CSCI 4360 Data Science II Project I

Ayush Kumar, Faisal Hoissain, Brandon Amirouche

February 23, 2021

Contents

1	Introduction and Methodology 1.1 Code Credits	1 1
2	Auto-MPG	1
3	Concrete Compressive Strength	1
4	Crime	1
5	Wine Quality 5.1 The Dataset 5.2 Exploratory Data Analysis 5.3 Multiple Linear Regression 5.4 Quadratic Regression 5.5 Quadratic Regression with Cross Terms 5.6 Cubic Regression 5.7 Cubic Regression with Cross Terms	2 4 6 6 6
6	Seoul Bike Rentals	6
7	Air Quality	6
1 1.		

- 2 Auto-MPG
- 3 Concrete Compressive Strength
- 4 Crime
- 5 Wine Quality
- 5.1 The Dataset

The wine quality data is actually two datasets, one for red wine and the other for white wine. Both of them have the same 11 features, but there may be differences in the features that matter, as well as the overall results of regression. A dummy variable could be created to meld the datasets into one overall set, but if there are substantial differences between the two it may substantially add to model complexity. The dataset has the following variables:

- 1. fixed.acidity
- 2. volatile.acidity
- 3. citric.acid
- 4. residual.sugar

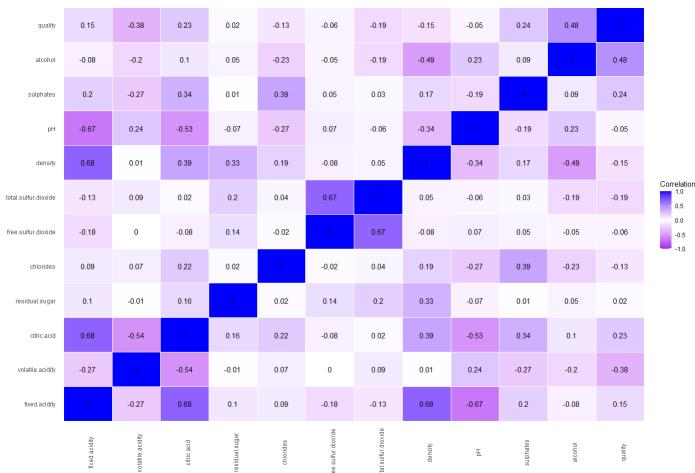
- 5. chlorides
- 6. free.sulfur.dioxide
- 7. total.sulfur.dioxide
- 8. density
- 9. pH
- 10. sulfates
- 11. alcohol
- 12. quality (the response variable)

The red wine dataset has 1,599 observations, and the white wine dataset has 4,898 observations. The two files can be found in the data/WineQuality folder, and were originally downloaded from the UCI Machine Learning Repository. [insert link here]

5.2 Exploratory Data Analysis

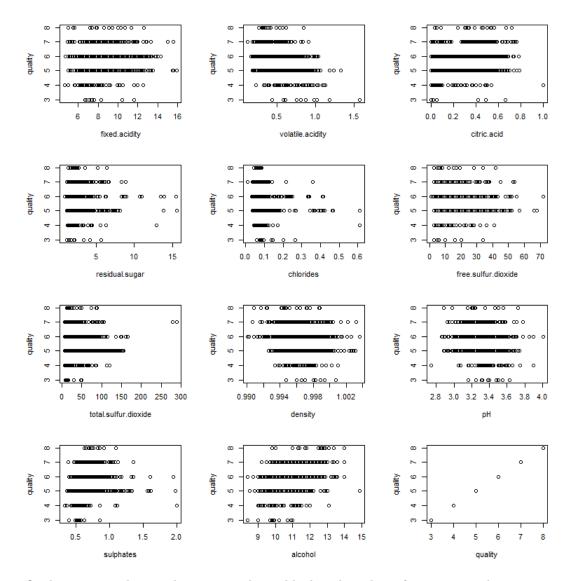
The first step in EDA was to checkout the collinearity of features, and how well they correlate with our response variables.

Red Wine Correlation Matrix (Plotted with R)



From the Red Wine Correlation Matrix (Figure 1) we can see that there are a few variables that have fairly strong correlations with each other. The citric acid content and the fixed acidity seem to be highly correlated with each other, and this pattern holds true for many of the features that depend on acidity. We can see that pH is highly correlated with fixed acidity and citric acid as well. This will be important to consider as it may create a problem in our regression. Based on the results of our variable screening methods, we may consider dropping one or more these variables, or using them as an instrumental variable to reduce the endogeneity issue with this dataset. Another highly correlated issue may be density and fixed acidity, as well as free sulfur dioxide and total sulfur dioxide. It may be worth our time to standardize some of these variables to limit collinearity, and this will be considered during variable selection.

Red Wine Scatter Plots (R)



Quality seems to be a multi-categorical variable, based on this information maybe regression is not the best way to predict on this dataset, but it may give a great deal of information regarding feature selection. Some features exhibit very peculiar behavior of having similar characteristics for both low and high quality wines, but not for middle quality wines. This can be illustrated when we take a look at total sulfur dioxide, chlorides, and residual sugar. This pattern may mislead us during variable selection, so it may be a good idea to add in quadratic terms for these variables to account for their curving behavior. If these variables fail to be selected initially then I will rerun variable selection methods taking into account their quadratic terms. There may be other transformations needed, but we can determine those after variable selection bases on partial residual plots.

5.3 Multiple Linear Regression

Variable Selection for Red Wine

Output has been modified for space. Run code for full output.

Start: AIC=-682.5 quality ~ 1

```
Df Sum of Sq
                                  RSS
                                           AIC
+ alcohol
                        236.295 805.87 -1091.65
+ volatile.acidity
                   1 158.967 883.20 -945.14
                       65.865 976.30 -784.89
+ sulphates
                    1
              1 53.405 988.76 -764.61
+ citric.acid
+ total.sulfur.dioxide 1 35.707 1006.46 -736.24
+ density
                   1 31.887 1010.28 -730.19
+ chlorides
                    1
                       17.318 1024.85 -707.29
                   1 16.038 1026.13 -705.29
+ fixed.acidity
                   1 3.473 1038.69 -685.84
+ pH
+ free.sulfur.dioxide 1 2.674 1039.49 -684.61
<none>
                               1042.17 -682.50
+ residual.sugar 1
                          0.197 1041.97 -680.80
```

Step: AIC=-1091.65
quality ~ alcohol

Df Sum of Sq RSS AIC + volatile.acidity 1 94.074 711.80 -1288.1

Step: AIC=-1288.14

quality ~ alcohol + volatile.acidity

Df Sum of Sq RSS AIC + sulphates 1 19.6916 692.10 -1331.0

Step: AIC=-1331

quality ~ alcohol + volatile.acidity + sulphates

Df Sum of Sq RSS AIC + total.sulfur.dioxide 1 8.2176 683.89 -1348.1

Step: AIC=-1348.1

quality ~ alcohol + volatile.acidity + sulphates + total.sulfur.dioxide

Df Sum of Sq RSS AIC + chlorides 1 8.0370 675.85 -1365.0

Step: AIC=-1365

Df Sum of Sq RSS AIC + pH 1 5.9189 669.93 -1377.1

```
Df Sum of Sq
                                      RSS
                                               AIC
+ free.sulfur.dioxide 1
                           2.39413 667.54 -1380.8
<none>
                                   669.93 -1377.1
Step: AIC=-1380.79
quality ~ alcohol + volatile.acidity + sulphates + total.sulfur.dioxide +
    chlorides + pH + free.sulfur.dioxide
                 Df Sum of Sq
                                 RSS
                                          AIC
                              667.54 -1380.8
<none>
Call:
lm(formula = quality ~ alcohol + volatile.acidity + sulphates +
    total.sulfur.dioxide + chlorides + pH + free.sulfur.dioxide,
   data = red_wine)
```

One of the variables that was omitted here was residual sugar, one of the variables that exhibited very strong quadratic behavior. I will be rerunning forward selection while including the quadratic term for residual sugar and it will be included for all of the following variable selection methods as well. This is the final call when I include the quadratic term in the forward step.

```
Call:
lm(formula = quality ~ alcohol + volatile.acidity + sulphates +
total.sulfur.dioxide + chlorides + pH + free.sulfur.dioxide,
data = red_wine)
```

As can be seen even the inclusion of the quadratic term did not change the results of the forward selection. Below are listed the final conclusions of backwards elimination and step wise regression.

Backward Elimination

```
Call:
```

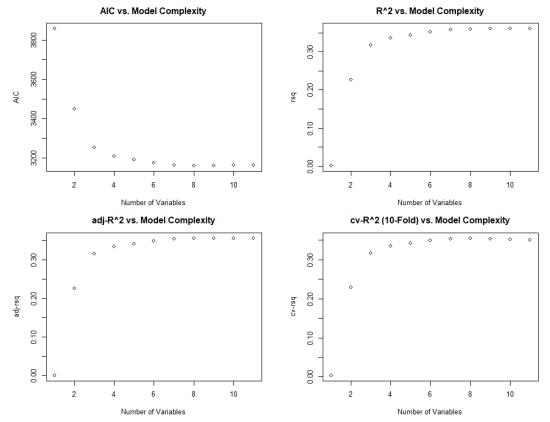
```
lm(formula = quality ~ volatile.acidity + chlorides + free.sulfur.dioxide +
total.sulfur.dioxide + pH + sulphates + alcohol, data = red_wine)
```

Step Regression

Call:

```
lm(formula = quality ~ alcohol + volatile.acidity + sulphates +
total.sulfur.dioxide + chlorides + pH + free.sulfur.dioxide,
data = red_wine)
```

While the methods may be different every single one of our variable screening methods chose the same seven variables to include: alcohol, volatile.acidity, sulphates, total.sulfur.dioxide, chlorides, pH, and free.sulfur.dioxide. These are the variables that will be included in all our models for red wine moving forward.



Here we can see that as we increase the number of variables, we see diminishing marginal improvement in quality of fit. For measures that penalize model complexity such as \mathbb{R}^2 and AIC we can even see a light bend towards the quality of fit worsening as model complexity increases. The diminishing returns can in part be explained by variables that have weak correlation

5.4 Quadratic Regression

All linear and quadratic terms were included for forward selection, backward elimination, and step wise regression in both ScalaTion and R. The optimal models are shown here in the table alongside the 4 quality of fit measures. R^2 , R_{cv}^2 , \bar{R}^2 , AIC.

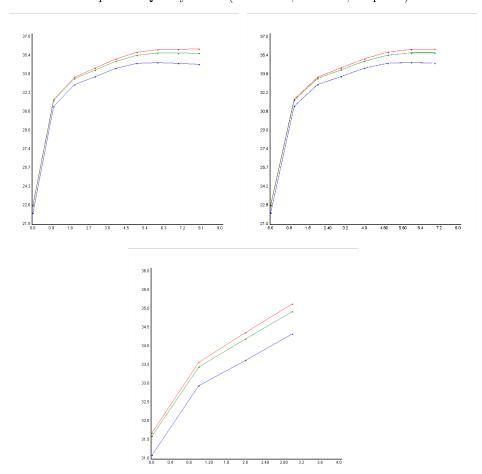
Here we can see that as we begin to increase the complexity of the model past a certain point that it begins to over-fit which results in the R^2 and $adj - R^2$ to continue increasing, but when we cross=validate the R^2 is substantially lower. This is a problem.

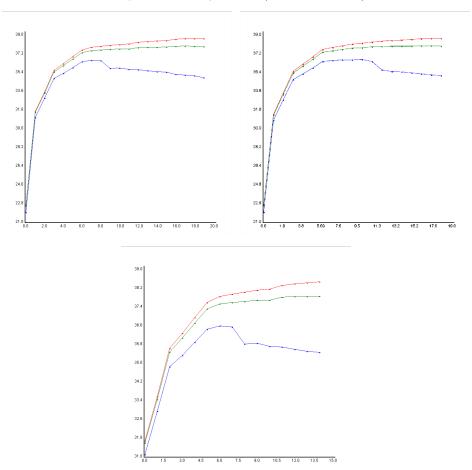
5.5 Quadratic Regression with Cross Terms

The effect of the drop in R_{cv}^2 and the non-cross validated measures show that increasing the number of variables results in models that are severely over fit. By using the Stepwise regression we can see that as soon as the non-cross validated measures start to decline we should stop adding more variables to maintain a model useful outside of the training dataset.

- 5.6 Cubic Regression
- 5.7 Cubic Regression with Cross Terms
- 6 Seoul Bike Rentals
- 7 Air Quality

Figure 1: Graphs for Quality of Fit (Backward, Forward, Stepwise)





 $\begin{tabular}{ll} Figure 3: \\ Graphs for Quality for Fit (Wine Quadratic-Cross) \end{tabular}$

