



Deliverable : Queries - SQL and Relation Algebra

Data Management Course

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1 Introduction

Writing queries in relational algebra and SQL helps learning how to use the database you've built. While the database design defines what data you have and how it's organized, queries are how you actually interact with it — asking questions, extracting information, and combining data from different tables. Relational algebra providing the theoretical foundation, and SQL turning these foundations to actual commands to manipulate data.

2 Requirements

For each query, provide RA and SQL:

- 1. Find the names of patients who have had at least one clinical activity handled by active staff.
- 2. Find Staff IDs of staff who are either 'Active' or have issued at least one prescription.
- 3. Find Hospital IDs of hospitals located in 'Benguerir' or having at least one department with the specialty 'Cardiology'.
- 4. Find Hospital IDs of hospitals that have both 'Cardiology' and 'Pediatrics' departments.
- 5. Find staff members who have worked in every department of the hospital with HID = 1.
- 6. Find staff members who participated in every clinical activity of the department with DEP_ID = 2.
- 7. Find pairs of staff members (s_1, s_2) such that s_1 has handled more clinical activities than s_2 .
- 8. Find Patient IDs of patients who had clinical activities with at least two different staff members.
- 9. Find CAIDs of clinical activities performed in September 2025 at hospitals located in 'Benguerir'.
- 10. Find Staff IDs of staff who have issued more than one prescription.
- 11. List IIDs of patients who have scheduled appointments in more than one department.
- 12. Find Staff IDs who have no scheduled appointments on the day of the Green March holiday (November 6).
- 13. Find departments whose average number of clinical activities is below the global departmental average.





- 14. For each staff member, return the patient who has the greatest number of completed appointments with that staff member.
- 15. List patients who had at least 3 emergency admissions during the year 2024.

Refinement: Derive functional dependencies from the MNHS schema.

3 Implementation & Results

Question 1

SQL:

Relational Algebra:

```
R = \rho_p(\text{Patient}) \bowtie_{\text{ca.iid} = \text{p.iid}} \rho_{ca}(\text{ClinicalActivity})
\pi_{\text{FullName}} \Big( \sigma_{s.\text{Status} = \text{``Active''}} \big( (R) \bowtie_{s.\text{staff\_id} = \text{ca.staff\_id}} \rho_s(\text{Staff}) \big) \Big)
```

Where:

• R: The join of patient on clinical activity on the same patient IDs.

Question 2





```
\pi_{STAFF\_ID}((\sigma_{Status='Active'}(Staff)) \cup (Prescription \bowtie Clinical activies \bowtie Staff))
```

Question 3

SQL:

```
-- 3. Find Hospital IDs of hospitals located in 'Benguerir'
-- or having at least one department with the specialty '
-- Cardiology'

SELECT DISTINCT H.HID
FROM Hospital H
WHERE H.City = 'Benguerir'
UNION
SELECT D.HID
FROM Department D
WHERE D.Specialty = 'Cardiology';
```

Relational Algebra:

```
R_1 = \pi_{HID}(\sigma_{City='Benguerir'}(Hospital))
R_2 = \pi_{HID}(\sigma_{Specialty='Cardiology'}(Department))
R = R_1 \cup R_2
Result: \pi_{HID}(R)
```

Where:

- R_1 : The set of all hospitals located in the city Benguerir.
- R_2 : The set of all the hospitals which have a department with the specialty Cardiology.
- R: The set of Hospital IDs of hospitals located in 'Benguerir' or having at least one department with the specialty 'Cardiology'.

Question 4

```
SELECT ca.STAFF_ID
FROM Prescription p
JOIN ClinicalActivity ca ON p.CAID = ca.CAID
```





```
GROUP BY ca.STAFF_ID
HAVING COUNT(p.PID) > 1;
```

```
R_1 = Prescription \bowtie_{Prescription.CAID = Clinical Activity.CAID} Clinical Activity
R_2 = \gamma_{STAFF\_ID,count(PID) \to cnt}(R_1)
R = \sigma_{cnt>1}(R_2)
Result = \pi_{STAFF\_ID}(R)
```

Where:

- R_1 : Jointure between Prescription and Clinical Activity on on CAID.
- R_2 : Counting the number of prescriptions by STAFF_ID.
- R_3 : Selecting staff with more than one prescription

Question 5

SQL:

```
-- 5. Find staff members who have worked in every department
-- of the hospital with HID = 1

SELECT s.STAFF_ID, s.FullName
FROM Work_in w
JOIN Department d ON d.DEP_ID = w.Dep_ID
JOIN Staff s ON s.STAFF_ID = w.STAFF_ID
WHERE d.HID = 1
GROUP BY s.STAFF_ID, s.FullName
HAVING COUNT(DISTINCT w.Dep_ID) = (
    SELECT COUNT(*) FROM Department WHERE HID = 1
);
```

Relational Algebra:

```
R_{1} = \pi_{\text{DEP\_ID}}(\sigma_{\text{HID}=1}(\text{Department}))
R_{2} = \delta(\pi_{\text{STAFF\_ID},\text{DEP\_ID}}(\text{Work\_in}))
R_{3} = R_{2} \div R_{1}
R_{4} = R_{3} \bowtie \text{Staff}
\text{Resultat} = \pi_{\text{Staff.STAFF\_ID}, \text{Staff.FullName}}(R_{4})
```

- R_1 : Departments belonging to the hospital with HID = 1.
- R_2 : Pairs of (STAFF_ID, DEP_ID) showing where each staff member worked (deduplicated).





- R_3 : Staff who worked in *all* departments of R_1 (division).
- R_4 : Join of R_3 with Staff to retrieve names.
- Resultat: STAFF_ID and FullName of those staff members.

Question 6

SQL:

```
-- 6. Find staff members who participated in every clinical

activity
-- of the department with DEP_ID = 2.

SELECT S.STAFF_ID FROM Staff S

JOIN clinicalactivity CA ON CA.STAFF_ID = S.STAFF_ID AND CA.

Dep_ID = 2

GROUP BY S.STAFF_ID

HAVING COUNT(*) = (

SELECT COUNT(*)

FROM clinicalactivity

WHERE Dep_ID = 2

);
```

Relational Algebra:

```
R_{1} = \pi_{CAID}(\sigma_{Dep\_ID=2}(ClinicalActivity))
R_{2} = \pi_{STAFF\_ID,CAID}(\sigma_{Dep\_ID=2}(ClinicalActivity))
R = R_{2} \div R_{1}
```

Result: $\pi_{STAFF_ID}(R)$

Where:

- R_1 : The set of all clinical activities belonging to department 2.
- R_2 : The set of $(STAFF_ID, CAID)$ pairs representing staff participation in department 2 activities.
- R: The set of staff members who participated in *every* clinical activity of department 2.

Question 7





```
FROM ClinicalActivity
GROUP BY staff_id)
SELECT s1.staff_id, ac1.ac_count AS s1_count, s2.staff_id, ac2.

\[
\to ac_count AS s2_count
\]
FROM Staff s1
JOIN Staff s2 ON 1=1
JOIN SActivityCount ac1 ON ac1.staff_id = s1.staff_id
JOIN SActivityCount ac2 ON (ac2.staff_id = s2.staff_id AND ac2.

\(
\to ac_count < ac1.ac_count);
\]
```

```
SActivityCount = \gamma_{\text{staff\_id, COUNT(*)}\rightarrow\text{ac\_count}} (ClinicalActivity)

R1 = (\rho_{s1}(\text{Staff}) \times \rho_{s2}(\text{Staff})) \bowtie_{ac1.\text{staff\_id}=s1.\text{staff\_id}} \rho_{ac1}(\text{SActivityCount})

R2 = \rho_{ac2}(\text{SActivityCount})
```

```
\pi_{s1.\text{staff\_id},ac1.\text{ac\_count},s2.\text{staff\_id},ac2.\text{ac\_count}}\left(\sigma\left(\left(R1\right)\bowtie_{ac2.\text{staff\_id}=s2.\text{staff\_id}\land\left(ac2.\text{ac\_count}\lessdot ac1.\text{ac\_count}\right)}R2\right)\right)
```

Where:

- SActivityCount: A temporary table that contains staff IDs associated to the corresponding number of clinical activities.
- R1: The join of the pairs of staff members (cartesian product) on their respective number of clinical activities.
- R2: An alias on SActivityCount for a better readability.

Question 8

SQL:

```
-- 8 . Find Patient IDs of patients who had clinical activities

→ with at least two different staff members

SELECT DISTINCT c1.IID FROM
clinicalactivity c1

JOIN
clinicalactivity c2
ON c1.IID = c2.IID
WHERE c1.STAFF_ID <> c2.STAFF_ID;
```

Relational Algebra:

 $\pi_{C1.IID}(\sigma_{C1.STAFF_ID \neq C2.STAFF_ID}(\rho_{C1}(\text{ClinicalActivity}) \bowtie_{\text{C1.IID}=\text{C2.IID}} \rho_{C2}(\text{ClinicalActivity})))$





Question 9

SQL:

```
-- 9. Find CAIDs of clinical activities performed in September

-- 2025
-- at hospitals located in "Benguerir"

SELECT CAID
FROM ClinicalActivity CA

JOIN Department D ON D.Dep_ID = CA.Dep_ID

JOIN Hospital H ON D.HID = H.HID

WHERE H.City = 'Benguerir'

AND CA.Date >= '2025-09-01'

AND CA.Date < '2025-10-01';
```

Relational Algebra:

```
R_{1} = \sigma_{City='Benguerir'}(Hospital)
R_{2} = R_{1} \bowtie Department
R_{3} = R_{2} \bowtie_{D.Dep\_ID=CA.Dep\_ID} ClinicalActivity
R_{4} = \sigma_{Date \geq '2025-09-01' \land Date < '2025-10-01'}(R_{3})
R = \pi_{CAID}(R_{4})
```

Result: R

Where:

- R_1 : The set of all the hospitals located in Benguerir.
- R_2 : The set of all the departments that belong to hospitals located in Benguerir.
- R_3 : The set of all the clinical activities linked to those departments.
- R_4 : Selecting only the clinical activities that occurred in the September of 2025.
- R: The CAIDs of these clinical activities.

Question 10

SQL:

Relational Algebra:

```
R = \sigma_{Specialty='Cardiology' \lor Specialty='Pediatrics'}(Department)
Result = \pi_{HID}(R)
```





• R: Selecting departents specialized in Cardiology or Pediatrics

Question 11

SQL:

```
-- 11. List IIDs of patients who have scheduled appointments
-- in more than one department

SELECT ca.IID
FROM ClinicalActivity ca
JOIN Appointment a ON a.CAID = ca.CAID
WHERE a.Status = 'Scheduled'
GROUP BY ca.IID
HAVING COUNT(DISTINCT ca.DEP_ID) > 1;
```

Relational Algebra (using Aggregation):

```
R_{1} = \sigma_{\text{Status}='Scheduled'}(\text{Appointment})
R_{2} = \text{ClinicalActivity} \bowtie_{\text{CAID}} R_{1}
R_{3} = \pi_{\text{IID},\text{DEP},\text{ID}}(R_{2})
R_{4} = \gamma_{\text{IID}; \text{ dcount}:=\text{COUNT},\text{DISTINCT}(\text{DEP},\text{ID})}(R_{3})
\text{Resultat} = \pi_{\text{IID}}(\sigma_{\text{dcount}>1}(R_{4}))
```

Where:

- R_1 : Appointments whose status is Scheduled.
- R₂: Join between ClinicalActivity and scheduled appointments.
- R₃: Pairs of (patient IID, department DEP_ID).
- R₄: Count of distinct departments per patient.
- Resultat: IIDs of patients with appointments in more than one department.

Question 12

```
-- 12. Find Staff IDs who have no scheduled appointments
-- on the day of the Green March holiday (November 6).

SELECT S.STAFF_ID FROM Staff S

WHERE (

SELECT COUNT(*) FROM clinicalactivity CA

JOIN appointment A ON CA.CAID = A.CAID

WHERE CA.STAFF_ID = S.STAFF_ID

AND A.Status = 'Scheduled'

AND MONTH(CA.Date) = 11

AND DAY(CA.Date) = 6

) = 0;
```





```
M = \rho(CA, Clinical Activity) \bowtie_{CA.CAID=A.CAID} \rho(A, Appointment)
R_{busy} = \pi_{CA.STAFF\_ID} (\sigma_{A.Status='Scheduled' \land MONTH(CA.Date)=11 \land DAY(CA.Date)=6}(M))
R_{all} = \pi_{STAFF\_ID}(Staff)
```

Result:
$$R := R_{all} - R_{busy}$$

Where:

- ullet M: The join between ClinicalActivity and Appointment, relating activities to their appointments.
- R_{busy} : The set of staff members who have at least one scheduled appointment on November 6.
- R_{all} : The set of all staff members.
- R: The resulting set of staff with no scheduled appointments on November 6 (i.e., $R_{all} R_{busy}$).

Question 13

SQL:

```
-- 13. Find departments whose average number of clinical

activities
-- is below the global departmental average.

WITH DActivityCount AS (
SELECT dep_id, COUNT(*) AS ac_count
FROM ClinicalActivity
GROUP BY dep_id),
GlobalAvg AS (
SELECT AVG(ac_count) AS ca_avg FROM DActivityCount)

SELECT d.dep_id, ac.ac_count, ga.ca_avg
FROM Department d
JOIN DActivityCount ac ON ac.dep_id = d.dep_id
JOIN GlobalAvg ga ON 1=1
WHERE ac.ac_count < ga.ca_avg;
```

Relational Algebra:

```
DActivityCount = \gamma_{\text{dep\_id}, COUNT(*) \to \text{ac\_count}}(ClinicalActivity})
```

```
GlobalAvg = \gamma_{\text{AVG(ac\_count)} \to \text{ca\_avg}}(DActivityCount)
R = (\rho_d(\text{Department}) \bowtie_{ac.\text{dep\_id} = d.\text{dep\_id}} \rho_{ac}(DActivityCount)) \times \rho_{ga}(GlobalAvg)
```





$$\pi_{d.\text{dep_id}, ac.\text{ac_count}, ga.\text{ca_avg}} = \left(\sigma_{ac.\text{ac_count} < ga.\text{ca_avg}}(R)\right)$$

Where:

- DActivityCount: A temporary table that contains department IDs associated to the corresponding number of clinical activities.
- Global Avg: A temporary table that contains the average value of the number of clinical activities in all the departments.
- R: The cartesian product (because it should be displayed for each row) of the global average with a join of department on the corresponding activity count for each one.

Question 14

SQL:

```
-- 14 . For each staff member, return the patient who has the
   \hookrightarrow greatest number of completed appointments with that staff
   \hookrightarrow member.
SELECT
    P.FullName As PatientName
FROM
    Appointment A
    JOIN Clinical Activity CA ON A. CAID = CA. CAID
    JOIN Staff S ON CA.STAFF_ID = S.STAFF_ID
    JOIN Patient P ON CA.IID = P.IID
WHERE
    A. Status = 'Completed'
GROUP BY
    S.STAFF_ID, P.IID
HAVING
    COUNT(*) = (
        SELECT MAX (PatientCount)
        FROM (
             SELECT CA2.IID, COUNT(*) AS PatientCount
             FROM Appointment A2
             JOIN Clinical Activity CA2 ON A2. CAID = CA2. CAID
             WHERE A2. Status = 'Completed'
               AND CA2.STAFF_ID = S.STAFF_ID
             GROUP BY CA2.IID
        ) AS StaffPatients
    );
```

Relational Algebra:





```
A_c := \sigma_{\text{Status}='Completed'}(\text{Appointment})
T := \gamma_{\text{STAFF\_ID}, \text{ IID}; \text{ cnt}=\text{COUNT}(*)}(A_c \bowtie_{A_c.\text{CAID}=\text{ClinicalActivities}.\text{CAID}} \text{ ClinicalActivities})
M := \gamma_{\text{STAFF\_ID}; \text{ maxcnt}=\text{MAX}(\text{cnt})}(T)
\pi_{\text{FullName}}\Big((T \bowtie_{T.\text{STAFF\_ID}=M.\text{STAFF\_ID}} \wedge T.\text{cnt}=M.\text{maxcnt}} M) \bowtie_{T.\text{IID}=\text{Patient.IID}} \text{Patient})\Big)
```

Question 15

SQL:

```
-- 15. List patients who had at least 3 emergency admissions
-- during the year 2024.

SELECT FullName
FROM Patient P
JOIN ClinicalActivity CA ON CA.IID = P.IID

JOIN Emergency E ON E.CAID = CA.CAID

WHERE CA.Date >= '2024-01-01'

AND CA.Date < '2025-01-01'

GROUP BY P.IID

HAVING COUNT(E.CAID) >= 3;
```

Relational Algebra:

```
R_{1} = \sigma_{Date \geq '2024\text{-}01\text{-}01' \wedge Date < '2025\text{-}01\text{-}01'}(Clinical Activity)
R_{2} = R_{1} \bowtie Emergency
R_{3} = \pi_{IID,E.CAID}(R_{2})
R = \pi_{FullName} \left(\sigma_{num\_emergency \geq 3}(\gamma_{P.IID,\ COUNT(E.CAID) \rightarrow num\_emergency}(R_{3} \bowtie Patient))\right)
```

Result: R

- R_1 : Clinical activities performed in 2024.
- R_2 : Emergency activities joined with those clinical activities.
- R_3 : The patient IID with the clinical activity id of R2 (which contain all the emergencies performed in 2024).
- R: The full name of all the patients that the number of emergencies is more than 3 (after grouping the emergencies per patient using γ).





Functional Dependencies in MNHS Database

In this section, we list the key functional dependencies (FDs) identified in the Moroccan National Health Services (MNHS) database.

We do not write the **trivial functional dependencies**, such as:

- \bullet $R \to R$
- ullet All attributes o all attributes

because they do not provide new information about the structure of the database.

We also use **Armstrong's axioms** to infer additional dependencies from the given ones. The main axioms are:

- 1. **Reflexivity:** If $Y \subseteq X$, then $X \to Y$. Example: $\{A, B\} \to \{A\}$.
- 2. **Augmentation:** If $X \to Y$, then $XZ \to YZ$. *Example:* If $A \to B$, then $AC \to BC$.
- 3. **Transitivity:** If $X \to Y$ and $Y \to Z$, then $X \to Z$. *Example:* If $A \to B$ and $B \to C$, then $A \to C$.

These axioms allow us to infer non-trivial FDs from the given ones and to reason about keys, superkeys, and normalization.

Functional Dependencies by Relation

Patients

$$I \to ICSFBSEP$$
 (PK), $C \to ICSFBSEP$ (CK)

- I: Patient ID (IID)
- C: CIN
- S: Sex
- F: FullName
- B: Birth
- E: BloodGroup
- P: Phone



Hospital

$$H \to HNCR$$
 (PK), $C \to R$ (CK), $NC \to HNCR$

(no pair of hospitals with same city and name)

Where:

- H: Hospital ID (HID)
- N: Name
- C: City
- R: Region

Department

$$D \to DHNS$$
 (PK), $HN \to DHNS$

(no hospital with a pair of department with the same name)

Where:

- D: Department ID (DEP_ID)
- H: Hospital ID (HID)
- N: Name
- S: Specialty

Staff

$$S \to SFSt$$
 (PK)

Where:

- S: Staff ID (STAFF_ID)
- F: FullName
- St: Status

Work_in

$$SD \to SD$$
 (PK)

- S: Staff ID
- D: Department ID





ClinicalActivity

$$C \to CISDDtT$$
 (PK), $ISTD \to C$

(no staff member performing a ca in a patient in 2 different departments at the same time)

- Where:
- C: ClinicalActivity ID (CAID)
- I: Patient ID (IID)
- S: Staff ID
- D: Department ID
- Dt: Date
- T: Time

Appointment

$$C \to CRS \text{ (PK)}$$

- Where:
- C: Clinical Activity ID (CAID)
- R: Reason
- S: Status

Emergency

$$C \to CTO$$
 (PK)

- Where:
- C: ClinicalActivity ID (CAID)
- T: TriageLevel
- O: Outcome

Insurance

$$I \to IT \text{ (PK)}$$

- Where:
- I: Insurance ID
- T: Type





Expense

$$E \to EICT$$
 (PK), $C \to EICT$ (CK)

Where:

- E: Expense ID
- I: Insurance ID
- C: Clinical Activity ID
- T: Total

Medication

$$M \to MNFSATMf$$
 (PK), $N \to NATMf$, $A \to T$

(no pair of medication with same NATMf but maybe different forms of strengh so id -eg: Doliprane) (A determine a big part of the effect)

Where:

- M: Medication ID (MID)
- N: Name
- F: Form
- S: Strength
- A: ActiveIngredient
- T: TherapeuticClass
- Mf: Manufacturer

Stock

$$MHS \rightarrow HMSUQR$$
 (PK)

- M: Medication ID
- H: Hospital ID
- S: StockTimestamp
- U: UnitPrice
- Q: Quantity
- R: ReorderLevel



Prescription

$$P \to PCD$$
 (PK), $C \to PCD$ (CK)

Where:

- P: Prescription ID
- C: ClinicalActivity ID
- D: DateIssued
- PC: Patient/Clinical details

Includes

$$PM \to PMDDu$$
 (PK)

Where:

- P: Prescription ID
- M: Medication ID
- D: Dosage
- Du: Duration

ContactLocation

$$C \to CCiPSNPoPh$$
 (PK), $Po \to Ci$, $P \to Ci$

(the postal code or province determine the city)

Where:

- C: ContactLocation ID (CLID)
- Ci: City
- P: Province
- S: Street
- N: Number
- Po: PostalCode
- Ph: Phone

Have

$$IC \to IC$$
 (PK)

- I: Patient ID
- C: ContactLocation ID





4 Discussion

Challenges faced

- Writing queries in Relational Algebra and SQL was sometimes tricky, especially when dealing with complex joins, nested queries, and aggregation functions.
- Identifying functional dependencies required paying attention to details and understanding how the different data components interact with each other.

Observations

- This step helped clarify parts of the database schema that were ambiguous; writing queries forced us to think carefully about keys and relationships.
- Functional dependencies can guide you to better understanding and optimization of the database to avoid redundancy or incorrect results.

Lessons learned

- Understanding relationships between entities is crucial before trying to write queries.
- Choosing the right attributes for selections, projections, and join conditions is key to producing accurate results.
- Writing queries and identifying functional dependencies helps uncover subtle aspects of the schema that impact both correctness and efficiency.

5 Conclusion

In this lab, we successfully translated instruction into concrete queries using Relational Algebra and SQL. We practiced writing queries to retrieve, manipulate, and combine data while respecting the structure of tables, keys, and relationships defined in the schema. During this process, we also identified functional dependencies giving a first idea of future optimizations, understanding how the data actually interact with itself. Overall, this lab highlighted how writing queries and analyzing functional dependencies are crucial steps in making a database not only theoretically correct, but also practically usable to answer real-world questions.