

K-Means Clustering

Unsupervised Learning

- Trying to find hidden structure in unlabeled data
- No error or reward signal to evaluate a potential solution
- Common techniques: K-Means clustering, Hierarchical clustering, hidden Markov models, etc.
 - It has a long history, and used in almost every field, e.g., medicine, psychology, botany, sociology, biology, archeology, marketing, insurance, libraries, etc.

Unsupervised Learning

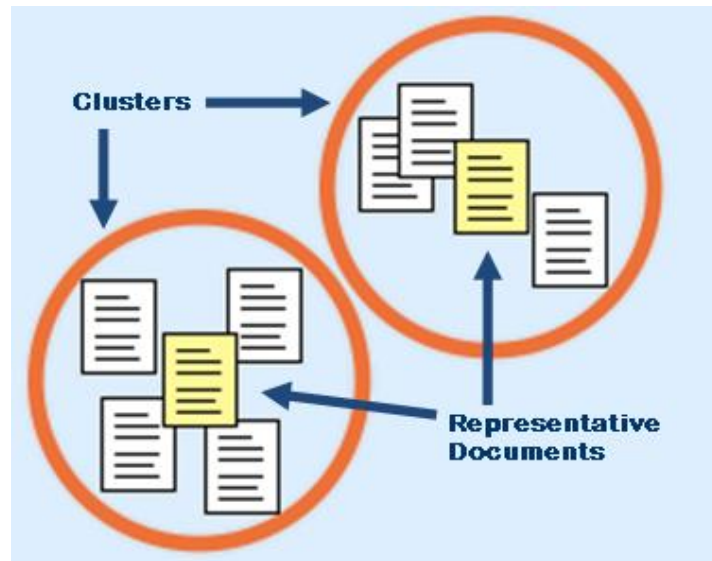
Example 1: Clothing size

- Tailor-made for each person is too expensive
- One-size-fits-all: does not work!
- Groups people of similar sizes together to make “small”, “medium”, and “large” t-shirts

Unsupervised Learning

Example 2: Text document organization

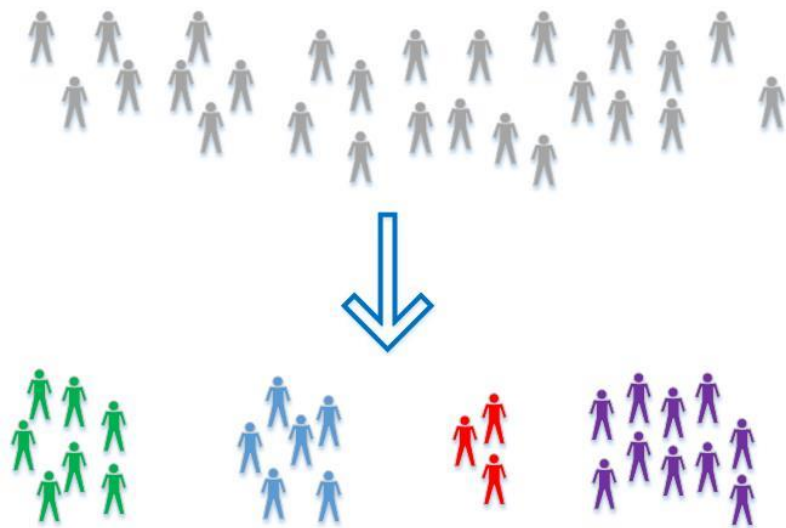
- To find groups of documents that are similar to each other based on the important terms appearing in them



Unsupervised Learning

Example 3: Target Marketing

- Subdivide market into distinct subsets of customers where any subset may conceivably be selected as a segment to be reached with a particular offer



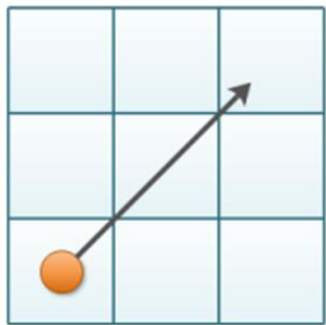
K-Means Clustering

- Process of partitioning data points into similarity clusters
- Unsupervised technique
- Only works for numeric data



Euclidean Distance

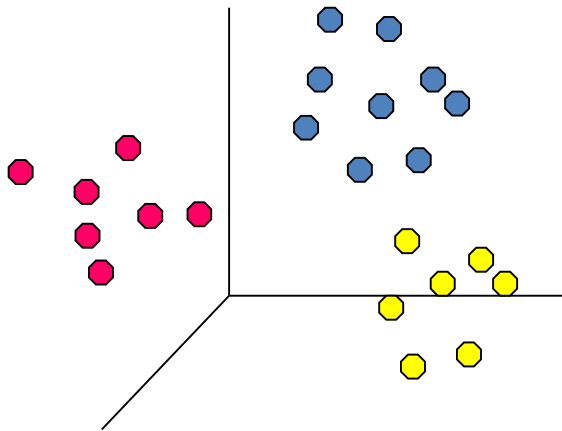
points in a two-dimensional space to determine intra- and inter-cluster similarity



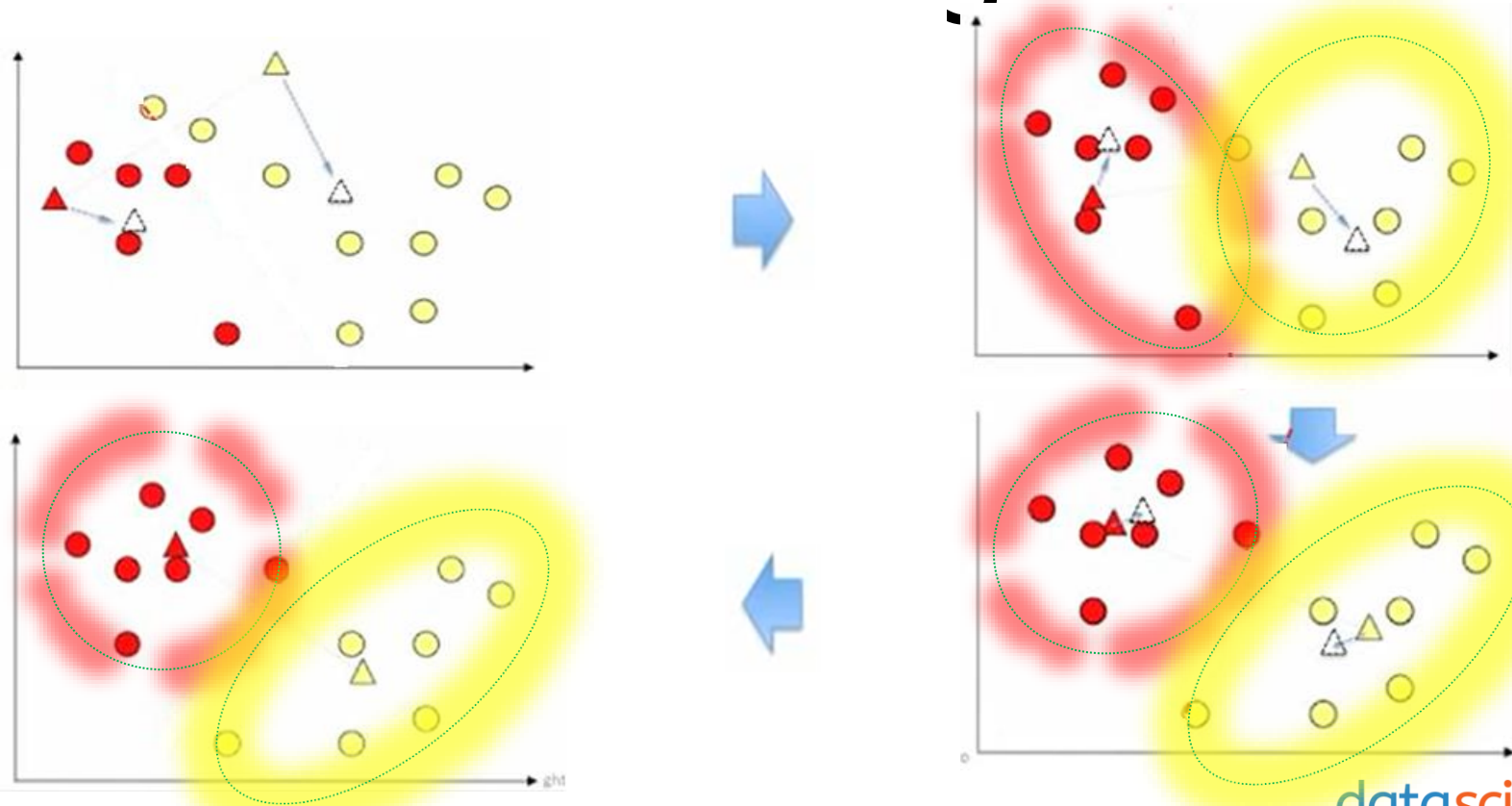
$$\sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

Intra-cluster distances
are minimized

Inter-cluster distances
are maximized



K-means Clustering



K-Means Clustering Algorithm

Suppose set of data points: $\{x_1, x_2, x_3, \dots, x_n\}$

- **Step 1:** Decide the number of clusters, $K=1,2,\dots,k$.
- **Step 2:** Place centroids at random locations
 - c_1, c_2, \dots, c_k
- **Step 3:** Repeat until convergence:
 - { for each point $x_i \longrightarrow$ find nearest centroid c_j (eg. Euclidean distance)
 \longrightarrow assign the point x_i to cluster j
 - for each cluster $j = 1 \dots k \longrightarrow$ calculate new centroid c_j
 $c_j = \text{mean of all points } x_i \text{ assigned to cluster } j \text{ in previous step}$
 - }
- **Step 4:** Stop when none of the cluster assignments change

K-Means Clustering

Minimizes aggregate intra-cluster distance

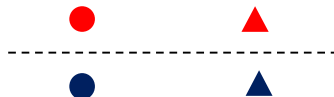
- Measure squared distance from point to center of its cluster.

$$\sum_j \sum_{x_j - c_i} D(c_j x_i)^2$$

Could converge to local minimum

- Different starting points → very different results
- Run many times with random starting points

Nearby points may not be assigned to the same cluster



K-means Clustering

■ Strengths:

- Simple: easy to understand and to implement
- Efficient: Complexity: $O(t \times k \times n)$
 - n = number of data points,
 - k = number of clusters, and
 - t = number of iterations

K-means Clustering

■ Weaknesses:

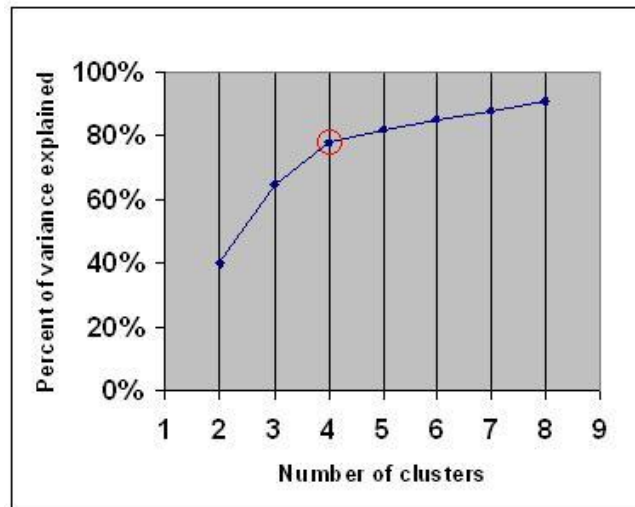
- The algorithm is only applicable if the mean is well defined
- The user needs to specify k
- The algorithm is sensitive to outliers

K-Means Clustering

Rule of thumb $k \approx \frac{\sqrt{n}}{2}$
n = number of data points

Elbow method

- percentage of variance explained as a function of the number of clusters
- choose a number of clusters so that adding another cluster doesn't give much better modeling of the data.



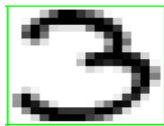
Other K Optimization Techniques

- Silhouette
- Calinsky criterion
- Bayesian Information Criterion
- Affinity propagation (AP) clustering
- Gap statistic

Example: Handwritten Digit Recognition



Extracting Features For Learning



$\{x_1, x_2, x_3, \dots, x_{256}, y = \text{'three'}\}$

- Each x_i corresponds to a feature value in the image
- y is a label of the training data; can be numeric or categorical, '3' or 'three'
- Each image is converted to row vectors and the appropriate learning algorithm is used
- Convention
 - x_i represents the i th feature in a training sample
 - y represents the label for the training sample

QUESTIONS