Assignment 2 Design Prof Veenstra Nguyen Vu

1. e()

I create a temporary denominator, numerator and e variable that starts at 0. After that I make a loop so that it keeps adding the new right terms using Taylor series to the e variable by reusing the denominator from previous term until the new term is smaller than EPSILON.

Pseudo Code:

 ${\rm denominator} = 0$

e = 0

term = 1

for loop

term = 1/denominator

make the new base for next term

add term to e

1.2. e_terms()

I create a loop count as the global variable and add 1 to it every time it loops in e()

Pseudo Code:

 $global\ loop = 0$

for every loop in e(), add 1 to global loop

2.1. pi_madhava()

I create a temporary denominator, numerator

$$(-3)^{-}k$$

and pi variable that starts at 0. After that I make a loop so that it keeps adding the new right terms using the Madhava's method to the pi variable by computing the new denominator multiply by the new

$$(-3)^{-}k$$

value. After the new term is smaller than EPSILON, I multiply the final value by

 $\sqrt{12}$

Pseudo Code:

term = 1

```
\begin{aligned} &\text{pi} = 0 \\ &\text{numerator} = 1 \\ &\text{for loop} \\ &\text{term} = \text{numerator} \; / \; (2k+1) \\ &\text{add term to pi} \\ &\text{compute new numerator} \\ &\text{compute} \end{aligned}
```

 $\sqrt{12}$

and multiply it to the final pi value

2.2. pi_madhava_terms()

I create a loop count as the global variable and add 1 to it every time it loops in pi_madhava()

Pseudo Code:

 $global\ loop = 0$

for every loop in pi_madhava(), add 1 to global loop

3.1. pi_euler()

I create a pi variable. After that I make a loop so that it keeps adding the new right terms using the Euler's method. After the new term is smaller than EPSILON, I multiply the pi variable by 6 then square root the result for the final pi value.

Pseudo Code:

pi = 0 for loop: term =

 $1/(k^2)$

add 1 to k add term to pi multiply pi by 6 square root the result

3.2. pi_euler_terms()

I create a loop count as the global variable and add 1 to it every time it loops in pi_euler()

Pseudo Code:

 $global\ loop = 0$

for every loop in pi_euler(), add 1 to global loop

4.1. pi_bbp()

I create a pi variable. After that I make a loop so that it keeps adding the new right terms using the Bailey-Borwein-Plouffe's method with k increases

by 1 every loop until the new term is smaller than EPSILON.

Pseudo Code:

pi = 0

base = 1

for loop:

term =
$$(1.0 / \text{base}) * ((4.0 / ((8.0 * k) + 1.0)) - (2.0 / ((8.0 * k) + 4.0)) - (1.0 / ((8.0 * k) + 5.0)) - (1.0 / ((8.0 * k) + 6.0)))$$

multiply base by 16

add term to pi

4.2. pi_bbp_terms()

I create a loop count as the global variable and add 1 to it every time it loops in pi_bbp()

Pseudo Code:

 $global\ loop = 0$

for every loop in pi_bbp(), add 1 to global loop

5.1. pi_viete()

First I find the square root of 2 then divide it by 2 and use it as the first term. After that I make a for loop and multiply the previous term by 2, add 2 then square root the result. Then I take the result and divide it by 2 and finally multiply is with the previous result. I keep repeating that process until the new result subtract the previous one is smaller than EPSILON.

Pseudo Code: term =

$$\sqrt{2}/2$$

add term to pi for loop:

new term =

$$\sqrt{2+(term*2)}$$

multiply pi by new term

update current term by multiplying with new term

5.2. pi_viete_factors()

I create a loop count as the global variable and add 1 to it every time it loops in pi_viete()

Pseudo Code:

global loop = 1 because the first term is

$$\sqrt{2}/2$$

for every loop in pi_viete(), add 1 to global loop

6.1. sqrt_newton()

I create an initial guess for the square root of the given value. After that I keep calculating new square root value using the Newton-Raphson method until the new guess subtract the old one is less than EPSILON.

Pseudo Code:

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guess = 1 for loop:
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function =

 $guess^2 - givenvalue$

derived function = 2*guess

guess = guess = function/(derived function)

6.2. sqrt_newton_iters()

I create a loop count as the global variable and add 1 to it every time it loops in sqrt_newton()

Pseudo Code:

 $global\ loop = 0$

for every loop in sqrt_newton(), add 1 to global loop

7. mathlib-test.c

I create every test for respective letter of operation similar to the example and set -s to turn on/off the return terms function and -h to shows the main menu.

Pseudo Code:

opt = 0

return term = 0

while loop for opt: switch (opt)

Print and compare value from respective functions and actual mathematical value with respective command letter

case 's': return term = 1

case 'h': prints the main menu

8. Makefile

I create commands to compiles the mathlib-test.c into executable and other math files into .o files.

Pseudo Code:

CC = clang

CFLAGS = -Wall -Wpedantic -Werror -Wextra

OBJS = e.o madhava.o euler.o bbp.o pi_viete.o newton.o

set all: command to compile mathlib-test

set mathlib-test: command to compile mathlib-test.c and other math files.c

set clean: command to remove all created files set format: command to clang format any .c files set %.o: %.c command to compile any .c files into .o files