

Assignment: 1

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SP-21-110

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Subject: Info Security

02	03	01	01
01	02	03	01
01	01	02	03
03	01	01	02

x

87	P2	4D	97
6E	4C	90	6C
46	E7	40	C3
A6	8C	08	95

$$(02 \times 87) \oplus (03 \times 6E) \oplus (01 \times 46) \oplus (01 \times A6)$$

$$02 = 0000010 = u$$

$$87 = 10000111 = u^7 + u^2 + u + 1$$

$$\begin{aligned}(02 \times 87) &= u(u^7 + u^2 + u + 1) = u^8 + u^3 + u^2 + u \\&= u^4 + u^3 + u^2 + u + u^3 + u^2 + u \\&= u^4 + u^2 + 1 \\&= 00010101\end{aligned}$$

$$03 = 00000011, \quad 6E = 01101110$$

$$46 = 01000110, \quad 01 = 00000001$$

$$\begin{aligned}03 \times 6E &= (u+1) \times (u^6 + u^5 + u^3 + u^2 + u) \\&= u^7 + u^6 + u^4 + u^3 + u^2 + u^6 + u^5 + u^3 + u^2 + u \\&= u^7 + u^5 + u^4 + u \\&= 10110010\end{aligned}$$

$$\begin{aligned}01 \times 46 &= 1 \times (u^6 + u^2 + u) \\&= u^6 + u^2 + u \\&= 01001110 \\&= 01000110\end{aligned}$$

$$01 \times A6$$

$$01 = 0000001 = 1$$

$$A6 = 10100110 = x^7 + x^5 + x^2 + x$$

$$01 \times A6 = 10100110$$

$$0 \ 0 \ 0 \ 1 \ 0 \ 1 \ 0 \ 1$$

$$1 \ 0 \ 1 \ 1 \ 0 \ 0 \ 1 \ 0$$

$$0 \ 1 \ 0 \ 0 \ 0 \ 1 \ 1 \ 0$$

$$1 \ 0 \ 1 \ 0 \ 0 \ 1 \ 1 \ 0$$

$$0 \ 1 \ 0 \ 0 \ 0 \ 1 \ 1 \ 1$$

$$47$$

$$02 = 0000 \ 0000 = x$$

$$F2 = 11110010 = x^7 + x^6 + x^5 + x^4 + x$$

$$02 \times F2 = x(x^7 + x^6 + x^5 + x^4 + x)$$

$$= x^8 + x^7 + x^6 + x^5 + x^2$$

$$= x + x^4 + x^3 + 1 + x^7 + x^6 + x^5 + x^2$$

$$= 1111111$$

$$03 = 00000011 = x+1$$

$$4C = 01001100 = x^6 + x^3 + x^2$$

$$03 \times 4C = 01001100$$

$$01 = 00000001 = 1$$

$$E7 = 11110011 = x^7 + x^6 + x^5 + x^2 + x + 1$$

$$01 \times E7 = 11110011$$

$$01 = 00000001$$

$$8C = 10001100$$

$$01 \times 8C = 10001100$$

1 1 1 1 1 1 1 1
 1 1 0 1 0 1 0 0
 1 1 1 0 0 1 1 1
 1 0 0 0 1 1 0 0
 0 1 0 0 0 0 0 0
 40

$$(02 \times 4D) \oplus (03 \times 90) \oplus (01 \times 4A) \oplus (01 \times D8)$$

$$02 = 00000010 = u$$

$$4D = 01001101 = u^6 + u^3 + u^2 + 1$$

$$02 \times 4D = u^7 + u^4 + u^3 + u$$

$$= 10011010$$

$$03 = 00000011 = u + 1$$

$$90 = 10010000 = u^7 + u^4$$

$$03 \times 90 = u^8 + u^5 + u^2 + u^4$$

$$= u^4 + u^3 + u + 1 + u^5 + u^7 + u^4$$

$$= 10101011$$

$$01 = 00000001 = 1$$

$$4A = 01001010 = u^6 + u^3 + u$$

$$01 \times 4A = 01001010 = u$$

$$01 = 00000001$$

$$D8 = 11011000$$

$$01 \times D8 = 11011000$$

$$= u^7 + u^6 + u^4 + u$$

1	0	0	1	1	0	1	0
1	0	1	0	1	0	1	1
0	1	0	0	1	0	1	0
1	1	0	1	1	0	0	0
1	0	1	0	0	0	1	1

A3

$$(02 \times 97) \oplus (03 \times EC) \oplus (01 \times C3) \oplus (01 \times 95)$$

$$02 = 00000010 = u$$

$$97 = 10010111 = u^7 + u^4 + u^2 + u + 1$$

$$= u^6 + u^5 + u^3 + u^2 + u$$

$$= u^4 + u^5 + u^2 + 1 + u^5 + u^3 + u^2 + u$$

$$= u^5 + u^4 + u^2 + 1$$

$$= 00110101$$

$$01 = 00000001$$

$$03 = 11000011$$

$$01 \times C3 = 11000011$$

$$01 = 00000001$$

$$95 = 10010101$$

$$01 \times 95 = 10010101$$

$$00110101$$

$$00101111$$

$$11010011$$

$$10000101$$

$$01001100$$

$$(01 \times 87) \oplus (02 \times 6E) \oplus (03 \times 46) \oplus (01 \times A6)$$

$$\sqrt{87} = 10000111$$

$$02 = 00000010$$

$$6E = 01101110$$

$$02 \times 6E = (u)(u^6 + u^5 + u^3 + u^2 + u)$$

$$= u^7 + u^6 + u^4 + u^3 + u^2$$

$$\boxed{= 11011100}$$

$$03 = 00000011$$

$$46 = 01000110$$

$$(03 \times 46) = (u+1)(u^6 + u^2 + u)$$

$$= u^7 + u^3 + u^2 + u + u$$

$$\boxed{= 11001010}$$

$$\boxed{A6 = 10100110}$$

$$10000111$$

$$11011100$$

$$11001010$$

$$10100110$$

$$00110111$$

$$3 \quad 7$$

$$(01 \times 4D) \oplus (02 \times 90) \oplus (03 \times 4A) \oplus (01 \times D8)$$

$$\boxed{4D = 01001101}$$

$$02 = 00000010 = u$$

$$90 = 10010000 = u^7 + u^4$$

$$20 \times 90 = u^8 + u^5$$

$$20 \times 90 = u^4 + u^3 + u + 1 + u^5$$

$$\boxed{= 00111011}$$

1/202

$$08 = 11010000$$

$$\begin{array}{cccccccc}
 0 & 1 & 0 & 0 & 1 & 1 & 0 & 1 \\
 0 & 0 & 1 & 1 & 1 & 0 & 1 & 1 \\
 1 & 1 & 0 & 1 & 1 & 1 & 1 & 0 \\
 1 & 1 & 0 & 1 & 1 & 0 & 0 & 0 \\
 \hline
 0 & 1 & 1 & 1 & 0 & 0 & 0 & 0 \\
 \hline
 & & & 7 & & & & 0
 \end{array}$$

$$(01 \times 97) \oplus (02 \times EC) \oplus (03 \times C3) + (01 \times 95)$$

$$97 = 1001011$$

$$02 = n -$$

$$\begin{aligned}
 EC &= 11101100 = n^7 + n^6 + n^5 + n^3 + n^2 \\
 &= n^8 + n^7 + n^6 + n^4 + n^3 \\
 &= n^8 + n^7 + n^6 + n^4 + n^3 \\
 &= n^8 + n^7 + n^6 + n^4 + n^3 \\
 &= n^8 + n^7 + n^6 + n^4 + n^3
 \end{aligned}$$

$$1 = 11000011$$

$$03 = n + 1$$

$$C3 = 11000011 = n^7 + n^6 + n^4 + n^3 + n^2 + n + 1$$

$$= n^8 + n^7 + n^6 + n^4 + n^3 + n^2 + n + 1$$

$$03 \times C3 = n^8 + n^7 + n^6 + n^4 + n^3 + n^2 + n + 1$$

$$= n^8 + n^7 + n^6 + n^4 + n^3 + n^2 + n + 1$$

$$= n^8 + n^7 + n^6 + n^4 + n^3 + n^2 + n + 1$$

$$= 01011110$$

$$95 = 10010101$$

1	0	0	1	0	1	1	1
1	1	0	0	0	0	1	1
0	1	0	1	1	1	1	0
1	0	0	1	0	1	0	1
1	0	0	1	1	1	1	1

9

P

$$(01 \times B2) \oplus (01 \times 6E) \oplus (02 \times 46) \oplus (03 \times A6)$$

$$B2 = 10000111$$

$$6E = 01101110$$

$$02 = u$$

$$46 = 01000110 = u^6 + u^2 + u$$

$$= u^7 + u^3 + u^2$$

$$= 10001100$$

$$03 = u+1$$

$$A6 = 10100110 = u^7 + u^5 + u^2 + u$$

$$03 \times A6 = u^8 + u^6 + u^3 + u^7 + u^5 + u^2 + u$$

$$= u^4 + u^3 + u + 1 + u^6 + u^3 + u^7 + u^5 + u^2$$

$$= 11110111$$

1	0	0	0	0	1	1	1
0	1	1	0	1	1	1	0
1	0	0	0	1	1	0	0
1	1	1	1	0	1	1	1
1	0	0	1	0	1	0	1

9

2

$$(01 \times F2) \oplus (01 \times 4C) \oplus (02 \times E7) \oplus (03 \times 8C)$$

1/202

$$F2 = 11110010$$

$$4C = 01001100$$

$$\begin{aligned} 02 \times E7 &= u(u^7 + u^6 + u^5 + u^4 + u^3 + u^2 + u + 1) \\ &= u^8 + u^7 + u^6 + u^5 + u^4 + u^3 + u^2 + u + 1 \\ &= 11010101 \\ &= \boxed{11010101} \end{aligned}$$

$$03 = u + 1$$

$$\begin{aligned} 8C &= 10001100 = u^7 + u^3 + u^2 \\ (03 \times 8C) &= (u+1)(u^7 + u^3 + u^2) \\ &= u^8 + u^4 + u^3 + u^7 + u^2 + u + 1 \\ &= \boxed{21000111} \end{aligned}$$

$$11110010$$

$$01001100$$

$$11010101$$

$$10001100$$

$$11100100$$

E4

$$(01 \times 4D) \oplus (01 \times 90) \oplus (02 \times 4A) \oplus (03 \times D8)$$

$$4D = 01001101$$

$$90 = 10010000$$

$$02 = u$$

$$\begin{aligned} 4A &= 01001010 = u^6 + u^3 + u \\ &= u^7 + u^4 + u^2 \end{aligned}$$

$$210010100$$

$$03 = u + 1$$

$$D8 = 11011000$$

$$= u^8 + u^7 + u^6 + u^5 + u^4 + u^3 + u^2 + u + 1$$

$$(03 \times 87) \oplus (01 \times 6E) \oplus (04 \times 46) \oplus (02 \times 46)$$

$$03 = u+1$$

$$\begin{aligned} 87 &= 10000111 = u^7 + u^2 + u + 1 \\ &= \cancel{u^8} + \cancel{u^7} + \cancel{u^6} + \cancel{u^5} + \cancel{u^4} + \cancel{u^3} + \cancel{u^2} + u + 1 \\ &= \cancel{u^8} + \cancel{u^7} + \cancel{u^6} + \cancel{u^5} + \cancel{u^4} + \cancel{u^3} + \cancel{u^2} + u + 1 \\ &= u^7 + u^4 + u \end{aligned}$$

$$\boxed{12 = 10010010}$$

$$02 = u$$

$$\begin{aligned} A6 &= 10100110 = u^7 + u^5 + u^2 \\ &= \cancel{u^8} + \cancel{u^7} + \cancel{u^6} + \cancel{u^5} + \cancel{u^4} + \cancel{u^3} + \cancel{u^2} + u + 1 \\ &= \cancel{u^8} + \cancel{u^7} + \cancel{u^6} + \cancel{u^5} + \cancel{u^4} + \cancel{u^3} + \cancel{u^2} + u + 1 \\ &= u^6 + u^4 + u^2 + u + 1 \end{aligned}$$

$$\boxed{1 = 01010111}$$

$$\boxed{46 = 01000110}$$

$$\boxed{A6 = 10100110}$$

$$\begin{array}{ccccccc} 1 & 0 & 0 & 1 & 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 & 0 & 1 & 1 & 1 \\ 0 & 1 & 0 & 0 & 0 & 1 & 1 & 0 \\ 1 & 0 & 1 & 0 & 0 & 1 & 1 & 0 \\ \hline 0 & 0 & 1 & 0 & 0 & 1 & 0 & 1 \\ \hline & & 2 & & 5 & & & \end{array}$$

$$(03 \times F2) \oplus (01 \times 4C) \oplus (01 \times E7) \oplus (02 \times 8C)$$

$$03 = u+1$$

$$\begin{aligned} F2 &= 11110010 \rightarrow u^7 + u^6 + u^5 + u^4 + u \\ &= \cancel{u^8} + \cancel{u^7} + \cancel{u^6} + \cancel{u^5} + \cancel{u^4} + \cancel{u^3} + \cancel{u^2} + \cancel{u^1} + u \\ &= \cancel{u^8} + \cancel{u^7} + \cancel{u^6} + \cancel{u^5} + \cancel{u^4} + \cancel{u^3} + \cancel{u^2} + \cancel{u^1} + u \\ &= u^3 + u^2 + 1 \end{aligned}$$

$$\boxed{12 = 00001101}$$

1/202

$$02 = u$$

$$BC = 10001100 = u^7 + u^3 + u^2$$

$$= u^7 + u^4 + u^3$$

$$= \cancel{u^7} + \cancel{u^4} + \cancel{u^3} + \cancel{u^2} + \cancel{u^1} + \cancel{u^0}$$

$$= u + 1$$

$$D = 00000011$$

$$14C = 01001100$$

$$E7 = 11100111$$

$$00001101$$

$$00000011$$

$$01001100$$

$$11100111$$

$$10100101$$

$$A \quad \quad \quad J$$

$$(03 \times 4D) \oplus (01 \times 90) \oplus (01 \times 4A) \oplus (02 \times D8)$$

$$03 = u + 1$$

$$4D = 01001101 = u^6 + u^3 + u^2 + 1$$

$$= u^7 + u^4 + \cancel{u^3} + u + u^6 + \cancel{u^2} + 1$$

$$= u^7 + u^6 + u^4 + u^2 + u + 1$$

$$D = 11010111$$

$$02 = u$$

$$D8 = 11011000 = u^7 + u^6 + u^4 + u^3$$

$$= u^8 + u^7 + u^5 + u^4$$

$$= \cancel{u^8} + \cancel{u^7} + \cancel{u^6} + \cancel{u^5} + \cancel{u^4} + \cancel{u^3} + \cancel{u^2} + \cancel{u^1} + \cancel{u^0}$$

$$= u^7 + u^5 + u^3 + u + 1$$

$$D = 10101011$$

$$9A = 10010000$$

$$4A = 01001010$$

$$\begin{array}{cccccccc} 1 & 1 & 0 & 1 & 0 & 1 & 1 & 1 \\ 1 & 0 & 1 & 0 & 1 & 0 & 1 & 1 \\ 1 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 1 & 0 & 1 & 0 \\ \hline 1 & 1 & 1 & 1 & 0 & 1 & 0 & 0 \end{array}$$

F Y

$$(03 \times 97) \oplus (01 \times EC) \oplus (01 \times C3) \oplus (01 \times 95)$$

$$03 = u+1$$

$$97 = 10010111 = u^7 + u^4 + u^2 + u + 1$$

$$= u^8 + u^5 + u^3 + u^2 + u + 1 + u^7 + u^4 + u^2 + u + 1$$

$$= u^8 + u^5 + u^3 + u^2 + u + 1 + u^7 + u^4 + u^2 + u + 1$$

$$= u^7 + u^5 + u$$

$$2 = 10100010$$

$$02 = u$$

$$95 = 10010101 = u^7 + u^4 + u^2 + 1$$

$$= u^8 + u^5 + u^3 + u + 1$$

$$= u^4 + u^3 + u + 1 + u^5 + u^3 + u + 1$$

$$= u^5 + u^4 + 1$$

$$2 = 00110001$$

$$C3 = 11000011$$

$$EC = 11101100$$

$$\begin{array}{cccccccc} 1 & 0 & 1 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 1 & 1 & 0 & 0 & 0 & 1 \\ 1 & 1 & 0 & 0 & 0 & 0 & 1 & 1 \\ 1 & 1 & 1 & 0 & 1 & 1 & 0 & 0 \\ \hline 1 & 0 & 1 & 1 & 1 & 1 & 0 & 0 \end{array}$$

B C

47	40	A3	4C
37	D4	70	9F
92	E4	3A	42
25	A5	F4	BC