho(x_3) \cdot \rho(y_3 x_3)] = 0.25 \qquad x_3 \qquad y_3 \qquad [\rho(y_3)] [\rho(x_3) \cdot \rho(y_3 x_2) + \rho(x_3) \cdot \rho(y_3 x_3) + \rho(x_3) \cdot \rho(x_3 x_3) + \rho(x_3 x_3)$
example: list True,False,True,False 4 states total, base 2. $H_0 = log_k(N)[k] -> H_0 = log_2(4)[bit] = 2$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
$\frac{\log \chi(1) / [n]}{\log \chi(1) / [n]} > \frac{110 - \log_2(1) [\log_2(1)]}{\log_2(1)} = 2$	0.025 0.025 0.95 0.5625 0.50.0250.250.0250.250.95





