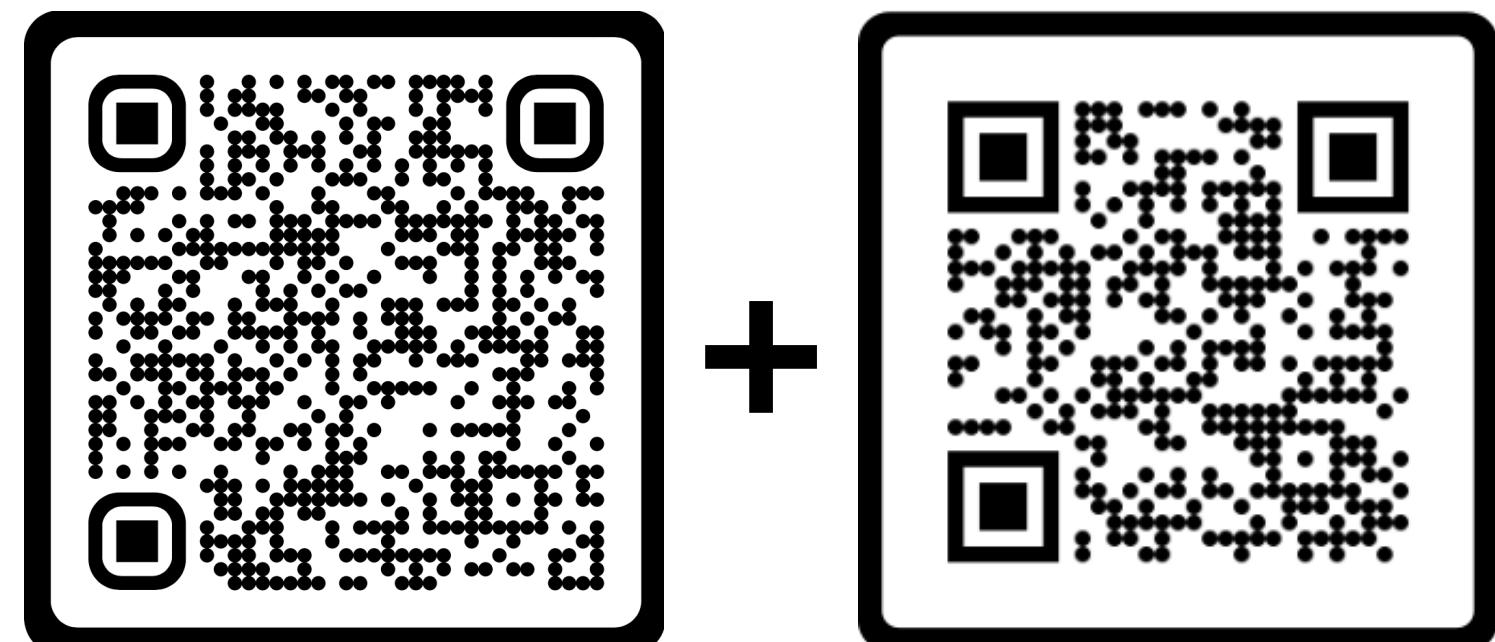


Disaggregated Interventions to Reduce Inequality + Counterfactuals for the Future

**DSGA-1017 Responsible Data Science
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Outline

1. Disaggregated interventions to reduce inequality

- Problem definition
- Causal inference and social categories
- A causal framework for addressing pre-existing inequalities

2. Counterfactuals for the future

- Motivating example
- Forward-looking counterfactuals
- Empirical exploration

Disaggregated Interventions to Reduce Inequality

Three types of algorithmic bias

[Friedman, Nissenbaum 1996], [Stoyanovich, Howe, Jagadish 2020]

- **Pre-existing bias**
 - Originates in society and exists independently of an algorithm
- **Technical bias**
 - Introduced or exacerbated by the technical properties of an algorithm
- **Emergent bias**
 - Arises in the context of an algorithm's use

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Problem definition

The “impact remediation problem”

Formalizing pre-existing bias

1. We observe an existing disparity. We consider it undesired.
2. We have the ability to perform an intervention.
3. We want to decrease the measured disparity.
 1. Gender imbalance in a job applicant pool
 2. Hosting booths at different career fairs
 3. Rebalance our applicant pool

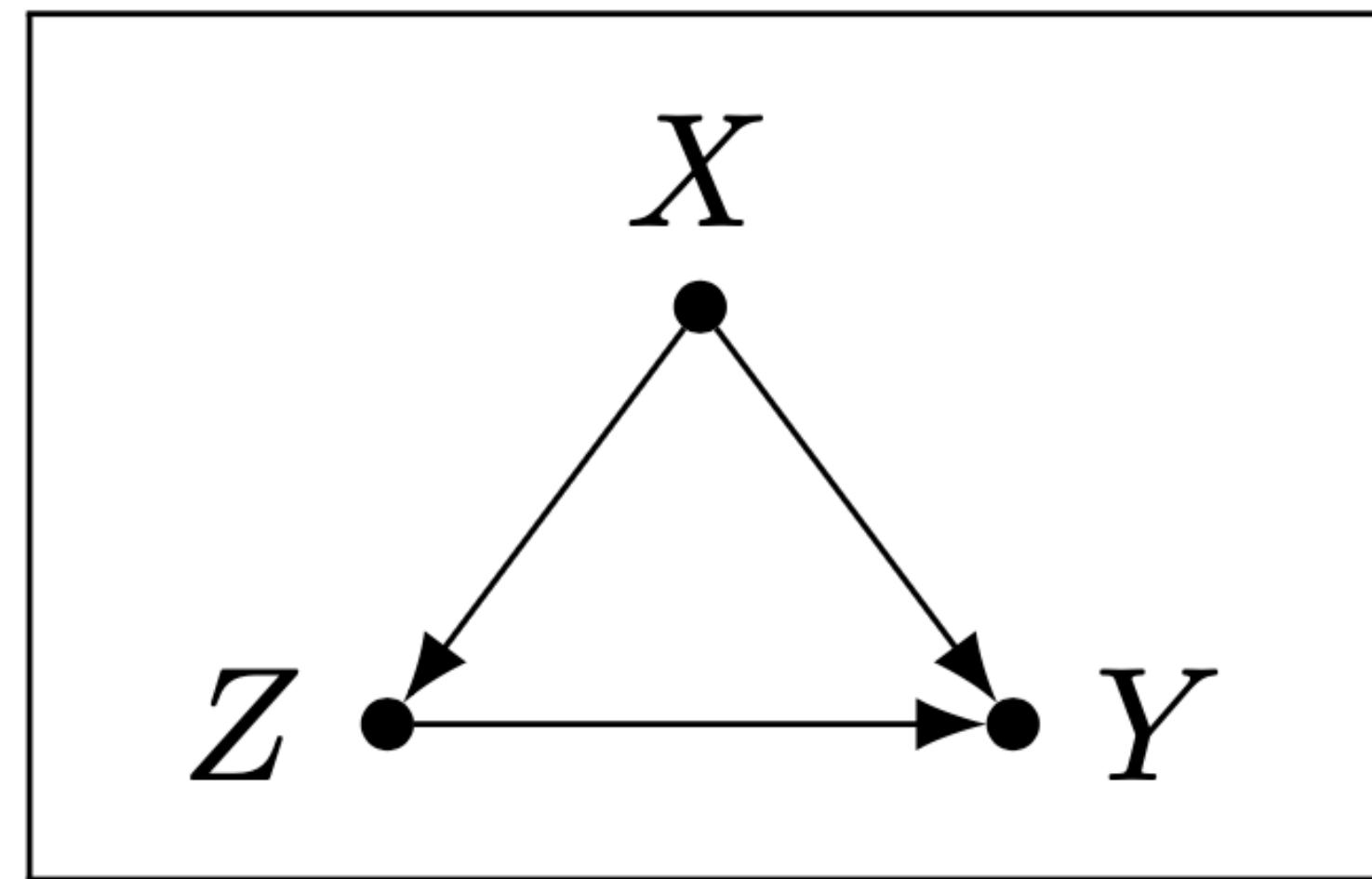
Example:

Causal inference and social categories

Structural causal models (SCMs)

[Pearl 2009], [Peters et al. 2017]

- An SCM is a four-tuple (U, V, F, P_U)
 - U : a set of exogenous background variables
 - V : a set of endogenous observed variables
 - F : a set of functions (structural equations) for each $V_i \in V$
 - P_U : a distribution over the exogenous variables U
- Each SCM entails a directed acyclic graph (DAG)

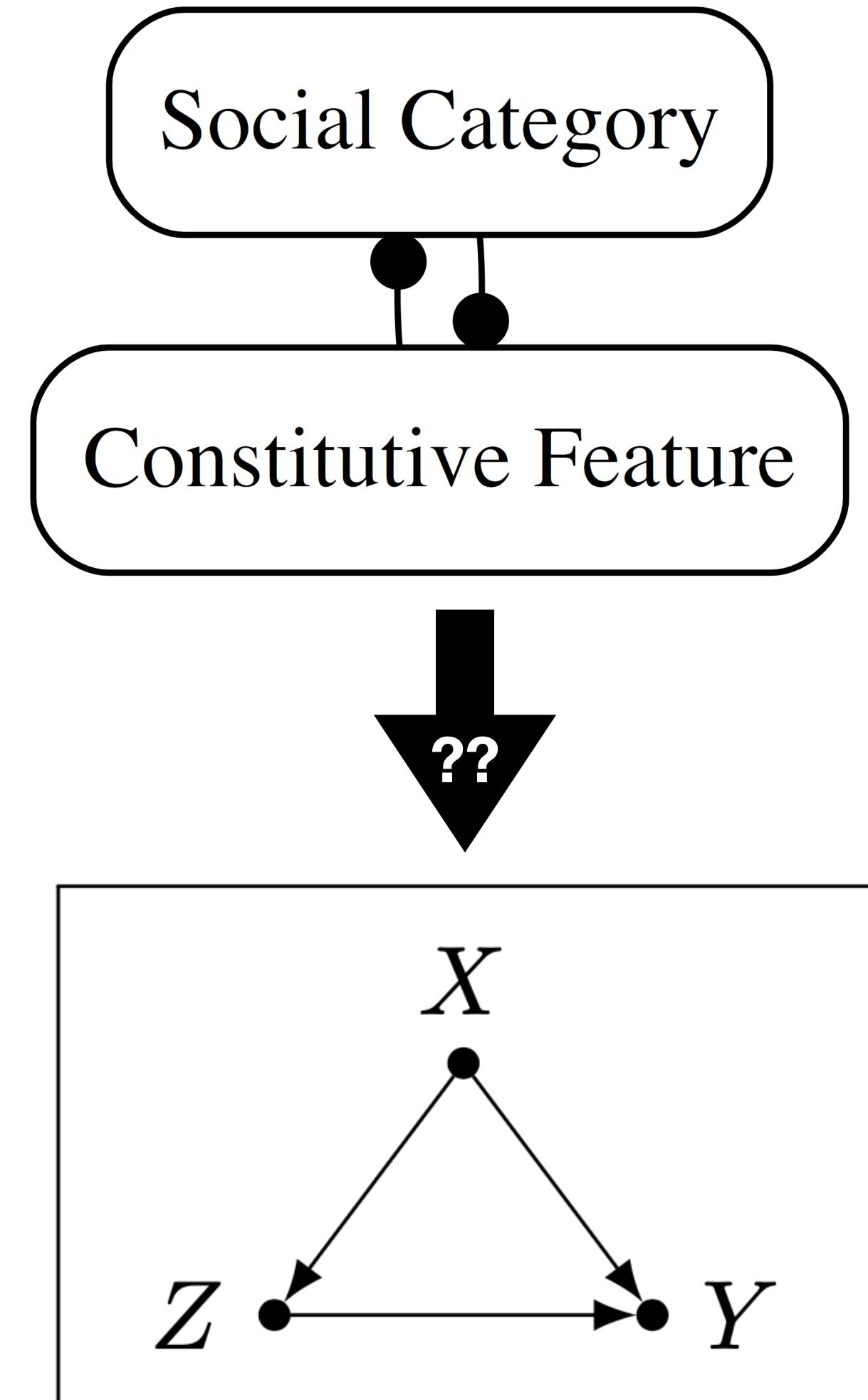


$$\begin{aligned} X &= \epsilon_X \\ Z &= -1 + X + \epsilon_Z \\ Y &= 2 \cdot Z + X + \epsilon_Y \\ \epsilon_X, \epsilon_Y, \epsilon_Z &\sim \mathcal{N}(0,1) \end{aligned}$$

Social categories and constitutive features

[Benthall and Haynes 2019], [Hanna et al. 2020], [Sen and Wasow 2016], [Hu and Kohler-Hausmann 2020], [Jacobs and Wallach 2021], [Kasirzadeh and Smart 2021]

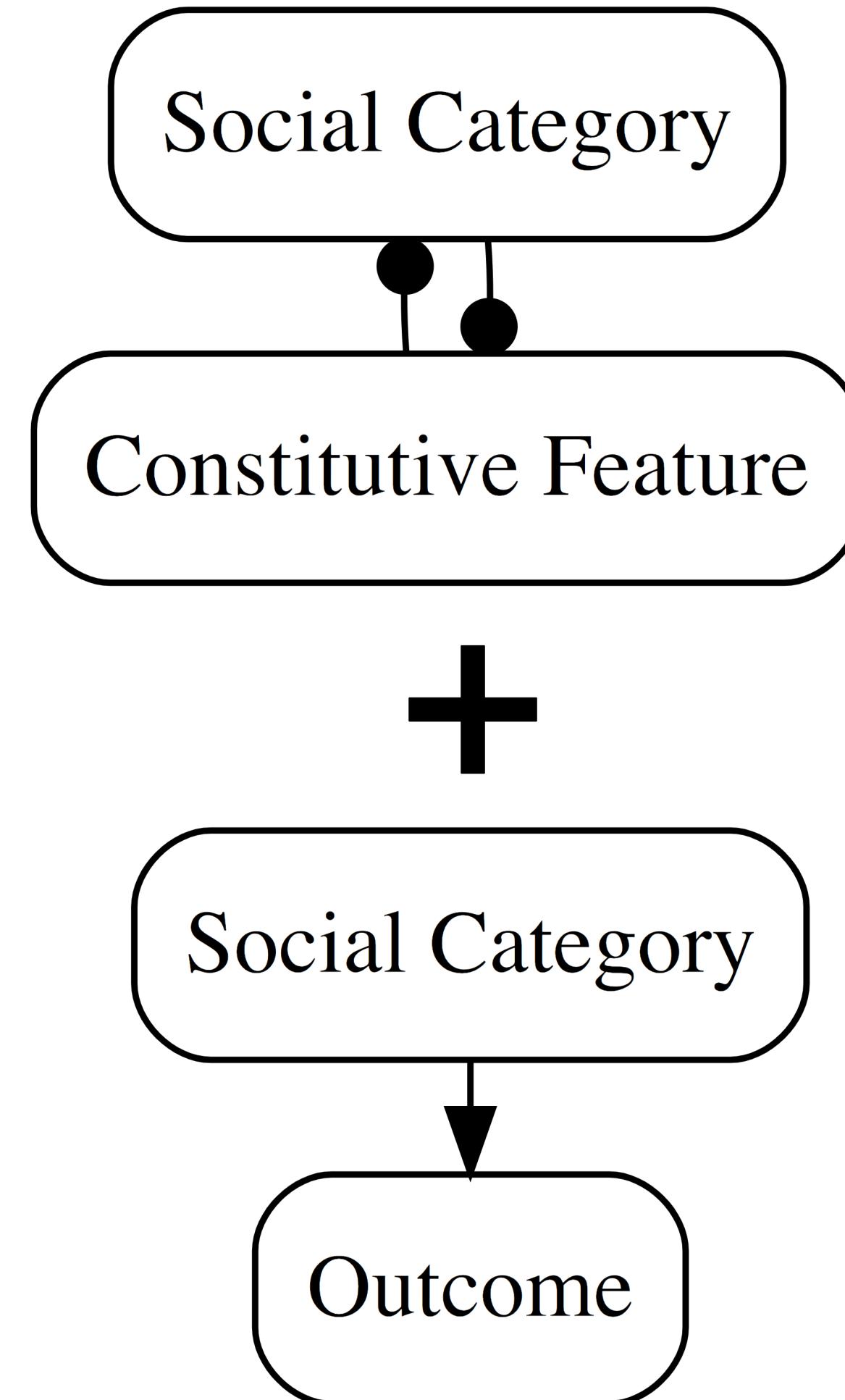
- Inequality involves social categories (e.g. race, gender)
- Two types of features:
 - **Regular feature:** causal, diachronic
 - Unfolding over time via cause-and-effect
 - “If A then B then C...”
 - **Constitutive feature:** a feature that defines a social category
 - Synchronous, definitional [Hu and Kohler-Hausmann 2020]
 - “If A then the definition of B has changed...”
- How to write down a DAG? —> instantaneous constitutive **cycle**
- Examples:
 - Intuition: water + number of hydrogen atoms
 - Racial categorization + socioeconomic history
 - Simple variables (e.g., race + net worth), complex constructs



Interventions on social categories

[Benthall and Haynes 2019], [Hanna et al. 2020], [Sen and Wasow 2016], [Hu and Kohler-Hausmann 2020], [Jacobs and Wallach 2021], [Kasirzadeh and Smart 2021]

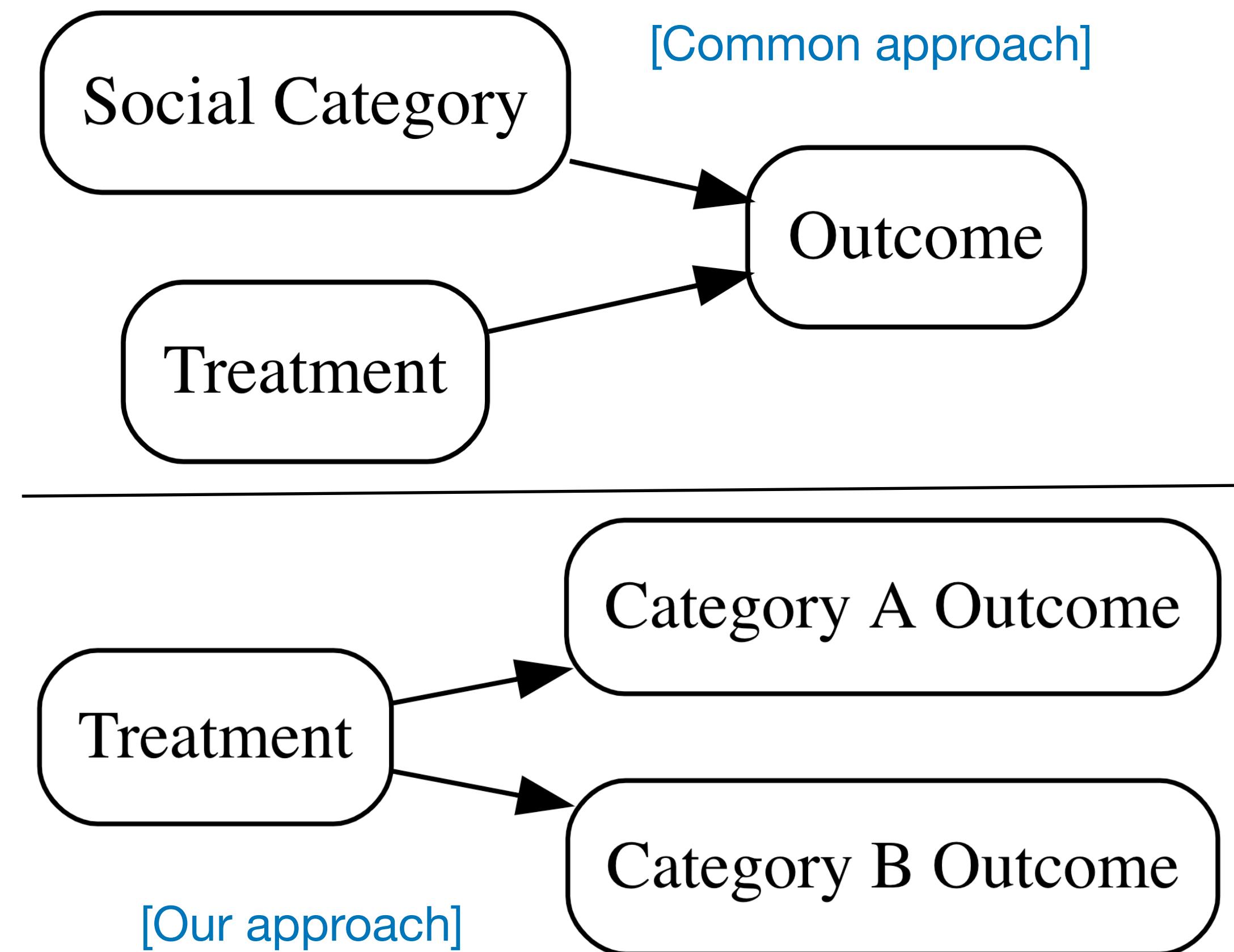
- Questions for interventions on race:
 - Are manipulations defined?
 - Post-treatment bias
 - Is the social category well-defined? Stable?
- **Simplified positions:**
 1. Defining counterfactuals via exposure to a racial cue
 - vs.
 2. Not using causal models with race at all
- **Unavoidable problem:** racial disparities still exist (and other social category disparities)



Social categories in impact remediation

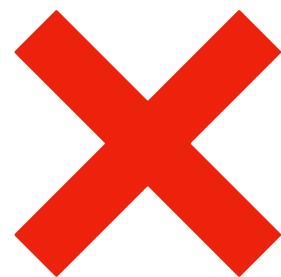
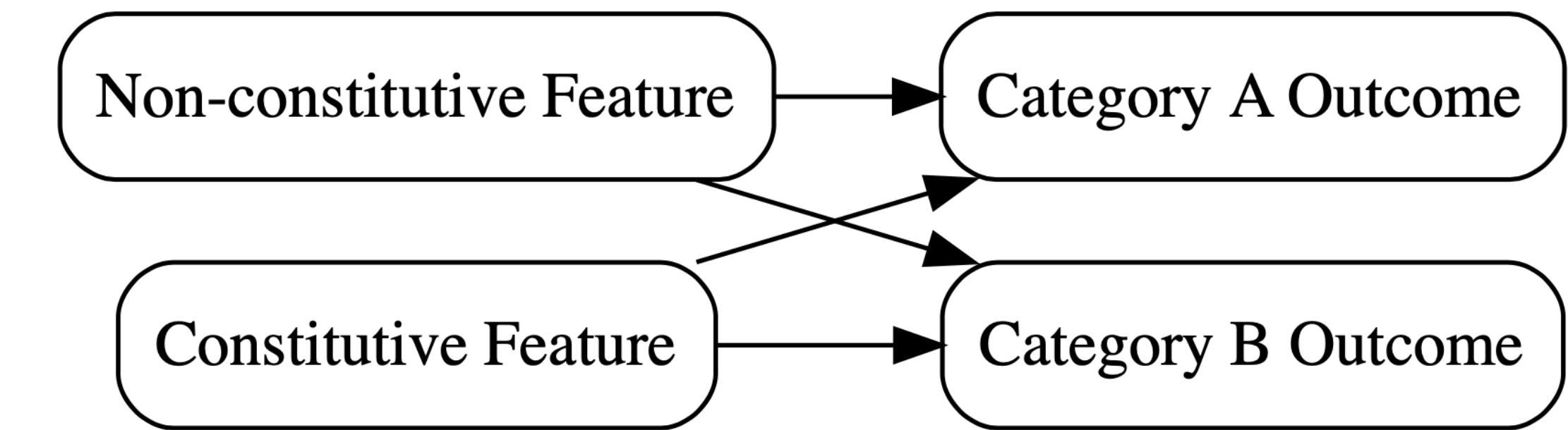
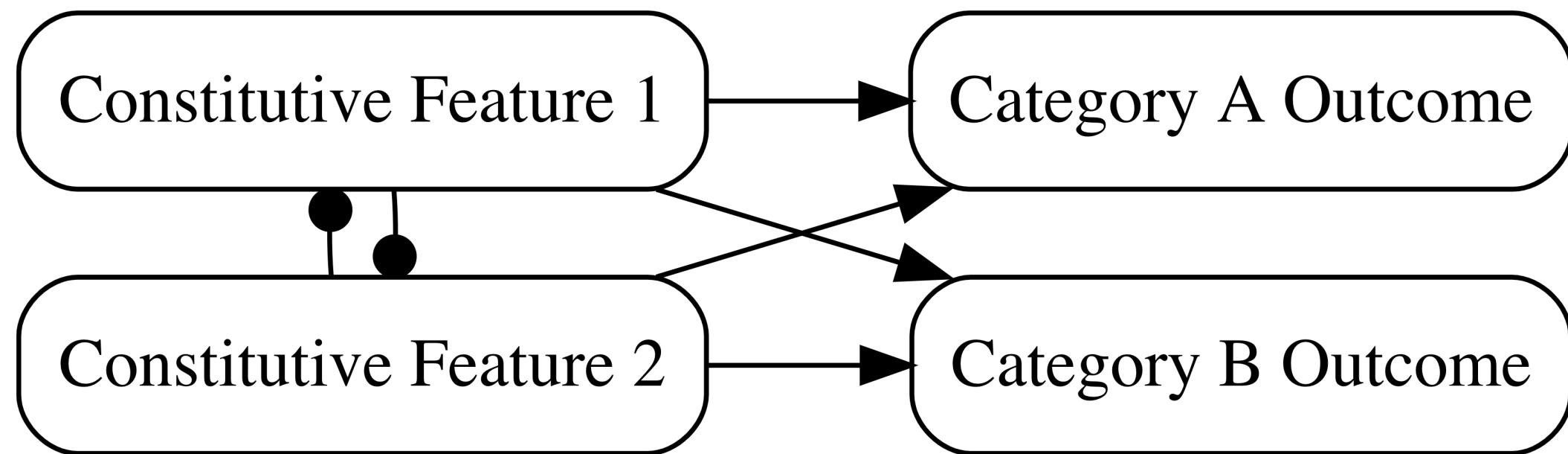
Disaggregation to the rescue!

- **Approach:** measure a disparity across groups of people
 - Racial categories, genders, disabilities
- Our required assumption about social categories:
 - “A social category consists of a group of people” — no shared attributes necessary
- **Takeaway:** we don’t need to resolve the philosophical debate to tackle pre-existing disparities



Social categories in impact remediation

Nuance: one constitutive feature at a time



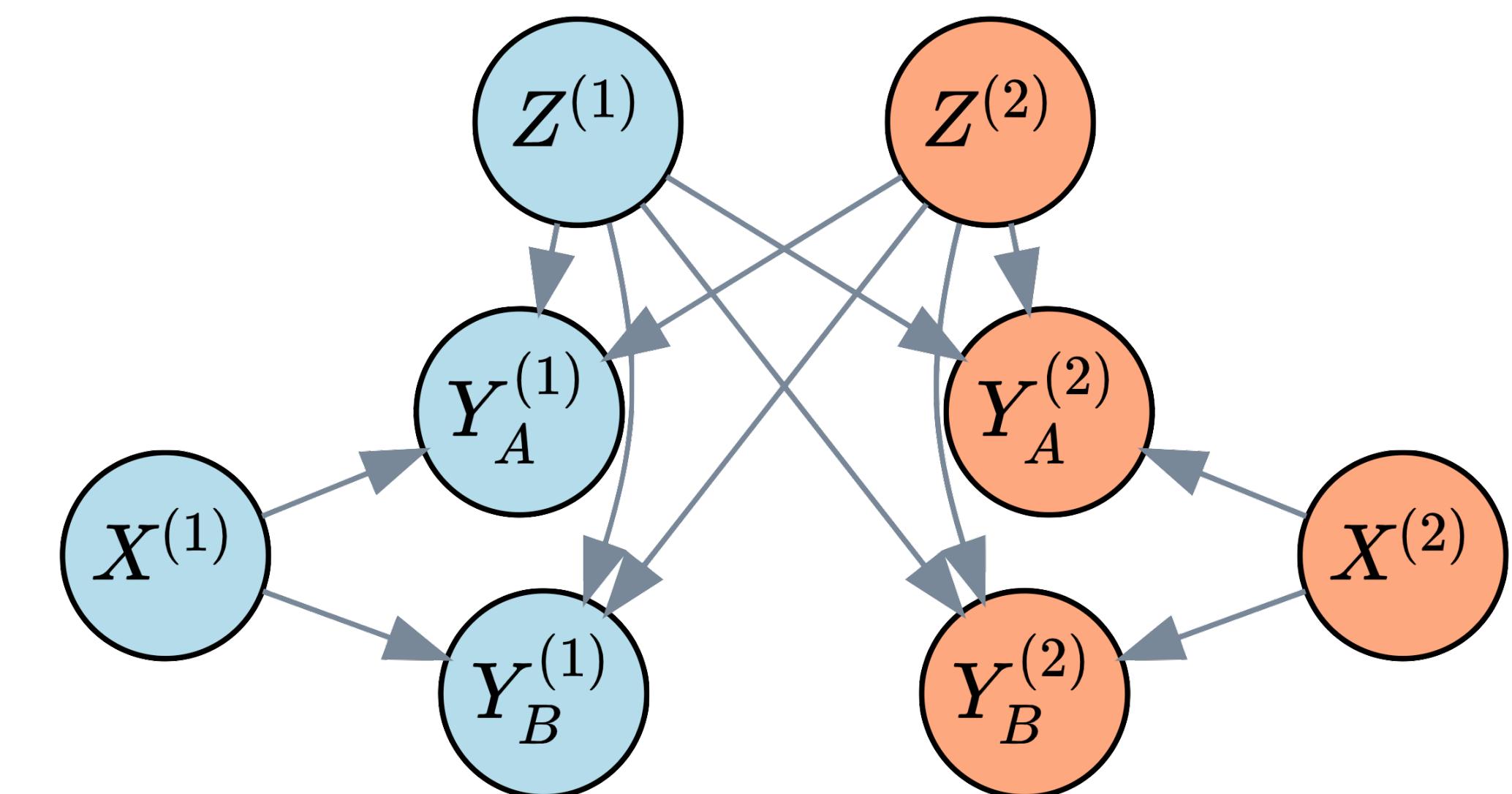
Framework formalization

Impact remediation – toy example

A multi-level, nested intervention structure

Framework	Example
n individuals	425 potential job applicants
m sub-populations on which we can intervene (“intervention sets”)	2 universities
r sub-populations across which we see disparity	Female (A) and Male (B) gender groups
outcome of interest Y, disaggregated across r groups	Y = fraction of students who applied for the job
real-world features X	X = number of career counselors
possible intervention Z	Z = whether or not we hosted a booth at the career fair

Causal graph relating X, Y, Z



extension of [Kusner et al. 2019] + disaggregation

Finding optimal interventions to decrease disparity

Example: outreach in a job applicant pool

- Students in each gender group:

$$n_A^{(1)} = 100, \quad n_A^{(2)} = 75, \quad n_B^{(1)} = 150, \quad n_B^{(2)} = 100$$

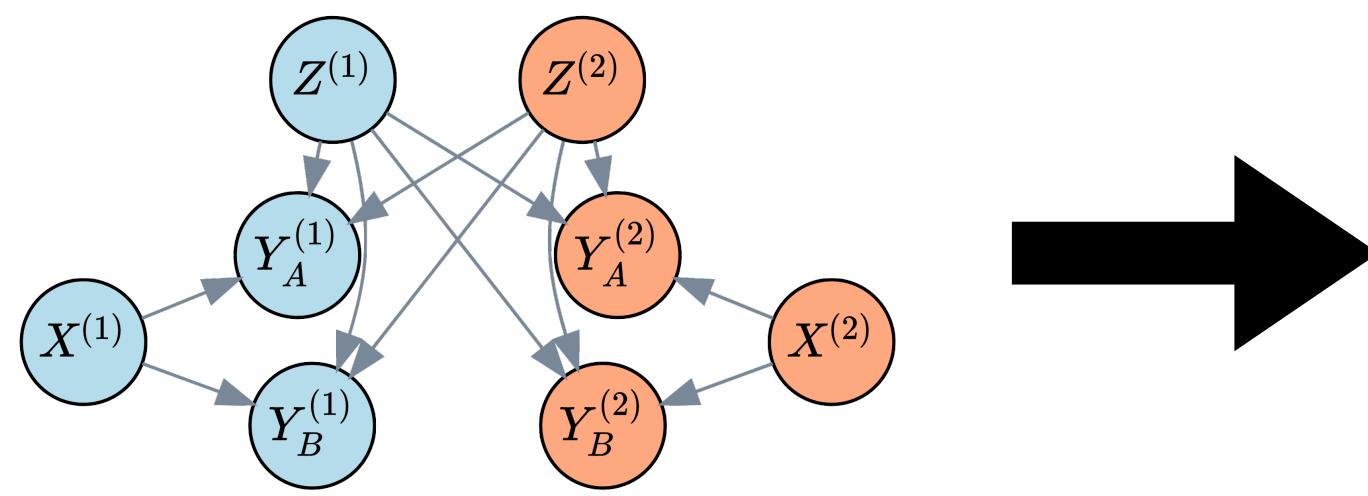
- Observed application rates:

$$(Y_A^{(1)}, Y_B^{(1)}) = (0.10, 0.20) \quad (Y_A^{(2)}, Y_B^{(2)}) = (0.05, 0.10)$$

- Measure of disparity:

$$\delta(z) = \left| \frac{1}{n_A} \sum_{i=1}^2 n_A^{(i)} \mathbb{E}[Y_A^{(i)}(z)] - \frac{1}{n_B} \sum_{i=1}^2 n_B^{(i)} \mathbb{E}[Y_B^{(i)}(z)] \right|$$

- Estimated application rates *after* intervention:



$$\begin{aligned}\mathbb{E}[Y_A^{(1)}([z^{(1)} = 1, z^{(2)} = 0])] &= 0.20 \\ \mathbb{E}[Y_A^{(2)}([z^{(1)} = 1, z^{(2)} = 0])] &= 0.10 \\ \mathbb{E}[Y_B^{(1)}([z^{(1)} = 1, z^{(2)} = 0])] &= 0.30 \\ \mathbb{E}[Y_B^{(2)}([z^{(1)} = 1, z^{(2)} = 0])] &= 0.15\end{aligned}$$

$$\begin{aligned}\mathbb{E}[Y_A^{(1)}([z^{(1)} = 0, z^{(2)} = 1])] &= 0.15 \\ \mathbb{E}[Y_A^{(2)}([z^{(1)} = 0, z^{(2)} = 1])] &= 0.15 \\ \mathbb{E}[Y_B^{(1)}([z^{(1)} = 0, z^{(2)} = 1])] &= 0.25 \\ \mathbb{E}[Y_B^{(2)}([z^{(1)} = 0, z^{(2)} = 1])] &= 0.15\end{aligned}$$

- Disparity after intervention:

$$\delta \approx 0.08$$

no intervention

$$\delta([z^{(1)} = 1, z^{(2)} = 0]) \approx 0.08$$

university one

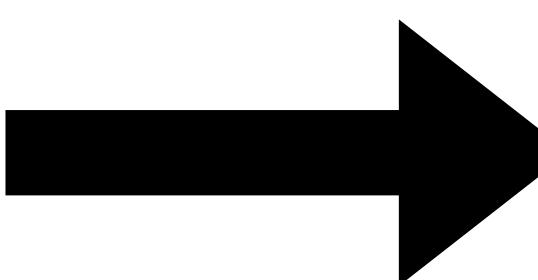
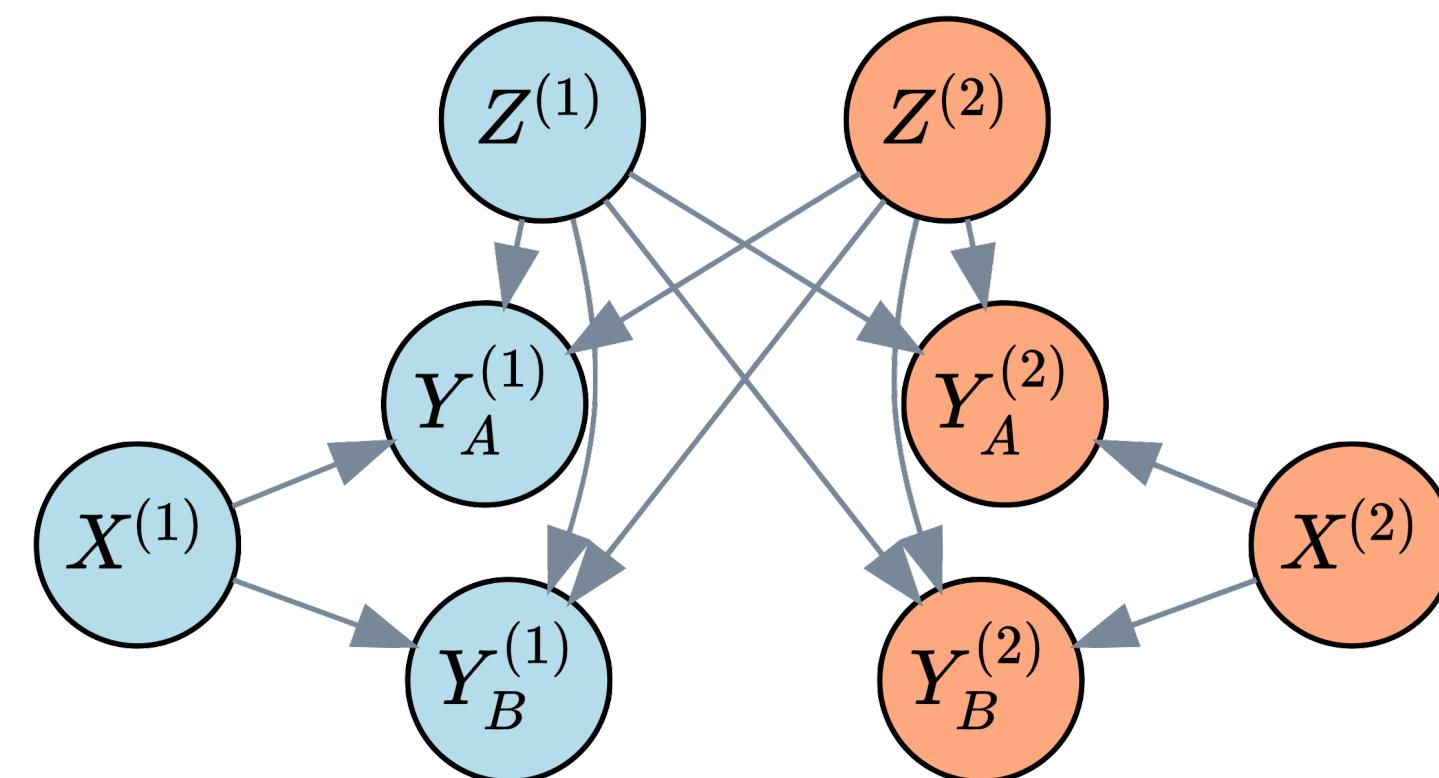
$$\delta([z^{(1)} = 0, z^{(2)} = 1]) = 0.06$$

university two

Impact remediation (IR) overview

Process overview:

1. Social categorization + data collection
2. Fit causal model to estimate intervention effects
3. Define our objective (how to mitigate disparity)
4. Find optimal interventions subject to constraints (budget, etc.)



$$\begin{aligned} & \min_{z \in \{0,1\}^m} \left| \frac{1}{n_A} \sum_{i=1}^2 n_A^{(i)} \mathbb{E}[Y_A^{(i)}(z)] - \frac{1}{n_B} \sum_{i=1}^2 n_B^{(i)} \mathbb{E}[Y_B^{(i)}(z)] \right| \\ & \text{s.t.} \\ & \quad \sum_{i=1}^m z^{(i)} \leq b \end{aligned}$$

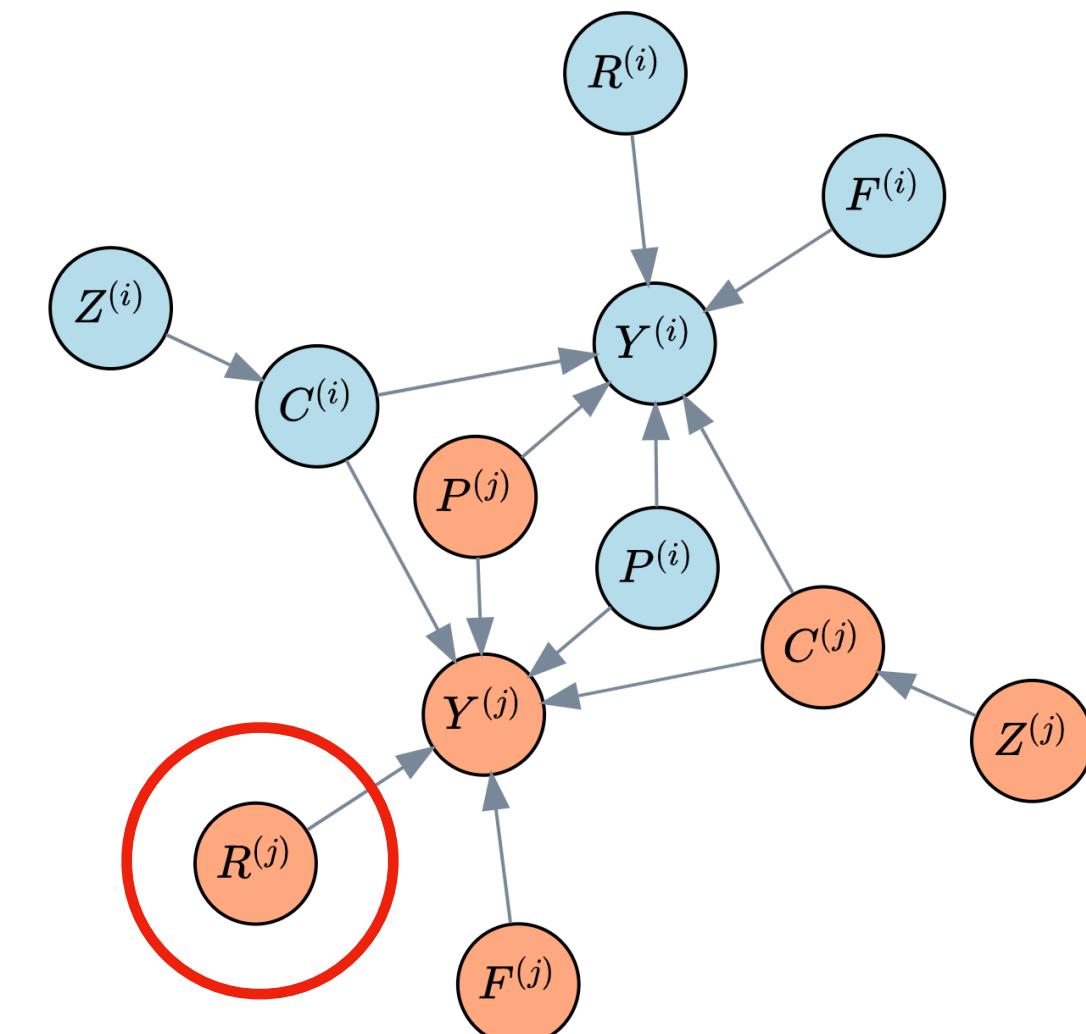
Case study

Stylized NYC schools example

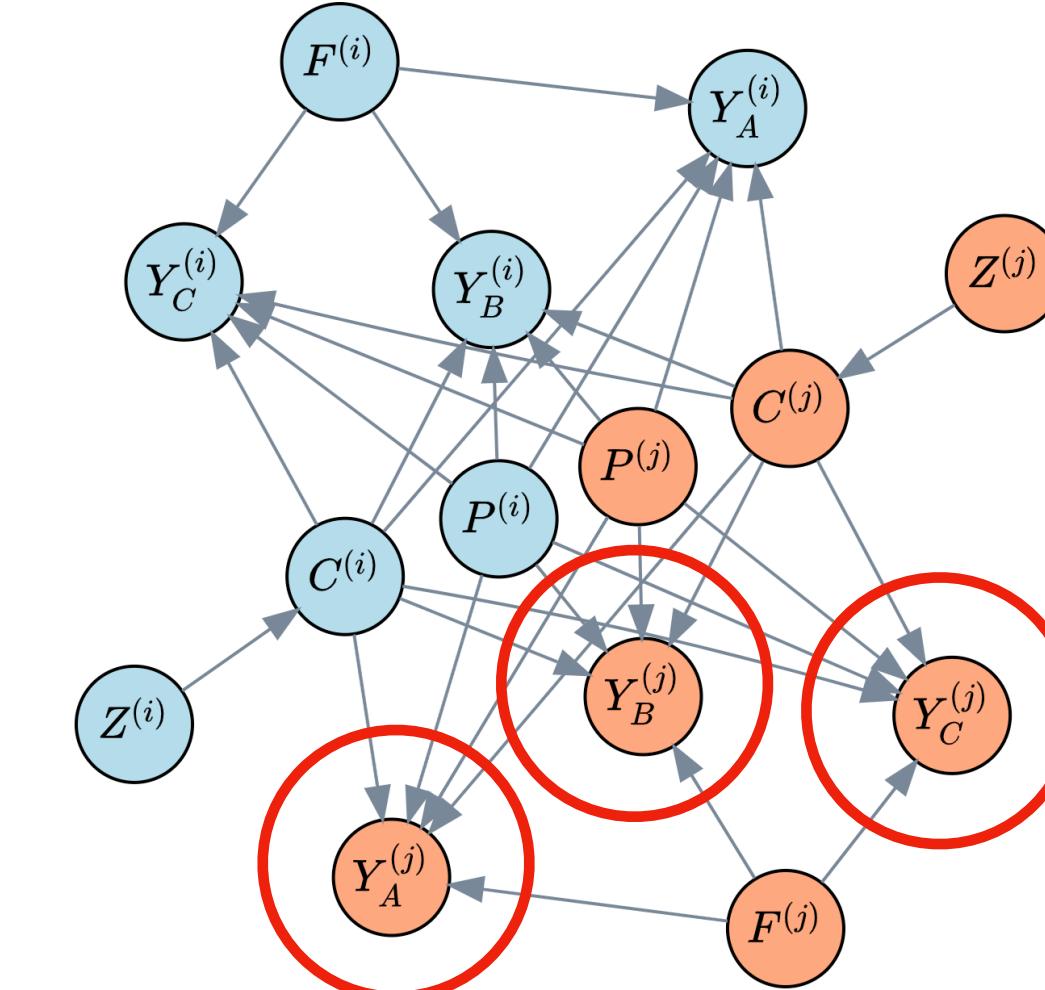
An IR case-study

- An example with realistic data:
 - **Setup:** The US DOE giving funding to NYC public schools to hire Calculus teachers
 - **Goal:** increase college attendance
 - **Subgroups:** racial and gender categories

Causal Fairness
[Kusner et al. 2019]



vs.

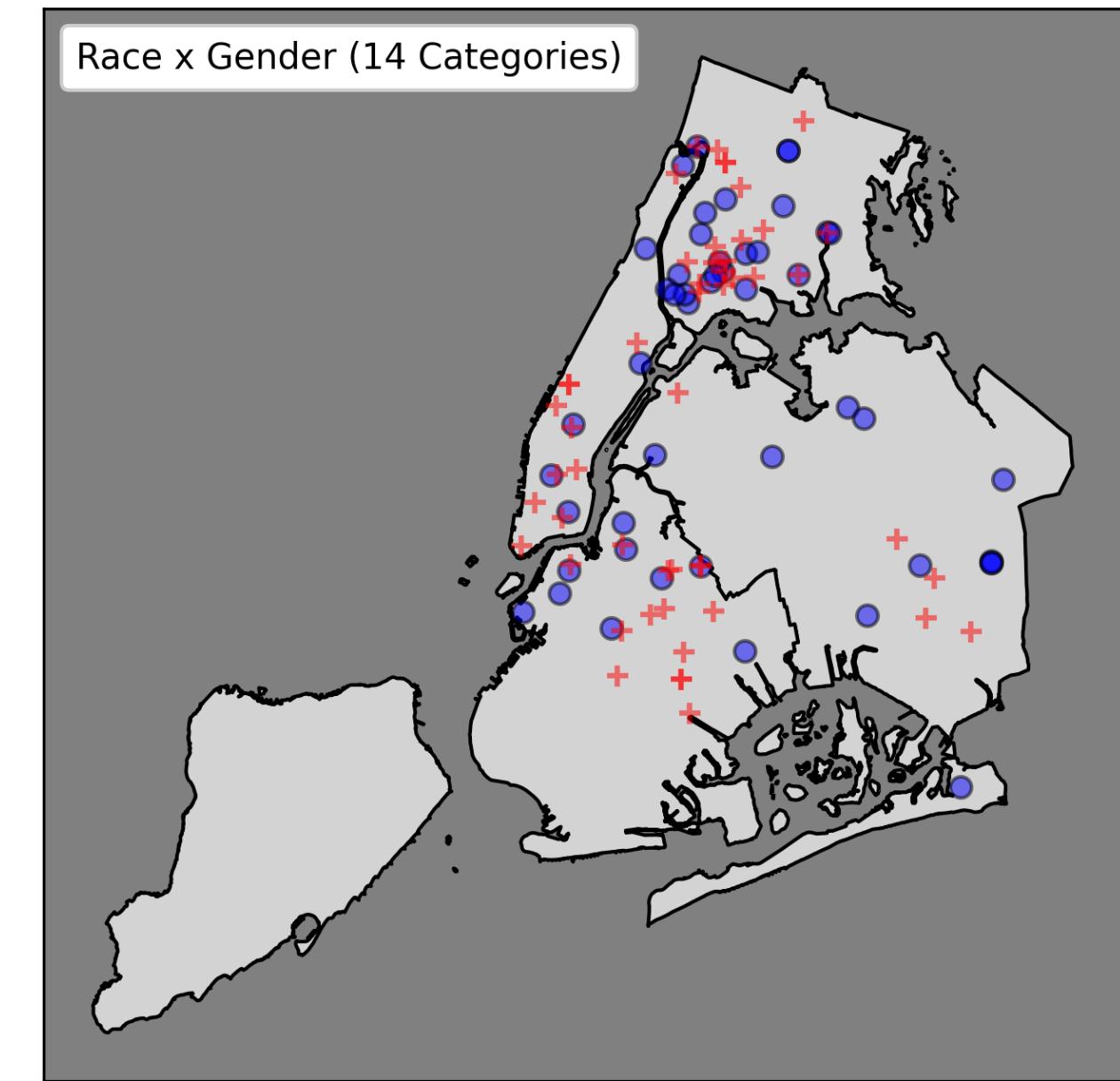
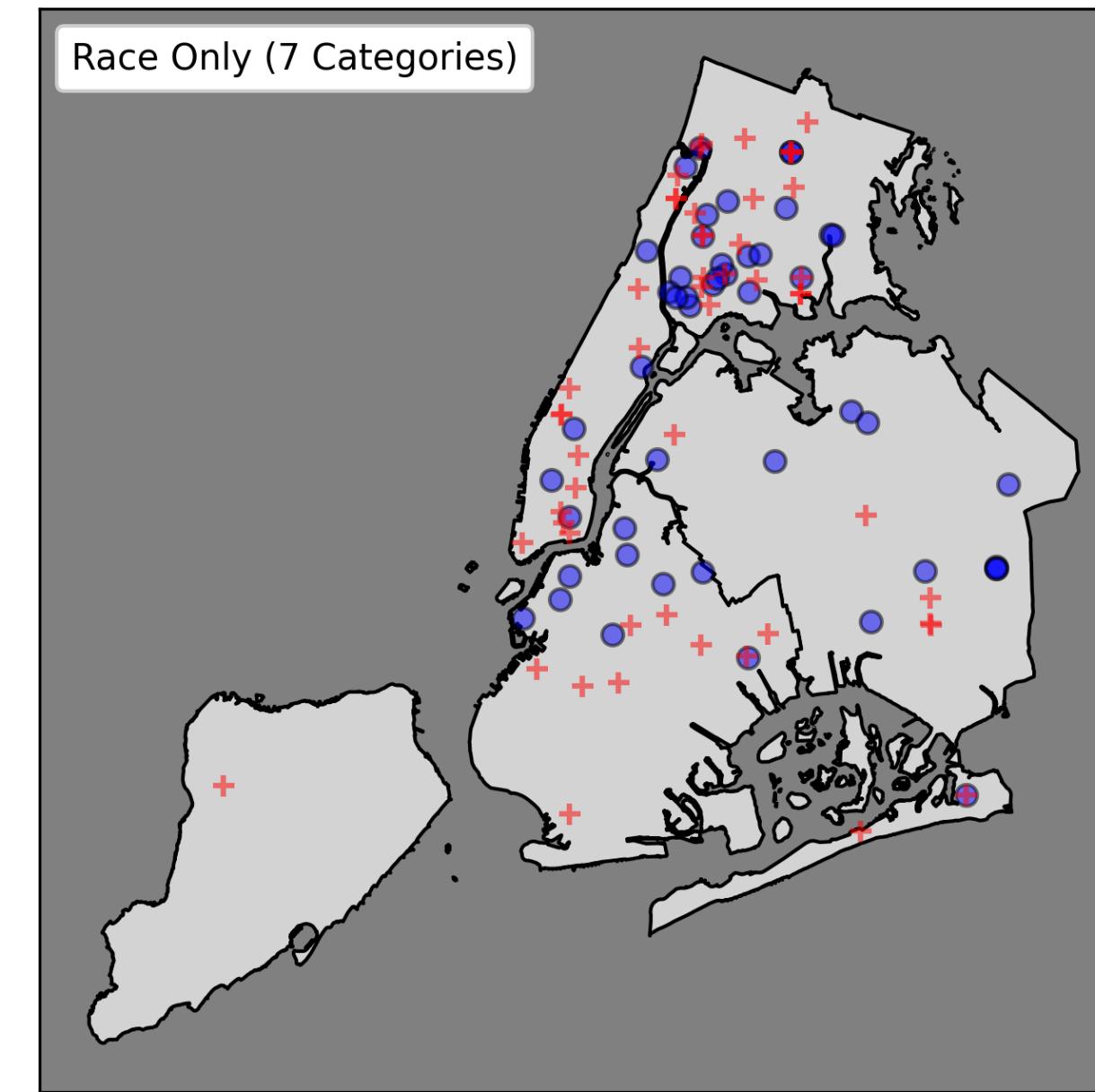


Focus on Inequality
(disaggregation)

Stylized NYC schools example

Takeaways from a case-study

- Social categorization (i.e., which partition) changes results
- Measuring subgroup outcomes better allows for focus on inequality
- With a focus on utility, inequality can increase
 - Even with strict fairness constraints
 - Even if group membership is known
 - Even if aggregate impact is larger



Approach	% Change in Impact Per-group							Aggregate % Impact	Disparity ($\delta(z)$)
	A	B	C	D	E	F	G		
No Intervention	±0.0	±0.0	±0.0	±0.0	±0.0	±0.0	±0.0	±0.0	1.429
IR	+1.76	+0.24	+0.42	+0.10	+0.16	+5.26	-1.35	+0.657	1.386
IR + 'no harm'	+1.78	+0.54	+0.74	+0.11	+1.02	+5.56	±0.0	+0.848	1.394
DIP, $\tau = 0.567$	+1.20	+0.69	+1.46	+0.63	+1.61	+3.50	+0.43	+0.953	1.435
DIP, Unconstrained	+1.21	+0.72	+1.48	+0.63	+1.64	+3.51	+0.47	+0.971	1.435

Counterfactuals for the Future

Motivating toy example

Treatment choice in a fixed sample

- Individualized treatment choice focused on **entire distribution of outcomes**
- **Allocating tutoring to students**
 - We want to allocate tutoring to students at a school in order to improve test performance
 - One time-step of past data on every student of interest
 - No confounding
 - We have a model of the data generating process
 - *Unobserved external factors about the students (e.g., family income, encouragement from parents) explain at least some of the variation in the outcome across units*



Two approaches to the same problem

Which approach is better?

- **Approach 1:**
 - Use our model to identify which students to treat based on their covariate values only
- **Approach 2:**
 - Use our model to identify which students to treat based on their covariate values *and modeled exogenous variables (i.e., noise)*

Two approaches to the same problem

Which approach is better?

- **Approach 1:**

Interventional

- Use our model to identify which students to treat based on their covariate values only

- **Approach 2:**

Counterfactual

- Use our model to identify which students to treat based on their covariate values *and modeled exogenous variables (i.e., noise)*

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Counterfactual

- Use our model to identify which students to treat based on their covariate values *and modeled exogenous variables (i.e., noise)*

- **Takeaway:** These two approaches can lead us to tutor a different set of students → **two different policies**

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Key question

What do we assume about family income and encouragement from parents year-to-year?

Interventional distributions

Notation

- Intuition:
 - “What will the distribution of test score Y be for a student described by SCM \mathfrak{C} if they are enrolled in tutoring Z ?”

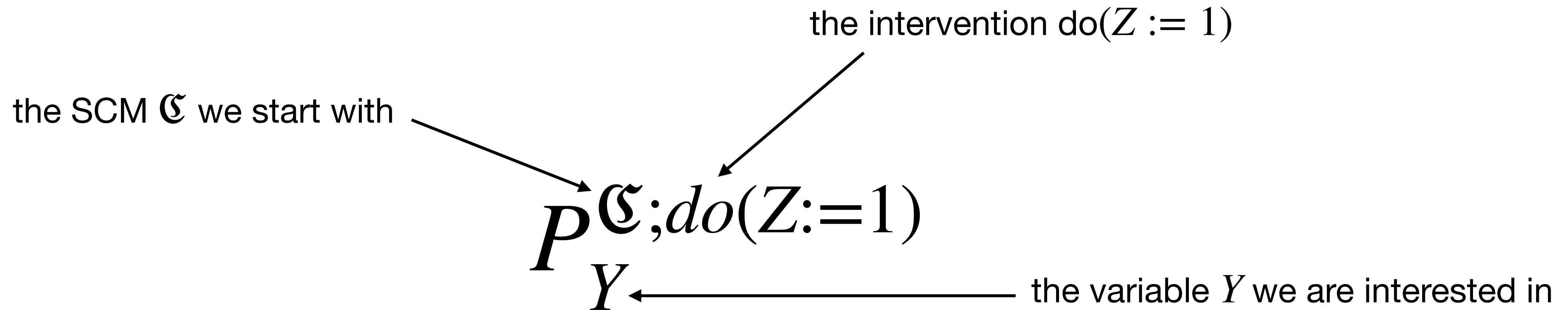


Image adapted from: [Peters et al. 2017]

Counterfactual distributions

Notation

- Intuition:
 - “What would the distribution of test score Y **have been** for a student described by SCM \mathfrak{C} if they **had been** enrolled in tutoring Z ? ”

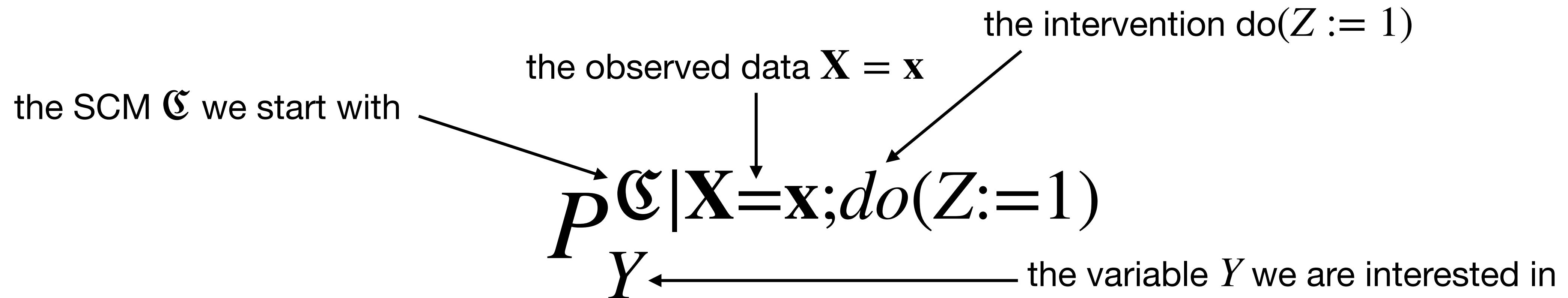


Image recreated from: [Peters et al. 2017]

Counterfactuals

The retrospective view

- Counterfactuals are typically described as *retrospective*
 - We condition on *observed circumstances* before simulating an intervention
 - Use posterior $P_{U|\mathbf{X}=\mathbf{x}}$ instead of prior P_U to obtain $P_Y^{\mathfrak{C}|\mathbf{X}=\mathbf{x}; do(\cdots)}$
- **Our work:** When can (or should) counterfactuals be forward-looking?

Why would we use past noise to make future decisions?

Assumptions about what we haven't observed

- Common for data with multiple time steps
 - “There are unobserved variables that play an important role in our model”
 - Large literature: time-series cross sectional data, mixed effects models, latent variable models, etc.
 - Can use repeated observations for estimation
- **Our setting: data with one time-step**
 - Noise decomposition is no longer an estimation problem
 - ▶ No repeated observations
 - Accounting for unobserved variables is instead *based on assumptions*

Forward-looking counterfactuals (FLCs)

An alternate view

- The ‘retrospective’ view is connected to assumptions about the **structure** and **stability** of exogenous variables (noise)
 - Structure:
 - ▶ How does a unit look exogenously compared to other units?
 - Stability:
 - ▶ How does a unit look exogenously compared to itself over time?
- **Spoiler:** FLCs useful when units’ exogenous factors are (1) sufficiently stable over time OR (2) sufficiently dissimilar to other units

Exploring FLCs empirically

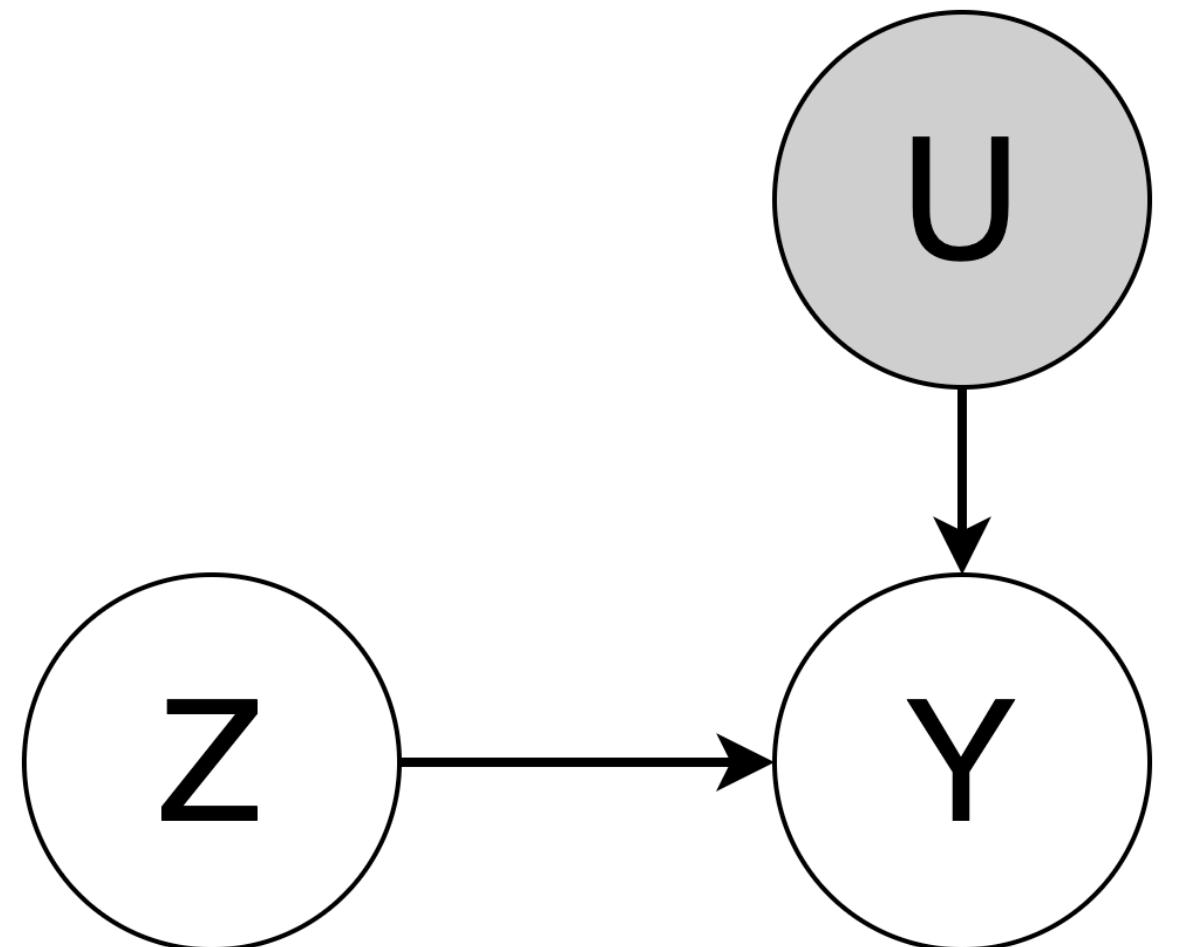
An illustrative parameterization

- Outcome Y , treatment Z , exogenous factors U , observed data $\{Z_0^{(i)}, Y_0^{(i)}\}_{i=1}^n$
- Intervention on unit i will increase Z by amount δ
- **Goal:** recover distribution P_{Y_1} after intervention on those for whom $Y_0 < 0$

$$(t = 0) : \begin{cases} Z_0^{(i)} \sim \mathcal{N}(\mu_Z, \sigma_Z^2) \\ Y_0^{(i)} = Z_0^{(i)} + U_0^{(i)} \end{cases}$$

$$(t = 1) : \begin{cases} Z_1^{(i)} = Z_0^{(i)} + \delta \cdot w(i) \\ Y_1^{(i)} = Z_1^{(i)} + U_1^{(i)} \end{cases}$$

Treatment choice



Exploring FLCs empirically

Model for exogenous noise terms

$$(t = 0) : \begin{cases} Z_0^{(i)} \sim \mathcal{N}(\mu_Z, \sigma_Z^2) \\ Y_0^{(i)} = Z_0^{(i)} + U_0^{(i)} \end{cases} \quad \begin{aligned} \mu_U^{(i)} &\sim \mathcal{N}(0, \sigma_\mu^2) \\ U_0^{(i)}, U_1^{(i)} &\stackrel{iid}{\sim} \mathcal{N}(\mu_U^{(i)}, \sigma_U^2) \end{aligned}$$
$$(t = 1) : \begin{cases} Z_1^{(i)} = Z_0^{(i)} + \delta \cdot w(i) \\ Y_1^{(i)} = Z_1^{(i)} + U_1^{(i)} \end{cases}$$

Exploring FLCs empirically

Model for exogenous noise terms

$$(t = 0) : \begin{cases} Z_0^{(i)} \sim \mathcal{N}(\mu_Z, \sigma_Z^2) \\ Y_0^{(i)} = Z_0^{(i)} + U_0^{(i)} \end{cases}$$

$$(t = 1) : \begin{cases} Z_1^{(i)} = Z_0^{(i)} + \delta \cdot w(i) \\ Y_1^{(i)} = Z_1^{(i)} + U_1^{(i)} \end{cases}$$

We can now explore structure
(σ_μ) and stability (σ_U)

$$\boxed{\begin{aligned} \mu_U^{(i)} &\sim \mathcal{N}(0, \sigma_\mu^2) \\ U_0^{(i)}, U_1^{(i)} &\stackrel{iid}{\sim} \mathcal{N}(\mu_U^{(i)}, \sigma_U^2) \end{aligned}}$$

Parameterizing exogenous structure and stability

Connecting assumptions to parameters

Assumption	Model	Interpretation
(A1) Exogenous factors are constant over time.	$\sigma_U = 0$	Among the relevant variables we haven't measured, each unit looks exactly the same next year as it does this year.
(A2) Exogenous factors vary over time.	$\sigma_U > 0$	Among the relevant variables we haven't measured, each unit looks somewhat the same next year as it does this year. Similarities grow weaker with larger σ_U values.
(A3) Exogenous factors exhibit unstructured variation.	$\sigma_\mu = 0$	Among the relevant variables we haven't measured, each unit looks the same as any other unit, apart from random variability with time.
(A4) Exogenous factors exhibit structured (unit-specific) variation.	$\sigma_\mu > 0$	Among the relevant variables we haven't measured, there are units that look unlike other units, in addition to random variability with time. Units look less like each other with larger σ_μ .

$$\begin{aligned}\mu_U^{(i)} &\sim \mathcal{N}(0, \sigma_\mu^2) \\ U_0^{(i)}, U_1^{(i)} &\stackrel{iid}{\sim} \mathcal{N}(\mu_U^{(i)}, \sigma_U^2)\end{aligned}$$

Counterfactual vs. interventional distributions

What happens with a ‘correct’ model?

$$\mu_U^{(i)} \sim \mathcal{N}(0, \sigma_\mu^2)$$

$$\text{Truth } (t = 0) : \begin{cases} Z_0^{(i)} \sim \mathcal{N}(\mu_Z, \sigma_Z^2) \\ U_0^{(i)} \sim \mathcal{N}(\mu_U^{(i)}, \sigma_U^2) \\ Y_0^{(i)} = Z_0^{(i)} + U_0^{(i)} \end{cases}$$

$$\text{Truth } (t = 1) : \begin{cases} Z_1^{(i)} = Z_0^{(i)} + \delta \cdot w(i) \\ U_1^{(i)} \sim \mathcal{N}(\mu_U^{(i)}, \sigma_U^2) \\ Y_1^{(i)} = Z_1^{(i)} + U_1^{(i)} \end{cases}$$

$$\text{Model } (t = 0) = \begin{cases} Z_0^{(i)} \sim \mathcal{N}(\mu_Z, \sigma_Z^2) \\ U_0^{(i)} \sim \mathcal{N}(0, \sigma_\mu^2 + \sigma_U^2) \\ Y_0^{(i)} = Z_0^{(i)} + U_0^{(i)} \end{cases}$$

$$\text{Interventional } (t = 1) = \begin{cases} Z_1^{(i)} = Z_0^{(i)} + \delta \cdot w(i) \\ U_1^{(i)} \sim \mathcal{N}(0, \sigma_\mu^2 + \sigma_U^2) \\ Y_1^{(i)} = Z_1^{(i)} + U_1^{(i)} \end{cases}$$

$$\text{Counterfactual } (t = 1) = \begin{cases} Z_1^{(i)} = Z_0^{(i)} + \delta \cdot w(i) \\ \tilde{U}_1^{(i)} = U_0^{(i)} \\ Y_1^{(i)} = Z_1^{(i)} + \tilde{U}_1^{(i)} \end{cases}$$

Counterfactual vs. interventional distributions

What happens with a ‘correct’ model?

$$\mu_U^{(i)} \sim \mathcal{N}(0, \sigma_\mu^2)$$

Truth ($t = 0$) :

$$\begin{cases} Z_0^{(i)} \sim \mathcal{N}(\mu_Z, \sigma_Z^2) \\ U_0^{(i)} \sim \mathcal{N}(\mu_U^{(i)}, \sigma_U^2) \\ Y_0^{(i)} = Z_0^{(i)} + U_0^{(i)} \end{cases}$$

Truth ($t = 1$) :

$$p_{Y_1} \quad \begin{cases} Z_1^{(i)} = Z_0^{(i)} + \delta \cdot w(i) \\ U_1^{(i)} \sim \mathcal{N}(\mu_U^{(i)}, \sigma_U^2) \\ Y_1^{(i)} = Z_1^{(i)} + U_1^{(i)} \end{cases}$$

Model ($t = 0$) =

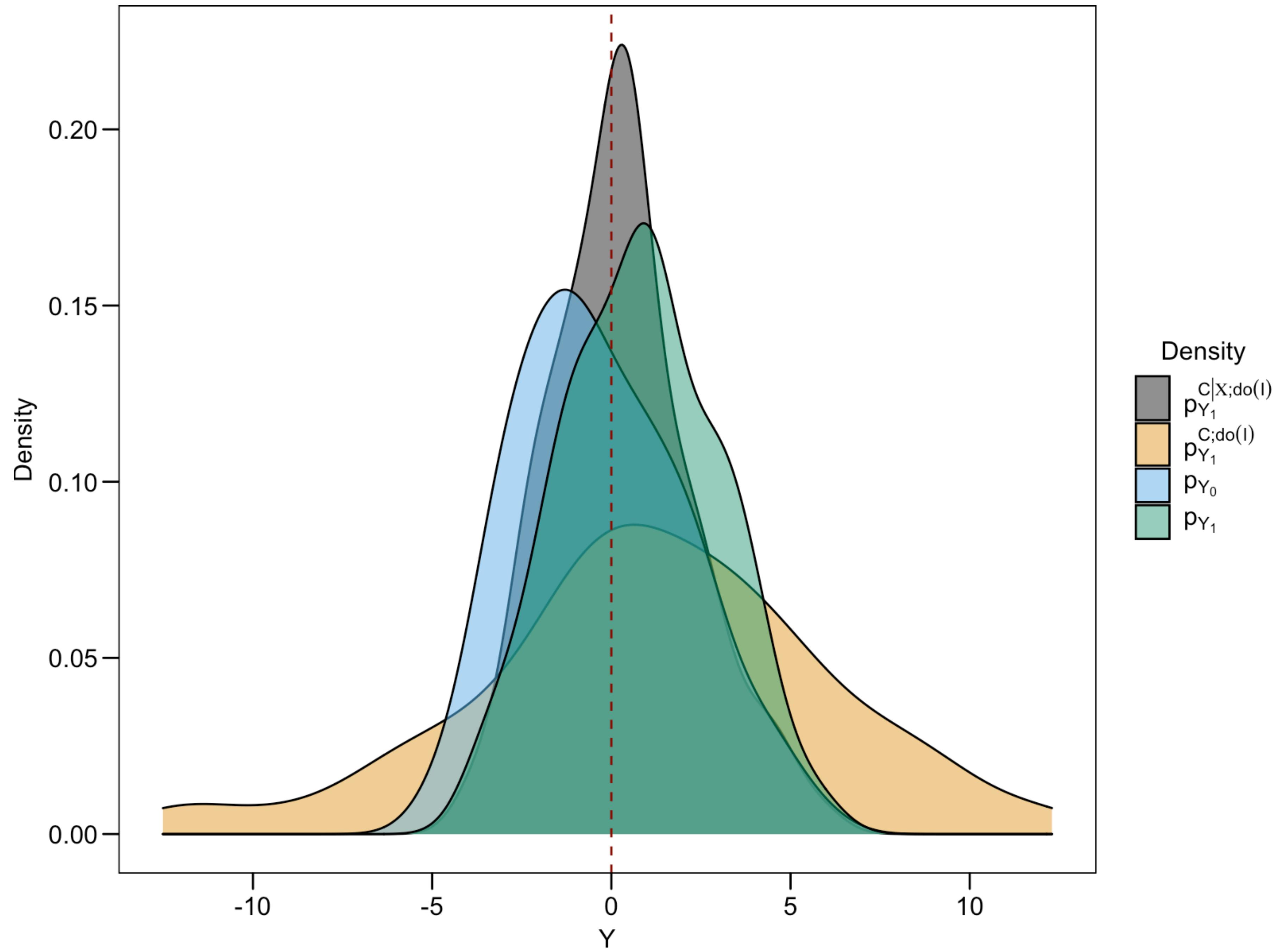
$$\begin{cases} Z_0^{(i)} \sim \mathcal{N}(\mu_Z, \sigma_Z^2) \\ U_0^{(i)} \sim \mathcal{N}(0, \sigma_\mu^2 + \sigma_U^2) \\ Y_0^{(i)} = Z_0^{(i)} + U_0^{(i)} \end{cases}$$

Interventional ($t = 1$) =

$$p_{Y_1}^{\mathfrak{C}; do(\dots)}$$
$$\begin{cases} Z_1^{(i)} = Z_0^{(i)} + \delta \cdot w(i) \\ U_1'^{(i)} \sim \mathcal{N}(0, \sigma_\mu^2 + \sigma_U^2) \\ Y_1^{(i)} = Z_1^{(i)} + U_1'^{(i)} \end{cases}$$

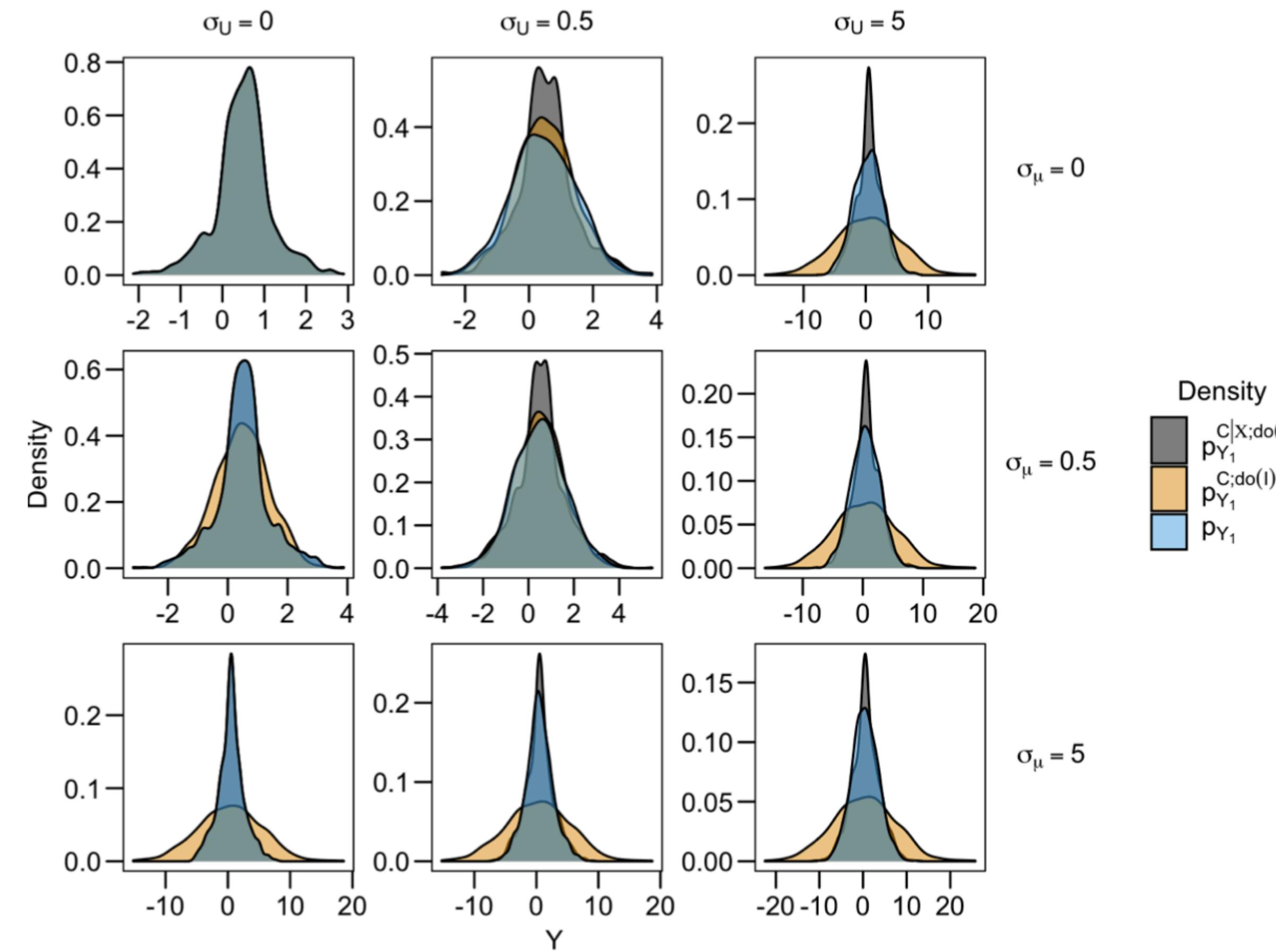
Counterfactual ($t = 1$) =

$$p_{Y_1}^{\mathfrak{C}|X=x; do(\dots)}$$
$$\begin{cases} Z_1^{(i)} = Z_0^{(i)} + \delta \cdot w(i) \\ \tilde{U}_1^{(i)} = U_0^{(i)} \\ Y_1^{(i)} = Z_1^{(i)} + \tilde{U}_1^{(i)} \end{cases}$$

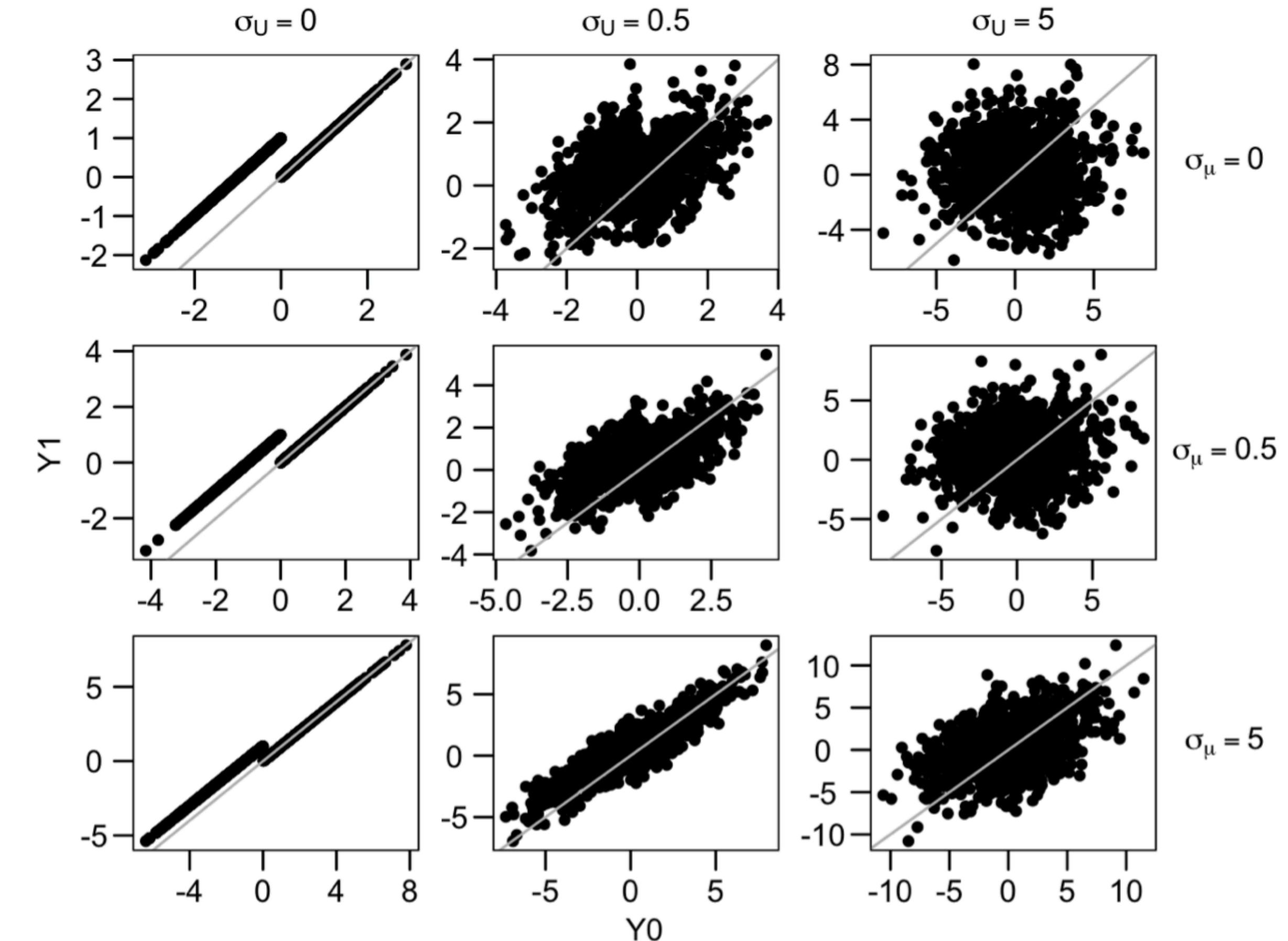


Takeaways

Unit-specific structure OR stability over time → FLCs



(a)

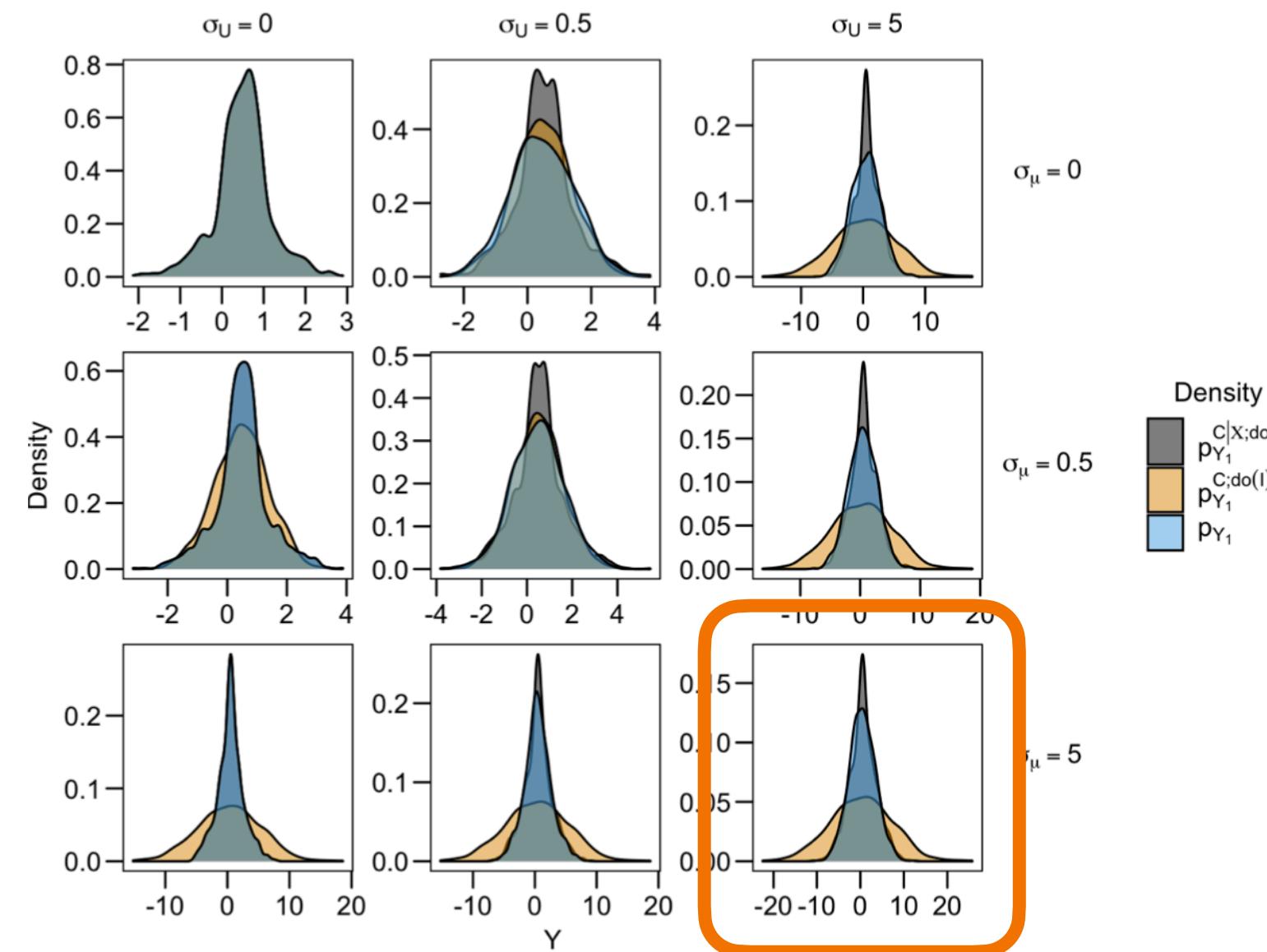


(b)

Why do we care?

Back to motivation

- We often can't measure every relevant variable
- We might not be able to collect lots of data over time
- Our assumptions can lead to **different policies** and **incorrect conclusions**



What if we want to decrease variance?

$$\frac{\mathbb{V}[P_{Y_0}]}{12.2} \quad \frac{\mathbb{V}[P_{Y_1}]}{9.36} \quad \frac{\mathbb{V}[P_{Y_1}^{\mathcal{C}|\mathcal{X}; \text{do}(I)}]}{9.61} \quad \frac{\mathbb{V}[P_{Y_1}^{\mathcal{C}; \text{do}(I)}]}{51.1}$$

References 1

- [1] Rediet Abebe, Jon Kleinberg, and S. Matthew Weinberg. 2020. Subsidy Allocations in the Presence of Income Shocks. *Proceedings of the AAAI Conference on Artificial Intelligence* 34, 05 (Apr. 2020), 7032–7039. <https://doi.org/10.1609/aaai.v34i05.6188>
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Thank you! Questions?