



# Degree centrality



#### Important nodes

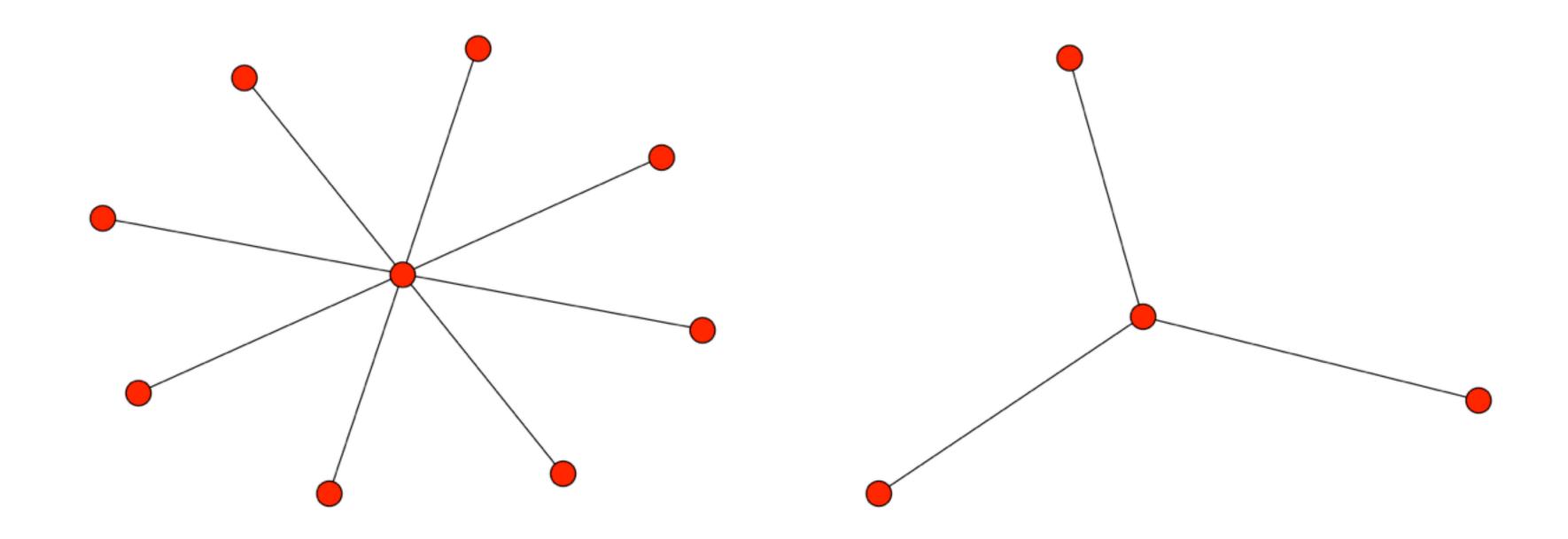
- Which nodes are important?
  - Degree centrality
  - Betweenness centrality





#### Important nodes

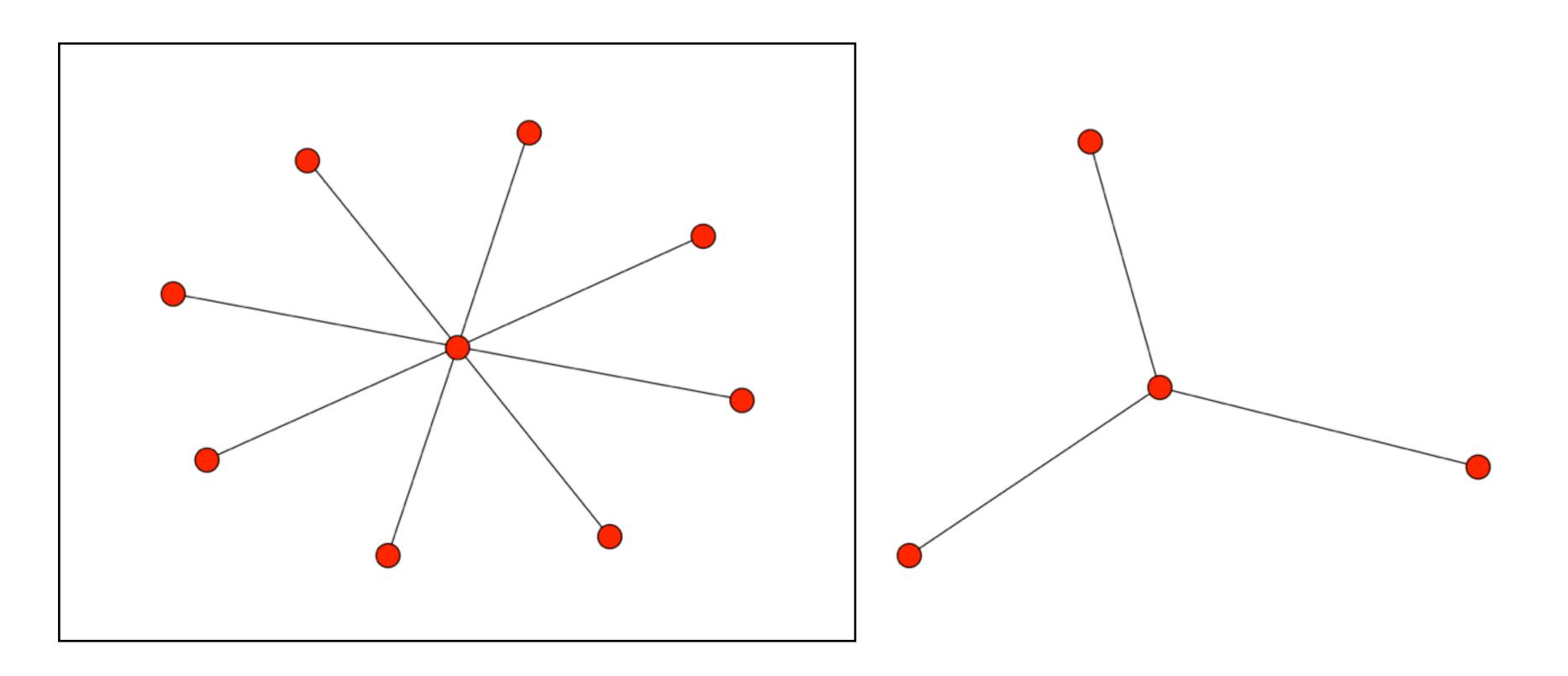
• Which centre node might be more important?





#### Important nodes

• Which centre node might be more important?





#### Degree centrality

Definition:

Number of Neighbours I Have

Number of Neighbours I Could Possibly Have

- Examples of nodes with high degree centrality:
  - Twitter broadcasters
  - Airport transportation hubs
  - Disease super-spreaders



#### Number of neighbors

```
In [1]: G.edges()
Out[1]: [(1, 2), (1, 3), (1, 4), (1, 5), (1, 6), (1, 7), (1, 8),
(1, 9)
In [2]: G.neighbors(1)
Out[2]: [2, 3, 4, 5, 6, 7, 8, 9]
In [3]: G.neighbors(8)
Out[3]: [1]
In [4]: G.neighbors(10)
NetworkXError: The node 10 is not in the graph.
```



#### Degree centrality

```
In [5]: nx.degree_centrality(G)
Out[5]:
{1: 1.0,
    2: 0.125,
    3: 0.125,
    4: 0.125,
    5: 0.125,
    6: 0.125,
    7: 0.125,
    8: 0.125,
    9: 0.125}
```





# Let's practice!





# Graph algorithms



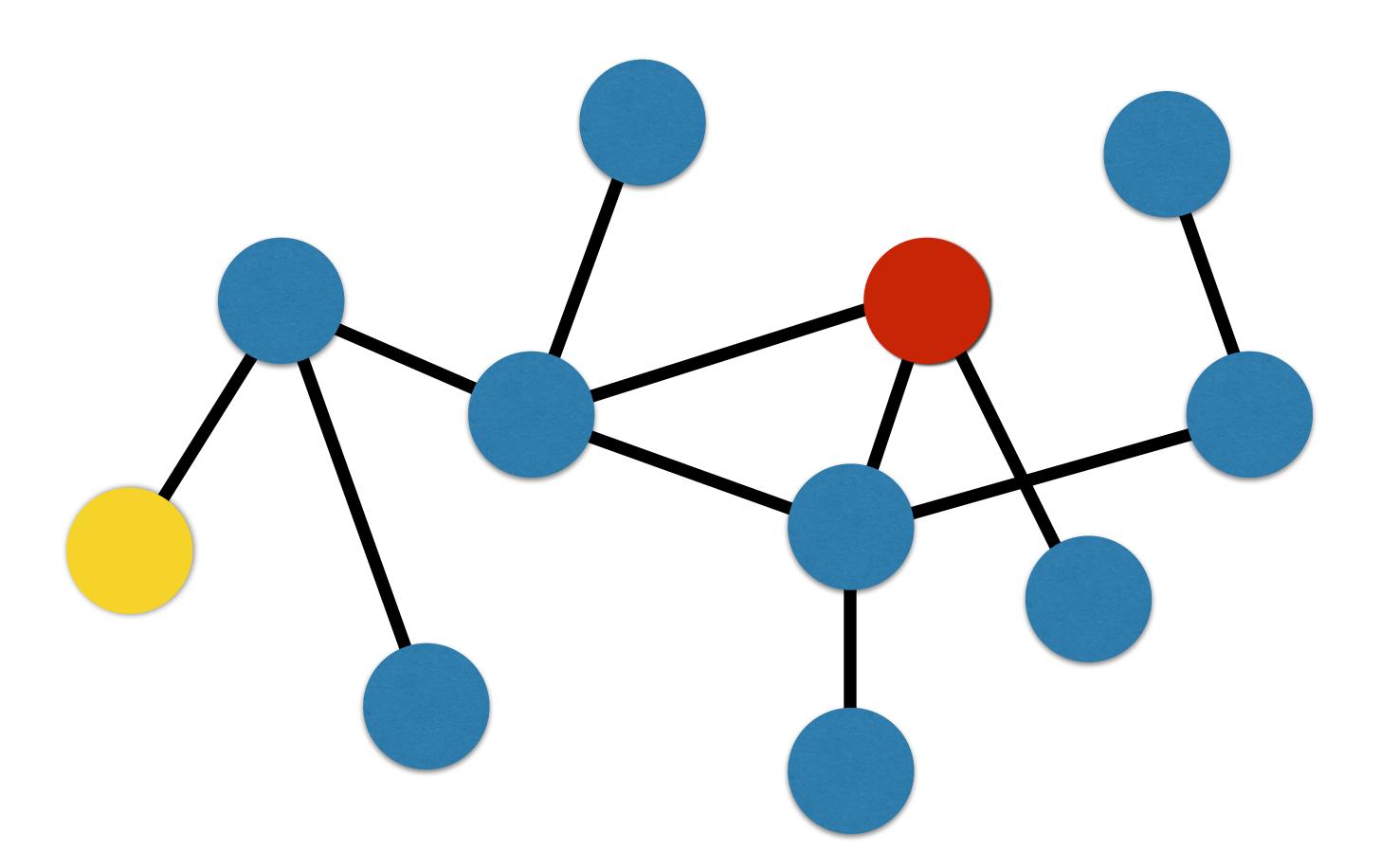
# Finding paths

- Pathfinding is important for
  - Optimization: e.g. shortest transport paths
  - Modeling: e.g. disease spread, information passing
- Algorithm: Breadth-first search





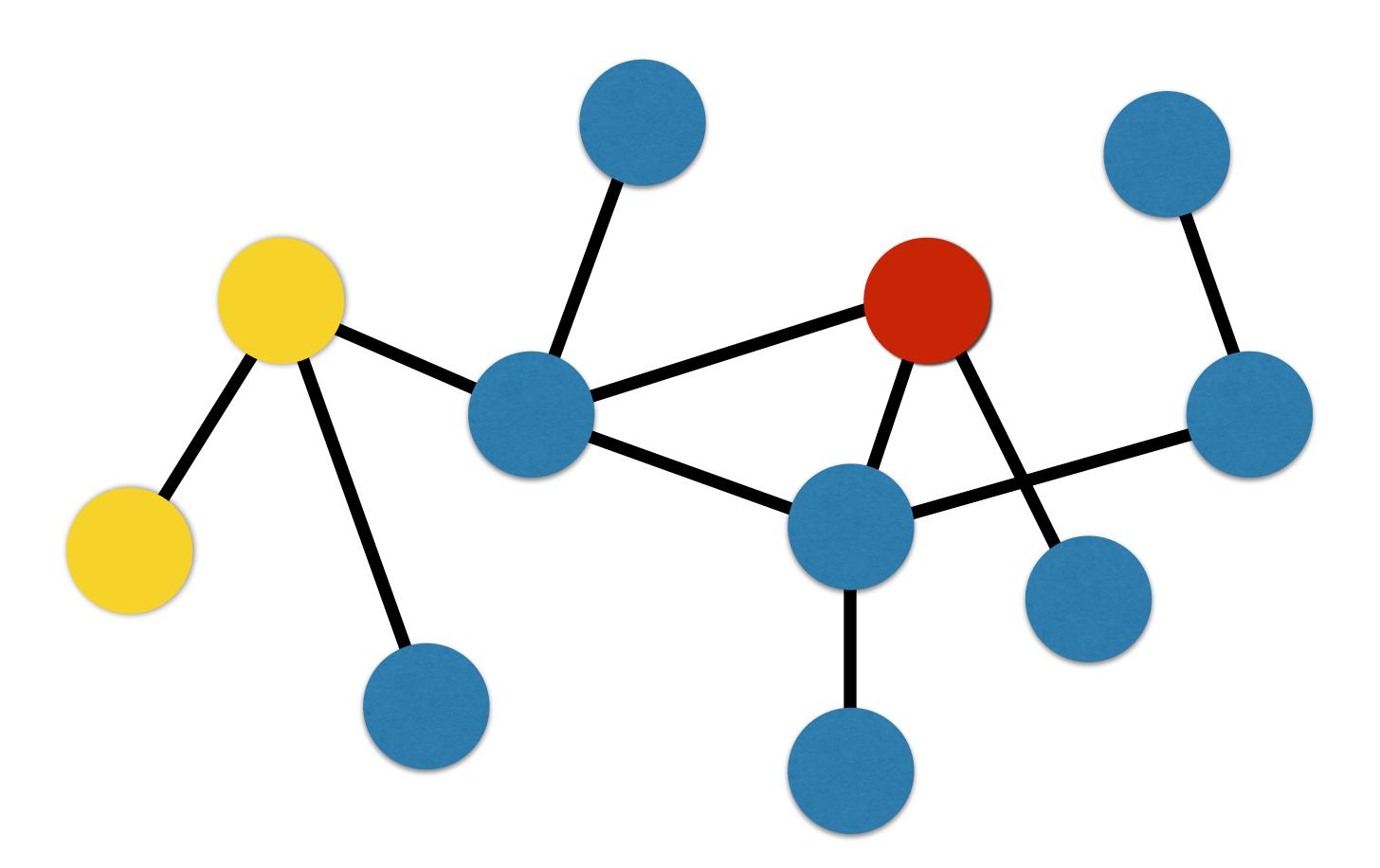
Example: Shortest path between two nodes







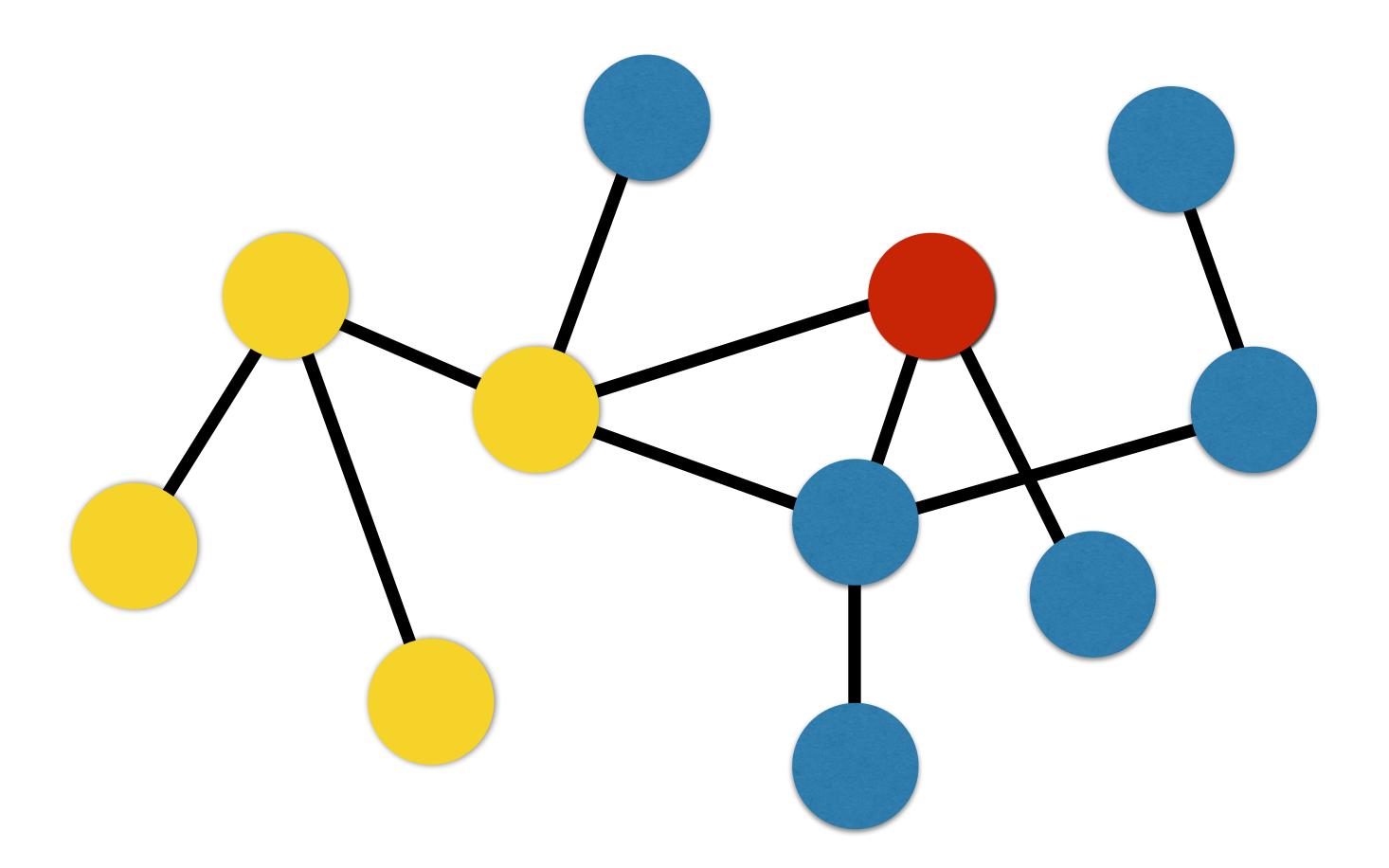
Example: Shortest path between two nodes





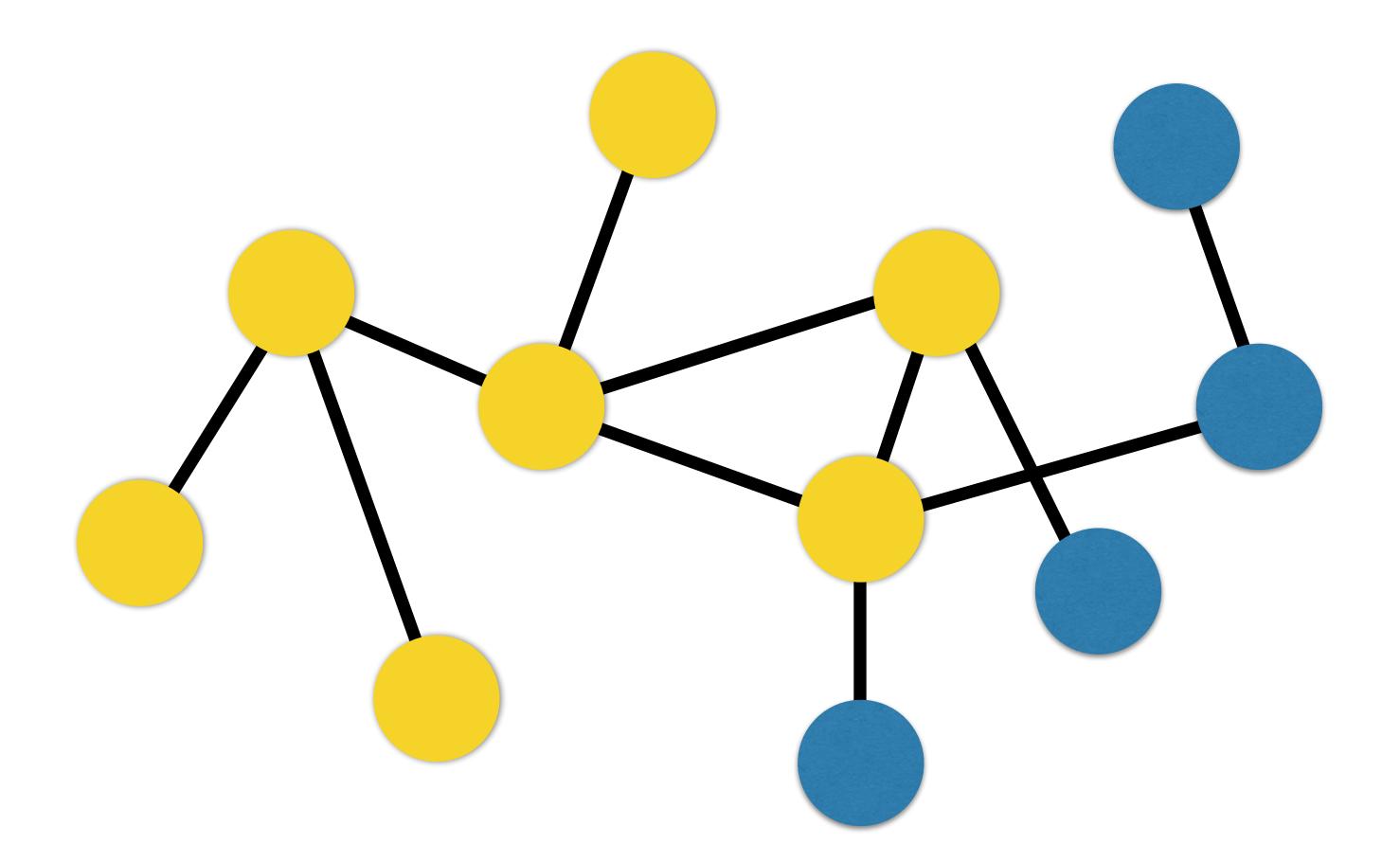


Example: Shortest path between two nodes





• Example: Shortest path between two nodes





## Recall: Neighbors

```
In [1]: G
Out[1]: <networkx.classes.graph.Graph at 0x10cc08828>
In [2]: len(G.edges())
Out[2]: 57
In [3]: len(G.nodes())
Out[3]: 20
In [4]: G.neighbors(1)
Out[4]: [10, 5, 14, 7]
In [5]: G.neighbors(10)
Out[5]: [1, 19, 5, 17, 8, 9, 13, 14]
```





# Let's practice!





# Betweenness centrality



### All shortest paths

- Set of paths
- Each path is shortest path between a given pair of nodes
- Done for all node pairs



#### Betweenness centrality

Definition:

num. shortest paths through node all possible shortest paths

- Application:
  - Bridges between liberal- and conservativeleaning Twitter users
  - Critical information transfer links





#### Examples

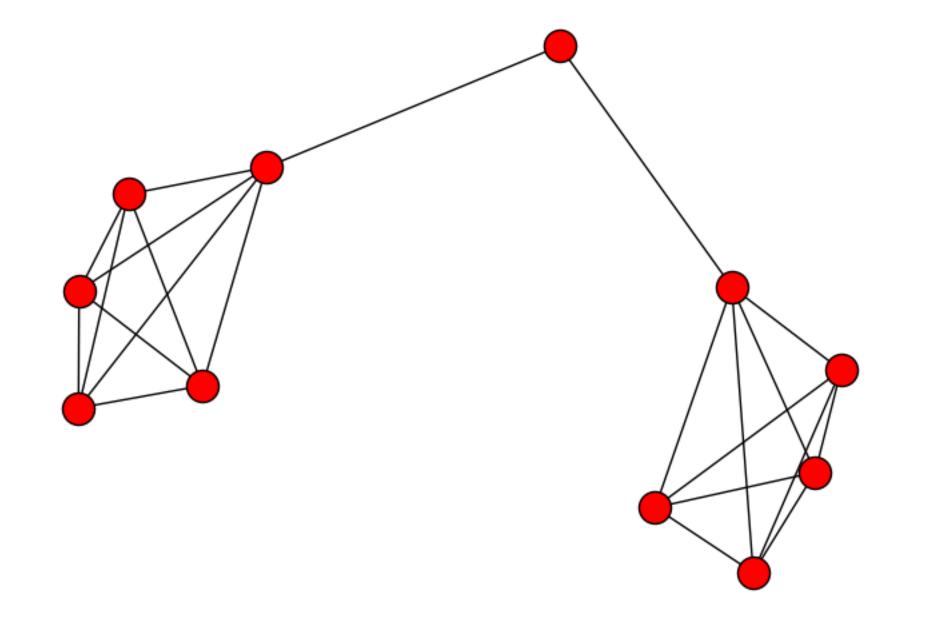
• Singapore: Raffles Place & Jurong East

#### Singapore MRT & LRT Network Map Khatib 🖨 Choa Chu Kang 🧲 **Bukit Gombak** Marymount Bukit Batok **Botanic Garde** Paya Lebar Kembangan Airport 🖨 Dakota Circle Line Haw Par Villa Pasir Panjang Labrador Park



## Example

• High betweenness centrality, low degree centrality?





#### Betweenness centrality

```
In [5]: import networkx as nx
In [6]: G = nx.barbell_graph(m1=5, m2=1)
In [10]: nx.betweenness_centrality(G)
Out[10]:
{0: 0.0,
1: 0.0,
2: 0.0,
3: 0.0,
5: 0.555555555555556,
7: 0.0,
8: 0.0,
9: 0.0,
10: 0.0}
```





# Let's practice!