NBA Shot Prediction

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ABSTRACT

The use of various predictive metrics in sports has been occurring as long as human beings have watched each other compete. Initially this started out as simple gut feeling or a subjective assessment of the competitors—the bets usually go to the bigger fighter! In more recent times, humanity has refined its predictive power with the advent of statistics and logical decision making (famously put to use in Major League Baseball, as shown in the film Moneyball). With the advent of the information age and the possibility for large-scale data analytics and machine learning, the National Basketball Association has decided to puruse this analysis to better understand player matchups (defender vs offender) and to assess & optimize shooter performance.

BUSINESS UNDERSTANDING

Detailed statistics are already available to the NBA as these have been tracked for many years, supporting classic statistical decision making. The goal is to run both unsupervised and supervised machine learning algorithms on the statistical data available. In technical terms, we aim to deliver predictive metrics for threat/benefit level at an individual player level, as well as an interactive application that identifies the likelihood of a shot landing from a specific offender shooting from a specific position on the court, against a specific defender located a certain distance away. This will allow coaches to run limited scenarios in the predictive model, to inform both their practice routines and to assist in making strategic decisions during live games.

As an example, consider the matchup of Lebron James on offence and Serge Ibaka on defence. Let's assume that Lebron typically tries to shoot from top of the key, and is being defended by Serge Ibaka, 5 feet away. The model takes these discrete inputs and outputs a real-world percentage success of 10.5% (example). If the average shooting success rate is 30%, we can identify this as a bad shot, and encourage Lebron to pass in these situations.

DATA UNDERSTANDING

We begin with understanding each feature available in the data. The available data set is data of all shots attempted at NBA games between 2014 and 2015. For each shot attempted, the most important outcome of that attempt, whether the shot was made or missed is available. This is seen in 2 columns SHOT_RESULTS and FGM. FGM stands for "Field Goal Made". In support of this outcome, there are a number of other data points to be seen, like the player who attempted the shot and who defended the sho, how far away was the defender, how far away from the basket was the shot attempted, was the match at home or away etc. With that data understanding, let's look at the "head" of the data.

GAME_ID	MATCHUP	LOCATION	W	FINAL_MARGIN	SHOT_NUMBER	PERIOD	GAME_CLOCK
21400899	MAR 04, 2015 - CHA @ BKN	A	W	24	1	1	1:09
21400899	MAR 04, 2015 - CHA @ BKN	A	W	24	2	1	0:14
21400899	MAR 04, 2015 - CHA @ BKN	A	W	24	3	1	0:00
21400899	MAR 04, 2015 - CHA @ BKN	A	W	24	4	2	11:47
21400899	MAR 04, 2015 - CHA @ BKN	A	W	24	5	2	10:34
21400899	MAR 04, 2015 - CHA @ BKN	A	W	24	6	2	8:15

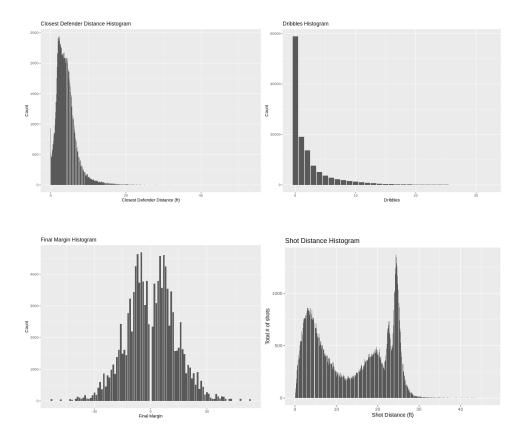
SHOT_CLOCK	DRIBBLES	TOUCH_TIME	SHOT_DIST	PTS_TYPE	SHOT_RESULT	CLOSEST_DEFENDER
10.80	2	1.90	7.70	2	made	Anderson, Alan
3.40	0	0.80	28.20	3	missed	Bogdanovic, Bojan
	3	2.70	10.10	2	missed	Bogdanovic, Bojan
10.30	2	1.90	17.20	2	missed	Brown, Markel
10.90	2	2.70	3.70	2	missed	Young, Thaddeus
9.10	2	4.40	18.40	2	missed	Williams, Deron

Table 1: Data Dictionary - NBA Data

Feature	Feature.Description
GAME_ID	A unique ID for each game
MATCHUP	Shows the date of the match and the teams the match is between
LOCATION	A - Away, H - Home. Shows the location of the match with respect to the first team in the match up column
W	Win or Loss. W means win and L means Loss, with respect to the first team in the match up column
FINAL_MARGIN	Points difference between the teams at the end of the game
SHOT_NUMBER	To be read in conjunction with the PERIOD column. Indicates the shot number in a given game period
PERIOD	Indicates the game period
GAME_CLOCK	Time elapsed since the period commenced. This datset shows the time at which the shot was attempted. Max 12 minutes per period
SHOT_CLOCK	The length of time for a given shot in seconds. Max - 24 seconds is a rule
DRIBBLES	The number of times the ball was dribbled before the shot was attempted
TOUCH_TIME	The length of time a player touched the ball
SHOT_DIST	The distance from which a shot was attempted. Distance in feet
PTS_TYPE	Points awarded if a shot was made. 2 pointer or 3 pointer shots
SHOT_RESULT	Indicates whether the shot was made or missed
CLOSEST_DEFENDER	Shows the name of the player that was the closest defender
CLOSEST_DEFENDER_PLAYER_ID	Unique ID of the closest defender
CLOSE_DEF_DIST	Distance of the closest defender in feet
FGM	An abbreviation for FIELD GOALS MADE. A proxy for SHOT_RESULT, 0 indicates missed shot and 1 indicates shot made
PTS	Points awarded for shots made
player_name	Name of the player who attempted the shot
player_id	Unique ID of the player who attempted the shot

Plots

We attempt to further understand the data using the following plots. A histogram of the "closest defender distance" shows that a majority of the shots were defended from within 5 feet of the player attempting the shot and it is safe to say that more than 90% of the shots were defended from within 10 feet. The "dribbles count" shows that most of the shots were attempted soon after getting the ball and that more than 80% of the shots were attempted within 3 dribbles. "Final Margin" histogram shows that most matches were won or lost within a 15 point margin. The "Shot distance" histogram shows that most of the shots were attempted from "top of the key" and followed by 2 to 4 feet range from the basket



DATA PREPARATION

SHOT_CLOCK

Looking at the data, some of the NA values need to be dealt with. The "SHOT_CLOCK" column has some NA values and the assumption is that the SHOT_CLOCK was equal to the GAME_CLOCK and therefore it may not be recorded. For such cases, the GAME_CLOCK is assumed to be equal to SHOT_CLOCK.

```
cleanData <- initialData
gameClock <- as.vector(second(fast_strptime(cleanData$GAME_CLOCK, "%M:%S"))) +
   as.vector(minute(fast_strptime(cleanData$GAME_CLOCK, "%M:%S"))) * 60
shotClock <- is.na(initialData$SHOT_CLOCK)
for(i in 1:length(gameClock)){
   if(shotClock[i] & gameClock[i] < 25){
     cleanData$SHOT_CLOCK[i] <- gameClock[i]
   }
}</pre>
```

Names

To further handle player names in this exercise, all names are standardized to read as "First Name" followed by "Last Name". A custom function was written to achieve this result.

```
}
```

All Shooter & Defender names are then put through the function to standardize names

```
shooterName <- cleanNoNAData$player_name
shooterName <- toupper(shooterName)
shooterName <- nameformatreverse(shooterName)

cleanNoNAData$player_name <- shooterName
cleanNoNAData$CLOSEST_DEFENDER <- toupper(cleanNoNAData$CLOSEST_DEFENDER)
cleanNoNAData$CLOSEST_DEFENDER <- gsub("[.]", "", cleanNoNAData$CLOSEST_DEFENDER)</pre>
```

Game Clock

It makes best sense to have the GAME_CLOCK expressed in seconds.

```
cleanNoNASecondsClockData <- cleanNoNAData
cleanNoNASecondsClockData$GAME_CLOCK <-
   as.vector(second(fast_strptime(cleanNoNAData$GAME_CLOCK, "%M:%S"))) +
   as.vector(minute(fast_strptime(cleanNoNAData$GAME_CLOCK, "%M:%S"))) * 60</pre>
```

Touch time

Any row that has TOUCH_TIME less than 0.1 seconds is not right and hence are omitted cleanNoNASecondsClockData <- cleanNoNASecondsClockData\$TOUCH TIME > 0,]

MODELLING

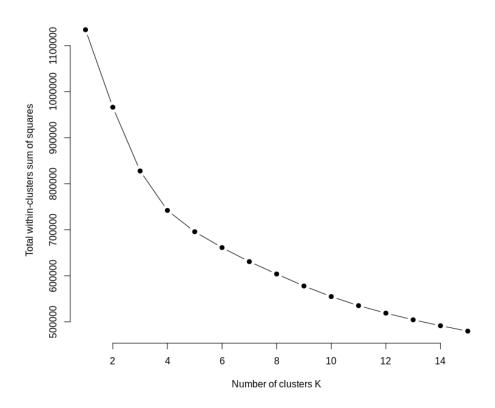
K-Means Clustering

The Elbow method is a popular, non computation intensive process of determining the most optimal number of clusters for a dataset by looking at a dropoff of variance. The other methods, eg, Bayesian Inference which we ran is more computation intensive, and produced optimal clusters that didnt agree with the visual Elbow method. Therefore, after plotting and analyzing a few different features against each other and highlighting the clusters by colouring the datapoints, we find that 3 clusters is likely the best compromise for the important features, namely, shot distance and closest defender distance.

To perform clustering, only the numeric columns from the data are selected.

We use the 'Elbow' method to determine the ideal number of clusters

The "number of clusters" vs "sum of squares" plot helps us identify the 'Elbow' and decide on the right number of clusters. From the plot, we will try creating clusters with k = 2,3 & 4

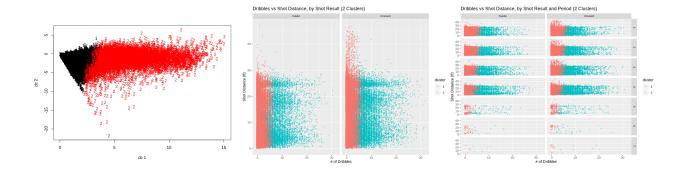


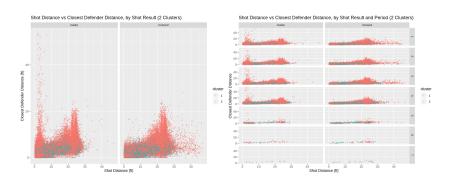
Bayesian Inference Criterion for k means to validate choice from Elbow Method

```
d_clust <- Mclust(as.matrix(kdata), G=1:10,</pre>
                  modelNames = mclust.options("emModelNames"))
d_clust$BIC
plot(d_clust)
# Let us apply kmeans for k=2 clusters
kmm.2 <- kmeans(kdata, 2, nstart = 50, iter.max = 15)
# Let us apply kmeans for k=3 clusters
kmm.3 <- kmeans(kdata, 3, nstart = 50, iter.max = 15)
\# Let us apply kmeans for k=3 clusters
kmm.4 <- kmeans(kdata, 4, nstart = 50, iter.max = 15)
# We keep number of iter.max=15 to ensure the algorithm converges and nstart=50 to
# Ensure that atleat 50 random sets are choosen
kmm.2
kmm.3
kmm.4
# Plot the clusters
clusplot(kdataunscaled, kmm.3$cluster, color=TRUE, shade=TRUE, labels=2, lines=0)
# Centroid Plot against 1st 2 discriminant functions
plotcluster(kdataunscaled, kmm.2$cluster)
```

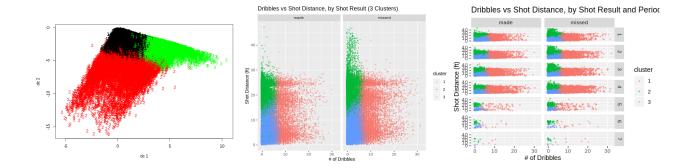
```
plotcluster(kdataunscaled, kmm.3$cluster)
plotcluster(kdataunscaled, kmm.4$cluster)
```

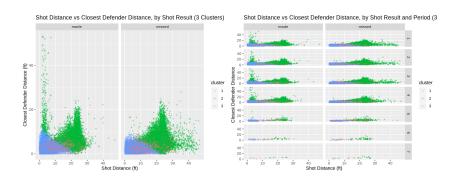
K2 plots



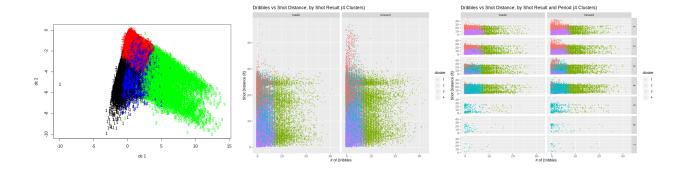


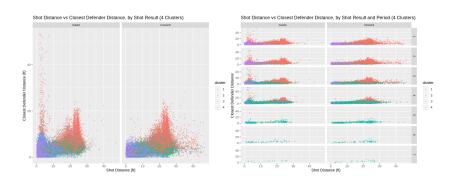
k3 plots





 ${\it k4~plots}$





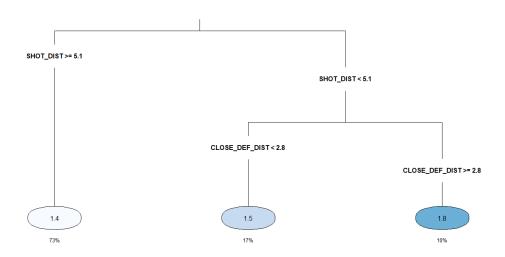
We chose a number of supervised machine learning models to predict the number of field goals made. We ran, evaluated, and compared the performance of the following models: * Decision Tree * Logistic Regression * GBM * GBM with PCA Before running the models, we converted the predictors and response variable to their correct data type. For example, numeric factors such as SHOT_DIST were explicitly converted into numeric, while categorical factors such as FGM were explicitly converted into categorical factors. Because the binary response variables of, 0 and 1, showcased a relatively balanced dataset, with the split being roughly 55%/45%, we did not need to undersample or oversample the data.

We also split the dataset into a training, and testing set. The split was set at 70% training, and 30% training, ensuring an equal

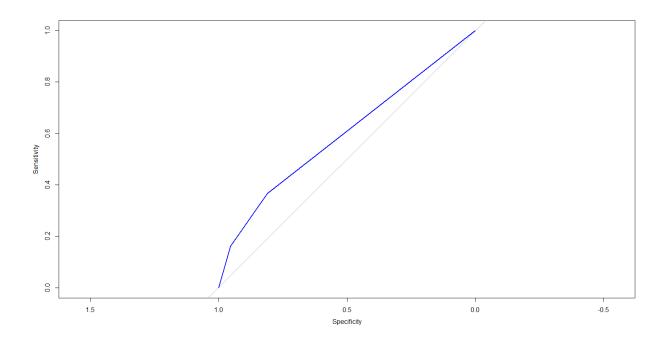
Decision Tree

The Decision tree algorithm is an algorithm that uses a tree-like data structure to make either predictions for regression, or classification problems. Given the business problem and context, a categorical variable decision tree was chosen as we wanted to classify, given the available data, whether or not an attempted shot made became a FGM (Field Goal Made); in this particular situation, there would be two categories for the response variable: either 0, denoting an attempted shot that missed, or 1, denoting an attempted shot that resulted in a field goal. A decision tree is suitable supervised machine learning algorithm because it is fairly easy to explain and visualize. For example, the following figure below is the generated decision tree diagram. Shot Distance, titled as SHOT_DIST, as well as the distance to the closest defender, titled as CLOSE_DEF_DIST, were the two most important variables in the decision tree, and of which the decisions are based upon.

Regression Tree

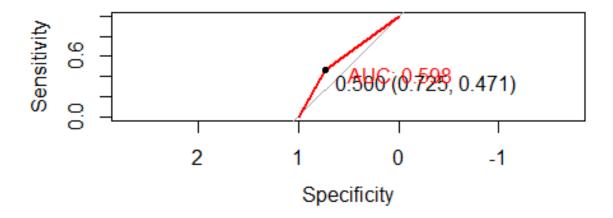


The ROC curve, and AUC of the decision tree algorithm showed similar results to the other models, as seen in the figure below. Nevertheless, it was decided not to use the decision tree algorithm as the model only showed 3 raw probabilities given the different permutations of SHOT_DIST and CLOSE_DEF_DIST. This would not have looked good on the Shiny app, as we wanted to show more probabilities on a more granular level, as there were other predictor variables that were not being used in the final model.



Logistic Regression

Logistic Regression is a parametric model used for binary classification, and it is based off the logistic function, hence the name. There are a few assumptions that were made with logistic regression: * There is a large enough dataset to make accurate predictions * Observations are independent of one another * Response variable is binary (0 or 1). * Predictor variables are related to logit function * Minimal multicollinearity among the predictor variables All assumptions except (4) and (5) are true, and due to the lack of time on our part, we were unable to ascertain whether the last two assumptions were, indeed, true. The results for the logistic regression showed similar results to other models. Listed below is the ROC curve/AUC results of the logistic regression model.



In terms of other metrics like accuracy, balanced accuracy, sensitivity, and specificity, the logistic regression model also showed similar results to the other models. Unfortunately, logistic regression took the longest amount of time to train compared to all the other models, at 2.5 hours. Listed below are the other metrics, as well as the runtime of the logistic regression model.

```
library(dplyr)
library(caTools)
library(pROC)
library(caret)
library(e1071)
# Read the data
shotDataRaw <- read.csv('.../../data/shot_longs_clean_noNA_secondsclock.csv', header = TRUE, na.strings</pre>
#columns to keep
shotData <- shotDataRaw[</pre>
  c(
    'LOCATION',
    'PERIOD',
    'GAME_CLOCK',
    'SHOT_CLOCK',
    'DRIBBLES',
    'TOUCH_TIME',
    'SHOT_DIST',
    'PTS_TYPE',
    'CLOSEST_DEFENDER',
    #'CLOSEST_DEFENDER_PLAYER_ID',
```

```
'CLOSE_DEF_DIST',
    'player_name',
    'FGM'
  )
1
#scaling not required for glm (logistic regression)
#kdataunscaled <- shotData[, c("PERIOD", "GAME_CLOCK", "SHOT_CLOCK", "DRIBBLES", "TOUCH_TIME", "SHOT_DI
#kdata <- scale(kdataunscaled)</pre>
#make sure columns are set as factor, ordered, or numerical
shotData$LOCATION <- as.factor(shotData$LOCATION)</pre>
shotData$PERIOD <- as.factor(shotData$PERIOD)</pre>
shotData$GAME_CLOCK <- as.numeric(shotData$GAME_CLOCK)</pre>
shotData$SHOT_CLOCK <- as.numeric(shotData$SHOT_CLOCK)</pre>
shotData$DRIBBLES <- as.numeric(shotData$DRIBBLES)</pre>
shotData$TOUCH_TIME <- as.numeric(shotData$TOUCH_TIME)</pre>
shotData$SHOT_DIST <- as.numeric(shotData$SHOT_DIST)</pre>
shotData$PTS_TYPE <- as.factor(shotData$PTS_TYPE)</pre>
shotData$CLOSEST_DEFENDER <- as.factor(shotData$CLOSEST_DEFENDER)</pre>
shotData$CLOSE_DEF_DIST <- as.numeric(shotData$CLOSE_DEF_DIST)</pre>
shotData$player_name <- as.factor(shotData$player_name)</pre>
#glm is a bit weird, doesn't accept 1 or 0, so we will convert FGM into "yes" or "no"
shotData$FGM <- as.factor(</pre>
  ifelse(shotData$FGM == 0, "no", "yes")
)
#no need to under/oversample, because FGM of 0 is close to 55%, and FGM of 1 is close to 45%
#so pretty balanced dataset!
#split the data into training and testing datasets
set.seed(123)
shotSample = sample.split(shotData$FGM, SplitRatio = 0.70)
shotTrain = subset(shotData, shotSample == TRUE)
shotTest = subset(shotData, shotSample == FALSE)
#set a train control
#use cross validation
glm.trainControl = trainControl(
 method = "cv",
 number = 5,
  #Estimate class probabilities
  classProbs = TRUE,
  #Evaluate performance using the following function
  summaryFunction = twoClassSummary,
  allowParallel = TRUE,
  verbose = TRUE
)
#no need to tuneGrid because logistic regression using glm has no parameters
```

```
#train model
set.seed(123)
ptm rf <- proc.time()</pre>
model_glm <- train(</pre>
 FGM ~ .,
 data = shotTrain,
 method = 'glm',
 trControl = glm.trainControl
)
proc.time() - ptm_rf
#make prediction against testData with the new model
print(model_glm)
pred.model_glm.prob = predict(model_glm, newdata = shotTest, type="prob")
pred.model_glm.raw = predict(model_glm, newdata = shotTest)
roc.model_glm = pROC::roc(
  shotTest$FGM,
  as.vector(ifelse(pred.model_glm.prob[,"yes"] > 0.5, 1, 0))
)
auc.model_glm = pROC::auc(roc.model_glm)
print(auc.model_glm)
#plot ROC curve
plot.roc(roc.model_glm, print.auc = TRUE, col = 'red', print.thres = "best")
#qenerate confusion matrix, as well as other metrics such as accuracy, balanced accuracy
confusionMatrix(data = pred.model_glm.raw, shotTest$FGM)
#summary of model
summary(model_glm)
# Save the model into a file
save(model_glm, file="model_glm.rda")
```

Stochastic Gradient Boosting (GBM)

Stochastic Gradient Boosting is a relatively complex supervised learning algorithm. The algorithm continuously iterates through several trees, at one at a time, so that it can boost the performance of its weakest learners.

When initially training the GBM model, we first decided to keep CLOSEST_DEFENDER_PLAYER_ID, and player_name, when training the GBM model, but the model itself was fairly big, and in terms of variable importance, both features were not that important unless if the players had a large enough data sample to draw meaningful conclusions from. For example, looking at the figure of output variable importance, one could see the top CLOSEST_DEFENDER and player_name names were highly regarded players from the 2015 season, or at least players who had a lot of playtime.

```
library(dplyr)
library(gbm)
library(caTools)
library(pROC)
library(doParallel)
library(caret)
library(MLmetrics)
```

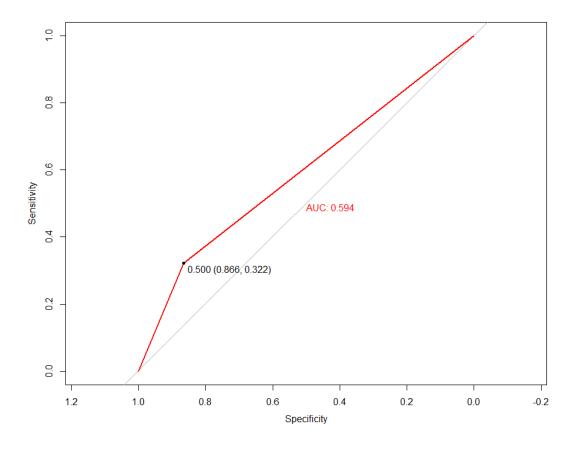
```
# Read the data
shotDataRaw <- read.csv('./source/data/shot_logs_clean_noNA_secondsclock.csv', header = TRUE, na.string</pre>
#columns to keep
shotData <- shotDataRaw[</pre>
  c(
    'LOCATION',
    'PERIOD',
    'GAME CLOCK',
    'SHOT_CLOCK',
    'DRIBBLES',
    'TOUCH_TIME',
    'SHOT_DIST',
    'PTS_TYPE',
    'CLOSEST_DEFENDER',
    #'CLOSEST_DEFENDER_PLAYER_ID',
    'CLOSE_DEF_DIST',
    'player_name',
    'FGM'
 )
1
#scaling not required for gbm
#kdataunscaled <- shotData[, c("PERIOD", "GAME_CLOCK", "SHOT_CLOCK", "DRIBBLES", "TOUCH_TIME", "SHOT_DI
#kdata <- scale(kdataunscaled)
#make sure columns are set as factor, ordered, or numerical
shotData$LOCATION <- as.factor(shotData$LOCATION)</pre>
shotData$PERIOD <- as.factor(shotData$PERIOD)</pre>
shotData$GAME_CLOCK <- as.numeric(shotData$GAME_CLOCK)</pre>
shotData$SHOT_CLOCK <- as.numeric(shotData$SHOT_CLOCK)</pre>
shotData$DRIBBLES <- as.numeric(shotData$DRIBBLES)</pre>
shotData$TOUCH_TIME <- as.numeric(shotData$TOUCH_TIME)</pre>
shotData$SHOT_DIST <- as.numeric(shotData$SHOT_DIST)</pre>
shotData$PTS_TYPE <- as.factor(shotData$PTS_TYPE)</pre>
shotData$CLOSEST_DEFENDER <- as.factor(shotData$CLOSEST_DEFENDER)</pre>
shotData$CLOSE_DEF_DIST <- as.numeric(shotData$CLOSE_DEF_DIST)</pre>
#gbm is a bit weird, doesn't accept 1 or 0, so we will convert FGM into "yes" or "no"
shotData$FGM <- as.factor(</pre>
  ifelse(shotData$FGM == 0, "no", "yes")
#split the data into training and testing datasets
shotSample = sample.split(shotData$FGM, SplitRatio = 0.70)
shotTrain = subset(shotData, shotSample == TRUE)
shotTest = subset(shotData, shotSample == FALSE)
#set trainControl
#5-fold cross validation
gbm.trainControl = trainControl(
```

```
method = "cv",
  number = 5,
  # Estimate class probabilities
  classProbs = TRUE,
  # Evaluate performance using the following function
  summaryFunction = twoClassSummary,
  allowParallel = TRUE,
  verbose = TRUE
#tuneGrid for GBM
gbmGrid <- expand.grid(</pre>
  #interaction.depth = c(10, 20),
  #n.trees = c(50, 100, 250),
 interaction.depth = c(5),
 n.trees = c(40),
 n.minobsinnode = 10,
  shrinkage = .1
#train model
set.seed(123)
ptm_rf <- proc.time()</pre>
model_gbm <- train(</pre>
  FGM ~ .,
  #data = data[trainSlices[[1]],],
  data = shotTrain,
 \#data = train_data,
  method = "gbm",
  #family="gaussian",
  #distribution = "qaussian",
 trControl = gbm.trainControl,
  #tuneLength = 5
  tuneGrid = gbmGrid
proc.time() - ptm_rf
#make predictions aginst testData with the new model
print(model_gbm)
pred.model_gbm.prob = predict(model_gbm, newdata = shotTest, type="prob")
pred.model_gbm.raw = predict(model_gbm, newdata = shotTest)
roc.model_gbm = pROC::roc(
  shotTest$FGM,
  as.vector(ifelse(pred.model_gbm.prob[,"yes"] >0.5, 1,0))
auc.model_gbm = pROC::auc(roc.model_gbm)
print(auc.model_gbm)
#plot ROC curve
plot.roc(roc.model_gbm, print.auc = TRUE, col = 'red' , print.thres = "best" )
```

```
#qenerate confusion matrix, as well as other metrics such as accuracy, balanced accuracy
confusionMatrix(data = pred.model_gbm.raw, shotTest$FGM)
#summary of model
summary(model gbm)
# Save the model into a file
save(model_gbm, file="gbm.rda")
Confusion Matrix and Statistics
         Reference
Prediction
                   yes
             no
      no 17477 11287
       ves 2703 5362
              Accuracy : 0.6201
                95% CI: (0.6152, 0.6251)
   No Information Rate: 0.5479
   P-Value [Acc > NIR] : < 2.2e-16
                  Kappa: 0.197
Mcnemar's Test P-Value : < 2.2e-16
            Sensitivity: 0.8661
           Specificity: 0.3221
         Pos Pred Value: 0.6076
         Neg Pred Value: 0.6648
            Prevalence: 0.5479
         Detection Rate: 0.4745
   Detection Prevalence: 0.7810
      Balanced Accuracy: 0.5941
       'Positive' Class : no
```

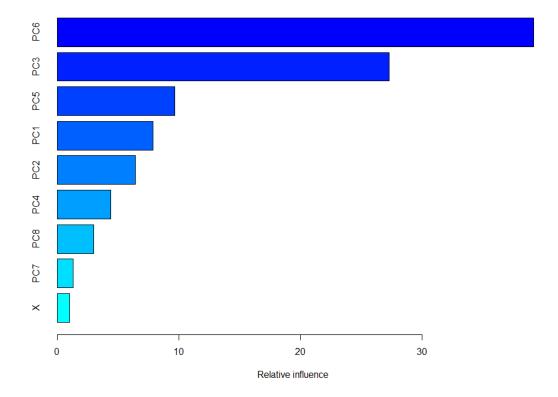
Also, including the features CLOSEST_DEFENDER_PLYAER_ID and player_name made the model size unnecessarily big for little to no improvement in the prediction of FGM. In relation to the size of the models, it also took a lot longer to train the model as well, at about 4 hours instead of the usual 1 hour. For hyper parameter optimization, we found that GBM produced the best results at with an interaction depth of 5, 40 trees, minimum of 10 observations in each node, and a shrinkage of 0.1. Using such hyper parameters offered a relatively fast training time of around 10 minutes

Listed below is the ROC curve, and AUC value for GBM without CLOSEST_DEFENDER_PLAYER_ID, and player_name predictor variables. Also listed below is the console output of training the GBM model, showing some of the metrics from the test dataset. Overall, the GBM model did the best compared to the other models, although not by a huge margin. It had an accuracy of 62.01%, a sensitivity of 0.8661 which were the highest of all the models. Unfortunately, its specificity was at the lower end compared to other models at 0.3221



Stochastic Gradient Boosting (GBM) with PCA

We also chose to perform GBM with the results generated from PCA. We used all 8 of the components for the GBM model. Listed below was the variable importance of each component:



Listed below are the metrics of the GBM with PCA. Overall the GBM with PCA model was fairly competitive with the previous GBM model, as it scored 61.58% accuracy, and a 0.8035 sensitivity. Its specificity was a bit better than the previous GBM model at 0.3884. In terms of runtime both GBM models were fairly similar with a training duration of around 10 minutes.

```
AUC: 0.596

AUC: 0.596

0.500 (0.803, 0.388)
```

```
> library(dplyr)
> library(caTools)
> library(pROC)
> library(caret)
> library(e1071)
> # Read the data
> shotDataRaw <- read.csv('.../../data/shot_logs_pca.csv', header = TRUE, na.strings = c('NA','','#NA'))
> shotData <- shotDataRaw
> #scaling not required for gbm
> #kdataunscaled <- shotData[, c("PERIOD", "GAME_CLOCK", "SHOT_CLOCK", "DRIBBLES", "TOUCH_TIME", "SHOT_
> #kdata <- scale(kdataunscaled)
> #make sure columns are set as factor, ordered, or numerical
> shotData$PC1 <- as.numeric(shotData$PC1)</pre>
> shotData$PC2 <- as.numeric(shotData$PC2)</pre>
> shotData$PC3 <- as.numeric(shotData$PC3)</pre>
> shotData$PC4 <- as.numeric(shotData$PC4)</pre>
> shotData$PC5 <- as.numeric(shotData$PC5)</pre>
> shotData$PC6 <- as.numeric(shotData$PC6)</pre>
> shotData$PC7 <- as.numeric(shotData$PC7)</pre>
> shotData$PC8 <- as.numeric(shotData$PC8)</pre>
> #glm is a bit weird, doesn't accept 1 or 0, so we will convert FGM into "yes" or "no"
> shotData$FGM <- as.factor(</pre>
```

```
+ ifelse(shotData$FGM == 0, "no", "yes")
+ )
>
>
> #no need to under/oversample, because FGM of 0 is close to 55%, and FGM of 1 is close to 45%
> #so pretty balanced dataset!
> #split the data into training and testing datasets
> set.seed(123)
> shotSample = sample.split(shotData$FGM, SplitRatio = 0.70)
> shotTrain = subset(shotData, shotSample == TRUE)
> shotTest = subset(shotData, shotSample == FALSE)
>
> #set trainControl
> #5-fold cross validation
> gbm.trainControl = trainControl(
+ method = "cv",
+ number = 5,
+ # Estimate class probabilities
   classProbs = TRUE,
+ # Evaluate performance using the following function
+ summaryFunction = twoClassSummary,
+ allowParallel = TRUE,
   verbose = TRUE
+ )
> #tuneGrid for GBM
> gbmGrid <- expand.grid(</pre>
  #interaction.depth = c(10, 20),
  #n.trees = c(50, 100, 250),
   interaction.depth = c(1, 2, 5, 10),
+ n.trees = c(25, 50, 100, 150, 200),
   n.minobsinnode = 10,
+
   shrinkage = .1
+ )
> #train model
> set.seed(123)
> ptm_rf <- proc.time()</pre>
> model_gbm <- train(</pre>
+ FGM ~ .,
  #data = data[trainSlices[[1]],],
   data = shotTrain,
  \#data = train_data,
+ method = "gbm",
   #family="gaussian",
   #distribution = "qaussian",
+ trControl = gbm.trainControl,
   #tuneLength = 5
   tuneGrid = gbmGrid
+ )
+ Fold1: shrinkage=0.1, interaction.depth= 1, n.minobsinnode=10, n.trees=200
```

```
Iter
       TrainDeviance
                         ValidDeviance
                                          StepSize
                                                       Improve
     1
               1.3734
                                             0.1000
                                                        0.0017
                                    nan
     2
               1.3702
                                             0.1000
                                                        0.0015
                                    nan
     3
                                                       0.0014
                                             0.1000
               1.3675
                                    nan
     4
               1.3648
                                    nan
                                             0.1000
                                                        0.0013
     5
               1.3622
                                    nan
                                             0.1000
                                                        0.0012
     6
               1.3601
                                             0.1000
                                                        0.0010
                                    nan
     7
                                                        0.0010
               1.3582
                                    nan
                                             0.1000
     8
               1.3564
                                             0.1000
                                                        0.0009
                                    nan
     9
               1.3548
                                    nan
                                             0.1000
                                                        0.0008
    10
               1.3533
                                    nan
                                             0.1000
                                                        0.0007
    20
               1.3432
                                             0.1000
                                                        0.0003
                                    nan
    40
               1.3330
                                             0.1000
                                                        0.0002
                                    nan
    60
               1.3272
                                             0.1000
                                                        0.0001
                                    nan
    80
               1.3230
                                                        0.0000
                                    nan
                                             0.1000
   100
               1.3200
                                    nan
                                             0.1000
                                                        0.0001
   120
               1.3176
                                             0.1000
                                                        0.0000
                                    nan
   140
               1.3159
                                             0.1000
                                                        0.0000
                                    nan
   160
                                                        0.0000
               1.3145
                                             0.1000
                                    nan
   180
                                             0.1000
                                                        0.0000
               1.3134
                                    nan
   200
               1.3124
                                    nan
                                             0.1000
                                                        0.0000
- Fold1: shrinkage=0.1, interaction.depth= 1, n.minobsinnode=10, n.trees=200
+ Fold1: shrinkage=0.1, interaction.depth= 2, n.minobsinnode=10, n.trees=200
       TrainDeviance
                         ValidDeviance
                                          StepSize
                                                       Improve
     1
               1.3718
                                             0.1000
                                                        0.0026
                                    nan
     2
               1.3673
                                    nan
                                             0.1000
                                                        0.0022
     3
               1.3635
                                             0.1000
                                                        0.0018
                                    nan
     4
               1.3598
                                             0.1000
                                                        0.0017
                                    nan
                                                       0.0014
     5
               1.3567
                                             0.1000
                                    nan
     6
               1.3540
                                             0.1000
                                                        0.0012
                                    nan
     7
               1.3512
                                             0.1000
                                                        0.0013
                                    nan
     8
               1.3489
                                             0.1000
                                                        0.0011
                                    nan
     9
               1.3471
                                             0.1000
                                                        0.0009
                                    nan
    10
               1.3452
                                             0.1000
                                                        0.0009
                                    nan
    20
               1.3322
                                                        0.0004
                                             0.1000
                                    nan
    40
               1.3192
                                                        0.0002
                                    nan
                                             0.1000
                                                       0.0001
    60
               1.3125
                                             0.1000
                                    nan
                                                        0.0000
    80
               1.3087
                                    nan
                                             0.1000
   100
               1.3061
                                    nan
                                             0.1000
                                                        0.0000
   120
               1.3042
                                             0.1000
                                                        0.0000
                                    nan
   140
               1.3026
                                    nan
                                             0.1000
                                                        0.0000
   160
               1.3016
                                    nan
                                             0.1000
                                                       0.0000
   180
               1.3006
                                             0.1000
                                                       -0.0000
                                    nan
   200
               1.2998
                                             0.1000
                                                       -0.0000
                                    nan
- Fold1: shrinkage=0.1, interaction.depth= 2, n.minobsinnode=10, n.trees=200
+ Fold1: shrinkage=0.1, interaction.depth= 5, n.minobsinnode=10, n.trees=200
Iter
       TrainDeviance
                         ValidDeviance
                                          StepSize
                                                       Improve
     1
                                             0.1000
                                                        0.0039
               1.3689
                                    nan
     2
                                                        0.0031
               1.3624
                                    nan
                                             0.1000
     3
               1.3570
                                             0.1000
                                                        0.0028
                                    nan
     4
               1.3517
                                    nan
                                             0.1000
                                                        0.0024
```

```
5
               1.3473
                                    nan
                                            0.1000
                                                       0.0021
     6
               1.3435
                                            0.1000
                                                       0.0018
                                    nan
     7
               1.3401
                                            0.1000
                                                       0.0016
                                    nan
     8
                                                       0.0013
               1.3371
                                            0.1000
                                    nan
     9
               1.3345
                                    nan
                                            0.1000
                                                       0.0012
    10
               1.3321
                                    nan
                                            0.1000
                                                       0.0011
    20
               1.3166
                                    nan
                                            0.1000
                                                       0.0005
    40
               1.3036
                                                       0.0000
                                    nan
                                            0.1000
    60
               1.2985
                                            0.1000
                                                       -0.0000
                                    nan
    80
                                                       -0.0000
               1.2952
                                    nan
                                            0.1000
   100
               1.2928
                                    nan
                                            0.1000
                                                       0.0000
   120
               1.2906
                                            0.1000
                                                      -0.0000
                                    nan
   140
               1.2886
                                            0.1000
                                                       0.0000
                                    nan
   160
               1.2866
                                            0.1000
                                                       -0.0000
                                    nan
   180
               1.2848
                                            0.1000
                                                       -0.0000
                                    nan
   200
               1.2830
                                    nan
                                            0.1000
                                                       -0.0000
- Fold1: shrinkage=0.1, interaction.depth= 5, n.minobsinnode=10, n.trees=200
+ Fold1: shrinkage=0.1, interaction.depth=10, n.minobsinnode=10, n.trees=200
       TrainDeviance
                         ValidDeviance
                                          StepSize
                                                      Improve
     1
               1.3676
                                            0.1000
                                                       0.0044
                                    nan
     2
               1.3594
                                    nan
                                            0.1000
                                                       0.0039
     3
               1.3528
                                            0.1000
                                                       0.0032
                                    nan
     4
               1.3471
                                            0.1000
                                                       0.0026
                                    nan
     5
                                                       0.0021
               1.3427
                                    nan
                                            0.1000
     6
               1.3381
                                            0.1000
                                                       0.0022
                                    nan
     7
               1.3344
                                    nan
                                            0.1000
                                                       0.0017
     8
               1.3311
                                            0.1000
                                                       0.0015
                                    nan
     9
               1.3280
                                            0.1000
                                                       0.0014
                                    nan
    10
                                                       0.0013
               1.3252
                                            0.1000
                                    nan
    20
               1.3084
                                            0.1000
                                                       0.0003
                                    nan
    40
               1.2957
                                            0.1000
                                                       0.0001
                                    nan
    60
               1.2899
                                            0.1000
                                                       -0.0000
                                    nan
    80
               1.2855
                                            0.1000
                                                       0.0000
                                    nan
   100
               1.2819
                                            0.1000
                                                       -0.0000
                                    nan
   120
                                            0.1000
                                                       -0.0001
               1.2780
                                    nan
   140
               1.2741
                                            0.1000
                                                       -0.0000
                                    nan
   160
               1.2705
                                            0.1000
                                                      -0.0001
                                    nan
   180
                                            0.1000
                                                       -0.0000
               1.2670
                                    nan
   200
               1.2633
                                    nan
                                            0.1000
                                                       -0.0000
- Fold1: shrinkage=0.1, interaction.depth=10, n.minobsinnode=10, n.trees=200
+ Fold2: shrinkage=0.1, interaction.depth= 1, n.minobsinnode=10, n.trees=200
       TrainDeviance
                         ValidDeviance
                                          StepSize
                                                       Improve
Iter
     1
               1.3731
                                            0.1000
                                                       0.0019
                                    nan
     2
               1.3699
                                    nan
                                            0.1000
                                                       0.0016
     3
               1.3668
                                            0.1000
                                                       0.0016
                                    nan
     4
               1.3641
                                    nan
                                            0.1000
                                                       0.0013
     5
               1.3615
                                            0.1000
                                                       0.0013
                                    nan
     6
               1.3592
                                            0.1000
                                                       0.0011
                                    nan
     7
                                                       0.0010
               1.3571
                                    nan
                                            0.1000
     8
               1.3553
                                            0.1000
                                                       0.0009
                                    nan
     9
               1.3536
                                            0.1000
                                                       0.0008
                                    nan
```

```
10
               1.3519
                                    nan
                                            0.1000
                                                       0.0008
    20
               1.3415
                                            0.1000
                                                       0.0003
                                    nan
    40
               1.3317
                                            0.1000
                                                       0.0002
                                    nan
    60
               1.3256
                                            0.1000
                                                       0.0001
                                    nan
    80
               1.3213
                                    nan
                                            0.1000
                                                       0.0001
   100
               1.3181
                                    nan
                                            0.1000
                                                       0.0001
   120
               1.3158
                                            0.1000
                                                       0.0000
                                    nan
   140
                                                       0.0000
               1.3140
                                    nan
                                            0.1000
   160
               1.3126
                                            0.1000
                                                       0.0000
                                    nan
   180
               1.3114
                                    nan
                                            0.1000
                                                       0.0000
   200
               1.3105
                                    nan
                                            0.1000
                                                       -0.0000
- Fold2: shrinkage=0.1, interaction.depth= 1, n.minobsinnode=10, n.trees=200
+ Fold2: shrinkage=0.1, interaction.depth= 2, n.minobsinnode=10, n.trees=200
       TrainDeviance
                         ValidDeviance
Iter
                                          StepSize
                                                      Improve
     1
               1.3716
                                    nan
                                            0.1000
                                                       0.0026
     2
               1.3670
                                            0.1000
                                                       0.0023
                                    nan
     3
               1.3628
                                            0.1000
                                                       0.0021
                                    nan
     4
               1.3594
                                            0.1000
                                                       0.0017
                                    nan
     5
                                            0.1000
                                                       0.0015
               1.3562
                                    nan
     6
                                                       0.0015
               1.3529
                                    nan
                                            0.1000
     7
               1.3506
                                    nan
                                            0.1000
                                                       0.0011
     8
               1.3483
                                                       0.0011
                                    nan
                                            0.1000
     9
               1.3462
                                            0.1000
                                                       0.0010
                                    nan
    10
                                                       0.0009
               1.3443
                                    nan
                                            0.1000
    20
               1.3313
                                            0.1000
                                                       0.0004
                                    nan
    40
               1.3182
                                    nan
                                            0.1000
                                                       0.0002
    60
                                            0.1000
                                                       0.0001
               1.3117
                                    nan
    80
               1.3073
                                            0.1000
                                                       0.0001
                                    nan
   100
                                                       0.0000
               1.3045
                                            0.1000
                                    nan
   120
               1.3026
                                            0.1000
                                                       0.0000
                                    nan
   140
               1.3007
                                            0.1000
                                                       0.0000
                                    nan
   160
               1.2994
                                            0.1000
                                                       0.0000
                                    nan
   180
               1.2985
                                            0.1000
                                                       -0.0000
                                    nan
   200
               1.2976
                                            0.1000
                                                       -0.0000
                                    nan
- Fold2: shrinkage=0.1, interaction.depth= 2, n.minobsinnode=10, n.trees=200
+ Fold2: shrinkage=0.1, interaction.depth= 5, n.minobsinnode=10, n.trees=200
       TrainDeviance
                         ValidDeviance
                                          StepSize
Iter
                                                      Improve
     1
               1.3691
                                    nan
                                            0.1000
                                                       0.0039
     2
                                                       0.0031
               1.3628
                                    nan
                                            0.1000
     3
                                                       0.0029
               1.3569
                                    nan
                                            0.1000
     4
               1.3519
                                    nan
                                            0.1000
                                                       0.0025
     5
               1.3479
                                    nan
                                            0.1000
                                                       0.0020
     6
               1.3441
                                            0.1000
                                                       0.0017
                                    nan
     7
               1.3408
                                            0.1000
                                                       0.0016
                                    nan
     8
               1.3378
                                                       0.0014
                                            0.1000
                                    nan
     9
               1.3352
                                    nan
                                            0.1000
                                                       0.0012
    10
               1.3328
                                            0.1000
                                                       0.0012
                                    nan
    20
                                            0.1000
                                                       0.0004
               1.3169
                                    nan
    40
               1.3032
                                                       0.0002
                                    nan
                                            0.1000
    60
               1.2978
                                            0.1000
                                                       0.0000
                                    nan
    80
               1.2944
                                            0.1000
                                                       -0.0000
                                    nan
```

```
100
               1.2918
                                    nan
                                             0.1000
                                                       -0.0000
   120
               1.2896
                                             0.1000
                                                       -0.0001
                                    nan
   140
               1.2876
                                             0.1000
                                                       -0.0000
                                    nan
   160
               1.2855
                                             0.1000
                                                       -0.0000
                                    nan
   180
               1.2836
                                    nan
                                             0.1000
                                                       -0.0000
   200
               1.2819
                                    nan
                                             0.1000
                                                       -0.0000
- Fold2: shrinkage=0.1, interaction.depth= 5, n.minobsinnode=10, n.trees=200
+ Fold2: shrinkage=0.1, interaction.depth=10, n.minobsinnode=10, n.trees=200
       {\tt TrainDeviance}
                         ValidDeviance
                                          StepSize
                                                       Improve
     1
               1.3678
                                    nan
                                             0.1000
                                                        0.0044
     2
               1.3595
                                             0.1000
                                                        0.0039
                                    nan
     3
                                                        0.0032
               1.3526
                                             0.1000
                                    nan
     4
               1.3465
                                             0.1000
                                                        0.0028
                                    nan
     5
               1.3415
                                                        0.0025
                                    nan
                                             0.1000
     6
               1.3370
                                    nan
                                             0.1000
                                                        0.0021
     7
               1.3330
                                             0.1000
                                                        0.0018
                                    nan
     8
               1.3297
                                             0.1000
                                                        0.0015
                                    nan
     9
                                                        0.0014
               1.3266
                                             0.1000
                                    nan
    10
                                             0.1000
                                                        0.0013
               1.3237
                                    nan
    20
                                                        0.0004
               1.3069
                                    nan
                                             0.1000
    40
               1.2941
                                    nan
                                             0.1000
                                                        0.0000
    60
               1.2879
                                             0.1000
                                                        0.0000
                                    nan
    80
               1.2831
                                             0.1000
                                                       -0.0000
                                    nan
   100
                                                       -0.0001
               1.2792
                                    nan
                                             0.1000
   120
               1.2754
                                             0.1000
                                                       -0.0001
                                    nan
   140
               1.2717
                                    nan
                                             0.1000
                                                       -0.0000
   160
                                             0.1000
                                                       -0.0001
               1.2681
                                    nan
   180
               1.2647
                                             0.1000
                                                       -0.0001
                                    nan
   200
               1.2610
                                             0.1000
                                                       -0.0000
                                    nan
- Fold2: shrinkage=0.1, interaction.depth=10, n.minobsinnode=10, n.trees=200
+ Fold3: shrinkage=0.1, interaction.depth= 1, n.minobsinnode=10, n.trees=200
                         ValidDeviance
Iter
       TrainDeviance
                                          StepSize
                                                       Improve
     1
               1.3732
                                             0.1000
                                                        0.0019
                                    nan
     2
               1.3700
                                             0.1000
                                                        0.0015
                                    nan
     3
               1.3669
                                             0.1000
                                                        0.0016
                                    nan
     4
               1.3640
                                             0.1000
                                                        0.0013
                                    nan
     5
                                                        0.0012
               1.3616
                                    nan
                                             0.1000
     6
               1.3593
                                    nan
                                             0.1000
                                                        0.0011
     7
               1.3573
                                             0.1000
                                                        0.0010
                                    nan
     8
                                                        0.0009
               1.3554
                                    nan
                                             0.1000
     9
               1.3537
                                    nan
                                             0.1000
                                                        0.0009
    10
                                                        0.0007
               1.3520
                                    nan
                                             0.1000
    20
               1.3413
                                             0.1000
                                                        0.0003
                                    nan
    40
               1.3309
                                             0.1000
                                                        0.0002
                                    nan
    60
               1.3248
                                                        0.0001
                                             0.1000
                                    nan
    80
               1.3205
                                    nan
                                             0.1000
                                                        0.0001
   100
               1.3174
                                             0.1000
                                                        0.0000
                                    nan
   120
                                             0.1000
                                                        0.0000
               1.3151
                                    nan
               1.3134
                                                        0.0000
   140
                                    nan
                                             0.1000
   160
               1.3122
                                             0.1000
                                                        0.0000
                                    nan
   180
               1.3111
                                             0.1000
                                                        0.0000
                                    nan
```

```
200
               1.3102
                                   nan
                                            0.1000
                                                      -0.0000
- Fold3: shrinkage=0.1, interaction.depth= 1, n.minobsinnode=10, n.trees=200
+ Fold3: shrinkage=0.1, interaction.depth= 2, n.minobsinnode=10, n.trees=200
       TrainDeviance
                        ValidDeviance
                                          StepSize
                                                      Improve
     1
               1.3717
                                            0.1000
                                                       0.0027
     2
               1.3669
                                   nan
                                            0.1000
                                                       0.0023
     3
                                                       0.0021
               1.3626
                                   nan
                                            0.1000
     4
               1.3590
                                            0.1000
                                                       0.0017
                                   nan
     5
               1.3560
                                   nan
                                            0.1000
                                                       0.0015
     6
               1.3529
                                   nan
                                            0.1000
                                                       0.0014
     7
               1.3504
                                            0.1000
                                                       0.0012
                                   nan
     8
               1.3480
                                            0.1000
                                                       0.0011
                                   nan
     9
               1.3458
                                            0.1000
                                                       0.0010
                                   nan
               1.3440
    10
                                                       0.0009
                                   nan
                                            0.1000
    20
               1.3307
                                   nan
                                            0.1000
                                                       0.0006
    40
               1.3175
                                            0.1000
                                                       0.0001
                                   nan
    60
               1.3103
                                            0.1000
                                                       0.0001
                                   nan
    80
               1.3061
                                                       0.0000
                                            0.1000
                                   nan
   100
                                            0.1000
                                                       0.0000
               1.3036
                                   nan
   120
               1.3018
                                   nan
                                            0.1000
                                                      -0.0000
   140
               1.3003
                                   nan
                                            0.1000
                                                      -0.0000
   160
               1.2992
                                                       0.0000
                                   nan
                                            0.1000
   180
               1.2983
                                            0.1000
                                                      -0.0000
                                   nan
   200
                                                      -0.0000
               1.2975
                                   nan
                                            0.1000
- Fold3: shrinkage=0.1, interaction.depth= 2, n.minobsinnode=10, n.trees=200
+ Fold3: shrinkage=0.1, interaction.depth= 5, n.minobsinnode=10, n.trees=200
                        {\tt ValidDeviance}
Iter
       TrainDeviance
                                          StepSize
                                                      Improve
     1
               1.3688
                                            0.1000
                                                       0.0040
                                   nan
     2
               1.3621
                                            0.1000
                                                       0.0034
                                   nan
     3
               1.3562
                                            0.1000
                                                       0.0028
                                   nan
     4
               1.3513
                                            0.1000
                                                       0.0023
                                   nan
     5
               1.3471
                                            0.1000
                                                       0.0020
                                   nan
     6
               1.3433
                                            0.1000
                                                       0.0018
                                   nan
     7
               1.3398
                                                       0.0016
                                            0.1000
                                   nan
     8
               1.3370
                                                       0.0014
                                   nan
                                            0.1000
     9
               1.3340
                                            0.1000
                                                       0.0013
                                   nan
    10
                                                       0.0013
               1.3314
                                   nan
                                            0.1000
    20
               1.3154
                                   nan
                                            0.1000
                                                       0.0004
    40
               1.3026
                                            0.1000
                                                       0.0001
                                   nan
    60
               1.2968
                                   nan
                                            0.1000
                                                      -0.0000
    80
               1.2938
                                   nan
                                            0.1000
                                                      -0.0000
   100
               1.2912
                                   nan
                                            0.1000
                                                      -0.0000
   120
               1.2891
                                            0.1000
                                                      -0.0000
                                   nan
   140
               1.2871
                                            0.1000
                                                      -0.0000
                                   nan
   160
               1.2848
                                            0.1000
                                                      -0.0000
                                   nan
   180
               1.2827
                                   nan
                                            0.1000
                                                      -0.0000
   200
               1.2809
                                            0.1000
                                                      -0.0000
                                   nan
- Fold3: shrinkage=0.1, interaction.depth= 5, n.minobsinnode=10, n.trees=200
+ Fold3: shrinkage=0.1, interaction.depth=10, n.minobsinnode=10, n.trees=200
       TrainDeviance
                        ValidDeviance
                                          StepSize
                                                      Improve
```

```
1
               1.3673
                                             0.1000
                                                        0.0046
                                    nan
     2
               1.3591
                                             0.1000
                                                        0.0040
                                    nan
     3
                                             0.1000
                                                        0.0032
               1.3523
                                    nan
     4
                                                        0.0028
               1.3465
                                             0.1000
                                    nan
     5
               1.3414
                                    nan
                                             0.1000
                                                        0.0023
     6
               1.3367
                                    nan
                                             0.1000
                                                        0.0022
     7
               1.3327
                                             0.1000
                                                        0.0018
                                    nan
     8
                                                        0.0015
               1.3294
                                    nan
                                             0.1000
     9
               1.3263
                                             0.1000
                                                        0.0014
                                    nan
                                                        0.0013
    10
               1.3234
                                    nan
                                             0.1000
    20
               1.3059
                                    nan
                                             0.1000
                                                        0.0004
    40
               1.2936
                                             0.1000
                                                       -0.0000
                                    nan
    60
               1.2877
                                             0.1000
                                                       0.0000
                                    nan
    80
               1.2834
                                             0.1000
                                                       -0.0001
                                    nan
                                                       -0.0000
   100
                                             0.1000
               1.2792
                                    nan
   120
               1.2750
                                    nan
                                             0.1000
                                                       0.0000
   140
               1.2716
                                             0.1000
                                                       -0.0000
                                    nan
   160
               1.2679
                                             0.1000
                                                       -0.0001
                                    nan
   180
               1.2644
                                                       -0.0001
                                             0.1000
                                    nan
   200
               1.2608
                                             0.1000
                                                       -0.0000
                                    nan
- Fold3: shrinkage=0.1, interaction.depth=10, n.minobsinnode=10, n.trees=200
+ Fold4: shrinkage=0.1, interaction.depth= 1, n.minobsinnode=10, n.trees=200
                         ValidDeviance
Iter
       TrainDeviance
                                          StepSize
                                                      Improve
     1
               1.3734
                                                        0.0018
                                             0.1000
     2
               1.3702
                                             0.1000
                                                        0.0015
                                    nan
     3
               1.3672
                                    nan
                                             0.1000
                                                        0.0016
     4
                                             0.1000
                                                        0.0012
               1.3646
                                    nan
     5
               1.3621
                                             0.1000
                                                        0.0012
                                    nan
     6
                                                        0.0011
               1.3599
                                             0.1000
                                    nan
     7
               1.3579
                                             0.1000
                                                        0.0010
                                    nan
     8
               1.3559
                                             0.1000
                                                        0.0009
                                    nan
     9
               1.3542
                                             0.1000
                                                        0.0008
                                    nan
    10
               1.3526
                                             0.1000
                                                        0.0008
                                    nan
    20
               1.3424
                                             0.1000
                                                        0.0003
                                    nan
    40
               1.3320
                                             0.1000
                                                        0.0001
                                    nan
    60
               1.3260
                                             0.1000
                                                        0.0001
                                    nan
    80
               1.3217
                                             0.1000
                                                        0.0001
                                    nan
   100
                                                        0.0000
               1.3186
                                    nan
                                             0.1000
                                             0.1000
   120
               1.3163
                                    nan
                                                        0.0000
   140
               1.3145
                                             0.1000
                                                        0.0000
                                    nan
   160
                                                        0.0000
               1.3132
                                    nan
                                             0.1000
   180
               1.3120
                                    nan
                                             0.1000
                                                        0.0000
   200
               1.3112
                                             0.1000
                                                       -0.0000
                                    nan
- Fold4: shrinkage=0.1, interaction.depth= 1, n.minobsinnode=10, n.trees=200
+ Fold4: shrinkage=0.1, interaction.depth= 2, n.minobsinnode=10, n.trees=200
Iter
       TrainDeviance
                         ValidDeviance
                                          StepSize
                                                       Improve
     1
               1.3718
                                             0.1000
                                                        0.0025
                                    nan
     2
               1.3667
                                             0.1000
                                                        0.0025
                                    nan
     3
                                                        0.0019
               1.3628
                                    nan
                                             0.1000
     4
               1.3592
                                             0.1000
                                                        0.0017
                                    nan
     5
                                                        0.0015
               1.3560
                                    nan
                                             0.1000
```

```
6
               1.3532
                                    nan
                                            0.1000
                                                       0.0013
     7
               1.3508
                                            0.1000
                                                       0.0012
                                    nan
     8
               1.3485
                                            0.1000
                                                       0.0010
                                    nan
     9
                                                       0.0010
               1.3463
                                            0.1000
                                    nan
    10
                                                       0.0009
               1.3444
                                    nan
                                            0.1000
    20
               1.3313
                                    nan
                                            0.1000
                                                       0.0004
    40
               1.3181
                                    nan
                                            0.1000
                                                       0.0002
    60
                                                       0.0001
               1.3112
                                    nan
                                            0.1000
    80
               1.3072
                                            0.1000
                                                       0.0000
                                    nan
   100
               1.3046
                                    nan
                                            0.1000
                                                       0.0000
   120
               1.3027
                                    nan
                                            0.1000
                                                       0.0000
   140
               1.3014
                                            0.1000
                                                       -0.0000
                                    nan
   160
                                                       -0.0000
               1.3000
                                            0.1000
                                    nan
   180
               1.2991
                                            0.1000
                                                       -0.0000
                                    nan
   200
                                            0.1000
                                                       -0.0000
               1.2982
                                    nan
- Fold4: shrinkage=0.1, interaction.depth= 2, n.minobsinnode=10, n.trees=200
+ Fold4: shrinkage=0.1, interaction.depth= 5, n.minobsinnode=10, n.trees=200
                         ValidDeviance
Iter
       TrainDeviance
                                          StepSize
                                                      Improve
     1
               1.3691
                                            0.1000
                                                       0.0039
                                    nan
     2
                                                       0.0032
               1.3627
                                    nan
                                            0.1000
     3
               1.3569
                                    nan
                                            0.1000
                                                       0.0028
     4
               1.3518
                                            0.1000
                                                       0.0025
                                    nan
     5
               1.3476
                                            0.1000
                                                       0.0020
                                    nan
     6
                                                       0.0017
               1.3439
                                    nan
                                            0.1000
     7
               1.3408
                                            0.1000
                                                       0.0015
                                    nan
     8
               1.3379
                                    nan
                                            0.1000
                                                       0.0013
     9
               1.3350
                                            0.1000
                                                       0.0013
                                    nan
    10
               1.3323
                                            0.1000
                                                       0.0012
                                    nan
    20
                                                       0.0005
               1.3165
                                            0.1000
                                    nan
    40
               1.3032
                                            0.1000
                                                       0.0002
                                    nan
    60
               1.2980
                                            0.1000
                                                       -0.0000
                                    nan
    80
               1.2950
                                            0.1000
                                                      -0.0000
                                    nan
   100
               1.2924
                                            0.1000
                                                       0.0000
                                    nan
   120
               1.2905
                                            0.1000
                                                      -0.0000
                                    nan
   140
                                            0.1000
                                                       -0.0000
               1.2887
                                    nan
   160
               1.2867
                                            0.1000
                                                       -0.0000
                                    nan
   180
               1.2846
                                            0.1000
                                                       -0.0000
                                    nan
   200
               1.2827
                                            0.1000
                                                       -0.0000
                                    nan
- Fold4: shrinkage=0.1, interaction.depth= 5, n.minobsinnode=10, n.trees=200
+ Fold4: shrinkage=0.1, interaction.depth=10, n.minobsinnode=10, n.trees=200
       TrainDeviance
                         ValidDeviance
Iter
                                          StepSize
                                                      Improve
     1
               1.3675
                                            0.1000
                                                       0.0046
     2
               1.3595
                                            0.1000
                                                       0.0039
                                    nan
     3
               1.3523
                                            0.1000
                                                       0.0033
                                    nan
                                            0.1000
     4
               1.3464
                                                       0.0027
                                    nan
     5
               1.3411
                                    nan
                                            0.1000
                                                       0.0024
     6
               1.3365
                                            0.1000
                                                       0.0022
                                    nan
     7
               1.3327
                                            0.1000
                                                       0.0018
                                    nan
               1.3292
                                                       0.0016
     8
                                    nan
                                            0.1000
     9
               1.3263
                                            0.1000
                                                       0.0013
                                    nan
    10
               1.3236
                                            0.1000
                                                       0.0011
                                    nan
```

```
20
               1.3068
                                    nan
                                            0.1000
                                                       0.0005
    40
               1.2943
                                            0.1000
                                                       0.0000
                                    nan
    60
               1.2881
                                            0.1000
                                                       0.0000
                                    nan
    80
               1.2836
                                            0.1000
                                                      -0.0000
                                    nan
   100
               1.2793
                                    nan
                                            0.1000
                                                       -0.0001
   120
               1.2752
                                    nan
                                            0.1000
                                                       -0.0000
   140
               1.2714
                                    nan
                                            0.1000
                                                       0.0000
                                                      -0.0000
   160
               1.2678
                                    nan
                                            0.1000
   180
               1.2642
                                            0.1000
                                                       -0.0001
                                    nan
   200
                                                       -0.0000
               1.2606
                                    nan
                                            0.1000
- Fold4: shrinkage=0.1, interaction.depth=10, n.minobsinnode=10, n.trees=200
+ Fold5: shrinkage=0.1, interaction.depth= 1, n.minobsinnode=10, n.trees=200
Iter
       TrainDeviance
                         ValidDeviance
                                          StepSize
                                                       Improve
     1
               1.3734
                                            0.1000
                                                       0.0018
                                    nan
     2
               1.3702
                                    nan
                                            0.1000
                                                       0.0015
     3
               1.3671
                                            0.1000
                                                       0.0015
                                    nan
     4
               1.3645
                                            0.1000
                                                       0.0012
                                    nan
     5
               1.3621
                                                       0.0012
                                    nan
                                            0.1000
     6
                                            0.1000
                                                       0.0009
               1.3600
                                    nan
     7
                                                       0.0010
               1.3581
                                    nan
                                            0.1000
     8
               1.3562
                                    nan
                                            0.1000
                                                       0.0009
     9
               1.3546
                                                       0.0008
                                    nan
                                            0.1000
    10
               1.3530
                                            0.1000
                                                       0.0008
                                    nan
    20
               1.3427
                                    nan
                                            0.1000
                                                       0.0003
    40
               1.3326
                                            0.1000
                                                       0.0002
                                    nan
    60
               1.3267
                                    nan
                                            0.1000
                                                       0.0001
    80
                                            0.1000
                                                       0.0001
               1.3227
                                    nan
   100
               1.3196
                                            0.1000
                                                       0.0000
                                    nan
   120
                                                       0.0000
               1.3174
                                            0.1000
                                    nan
   140
               1.3157
                                            0.1000
                                                       0.0000
                                    nan
   160
               1.3143
                                            0.1000
                                                       0.0000
                                    nan
   180
               1.3133
                                            0.1000
                                                       0.0000
                                    nan
   200
               1.3124
                                            0.1000
                                                       -0.0000
                                    nan
- Fold5: shrinkage=0.1, interaction.depth= 1, n.minobsinnode=10, n.trees=200
+ Fold5: shrinkage=0.1, interaction.depth= 2, n.minobsinnode=10, n.trees=200
Iter
       TrainDeviance
                         ValidDeviance
                                          StepSize
                                                      Improve
     1
               1.3720
                                            0.1000
                                                       0.0024
                                    nan
     2
               1.3672
                                    nan
                                            0.1000
                                                       0.0023
     3
               1.3633
                                    nan
                                            0.1000
                                                       0.0019
     4
                                                       0.0018
               1.3595
                                    nan
                                            0.1000
     5
               1.3563
                                    nan
                                            0.1000
                                                       0.0015
     6
                                                       0.0013
               1.3538
                                    nan
                                            0.1000
     7
               1.3513
                                            0.1000
                                                       0.0011
                                    nan
     8
               1.3490
                                            0.1000
                                                       0.0011
                                    nan
     9
                                                       0.0009
               1.3470
                                            0.1000
                                    nan
    10
               1.3450
                                    nan
                                            0.1000
                                                       0.0009
    20
               1.3323
                                            0.1000
                                                       0.0004
                                    nan
    40
                                            0.1000
                                                       0.0001
               1.3196
                                    nan
    60
                                                       0.0001
               1.3127
                                    nan
                                            0.1000
    80
               1.3087
                                            0.1000
                                                       0.0001
                                    nan
   100
                                            0.1000
                                                       -0.0000
               1.3062
                                    nan
```

```
120
               1.3044
                                    nan
                                             0.1000
                                                       0.0000
   140
               1.3030
                                             0.1000
                                                       -0.0000
                                    nan
   160
               1.3021
                                             0.1000
                                                       -0.0000
                                    nan
   180
               1.3013
                                             0.1000
                                                       -0.0000
                                    nan
   200
               1.3003
                                    nan
                                             0.1000
                                                        0.0000
- Fold5: shrinkage=0.1, interaction.depth= 2, n.minobsinnode=10, n.trees=200
+ Fold5: shrinkage=0.1, interaction.depth= 5, n.minobsinnode=10, n.trees=200
Iter
       TrainDeviance
                         ValidDeviance
                                          StepSize
                                                       Improve
     1
               1.3695
                                                        0.0037
                                    nan
                                             0.1000
     2
               1.3630
                                    nan
                                             0.1000
                                                        0.0032
     3
               1.3574
                                             0.1000
                                                        0.0027
                                    nan
     4
               1.3525
                                             0.1000
                                                        0.0024
                                    nan
     5
               1.3480
                                             0.1000
                                                        0.0022
                                    nan
     6
                                                        0.0016
               1.3445
                                    nan
                                             0.1000
     7
               1.3415
                                    nan
                                             0.1000
                                                        0.0013
     8
               1.3382
                                             0.1000
                                                        0.0016
                                    nan
     9
               1.3355
                                             0.1000
                                                        0.0012
                                    nan
    10
               1.3330
                                                        0.0012
                                             0.1000
                                    nan
    20
                                             0.1000
                                                        0.0006
               1.3172
                                    nan
    40
                                                        0.0001
               1.3042
                                    nan
                                             0.1000
    60
               1.2990
                                    nan
                                             0.1000
                                                        0.0000
    80
               1.2959
                                             0.1000
                                                       -0.0000
                                    nan
   100
               1.2932
                                             0.1000
                                                       -0.0001
                                    nan
   120
               1.2909
                                             0.1000
                                                       0.0000
                                    nan
   140
               1.2888
                                             0.1000
                                                       -0.0000
                                    nan
   160
               1.2868
                                    nan
                                             0.1000
                                                       -0.0000
   180
               1.2848
                                             0.1000
                                                       -0.0000
                                    nan
   200
               1.2829
                                             0.1000
                                                       -0.0000
                                    nan
- Fold5: shrinkage=0.1, interaction.depth= 5, n.minobsinnode=10, n.trees=200
+ Fold5: shrinkage=0.1, interaction.depth=10, n.minobsinnode=10, n.trees=200
Iter
       TrainDeviance
                         ValidDeviance
                                          StepSize
                                                       Improve
     1
               1.3674
                                             0.1000
                                                        0.0046
                                    nan
     2
               1.3596
                                             0.1000
                                                        0.0036
                                    nan
     3
                                             0.1000
                                                        0.0032
               1.3528
                                    nan
     4
               1.3468
                                                        0.0028
                                    nan
                                             0.1000
     5
               1.3419
                                             0.1000
                                                        0.0023
                                    nan
     6
                                                        0.0020
               1.3378
                                    nan
                                             0.1000
     7
                                            0.1000
               1.3341
                                    nan
                                                        0.0018
     8
               1.3306
                                             0.1000
                                                        0.0015
                                    nan
     9
                                                        0.0014
               1.3274
                                    nan
                                             0.1000
    10
               1.3245
                                    nan
                                             0.1000
                                                        0.0013
    20
                                                        0.0004
               1.3079
                                    nan
                                             0.1000
    40
               1.2960
                                             0.1000
                                                        0.0000
                                    nan
    60
               1.2903
                                             0.1000
                                                       -0.0000
                                    nan
                                            0.1000
    80
               1.2857
                                                       -0.0001
                                    nan
   100
               1.2812
                                    nan
                                             0.1000
                                                       -0.0001
   120
               1.2774
                                             0.1000
                                                       -0.0000
                                    nan
   140
                                             0.1000
                                                       -0.0000
               1.2739
                                    nan
   160
                                                       -0.0000
               1.2701
                                    nan
                                             0.1000
   180
               1.2663
                                             0.1000
                                                       -0.0000
                                    nan
   200
               1.2629
                                             0.1000
                                                       -0.0001
                                    nan
```

```
- Fold5: shrinkage=0.1, interaction.depth=10, n.minobsinnode=10, n.trees=200
Aggregating results
Selecting tuning parameters
Fitting n.trees = 100, interaction.depth = 5, shrinkage = 0.1, n.minobsinnode = 10 on full training set
     TrainDeviance ValidDeviance
                                     StepSize
                                                Improve
             1.3695
                                       0.1000
                                                 0.0037
                               nan
             1.3625
                                       0.1000
                                                0.0035
    2
                               nan
    3
             1.3568
                               nan
                                       0.1000
                                                0.0028
    4
             1.3518
                                                0.0025
                                       0.1000
                               nan
    5
             1.3474
                                       0.1000
                                                0.0021
                               nan
    6
             1.3440
                                       0.1000
                                              0.0017
                               nan
    7
             1.3408
                                              0.0015
                               nan
                                       0.1000
    8
             1.3378
                               nan
                                       0.1000
                                                0.0013
    9
             1.3350
                               nan
                                      0.1000
                                                0.0013
   10
                                              0.0010
             1.3328
                               nan
                                      0.1000
   20
             1.3178
                                       0.1000
                                                0.0004
                               nan
   40
             1.3046
                               nan
                                       0.1000
                                                0.0001
   60
             1.2993
                                       0.1000
                                                0.0000
                               nan
   80
             1.2965
                               nan
                                       0.1000
                                                0.0000
  100
             1.2944
                                       0.1000 -0.0000
                               nan
Warning message:
In train.default(x, y, weights = w, ...) :
 The metric "Accuracy" was not in the result set. ROC will be used instead.
> proc.time() - ptm_rf
  user system elapsed
217.28
          0.20 217.50
> #make predictions aginst testData with the new model
> print(model_gbm)
Stochastic Gradient Boosting
85937 samples
   9 predictor
   2 classes: 'no', 'yes'
No pre-processing
Resampling: Cross-Validated (5 fold)
Summary of sample sizes: 68749, 68751, 68749, 68750, 68749
Resampling results across tuning parameters:
 interaction.depth n.trees ROC
                                       Sens
                                                 Spec
                            0.6143768 0.8101849
  1
                     25
                                                 0.3479370
  1
                     50
                            0.6218183 0.7722348 0.4061879
                    100
  1
                            0.6286359 0.7611705 0.4292260
  1
                    150
                            0.6308180 0.7564134 0.4355067
                    200
                            0.6320101 0.7534404 0.4391103
  1
  2
                    25
                            2
                    50
                            0.6294636 0.7975916 0.3916188
  2
                    100
                            0.6333549 0.7873979 0.4075264
  2
                    150
                            0.6345888 0.7856353 0.4097659
  2
                    200
                            0.6346425 0.7863786 0.4087106
  5
                            25
```

```
0.6344025 0.8118839 0.3804988
  5
                    100
                            0.6359683 0.8056829 0.3900229
  5
                    150
  5
                    200
                            10
                            0.6327044 0.8366461 0.3499189
                    25
 10
                    50
                            0.6351102 0.8202513 0.3708203
 10
                    100
                            0.6351320 0.8144112 0.3771010
 10
                    150
                            0.6339422 0.8109921 0.3791602
 10
                    200
                            0.6331116  0.8096541  0.3803187
Tuning parameter 'shrinkage' was held constant at a value of 0.1
Tuning parameter 'n.minobsinnode' was held constant at a value of 10
ROC was used to select the optimal model using the largest value.
The final values used for the model were n.trees = 100, interaction.depth =
5, shrinkage = 0.1 and n.minobsinnode = 10.
> pred.model_gbm.prob = predict(model_gbm, newdata = shotTest, type="prob")
> pred.model_gbm.raw = predict(model_gbm, newdata = shotTest)
> roc.model_gbm = pROC::roc(
   shotTest$FGM,
   as.vector(ifelse(pred.model_gbm.prob[,"yes"] >0.5, 1,0))
+ )
Setting levels: control = no, case = yes
Setting direction: controls < cases
> auc.model_gbm = pROC::auc(roc.model_gbm)
> print(auc.model_gbm)
Area under the curve: 0.596
> #plot ROC curve
> plot.roc(roc.model_gbm, print.auc = TRUE, col = 'red', print.thres = "best")
> #generate confusion matrix, as well as other metrics such as accuracy, balanced accuracy
> confusionMatrix(data = pred.model_gbm.raw, shotTest$FGM)
Confusion Matrix and Statistics
         Reference
Prediction
           no
                 yes
      no 16214 10182
      yes 3966 6467
              Accuracy : 0.6158
                95% CI: (0.6109, 0.6208)
   No Information Rate: 0.5479
   P-Value [Acc > NIR] : < 2.2e-16
                 Kappa: 0.1984
Mcnemar's Test P-Value : < 2.2e-16
           Sensitivity: 0.8035
           Specificity: 0.3884
```

```
Pos Pred Value : 0.6143
        Neg Pred Value: 0.6199
            Prevalence: 0.5479
        Detection Rate: 0.4403
  Detection Prevalence : 0.7167
     Balanced Accuracy: 0.5960
      'Positive' Class : no
> #summary of model
> summary(model_gbm)
 var rel.inf
PC6 PC6 39.162726
PC3 PC3 27.261858
PC5 PC5 9.652336
PC1 PC1 7.877662
PC2 PC2 6.407543
PC4 PC4 4.380920
PC8 PC8 2.955187
PC7 PC7 1.287303
X X 1.014465
> # Save the model into a file
> save(model_gbm, file="gbm_pca.rda")
```

EVALUATION