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Study on the Anode-to-Cathode Distance in an Aluminum Reduction Cell

DAG HERMAN ANDERSEN and ZHILIANG L. ZHANG

A two-dimensional (2D) finite element model (FEM) of an anode immersed in an aluminum reduction cell was developed to study the initial current distribution in the anode as a function of anode geometry and electrical anode conductivity gradients. The numerical results of the initial state of the anode electrical current were used to describe analytically how this will affect the variation in the anode-to-cathode distance (ACD) in a steady-state scenario after several hours in the electrolysis bath. The electrical power loss in the anode has also been studied at different anode geometries and material properties. The slot positioning, slot depths, and stub hole dimensions have been considered in the FEM. The anode is implemented as an inhomogeneous orthotropic material with a defined six-parameter equation. The degree of initial inhomogeneous anode current density, which is expressed with a defined parameter k_0 , can reach values to cause variations in the ACD typically measured in the aluminum industry. To avoid a variation in the ACD for this case, the defined bath conductivity relation n should be within certain limits for the analyzed industrial reduction cell. The lowest degree of initial inhomogeneous current in the anode is achieved with deeper slots closer to each other and with an electrical current entering the anode in the bottom of the anode stub hole.

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I. INTRODUCTION

THE metal capacity from the aluminum reduction cell increases proportionally with a current increase as long as the current efficiency (CE) is constant. The electrical power loss from the bath resistance as a result of the current increase can be reduced by decreasing the anode-to-cathode distance (ACD). This is preferred to make sure that the pots stay inside an operational resistance load window where sufficient frozen side ledge is retained. When the average of the ACD is reduced by current increase actions, it is important to reduce the variation/noise in the ACD resistance. If not, the process will be directed toward an unstable state with reduced current efficiency and higher probability for dynamic short circuiting, which is caused by magneto hydrodynamic waves and the risk of growing spikes at the anodes wear surface.

Over the last 10 years, there has been focus on current increase actions and also on reducing the noise in the ACD resistance in the aluminum industry. One of the major improvements of reducing the noise was the implementation of slots in the wear surface as illustrated in Figure 1.^[1] The produced carbon dioxide creates

bubbles in the bath and the slots function as an escape route for the bubbles. The low-frequency noise components in the liquid metal have also been studied in a magnetohydrodynamic (MHD) aspect that has influenced design optimizations of the cell and also the bus bar system.^[2] There is also a focus on how the inhomogeneous density of the bath creates inhomogeneous ACDs.^[3] This gives motivation for alumina distribution to the cell through individual feeder control to reduce the density differences in the bath. Still, variations exist in the ACD resistance. In normal situations, it is reported that the standard deviation in the current load on individual anodes in the same cell often are more than 10 pct of the average current.^[4] The actions for reducing the noise in the ACD resistance by slots in the anode have led to negative effects on other parameters, like current efficiency and increased inhomogeneous anode consumptions.^[5] It is emphasized that each slot implementation must be treated individually for each plant^[6] to avoid pitfalls.

This article will focus on one special effect on the ACD variation, that is, the initial electric current distribution (the anode in an initial state in the bath as explained previously). The first section of the article defines the k_0 parameter to describe the degree of initial inhomogeneous current densities in the anode. The parameter is coupled even more by a proposed analytical equation to the ACD to explain how the k_0 parameter affects the ACD. The anode conductivity gradients are also parameterized with linear and non-linear parameters by a six-parameter equation to study how different conductivity gradients can affect the ACD through the k_0 parameter.

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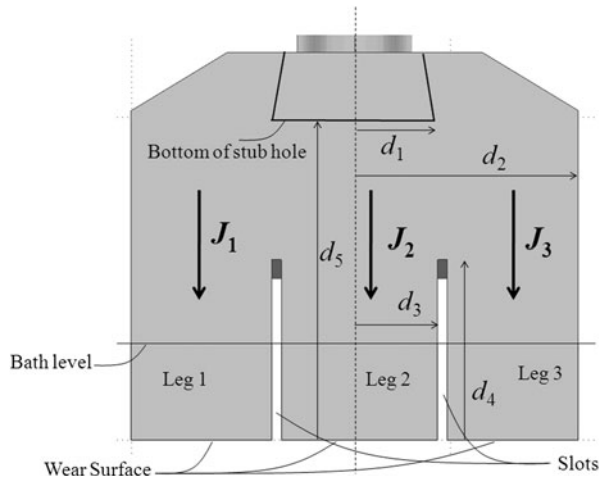


Fig. 1—The anode immersed in the electrolysis bath (the longitudinal direction of the anode is into the paper). The slots divide the lower part of the anode into three longitudinal “legs” with height d_4 . Dimension d_1 is the radius of the stub hole bottom.

In the second part of the article, a two-dimensional (2D) numerical model is developed to determine a typical variation in k_0 for some realistic anode geometries and anode conductivity gradients. The electric conductivity is implemented in the finite element model (FEM) as an orthotropic inhomogeneous material property with the proposed six-parameter equation. The numerical study of the defined parameter k_0 is a first study of its kind. We therefore decided to use a 2D model to reduce the complexity and computational burden. The aim was to determine a typical range in the k_0 parameter and find effects from the anode design that will decrease this parameter. The expected differences in the results from a three-dimensional (3D) FEM compared with a 2D FEM are discussed subsequently in this article.

II. PARAMETERIZATION OF INHOMOGENEOUS PROPERTIES IN THE ELECTROLYSIS CELL

A parameter describing the degree of inhomogeneous electrical current distribution (k_0) in the anode is defined. It is used in a proposed analytical equation to describe its effect on the variation in the ACD.

A. The k Parameter

For simplicity, we can introduce a parameter k to describe a relation of ideal electrical current density J_2 in the inner leg of the anode and a current density J_3 in the outer leg of the anode as shown in Figure 1. The current density, J_3 can be taken as an abnormal current density and J_2 as a reference current density.

For the ideal initial state ($k = k_0$), we have

$$J_3 = k_0 J_2 \quad [1]$$

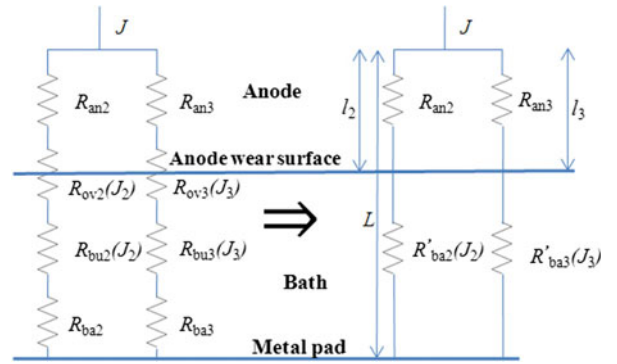


Fig. 2—Equivalent DC circuit of an anode in the bath. The current density J is affected by anode resistance R_{an} , surface overvoltage resistance R_{ov} , bubble resistance R_{bu} , and the resistance in the bath R_{ba} . The left circuit can be simplified to the right DC circuit where R'_{ba} is the resistance that includes R_{ov} , R_{bu} , and R_{ba} . The length l_2 is the height of the anode where J_2 is dominant. The length l_3 is the height of the anode where J_3 is dominant. The length L is the total vertical length from a common reference horizontal plane in the anode down to the metal pad.

Equation [1] can also be expressed with electrical current and cross section as

$$\frac{I_3}{A_3} = k_0 \frac{I_2}{A_2} \quad [2]$$

For the ideal steady state, after several hours in the bath, different processes like surface overvoltage on the anode wear surface, production of CO_2 , and anode consumption will result in a homogeneously distributed current near the anode wear surface. This means that $k \rightarrow 1$ and $J_3 = kJ_2 = J_2$. The initial degree of inhomogeneous current distribution k_0 has been transferred over to the steady state by Eq. [3]. The resistances for path 2 and path 3 (the paths down to the metal pad in Figure 2) get the relation

$$A_3 R_3 = k_0 A_2 R_2 \quad [3]$$

The equivalent direct current (DC) circuits of the anode in the bath, which are shown in Figure 2, are used to describe how inhomogeneous current density can affect the ACD. The high resistances in the cell and the resistances that are highly affected by the current density are included in the equivalent DC circuit (the Nernst potential, anode concentration overvoltage, and the cathode overvoltage are therefore neglected).

Equation [3] can further be expressed, with components described in Figure 2, as

$$A_3 (R_{an3} + R'_{ba3}) = A_2 k_0 (R_{an2} + R'_{ba2}) \quad [4]$$

By expressing the resistances as a function of its conductivities and dimensions ($R = l/\sigma A$) we get

$$\frac{l_3}{\sigma_{an3}} + \frac{L - l_3}{\sigma'_{ba3}} = k_0 \frac{l_2}{\sigma_{an2}} + k_0 \frac{L - l_2}{\sigma'_{ba2}} \quad [5]$$

We assume homogenous conductivity in the anode and introduce the conductivity relations $m = \sigma_{\text{an}}/\sigma'_{\text{ba2}}$ and $n = \sigma'_{\text{ba3}}/\sigma'_{\text{ba2}}$. Equation [5] can then be expressed as

$$\frac{l_3}{m} + \frac{L - l_3}{n} = k_0 \frac{l_2}{m} + k_0(L - l_2) \quad [6]$$

By finding an expression for l_3 from Eq. [6], we get Eq. [7] for the ideal steady state.

$$l_3 = \frac{k_0 n l_2 + k_0 m n (L - l_2) - m L}{n - m} \quad [7]$$

For the case of $n = k_0 = 1$, no difference in the ACD, because of the anode design, will appear because $l_3 = l_2$ in Eq. [7] ($ACD_{\text{ref}} = L - l_2 = ACD_{\text{abnorm}} = L - l_3$), and no inhomogeneous anode consumption, because of anode design, will occur. If the reduction cell and the anode are designed and will run with k_0 , m , and n values that result in $l_3 \neq l_2$ in Eq. [7], inhomogeneous consumption of the anode take place and a difference in the ACD appears. Equation [7] can be used in an anode design to reduce the ACD when the bath effects on the ACD are isolated (m and n are set to constants).

The bath conductivity relation n is defined with virtual conductivities. We can express this relation with real physical properties. It is mainly given by phenomena such as surface anode overvoltage and the presence of bubbles in the bath caused by formation of CO_2 . From Figure 2, a real physical expression for n can be derived from the voltage drops over each resistance in the bath.

$$\frac{U'_{\text{ba2}}}{U'_{\text{ba3}}} = \frac{U_{\text{ov2}} + U_{\text{bu2}} + U_{\text{ba2}}}{U_{\text{ov3}} + U_{\text{bu3}} + U_{\text{ba3}}} \quad [8]$$

Equation [8] can further be expressed by resistances and current densities^[7] shown in Eq. [9].

$$\frac{\frac{(L-l_2)J_2}{\sigma'_{\text{ba2}}}}{\frac{(L-l_3)J_3}{\sigma'_{\text{ba3}}}} = \frac{\frac{RT}{1.08F} \ln\left(\frac{J_2}{J_0}\right) + \frac{d_{b2}J_2}{\sigma_{\text{ba2}}(1-\phi_2)} + \frac{(L-l_2-d_{b2})J_2}{\sigma_{\text{ba2}}}}{\frac{RT}{1.08F} \ln\left(\frac{J_3}{J_0}\right) + \frac{d_{b3}J_3}{\sigma_{\text{ba3}}(1-\phi_3)} + \frac{(L-l_3-d_{b3})J_3}{\sigma_{\text{ba3}}}} \quad [9]$$

where R is the universal gas constant, F is the Faraday constant, J_0 is the limiting current density in the surface overvoltage term, and d_b the bubble layer thickness, which has a tendency to decrease with current in an electrolysis cell.^[7] The bubble coverage ϕ increases with the current density and isolates the anodes' wear surface with bubbles in a higher degree.^[8]

We rearrange Eq. [9] to get an equation for n with real physical properties that can be used experimentally.

$$n = \frac{\sigma'_{\text{ba3}}}{\sigma'_{\text{ba2}}} = \frac{(L-l_3)J_3}{(L-l_2)J_2} \left[\frac{\frac{RT}{1.08F} \ln\left(\frac{J_2}{J_0}\right) + \frac{d_{b2}J_2}{\sigma_{\text{ba2}}(1-\phi_2)} + \frac{(L-l_2-d_{b2})J_2}{\sigma_{\text{ba2}}}}{\frac{RT}{1.08F} \ln\left(\frac{J_3}{J_0}\right) + \frac{d_{b3}J_3}{\sigma_{\text{ba3}}(1-\phi_3)} + \frac{(L-l_3-d_{b3})J_3}{\sigma_{\text{ba3}}}} \right] \quad [10]$$

The expression for n can also be modified and include extra effects like anodic and cathodic concentration overvoltage in the bath. The voltage drops from these effects must be added to the right side of Eq. [8], and a

modified expression for n is derived from the extended equation (an extra resistance in each branch in the left DC circuit in Figure 2 will appear). We can also simplify Eq. [10] if the surface overvoltage term is linearized. The current densities J_2 and J_3 in Eq. [10] will be omitted.

The anode-bath conductivity relation, m , has also a virtual component in its expression. This can also be represented with physical parameters by Ohms law. From $U = RI$, $R = 1/\sigma A$, and using Figure 2, the physical expression for m is shown in Eq. [11].

$$m = \frac{\sigma_{\text{an}}}{\sigma'_{\text{ba2}}} = \frac{\sigma_{\text{an}} A_{\text{an}} U_{\text{ba-meas}}}{ACD_{\text{ref}} I_{\text{an}}} \quad [11]$$

The area A_{an} is the anode wear surface, σ_{an} is the anode conductivity, $ACD_{\text{ref}} = L - l_2$ the reference ACD, I_{an} is the electrical current through one anode, and $U_{\text{ba-meas}}$ is the measured/calculated voltage drop between the anode and the metal. The real conductivity of the bath is normally around 200 to 300 S/m. The total virtual conductivity of the bath σ'_{mba} , which also includes surface overvoltage and bubble overvoltage will be much less (Figure 2). For example, a conservative cell with $ACD_{\text{ref}} = 0.04$ m and $I_{\text{an}} = 8,000$ A is approximately $m \approx 195$. There is a different m for each aluminum plant, and it depends on how the manager decides to run the cell. For a current increase project in a plant, the reference ACD will be decreased. Typical values^[9] can be $ACD_{\text{ref}} = 0.03$ m and a chosen $I_{\text{an}} = 10,000$ A. This results in $m \approx 220$ from Eq. [11].

In the numerical study, k_0 will be determined and the results will be linked to the variation in the ACD in Eq. [7] with specific values on m and n . It is not the intention of this article to calculate m and n for many different aluminum reduction cells. The purpose of this study is to define the parameters and illustrate them with one cell solution ($m = 200$, $ACD_{\text{ref}} = 0.04$ m).

B. Parametric Implementation of Anode Conductivity Gradients

It is well known that the physical properties of the carbon anode are inhomogeneous. There is a need to systemize these properties so that parametric numerical studies on the anode gradients can be performed. The parameters that describe the degree of inhomogeneous material properties will be used to study how they will affect k_0 . A six-parametric equation, which is shown in Eq. [12], has been proposed to describe the gradient in 3D. Electrical conductivity and all other properties that correlate well with the conductivity can be described with the parametrical equation. The equation was developed with fewest possible parameters for describing a realistic gradient of the physical property from laboratory test data.^[10] The anode data from the core analyses show an orthotropic property in the electric resistivity. In the forming process of the anode from the paste plant, the anode is mainly compacted by vibration. With coke particles of an aspect ratio lower than unity, the vibration will orient the particles in a horizontal direction, normal to the direction of vibration. This can

be the main reason that the resistivity in horizontal direction is lower than in the vertical direction; the number of particles in the horizontal direction will probably be lower than in the vertical direction. The experimental data also show that the resistivity increases further away from the walls of the mold of vibration, especially in the upper part of the anode. A skewed filling of the anode paste in the mold of vibration will also produce a skewed anode resistivity. Segregation of coke particles in the mixing stage in the paste plant also contributes to larger resistivities at local areas in the anode.

The equation is developed so that the average value of the physical property is placed in one term ρ_0 . The other terms are deviatory parts without the average value component. The other parts are used to describe the inhomogeneous material data. The terms with A parameters describe the nonlinear gradients, and the terms with the B parameters describe the linear gradients.

$$\begin{aligned} \rho(x, y, z) &= \rho_0 + A_{0y} \left(\frac{z}{h} \right)^2 \left[g(y) - \int_0^b g(y) dy \right] \\ &+ \left(A_{01x} \left(\frac{z}{h} \right)^2 - A_{02x} \left(1 - \frac{z}{h} \right)^2 \right) \left[f(x) - \int_0^l f(x) dx \right] \\ &+ \left(\frac{z}{h} \right)^3 \left[\frac{2B_{0y}}{b} y - B_{0y} + \frac{2B_{0x}}{l} x - B_{0x} \right] + \frac{2B_{0z}}{h} z - B_{0z} \end{aligned} \quad [12]$$

The dimensions b , h , and l are the width, height, and length of the anode, respectively. The x axis is along l , y axis along b , and z axis along h . The term ρ_0 is the average value of the physical parameter, B_{0x} is the slope of a linear function in the x direction, B_{0y} the slope of a linear function in the y direction, B_{0z} is the slope of a linear function in the z direction, A_{01x} is the amplitude of a nonlinear function in the x direction in the anode top, A_{02x} is the amplitude of a nonlinear function in the x direction in the anode wear surface, A_{0y} is the amplitude of a nonlinear function in the y direction, $f(x)$ is the nonlinear function describing the nonlinear variation in the x direction, and $g(y)$ is the nonlinear function describing the nonlinear variation of the anodes physical property in the y direction.

The nonlinear functions $f(x)$ and $g(y)$ can be found by curve fitting from the carbon core analysis. In the work described in this article, the functions is set to $f(x) = \sin(\pi \frac{x}{l})$ and $g(y) = \sin(\pi \frac{y}{b})$. We then have $\int_0^l \sin(\pi \frac{x}{l}) dx = \frac{2l}{\pi}$ and $\int_0^b \sin(\pi \frac{y}{b}) dy = \frac{2b}{\pi}$.

Because the longitudinal anode slots are studied here, the most interesting parameters for resistivity/conductivity gradients in the anode are A_{0y} and B_{0y} from Eq. [12]. For the numerical analyses, only the parameters $A = A_{0y}$, and $B = B_{0y}$ were used for parametric numerical study of the material. The values of A and B used in the numerical analysis are shown in Figure 3.

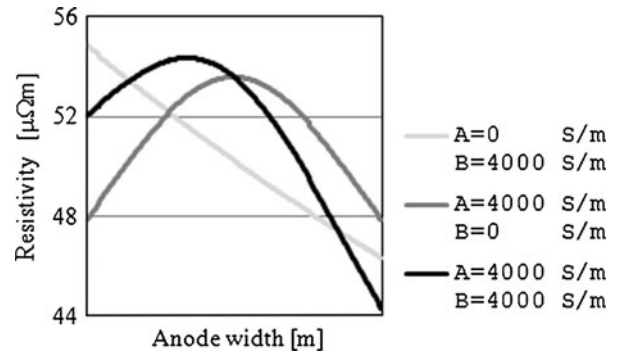


Fig. 3—Electrical resistivity in the anode as function of the anode width, 15 cm under the anode top. In the numerical study, four different A , B parametric value pairs was chosen: (0,0), (0,4000), (4000,0), and (4000,4000). The value pair (0,0) represents an anode with a constant homogenous resistivity for each direction.

In the electrolysis bath, we have a maximum thermal gradient mainly in the z direction in the anode. A typical temperature range in the z direction of the anode is from 673 K (400 °C) in the top to 1233 K (960 °C) in the wear surface. The resistivity of the anode will decrease by approximately 1 $\mu\Omega m$ pr. 373 K (100 °C)^[12] in this range. Because we only have an electric FEM, the parameter B_{0z} in Eq. [12] can be used to verify the effect of the thermal contribution on k_0 by having a decreasing average resistivity from top to bottom in the anode. In the horizontal plane in the anode, the temperature range in the anode is much smaller than for the z direction. It can only contribute to a change in resistivity by a maximum of 2 to 3 $\mu\Omega m$ in the steady state. This is less than the ranges of the A and B parameters from Figure 3. We should keep this thermal effect in mind when we study the current distribution with an electric FEM.

III. MODELING PROCEDURES

The 2D model was developed mainly to find typical variations in the k_0 parameter from different anode dimensions. The conductivity gradients of the anode were also implemented in the model by the six-parameter equation to evaluate the effect on the k_0 parameter.

A. Geometry and Dimensions

The parameter, k_0 , was found with different slot depths, slot positions and stub hole dimensions β , γ , and δ as shown in Table I. For each slot and stub design, the current entered the anode in four ways (i_0 to i_3), as described in Figure 4, so that $k_0 = k_0$, and i) was found numerically.

The stub has a conic angle and the radius of the hole increases downward to the bottom of the hole, d_1 (Figure 1). This is a typical machined stub hole made after the anode baking furnace process.^[11] In the numerical analyses, the contact resistance has been neglected (zero voltage drop from cast iron to anode and from yoke to cast iron when the contact is established). The current has been parameterized to enter in four

Table I. Chosen Anode Stub and Slot Design in the FE Analysis*

$\beta = \frac{d_5}{d_4}$	$\gamma = \frac{d_3}{d_1}$	$\delta = \frac{d_2}{d_1}$	i
Slot depth $\beta_0 = 1.40$	Slot position $\gamma_0 = 1.000$	Stub hole dimension $\delta_0 = 3.18$	Path of current in the stub-anode interface i_0
			Current enters upper half area of the conic anode stub hole walls
$\beta_1 = 1.75$	$\gamma_1 = 1.176$	$\delta_1 = 3.20$	i_1
			Current enters whole area of conic anode stub hole walls
	$\gamma_2 = 1.357$	$\delta_2 = 3.14$	i_2
			Current enters whole area of conic anode stub hole wall plus the bottom of the stub hole
			i_3
			Current enters the bottom of the stub hole, not on the side walls

*See Figure 1 for explanation of the anode geometry dimensions d . The parameter i represents the stub-anode interface, and the path of the current as illustrated in Figure 4.

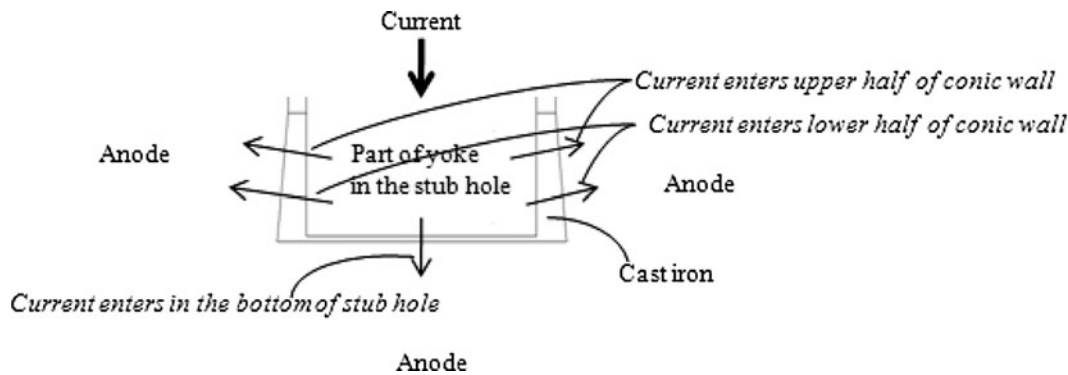


Fig. 4—Path of the electrical current in the stub-anode interface. The current enters the anode from the stub hole in four ways in the FE analyses. For current input setting i_0 , it enters the upper-half area of the conic anode stub hole wall; with i_1 it enters the whole conic stub hole wall, with i_2 the current enters the bottom plus the whole conic stub hole wall, and for i_3 the current enters only the bottom of the stub hole.

different ways: from the situation where the current enters the bottom of the stub hole, to the opposite situation where the current enters the upper part of the stub hole wall. Table I shows the different geometrical anode slot and stub dimensions for numerical study and how the current enters the anode in the numerical analyses. Each geometrical configuration is tested with different gradients of anode resistivity with the four combinations on A and B as described previously.

An ACD of 0.04 m was used in the FE analyses (distance from the anode wear surface to the metal pad). The ACD was constant during the analysis. The metal pad was defined as the boundary of ground.

B. Mesh, Material Data, and Boundary Conditions

The conductive Media DC module in the FE software, COMSOL 3.4 (COMSOL, Inc., Burlington, MA), was used with 2D quadratic Lagrange elements. A mesh was defined for the whole domain with maximum element size scaling factor = 0.08, element grow rate = 1.2, mesh curvature factor = 0.25, mesh curvature cutoff = 0.0003, and resolution of narrow regions = 1. This gave an element number of 75,000 for the whole domain shown in Figure 5.

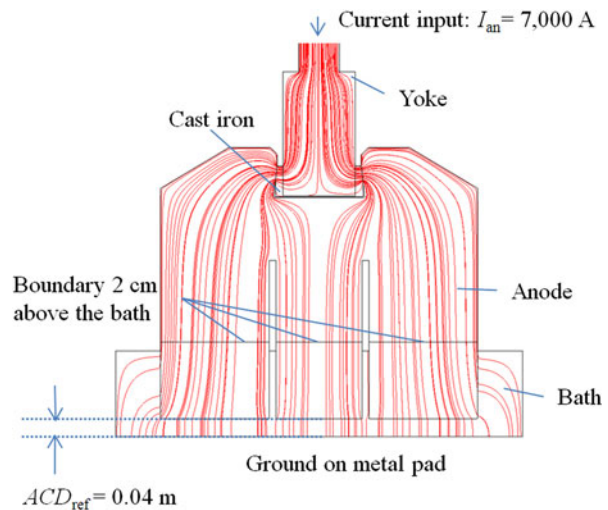


Fig. 5—The 2D domain consists of the subdomains yoke, cast iron, anode, and bath. The current enters from the top of the yoke and penetrates down to the metal pad defined as the boundary of ground. All outer boundaries got an electrical insulated property. The internal boundaries were defined with continuity. The current lines on the figure are shown for current setting i_0 , which is described in Table I.

The material data for the four subdomains (Figure 5) are as follows:

- Yoke: Electrical conductivity of 5E6 S/m.
- Cast iron: Electrical conductivity of 2E6 S/m.
- Anode: In the subdomain setting in COMSOL the anode was defined orthotropic. In the x and y direction, the value of conductivity was set by the expression in Eq. [12] with a mean conductivity, $\rho_0 = 20,408$ S/m, and for the z direction the value was set to the expression in Eq. [12] by the mean conductivity of $\rho_0 = 19,230$ S/m. The gradient parameters $A = A_{0y}$ and $B = B_{0y}$ were used in the numerical study of the material and set to values shown in Figure 3. The other gradient terms of Eq. [12] were omitted in the 2D study. The parameters A (nonlinear gradient), B (linear gradient), and ρ_0 (mean value) were defined in the list of constants in COMSOL.
- Bath: The electrical conductivity of 95 S/m (the surface overvoltage and bubble coverage) reduces the value compared with the bath's real conductivity of 200 to 300 S/m. This value was tuned to get a voltage loss over the whole domain of 3.6 V. The anode-bath conductivity relation m (Eq. [11]) was therefore numerically found and set to $m = 19,000/95 = 200$ for the analysis.

The data for estimating k_0 were found on the boundary 2 cm above the bath shown in figure 5 (or 17 cm above the anode wear surface). The current density J_3 is found by integrating the current along the boundary crossing the outer leg of the anode. The current density J_2 is found by integrating the current along the boundary crossing the inner leg of the anode. The widths of the anode legs are defined by the position

of the longitudinal slots in the anode. The k_0 parameter was calculated by Eq. [1].

IV. RESULTS AND DISCUSSION

The parameter k_0 was found as function of slot position, slot depth, stub size, and the current input setting of the anode ($k_0 = k_0[\beta, \gamma, \delta, \text{and } i]$). Figure 6 shows the results. Within realistic designs of the anode (Table I), k_0 can change from 1.06 to 1.20.

The current input setting, slot depth, and slot position (i, β , and γ) all influence the k_0 (Figure 6). The variation in the stub hole δ has a minor effect on k_0 , which increases slightly with decreasing δ (a decrease of the stub hole extension of $\delta = 3.14$ to $\delta = 3.20$ decreases k_0 within 0.01 for every parametric study). Figure 6 shows the k_0 for $\delta = 3.18$.

With the electrical current entering the bottom of the anode stub hole (i_2 and i_3 setting), a greater part of the current will travel through leg 2 of the anode. The current distribution in the anode will be distributed more homogeneously and k_0 will be decreased. In a 3D model, the variation in k_0 resulting from the current input settings, i_0 to i_3 , would have been slightly reduced, but it would have kept the same trend as shown in the left plot in Figure 6. The current input setting i_0 in the 2D model, where the current enters the upper conic side walls of the stub hole, is the case in 3D where the current enters this way for each position along the anode length. The current input setting i_3 in 2D, where the current enters the bottom of the stub hole, will be the situation in 3D where the current enters this way for every position along the anode length.

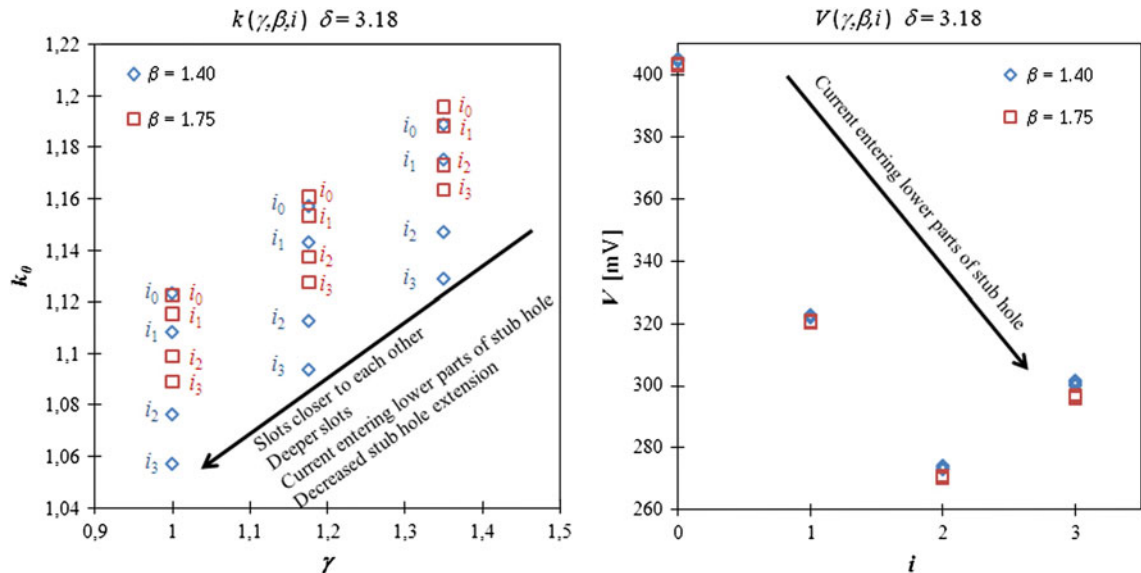


Fig. 6—The left plot for the stub dimension, $\delta = 3.18$, shows k_0 as function of slot position g , slot depth b , and electrical current input setting i_0 to i_3 (Table I) for an orthotropic homogenous anode material ($A = B = 0$). The k_0 parameter decreases mainly with decreasing distance between the longitudinal slots (decreasing g), deeper slots (decreased b), and with a greater part of the current entering the bottom of the stub hole (toward i_3). For every slot position g , the parameter k_0 is decreasing with electrical current input settings, from i_0 to i_3 , for a specific slot depth. The right plot shows the corresponding voltage drops for the electrical current input settings i_0, i_1, i_2 , and i_3 along the x axis.

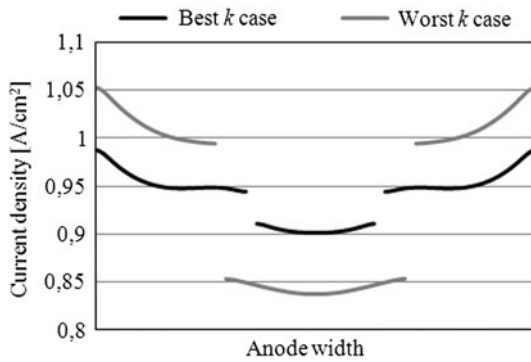


Fig. 7—Electrical normal current density distribution over the anode width along the boundary 2 cm above the bath for the best k case ($k_0 = 1.06$ for $\gamma = 1$, $\beta = 1.4$, $i = i_3$, $\delta = 3.20$) and worst k case ($k_0 = 1.20$ for $\gamma = 1.36$, $\beta = 1.75$, $i = i_0$, and $\delta = 3.14$).

For a deeper anode slot (lower β) the variation in k_0 is greater than for a shorter slot (left plot in Figure 6). This means that different slot positions and current input settings create larger variation in k_0 when the slots are deeper. The best case $k_0 = 1.06$ has a slot position of $\gamma = 1$, slot depth of $\beta = 1.4$, and electrical current input setting i_3 . This is an anode with deeper slots closer to each other and with an electrical current entering the anode in the bottom of the anode stub hole. The worst case, $k_0 = 1.20$, has a slot position of $\gamma = 1.36$, slot depth of $\beta = 1.75$, and electrical current input setting i_0 . This is an anode with shorter slots further away from each other and with electrical current entering in the upper half region of the conic stub hole wall. The current density distribution along the boundary 2 cm above the bath level for the best and worst k case is shown in Figure 7.

The worst k case can induce lot of implications. From initial to steady state, the outer legs of the anode will be shorter than the center leg because the chemical processes consumes the anode at a higher rate where the current density is higher. This creates an unnecessary variation in the ACD and prevents the manager of the plant to lower the average of the ACD by current increase action programs to increase the metal capacity.

With k_0 found previously and with a simulated cell setting of $m = 200$, we can set these values into Eq. [7] and study how an initial current distribution in the anode can affect the ACD. Figure 8 describes the critical n (n_c) we must have for keeping $l_2 = l_3$ for different k_0 when $m = 200$, using Eq. [7].

The worst case of anode design $k_0 = 1.20$ demands a bath conductivity relation $n = 0.83$ to avoid a variation in the ACD by k_0 . If $n = 0.9$, then it is observed from Figure 9 that $l_2/l_3 = 1.006$. With $l_2 = 600$ mm, we have $l_3 = 596.5$ mm, which means a difference in the ACD of 3.5 mm. The values of k_0 , which are found from realistic anode designs, can easily induce a difference in the ACD around 10 pct of its value if the critical n is not reached.

We should keep in mind that the k_0 found from the numerical analyses are based on average values of current densities. In real cases, if we take into account

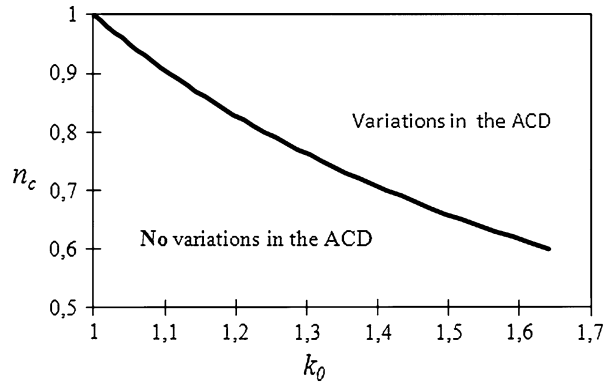


Fig. 8—The critical n for different k_0 to keep $l_2 = l_3$ so that no difference in the ACD will occur. The anode-bath conductivity relation is set to $m = 200$, $ACD_{ref} = 0.04$ m, and $l_2 = 600$ mm in Eq. [7].

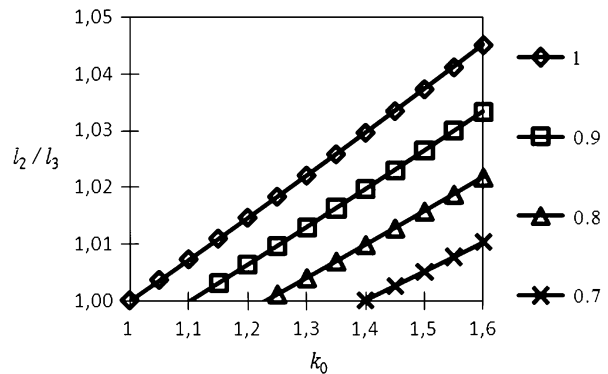


Fig. 9—The relation l_2/l_3 as function of initial anode current distribution k_0 and the bath conductivity relation n for a reference anode height, $l_2 = 600$ mm, $m = 200$, and $ACD_{ref} = 0.04$ m.

inhomogeneous frozen bath on the anode wear surface, the “real k ” can be much higher than the model shows. It can also increase by asymmetric electrical coupling of the yoke to the anode with cast iron. The electrical coupling between the stub holes in one anode can also differ and increase k_0 . A real k_0 of 1.4 demands a bath conductivity relation $n < 0.71$ if a variation in the ACD is to be avoided (Figure 8). Another point to remember is that the bubble coverage under the anode wear surface as function of anode current density has a lower slope for current densities above 1 A/cm^2 than for current densities beneath 1 A/cm^2 .^[8] This means that the bath conductivity relation n is larger for high-amperage cells. The risk is higher such that the initial electrical current distribution in the anode creates variations in the ACD for a high-amperage cell.

For each parametric setting in the numerical analyses, the voltage drop in the anode was calculated by integrating the resistive heat loss over the anode. The lowest anode voltage drop is found when a greater part of the anode current enters the bottom of the stub hole (i_2 and i_3 setting in Figure 6). Voltage drops up to 80 mV can be saved.

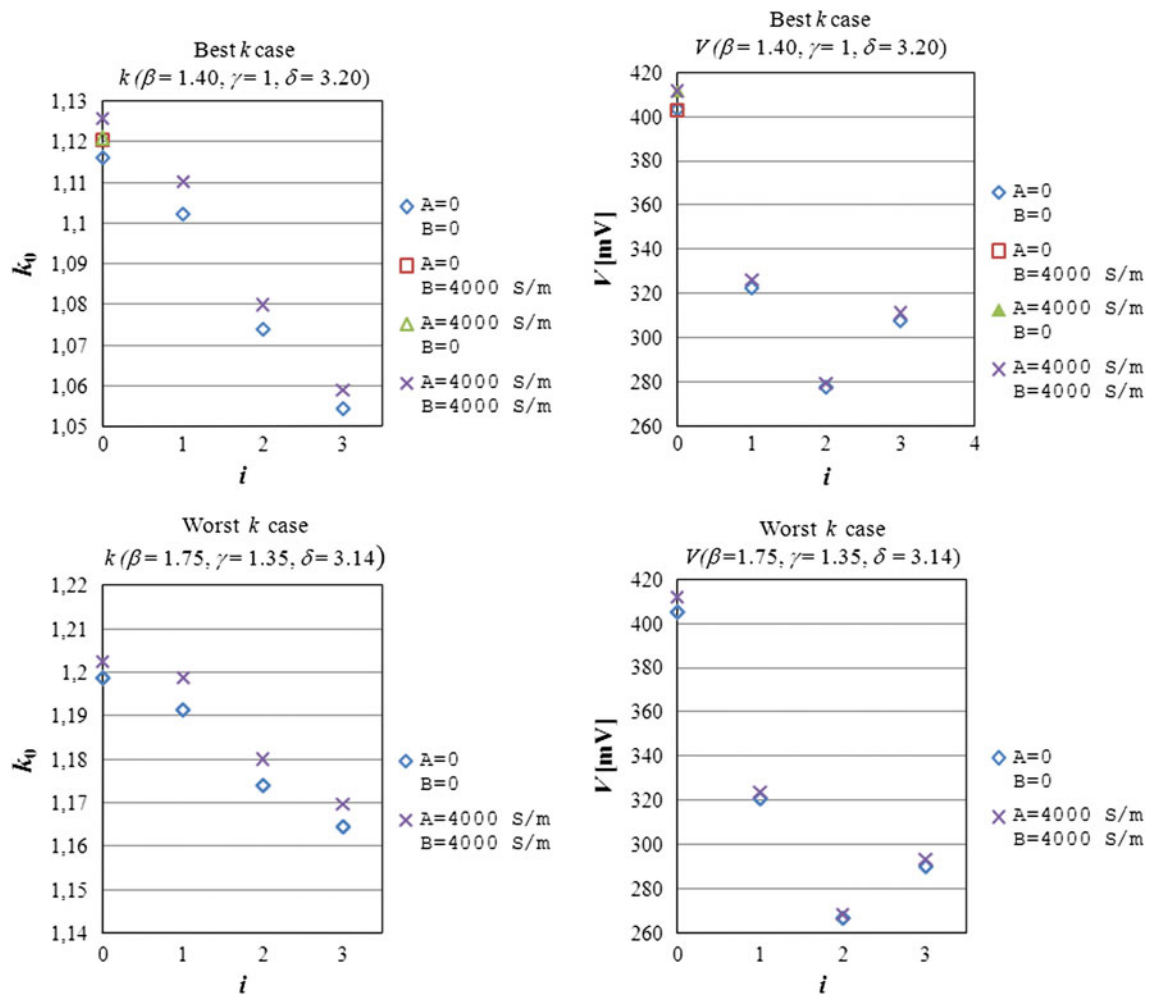


Fig. 10—The left figures show k_0 as function of the resistivity gradients of the anode for two different anode designs, the best k case, and the worst k case. The right plots show the corresponding voltage drops. Both k_0 and the voltage drop are plotted with the electrical current input setting i_0 to i_3 on the x axis. There are no anode resistivity gradients when $A = B = 0$, but the orthotropic property of the material is present for each A, B value pair.

The effects on voltage drop from slot design are strongest for the electrical current input setting i_3 . Even for this setting, the model shows a minor increase of with deeper slots (decreased β from Figure 6).

Electrical anode resistivity gradients with $A = B = 4000 \text{ S/m}$ in Eq. [12] can only increase k_0 with 0.01 (Figure 10). This value is under 10 pct of the variation in k_0 . The effects from anode geometry and current input settings explain the rest of the variation in k_0 . The A, B value pairs (4000,0) and (0,4000) gives more or less the same k_0 value. The anode voltage drop is specially affected by anode resistivity gradients for the current input setting i_0 , where resistivity gradients of $A = B = 4000 \text{ S/m}$ can increase the anode voltage drop by 10 mV (Figure 9). The other anode current input settings for such resistivity gradients can only create a 5-mV increase by the 2D model. It is specially the nonlinear gradient A that contributes to the extra voltage drop. If we add the linear gradient B , this will not create any extra voltage drop.

V. CONCLUSIONS

For realistic anode designs, the k_0 , describing the degree of initial inhomogeneous electrical current distribution in the anode, can range from 1.06 to 1.20. If the anode is designed with a $k_0 = 1.20$, the bath conductivity relation n should be less than 0.83 for the analyzed cell if the variation in the ACD is to be avoided. The best k case (low k_0) describes an anode with deeper slots closer to each other and with an electrical current entering the anode in the lower parts of the anode stub hole. The k_0 values found from numerical analyses are based on the average values of current densities in the anode. In real cases, if we take into account inhomogeneous frozen bath on the anode wear surface, the “real k_0 ” can be much higher than the model shows. It can also increase by asymmetric electrical coupling of the yoke to the anode with cast iron. A real k_0 of 1.4 demands a bath conductivity relation $n < 0.71$ for the analyzed cell if

a variation in the ACD is to be avoided. For high-amperage cells, the bubble coverage as a function of anode current density has a lower slope above 1 A/cm² than for current densities beneath. This increases n , and the risk is higher for the initial current distribution in the anode to affect the variation in the ACD.

The anode voltage drop was found for each anode design in the numerical study. The 2D model showed that voltage drops over 50 mV can be saved if a greater part of the current is entering the bottom of the stub holes instead of the upper part of the stub hole walls. Different slot designs have minor effect on the voltage drop. The 2D FEM can only trace a 5-mV increase when the slot becomes deeper.

The electrical anode resistivity gradients within the defined gradients of $A = B = 4000$ S/m creates a minor increase in k_0 of 0.01, but they can increase the anode voltage drop by 10 mV for current input setting i_0 (current enters upper part of the stub hole walls in the 2D model). It is the nonlinear anode gradient A that contributes to the increased voltage drop.

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NOMENCLATURE AND DEFINITIONS

VARIABLES

J_2	reference current density through the anode or the average current density between the longitudinal slots in the carbon anode
J_3	abnormal current density through the anode or the average current density through the outer leg of the anode (with two longitudinal slots in the anode's wear surface, the anode has three "legs")

$$k = J_3/J_2$$

$$\sigma'_{ba3}$$

$$\sigma'_{ba2}$$

$$n = \sigma'_{ba3}/\sigma'_{ba2}$$

$$m = \sigma_{an}/\sigma'_{ba2}$$

$$l_2$$

$$l_3$$

$$L$$

$$ACD_{ref} = L - l_2$$

$$ACD_{abnorm} = L - l_3$$

$$A = A_{0y}$$

$$B = B_{0y}$$

$$\beta$$

$$\gamma$$

$$\delta$$

$$i_0$$

$$i_1$$

$$i_2$$

$$i_3$$

degree of inhomogeneous electrical current distribution in the carbon anode. k is a function of time. k_0 is the initial value of k in the defined initial anode state described in this section. Range: $k \geq 1$
total conductivity in the electrolysis bath where J_3 is penetrating, which includes effects of surface overvoltage on the anode wear surface and bubble coverage by production of CO₂ in the bath
total conductivity in the electrolysis bath where J_2 is penetrating, which includes effects of surface overvoltage on the anode wear surface and bubble coverage by production of CO₂ in the bath
electrolysis bath conductivity relation between two volumes under the anode in the bath. Range: $0 < n \leq 1$.
conductivity relation between the anode and the bath part, which acts as a reference volume
height of anode where J_2 is penetrating or a reference anode height
height of anode where J_3 is penetrating or an abnormal anode height
total height from anode top down to the metal pad
reference anode-to-cathode distance or an ACD where J_2 is penetrating
abnormal anode- to cathode distance or an ACD where J_3 is penetrating
nonlinear anode resistivity gradient
linear anode resistivity gradient
anode slot depth design
parameter
anode slot position design
parameter
anode stub size design
parameter
electrical current enters upper half region in anode stub hole wall
electrical current enters whole area of anode stub hole wall
electrical current enters whole area of anode stub hole (wall plus the bottom of stub hole)
electrical current enters the bottom of anode stub hole

DEFINITIONS

Initial anode state: The state is defined as an ideal or virtual initial state of the anode placed in a bath with homogenous electric conductivity. The electric current distribution is not changed by the inhomogeneous effects from the electrolysis bath or by asymmetric coupling of the anode to the yoke by the cast iron. The frozen bath layer on the anode is distributed homogeneously and also dissolves in a homogenous manner. The current distribution in the anode is changed neither by anode consumption nor the bubble regime of CO₂ or by a change in the surface overvoltage on the anodes wear surface. We do not take into account the creation of spikes and deformations in the anodes wear surface caused by inhomogeneous frozen bath on the anode. The initial current distribution is therefore set by the anode itself, its geometries, and conductivity gradients.

Steady state of the anode: The state when anode has been consumed so that the electric current distribution in the anode converges to a homogenous distribution over the anode wear surface.

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