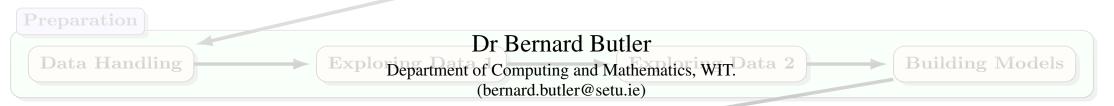
Data Mining (Week 1)

BSc - Data Mining1

Topic 02: Motivating Example

Part 01: Top X pandas commands



Autumn Semester, 2022

Prediction

Outline

- Reading data formats
- Computing descriptive statistics
- Processing data by filtering and grouping

Wrap up

Part I

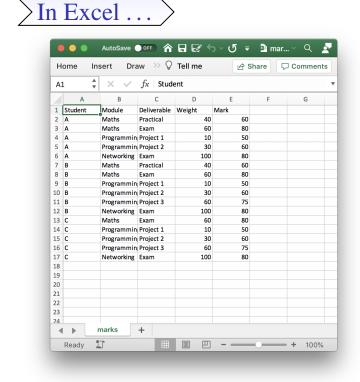
Introduction

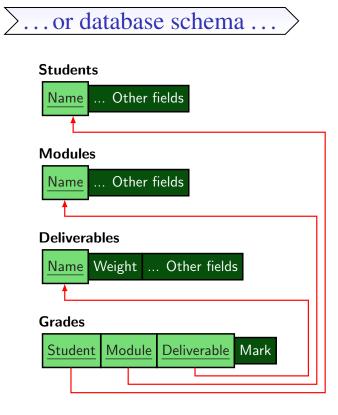
Before we start....

- The slides today are based on those prepared by my colleague Dr Kieran Murphy.
- Thanks Kieran!

Minimal Dataset

To better understand the various pandas operations we are going use a tiny* dataset based on (fictional) student results. (marks.csv)





\cdots...like to know ... \cdot

- Student performance weighted mark on each module, missing deliverables etc.
- Module performance number of attempts and average mark.
- Deliverable performance number of attempts and average mark, predictor of overall module grade, etc.

^{*}Dataset is small enough that you can verify operation results by hand.

Terminology

df.head(1000)							
	Student	Module	Deliverable	Weight	Mark		
0	А	Maths	Practical	40	60		
1	Α	Maths	Exam	60	80		
2	Α	Programming	Project 1	10	50		
3	Α	Programming	Project 2	30	60		
4	Α	Networking	Lab Work	100	80		
5	В	Maths	Practical	40	60		
6	В	Maths	Exam	60	80		
7	В	Programming	Project 1	10	50		
8	В	Programming	Project 2	30	60		
9	В	Programming	Project 3	60	75		
10	В	Networking	Project	100	80		
11	С	Maths	Exam	60	80		
12	С	Programming	Project 1	10	50		
13	С	Programming	Project 2	30	60		
14	С	Programming	Project 3	60	75		
15	С	Networking	Lab Work	100	80		

- A DataFrame is a table of data values.
 - df = pd.read_csv("marks.csv")
- A Series is a list of data values typically columns in a dataframe. We can access an individual column using

```
    df.Deliverable
    df["Deliverable"]
    df.iloc[:,2]
    (dot notation)
    (numpy, index notation)
```

- The index is a special column whose values can be used to access rows rather using row number.
 - The default index is equal to the row number.

Part II

Input and Output

Setup

> Minimal >

We begin every data mining project with importing the three core data science packages:

```
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
plt.style.use('seaborn-darkgrid')
numpy — fast array operations
pandas — data manipulation
matplotlib — visualisation
```

• We give modules nicknames (np, pd, ...) to simplify their later use, and we access properties/functions of a package using the dot notation (np.max, pd.DataFrame, ...).

Extra

```
import seaborn as sns
import statsmodels.api as sm

pd.set_option('display.max_columns', 500)
pd.set_option('display.width', 1000)
seaborn — statistical visualisation
statsmodels — statistical data exploration
pandas options to show all columns for wider datasets
pd.set_option('display.width', 1000)
```

Reading data from a CSV file

Pandas supports a huge variety of input/output formats so best approach is to focus on what is needed to process the given data and verify input. Our marks dataset is in CSV format so we start with

```
import numpy as np
  import pandas as pd
  import matplotlib.pyplot as plt
 plt.style.use('seaborn-darkgrid')
                                                                                  (16, 5)
                                                                                    Student
                                                                                            Module Deliverable Weight Mark
and input using
                                                                                            Maths
                                                                                                             60
                                                                                                  Practical
 df = pd.read_csv('data/marks.csv', sep=',')
                                                                                                             50
                                                                                                             60
 print(df.shape)
                                                                                          Networking
                                                                                                  Lab Work
  df.head()
                                                (16, 5)
```

Always verify input by checking dataset dimensions and looking at some rows!!!

Datatypes

Pandas data types:

- **object** used for text or mixed numeric and non-numeric values.
- int64 integer values,
 - Does not support missing values, so an int column containing at least one missing value will automatically be converted to float.
- float64 floating point numbers.
- bool True/False values
- datetime64 date and time values
- category Finite (typically small) list of text values

Student	object
Module	object
Deliverable	object
Weight	int64
Mark	int64
dtyne: ohiect	

df.dtypes

Regularly verifying datatypes is vital[†]:

- Operations differ based on datatype, eg, '+' concatenate strings but adds numerical values.
- Datatype can change based on results, eg, int converts to float due to missing values.

[†]Google "Detecting Excel's gene auto-conversions."

Datatypes — Converting

We will deal with modifying and creating new columns later, but while we are on datatypes, we will look at changing datatype . . .

Using the Series function astype

```
df["Weight"] = df["Weight"].astype('float')
df["Weight"].dtype

dtype('float64')
```

- New datatype is required argument 'int', 'float', 'str', 'object', 'category', etc.
- Simple, but fragile if data conversion is possible.

or using pandas function to_numeric

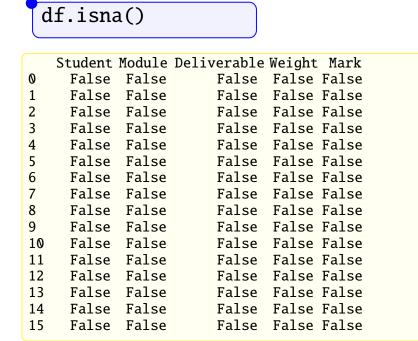
```
df["Weight"] = pd.to_numeric(df["Weight"])
df["Weight"].dtype

dtype('float64')
```

- More powerful, can specify what to do in cases where the conversion fails etc
- Have functions to_numeric, to_datetime, and to_timedelta.

Missing Values

Identifying and dealing with missing values is critical step in data preparation. What should you do? delete rows containing missing values? or impute then? Here we will just look at identifying missing values.



```
df.isna().sum()

Student 0
Module 0
Deliverable 0
Weight 0
Mark 0
dtype: int64
```

- Use dataframe function **fillna** to replace missing values.
- Recall False and True map to 0 and 1 respectively.
- Use df.isna().sum(axis=1) to sum along rows.

Output

Saving dataframe to CSV is straightforward (I rarely include the (default) index when saving datasets).

```
df.to_csv('marks_2.csv', index=False)
```

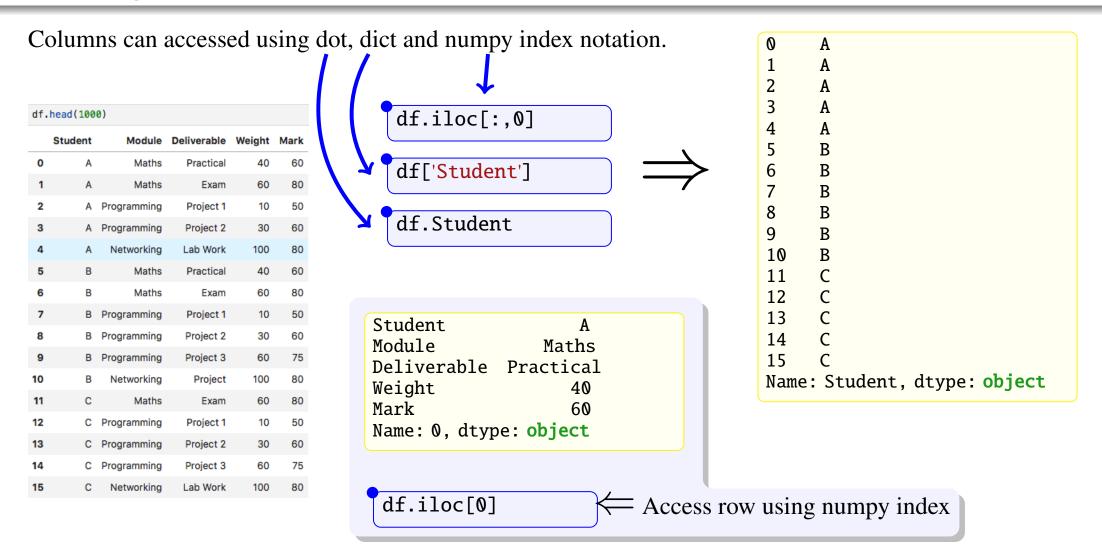
- CSV has become the default file format in Data Mining application especially for 'informal' datasets.
 - ✓ human readable, easy to generate / parse (if correct).
 - X Can be highly redundant, slow to input/output.
 - X No meta information.
- Other formats are better for speed and resulting file size and for saving meta data not supported by CSV (such as columns datatypes, category information, etc).

data science: The Best Format to Save Pandas Data

Part III

Filtering

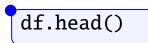
Selecting individual rows/columns results in a series



Head and Tail

Commands head and tail return the first and last n rows (default n = 5) of a dataframe/series.

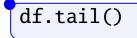
	Student	Module	Deliverable	Weight	Mark
0	A	Maths	Practical	40	60
1	A	Maths	Exam	60	80
2	A	Programming	Project 1	10	50
3	A	Programming	Project 2	30	60
4	A	Networking	Lab Work	100	80
5	В	Maths	Practical	40	60
6	В	Maths	Exam	60	80
7	В	Programming	Project 1	10	50
8	В	Programming	Project 2	30	60
9	В	Programming	Project 3	60	75
10	В	Networking	Project	100	80
11	С	Maths	Exam	60	80
12	С	Programming	Project 1	10	50
13	С	Programming	Project 2	30	60
14	С	Programming	Project 3	60	75
15	С	Networking	Lab Work	100	80



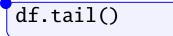
Student	Module	Deliverable	Weight	Mark
0 A	Maths	Practical	40	60
1 A	Maths	Exam	60	80
2 A	Programming	Project 1	10	50
3 A	Programming	Project 2	30	60
4 A	Networking	Lab Work	100	80



	Student	Module	Deliverable	Weight	Mark
0	A	Maths	Practical	40	60



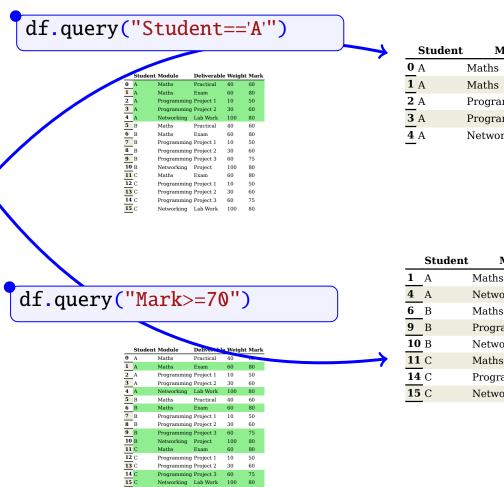
	Student	Module	Deliverable	Weight	Mark
11	С	Maths	Exam	60	80
12	С	Programming	Project 1	10	50
13	С	Programming	Project 2	30	60
14	C	Programming	Project 3	60	75
15	С	Networking	Lab Work	100	80



Stu	dent	Module	Deliverable	Weight	Mark
15 C	Net	working	Lab Work	100	80

Query — on a single-column criteria

	Student	Module	Deliverable	Weight	Mark
0	A	Maths	Practical	40	60
1	A	Maths	Exam	60	80
2	A	Programming	Project 1	10	50
3	A	Programming	Project 2	30	60
4	A	Networking	Lab Work	100	80
5	В	Maths	Practical	40	60
6	В	Maths	Exam	60	80
7	В	Programming	Project 1	10	50
8	В	Programming	Project 2	30	60
9	В	Programming	Project 3	60	75
10	В	Networking	Project	100	80
11	С	Maths	Exam	60	80
12	С	Programming	Project 1	10	50
13	С	Programming	Project 2	30	60
14	С	Programming	Project 3	60	75
15	С	Networking	Lab Work	100	80



Student	Module	Deliverable	Weight	Mark
0 A	Maths	Practical	40	60
1 A	Maths	Exam	60	80
2 A	Programming	Project 1	10	50
3 A	Programming	Project 2	30	60
<u>4</u> A	Networking	Lab Work	100	80

	Student	Module	Deliverable	Weight	Mark
1	A	Maths	Exam	60	80
4	A	Networking	Lab Work	100	80
6	В	Maths	Exam	60	80
9	В	Programming	Project 3	60	75
10	В	Networking	Project	100	80
11	С	Maths	Exam	60	80
14	С	Programming	Project 3	60	75
15	С	Networking	Lab Work	100	80

Query — on multiple columns (using python logical operators)

	Student	Module	Deliverable	Weight	Mark
0	A	Maths	Practical	40	60
1	A	Maths	Exam	60	80
2	A	Programming	Project 1	10	50
3	A	Programming	Project 2	30	60
4	A	Networking	Lab Work	100	80
5	В	Maths	Practical	40	60
6	В	Maths	Exam	60	80
7	В	Programming	Project 1	10	50
8	В	Programming	Project 2	30	60
9	В	Programming	Project 3	60	75
10	В	Networking	Project	100	80
11	С	Maths	Exam	60	80
12	С	Programming	Project 1	10	50
13	С	Programming	Project 2	30	60
14	С	Programming	Project 3	60	75
15	С	Networking	Lab Work	100	80

	Student	Module	Deliverable	Weight	Mar
0	A	Maths	Practical	40	60
1	A	Maths	Exam	60	80
=	A	Programming	Project 1	10	50
3	A	Programming	Project 2	30	60
4	A	Networking	Lab Work	100	80
5	В	Maths	Practical	40	60
6	В	Maths	Exam	60	80
7	В	Programming	Project 1	10	50
8	В	Programming	Project 2	30	60
9	В	Programming	Project 3	60	75
10	В	Networking	Project	100	80
11	С	Maths	Exam	60	80
12	С	Programming	Project 1	10	50
13	С	Programming	Project 2	30	60
14	С	Programming	Project 3	60	75
15	С	Networking	Lab Work	100	80

_	Student	Module	Deliverable	Weight	Mark
0	A	Maths	Practical	40	60
1	A	Maths	Exam	60	80
2	A	Programming	Project 1	10	50
3	A	Programming	Project 2	30	60
4	A	Networking	Lab Work	100	80
5	В	Maths	Practical	40	60
6	В	Maths	Exam	60	80
7	В	Programming	Project 1	10	50
8	В	Programming	Project 2	30	60
9	В	Programming	Project 3	60	75
10	В	Networking	Project	100	80
11	С	Maths	Exam	60	80
12	С	Programming	Project 1	10	50
13	С	Programming	Project 2	30	60
14	C	Programming	Project 3	60	75
15	С	Networking	Lab Work	100	80

df.query("Mark<70 and Module=='Maths'")</pre>

	Student	Module	Deliverable	Weight	Mark
0	A	Maths	Practical	40	60
5	В	Maths	Practical	40	60

	Student	Module	Deliverable	Weight	Mark
0	A	Maths	Practical	40	60
1	A	Maths	Exam	60	80
2	A	Programming	Project 1	10	50
3	A	Programming	Project 2	30	60
5	В	Maths	Practical	40	60
6	В	Maths	Exam	60	80
7	В	Programming	Project 1	10	50
8	В	Programming	Project 2	30	60
11	<u> </u> C	Maths	Exam	60	80
12	<u>C</u>	Programming	Project 1	10	50
13	C	Programming	Project 2	30	60

df.query("Mark<70 or Module=='Maths'")</pre>

Query — on multiple columns (using pandas logical operators)

	Student	Module	Deliverable	Weight	Mark
0	A	Maths	Practical	40	60
1	A	Maths	Exam	60	80
2	A	Programming	Project 1	10	50
3	A	Programming	Project 2	30	60
4	A	Networking	Lab Work	100	80
5	В	Maths	Practical	40	60
6	В	Maths	Exam	60	80
7	В	Programming	Project 1	10	50
8	В	Programming	Project 2	30	60
9	В	Programming	Project 3	60	75
10	В	Networking	Project	100	80
11	С	Maths	Exam	60	80
12	С	Programming	Project 1	10	50
13	С	Programming	Project 2	30	60
14	С	Programming	Project 3	60	75
15	С	Networking	Lab Work	100	80

	Student	Module	Deliverable	Weight	Mar
0	A	Maths	Practical	40	60
1	A	Maths	Exam	60	80
=	A	Programming	Project 1	10	50
3	A	Programming	Project 2	30	60
4	A	Networking	Lab Work	100	80
5	В	Maths	Practical	40	60
6	В	Maths	Exam	60	80
7	В	Programming	Project 1	10	50
8	В	Programming	Project 2	30	60
9	В	Programming	Project 3	60	75
10	В	Networking	Project	100	80
11	С	Maths	Exam	60	80
12	С	Programming	Project 1	10	50
13	С	Programming	Project 2	30	60
14	С	Programming	Project 3	60	75
15	С	Networking	Lab Work	100	80

	Student	Module	Deliverable	Weight	Mark
0	A	Maths	Practical	40	60
1	A	Maths	Exam	60	80
2	A	Programming	Project 1	10	50
3	A	Programming	Project 2	30	60
4	A	Networking	Lab Work	100	80
5	В	Maths	Practical	40	60
6	В	Maths	Exam	60	80
7	В	Programming	Project 1	10	50
8	В	Programming	Project 2	30	60
9	В	Programming	Project 3	60	75
10	В	Networking	Project	100	80
11	С	Maths	Exam	60	80
12	С	Programming	Project 1	10	50
13	С	Programming	Project 2	30	60
14	С	Programming	Project 3	60	75
15	С	Networking	Lab Work	100	80

df.query("(Mark<70) & (Module=='Maths')")</pre>

	Student	Module	Deliverable	weight	Mark
0	A	Maths	Practical	40	60
5	В	Maths	Practical	40	60

		Student	Module	Deliverable	Weight	Mark
()	A	Maths	Practical	40	60
1	L	A	Maths	Exam	60	80
2	2	A	Programming	Project 1	10	50
3	3	A	Programming	Project 2	30	60
5	5	В	Maths	Practical	40	60
•	ŝ	В	Maths	Exam	60	80
_	7	В	Programming	Project 1	10	50
8	3	В	Programming	Project 2	30	60
_1	L1	С	Maths	Exam	60	80
1	L2	С	Programming	Project 1	10	50
_1	13	С	Programming	Project 2	30	60

df.query("(Mark<70) | (Module=='Maths')")</pre>

Filtering using 10c

Student Module Deliverable Weight Mark 0 A Maths Practical 40 60 1 A Maths Exam 60 80 Programming Project 1 10 50 Programming Project 2 30 60 **4** A Networking Lab Work 100 80 Maths Practical 40 60 **6** B Maths Exam 60 80 Programming Project 1 10 50 **8** B Programming Project 2 30 60 75 Programming Project 3 60 **10** B Networking Project 80 100 **11** C Maths Exam 60 80 **12** C Programming Project 1 10 50 **13** C Programming Project 2 60 **14** C Programming Project 3 60 75 **15** C Networking Lab Work 100 80

Note the square (not round) brackets — think of loc as array indexing not a function call.

df.loc[ROW_SELECTION, COL_SELECTION] where row and columns selection can be

- Single values: row number or column name
- An integer list for rows or list of column names
- A boolean list for logical indexing of rows
- A colon to indicate every row/column

		Student	Module	Deliverable	Weight	Mark
	0	A	Maths	Practical	40	60
•	1	A	Maths	Exam	60	80
		A	Programming	Project 1	10	50
	3	A	Programming	Project 2	30	60
		A	Networking	Lab Work	100	80
	5	В	Maths	Practical	40	60
ĺ	6	В	Maths	Exam	60	80
	7	В	Programming	Project 1	10	50
	8	В	Programming	Project 2	30	60
	9	В	Programming	Project 3	60	75
	10	В	Networking	Project	100	80
	11	С	Maths	Exam	60	80
	12	С	Programming	Project 1	10	50
į	13	С	Programming	Project 2	30	60
	14		Programming	Project 3	60	75
	15	С	Networking	Lab Work	100	80
J						

 0
 A
 60

 1
 A
 80

 5
 B
 60

 6
 B
 80

 11
 C
 80

Student Mark

df.loc[df.Module=="Maths", ["Student", "Mark"]]

More complicated example

I prefer to define define row selection criteria, and the column list and order, separately to the loc statement.

Student Module Deliverable Weight Mark

O A Maths Practical 40 60

							<u>U</u> A	Matns	Practical	40	60
							1 A	Maths	Exam	60	80
							2 A 3 A	Programming Programming		10 30	50 60
	Stude	nt Module	Deliverable	Weight	t Mark		4 A		Lab Work	100	80
0	A	Maths	Practical	40	60	•	5 B	Maths	Practical	40	60
÷	_						6 B 7 B	Maths Programming	Exam Project 1	60 10	80 50
1	_A	Maths	Exam	60	80		8 B	Programming		30	60
2	A	Programming	Project 1	10	50		9 B 10 B	Programming Networking		60 100	75 80
3	_ A	Programming	Project 2	30	60		11 C	Maths	Exam	60	80
	_ A	0 0	Froject 2	30			12 C 13 C	Programming		10	50
4	A	Networking	Lab Work	100	80		14 C	Programming Programming		30 60	60 75
5	В	Maths	Practical	40	60		15 C	Networking	Lab Work	100	80
6	В	Maths	Exam	60	80						
7	В	Programming		10	50						
	_ D	Programming	Project 1	10	30						
8	В	Programming	Project 2	30	60						
9	В	Programming	Project 3	60	75						
10	_	0 0									
10) B	Networking	Project	100	80						
11	L C	Maths	Exam	60	80						
12	C C	Programming	Project 1	10	50						
13	C	Programming	Project 2	30	60						

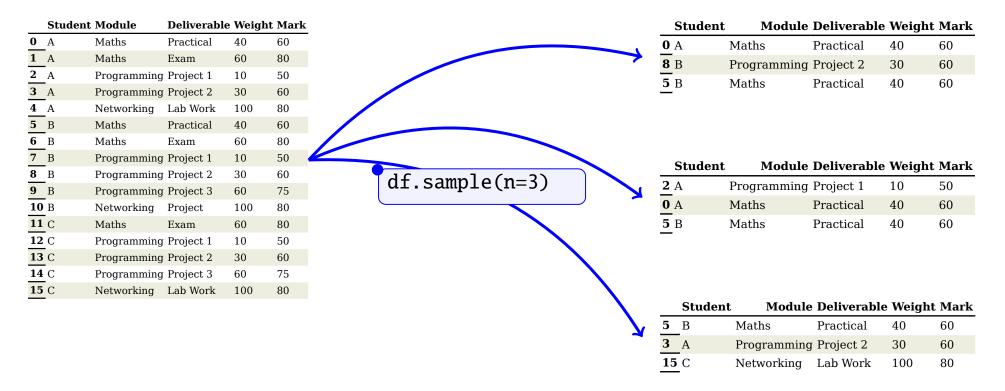
```
Deliverable Weight Mark
dule
       Practical 40
                       80
       Exam
gramming Project 1 10
                       50
gramming Project 2 30
working Lab Work 100
       Practical 40
gramming Project 1 10
                       50
gramming Project 2 30
gramming Project 3 60
working Project
       Exam
gramming Project 1 10
gramming Project 3 60
                       75
working Lab Work 100 80
```

```
criteria = ((df.Mark<50) & (df.Module=='Maths')) | ((df.Mark<70) & (df.Module!='Maths'))
columns = ['Module', 'Student', 'Mark']
df.loc[criteria, columns]</pre>
```

Sampling

The sample function selects a random subset of the dataframe rows.

- Either specify the number of rows (as an integer) or fraction of the data (as a float).
- Can set the seed using random_state parameter for reproducible samples.



Part IV

Sorting

Sorting

A pandas dataframe has two sorting operations:

- sort_index() orders rows based on current index.
- sort_values(COLUMNS) orders rows based on single column or list of columns.

Two important modifications:

- By default, the sort order is in ascending. Set parameter ascending=False to reverse this.
- By default, a new dataframe is returned with desired sort order, set parameter inplace=True to update current dataframe instead (then no output is generated).

Stude	nt Module	Deliverable	e Weigh	t Mark		Stude	nt Module	e Deliverabl	e Weigl	nt Mark
0 A	Maths	Practical	40	60		1 A	Maths	Exam	60	80
1 A	Maths	Exam	60	80		6 B	Maths	Exam	60	80
2 A	Programming	Project 1	10	50		11 C	Maths	Exam	60	80
3 A	Programming	Project 2	30	60		0 A	Maths	Practical	40	60
4 A	Networking	Lab Work	df.	sort	_values(['Module','Deliverable'])	В	Maths	Practical	40	60
5 B	Maths	Practical	("- "			A	Networking	Lab Work	100	80
6 B	Maths	Exam	60	80		15 C	Networking	Lab Work	100	80
7 B	Programming	Project 1	10	50		10 B	Networking	Project	100	80
8 B	Programming	Project 2	30	60		2 A	Programming	roject 1	10	50
9 B	Programming	Project 3	60	75		7 B	Programming	Project 1	10	50
10 B	Networking	Project	100	80		12 C	Programming	g Project 1	10	50
11 C	Maths	Exam	60	80		3 A	Programming	g Project 2	30	60
12 C	Programming	Project 1	10	50		8 B	Programming	g Project 2	30	60
13 C	Programming	Project 2	30	60		13 C	Programming	g Project 2	30	60
14 C	Programming	Project 3	60	75		9 B	Programming	g Project 3	60	75
15 C	Networking	Lab Work	100	80		14 C	Programming	g Project 3	60	75

Part V

Defining New Columns

Defining new columns — row-wise operation

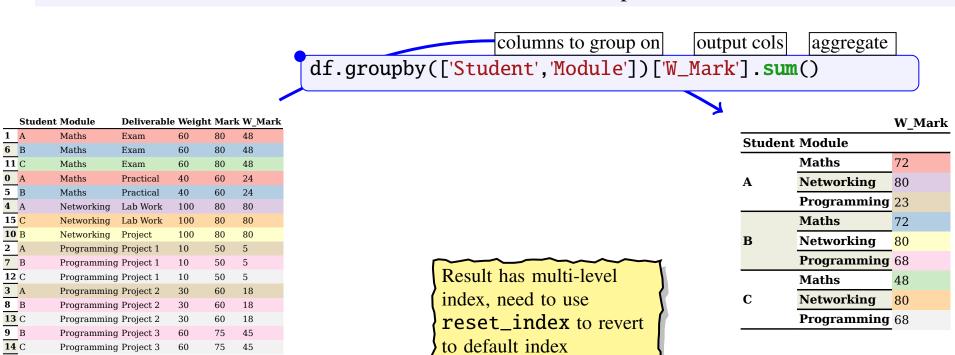
We want to compute the weighted mark for each module for each student. Two steps:

- Create column, W_Mark, to store the weighted mark for each deliverable. This is a row by row calculation only need data in current row to compute the result.
- Create column, M_Mark, to store the module mark for each student. This is a group calculation need all rows for that student and module to compute the result.

Student	Module	Deliverable	Weig	ht Mark								Stude	nt Module	Deliverable	Weight	Mark	W_Mark
1 A	Maths	Exam	60	80								1 A	Maths	Exam	60	80	48
6 B	Maths	Exam	60	80								6 B	Maths	Exam	60	80	48
11 C	Maths	Exam	60	80								11 C	Maths	Exam	60	80	48
0 A	Maths	Practical	40	60								0 A	Maths	Practical	40	60	24
5 B	Maths	Practical	40	60								5 B	Maths	Practical	40	60	24
4 A	Networking	Lab Work	100	80								4 A	Networking	Lab Work	100	80	80
15 C	Networking	Lab Work	100	df['\ii	7 Mai	rk'l	= df	- Wei	aht	* 4t	Mark //	100	letworking	Lab Work	100	80	80
10 B	Networking	Project	100	ar L "	·		– u i	WC1	girc	· al.	ilain //	100	Vetworking	Project	100	80	80
2 A	Programming	Project 1	10	50								2 A	Programming	Project 1	10	50	5
7 B	Programming	Project 1	10	50								7 B	Programming	Project 1	10	50	5
12 C	Programming	Project 1	10	50								12 C	Programming	Project 1	10	50	5
3 A	Programming	Project 2	30	60								3 A	Programming	Project 2	30	60	18
8 B	Programming	Project 2	30	60			<u> </u>		~		~~~	8 B	Programming	Project 2	30	60	18
13 C	Programming	Project 2	30	60	1	Nee	d to	use di	ct no	tation	(not dot	13 C	Programming	Project 2	30	60	18
9 B	Programming	Project 3	60	75							· ·	9 B	Programming	,	60	75	45
14 C	Programming	Project 3	60	75	l			when	i delli	ning a	new	14 C	Programming		60	75	45
					}	colu	ımn.					_	5.	, 5			
					· ·	$\overline{}$		~~		~	~~~						

Defining new columns — group aggregate result

- Create column, W_Mark, to store the weighted mark for each deliverable. This is a row by row calculation only need data in current row to compute the result.
- Create column, M_Mark, to store the module mark for each student. This is a group calculation need all rows for that student and module to compute the result.



Defining new columns — group aggregate result

columns to group on output cols aggregate df.groupby(['Student','Module'])[['W_Mark']].sum().reset_index()

	Student	Module	Deliverable	Weight	Mark	W_Mark
1	A	Maths	Exam	60	80	48
6	В	Maths	Exam	60	80	48
11	С	Maths	Exam	60	80	48
0	A	Maths	Practical	40	60	24
5	В	Maths	Practical	40	60	24
4	A	Networking	Lab Work	100	80	80
15	С	Networking	Lab Work	100	80	80
10	В	Networking	Project	100	80	80
2	A	Programming	Project 1	10	50	5
7	В	Programming	Project 1	10	50	5
12	С	Programming	Project 1	10	50	5
3	A	Programming	Project 2	30	60	18
8	В	Programming	Project 2	30	60	18
13	С	Programming	Project 2	30	60	18
9	В	Programming	Project 3	60	75	45
14	С	Programming	Project 3	60	75	45
2 7 12 3 8 13 9	A B C A B C B	Programming Programming Programming Programming Programming Programming Programming	Project 1 Project 1 Project 1 Project 2 Project 2 Project 2 Project 3	10 10 10 30 30 30 30 60	50 50 50 60 60 60 75	5 5 5 18 18 18 45

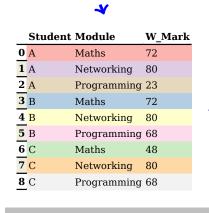
This is the required result and we can save this to a new dataframe. However, we often want to put this into to out original dataframe as an extra column. Only problem we have different rows so can't just assign to a new column — need to use transform function.

	Student	Module	W_	Mark
0	A	Maths	72	
1	A	Networking	80	
	A	Programming	23	
3	В	Maths	72	
4	В	Networking	80	
5	В	Programming	68	
6	С	Maths	48	
7	С	Networking	80	
8	С	Programming	68	

Defining new columns — group aggregate result

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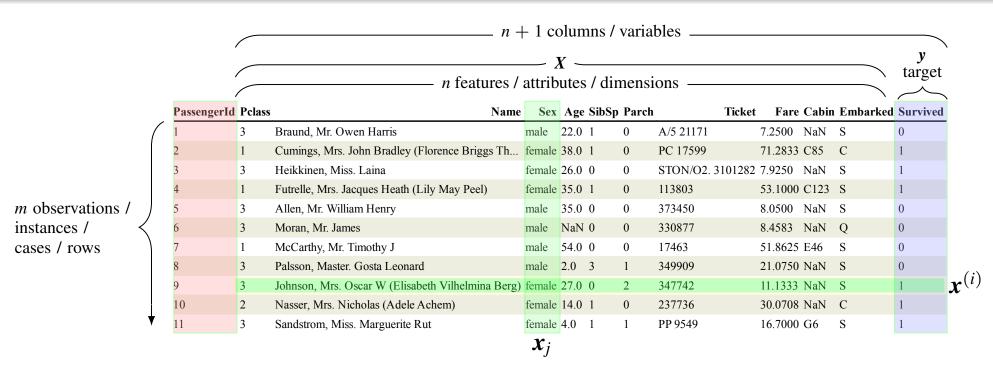
	Student	Module	Deliverable	Weight	Mark	W_Mark
1	A	Maths	Exam	60	80	48
6	В	Maths	Exam	60	80	48
11	С	Maths	Exam	60	80	48
0	A	Maths	Practical	40	60	24
5	В	Maths	Practical	40	60	24
4	A	Networking	Lab Work	100	80	80
15	С	Networking	Lab Work	100	80	80
10	В	Networking	Project	100	80	80
2	A	Programming	Project 1	10	50	5
7	В	Programming	Project 1	10	50	5
12	С	Programming	Project 1	10	50	5
3	A	Programming	Project 2	30	60	18
8	В	Programming	Project 2	30	60	18
13	С	Programming	Project 2	30	60	18
9	В	Programming	Project 3	60	75	45
14	С	Programming	Project 3	60	75	45



	Student	Module	Deliverable	Weight	Mark	W_Mark	M_Mark
1	A	Maths	Exam	60	80	48	72
6	В	Maths	Exam	60	80	48	72
11	С	Maths	Exam	60	80	48	48
0	A	Maths	Practical	40	60	24	72
5	В	Maths	Practical	40	60	24	72
4	A	Networking	Lab Work	100	80	80	80
15	С	Networking	Lab Work	100	8 0-	80	80
10	В	Networking	Project	100	80	80	80
2	A	Programming	Project 1	10	50	5	23
7_	В	Programming	Project 1	10	50	5	68
12	С	Programming	Project 1	10	50	5	68
3	A	Programming	Project 2	30	60	18	23
8	В	Programming	Project 2	30	60	18	68
13	С	Programming	Project 2	30	60	18	68
9	В	Programming	Project 3	60	75	45	68
14	С	Programming	Project 3	60	75	45	68
	6 11 0 5 4 15 10 2 7 12 3 8 13 9	1 A 6 B 11 C 0 A 5 B 4 A 15 C 10 B 2 A 7 B 12 C 3 A	6 B Maths 11 C Maths 0 A Maths 5 B Maths 4 A Networking 15 C Networking 10 B Networking 2 A Programming 7 B Programming 12 C Programming 3 A Programming 8 B Programming 9 B Programming	1 A Maths Exam 6 B Maths Exam 11 C Maths Exam 0 A Maths Practical 5 B Maths Practical 4 A Networking Lab Work 15 C Networking Lab Work 10 B Networking Project 2 A Programming Project 1 7 B Programming Project 1 12 C Programming Project 1 3 A Programming Project 2 8 B Programming Project 2 9 B Programming Project 3	1 A Maths Exam 60 6 B Maths Exam 60 11 C Maths Exam 60 0 A Maths Exam 60 0 A Maths Practical 40 5 B Maths Practical 40 4 A Networking Lab Work 100 15 C Networking Project 100 2 A Programming Project 1 10 7 B Programming Project 1 10 12 C Programming Project 2 30 3 A Programming Project 2 30 4 Programming Project 3 30 30 9 B Programming Project 3 60	1 A Maths Exam 60 80 6 B Maths Exam 60 80 11 C Maths Exam 60 80 0 A Maths Practical 40 60 5 B Maths Practical 40 60 4 A Networking Lab Work 100 80 15 C Networking Project 100 80 2 A Programming Project 10 50 7 B Programming Project 1 10 50 12 C Programming Project 2 30 60 3 A Programming Project 2 30 60 8 B Programming Project 2 30 60 9 B Programming Project 3 60 75	1 A Maths Exam 60 80 48 6 B Maths Exam 60 80 48 11 C Maths Exam 60 80 48 0 A Maths Practical 40 60 24 5 B Maths Practical 40 60 24 4 A Networking Lab Work 100 80 80 15 C Networking Lab Work 100 80 80 10 B Networking Project 100 80 80 2 A Programming Project 100 80 80 2 A Programming Project 100 80 80 3 A Programming Project 100 50 5 3 A Programming Project 2 30 60 18 3 B Programmin

The transform broadcasts the result for each group over every row in that group.

Dataset Terminology / Notation



- A labeled dataset consists of m rows \times (n+1) columns / variables.
- Use bold to represent vectors and matrices.
- Use superscript in parenthesis to indicate particular observation / instance/ case / row