

# Association Rules

# Association Rules

## Introduction

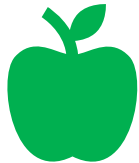
- Goal is
  - to find associations between different objects
  - to find patterns in objects
  - to derive strategies (store layout, catalogue design, customizing emails, recommender engines, ...)
- Applicable for
  - Marketing
  - Clustering
  - Classification
  - Retailing

# Association Rules

## Principle

- Example: Supermarket

Product Portfolio → Item Set

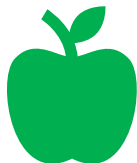


...

# Association Rules

## Principle

- Input: Transactions



Transaction 1



Transaction 2



Transaction 3

# Association Rules

## Principle

- Transactions

| Transaction | Items        |
|-------------|--------------|
| 1           | {apple, ice} |
| 2           | {cake}       |
| 3           | {ice, cake}  |
| ...         | {...}        |
| N           | {...}        |

# Association Rules

## Principle

- Output: Rules

| [LHS]         | [RHS]  |
|---------------|--------|
| {ice}         | {cake} |
| {apple, cake} | {ice}  |
| ...           |        |

# Association Rules












Key Parameters: Support

- $Support(X) = \frac{\text{Number Transactions including } X}{\text{Total Transactions Number}} = \frac{count(X)}{N}$
- $Support(\{X\} \rightarrow \{Y\}) = \frac{\text{Transactions containing } X \text{ AND } Y}{\text{Total Transaction Number}}$
- Support threshold can be defined to exclude infrequent transactions

# Association Rules

Key Parameters: Support - Example

- Calculate Support(Apple  $\rightarrow$  Pie)!
- Minimum Support = 0.4
- Count(apple&pie) = 3
- Total Number= 5
- Min Support excludes infrequent itemsets from further analysis

| Transact. ID |   |   |   |
|--------------|---|---|---|
| 1            |  |   |   |
| 2            |  |  |   |
| 3            |  |  |   |
| 4            |  |  |  |
| 5            |  |  |  |



# Association Rules

Key Parameters: Confidence

- $Confidence(X \rightarrow Y) = \frac{Support(X,Y)}{Support(X)}$
- How often is Y bought, after X was bought?
- Problem: only considers popularity of X (not of Y)
  - If X and Y are popular, buying X and Y together is likely. So high confidence occurs by chance.

# Association Rules

Key Parameters: Lift

- $Lift(X \rightarrow Y) = \frac{Support(X,Y)}{Support(X)*Support(Y)}$
- How often is Y bought, after X was bought?
- This takes popularity of Y into account.