#### Problem

- Dataset with MANY features
- Includes a lot of noise
- Model that takes all features into account
  - Very flexible
  - Very prone to overfitting
- How can you know which features are relevant?
  - Domain knowledge
  - Feature engineering
  - Dimensionality reduction methods
  - Use regularization!

#### Introduction

- Type of regression
- Model coefficients penalized
- Avoids overfitting by not-learning a too complex model
- Reduces model variance at the cost of bias increase
- How: by adding a penalty term to cost function

Multivariate

**Regression Model** 

Minimize Cost Function

$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \dots + \beta_n X_n$$

$$\beta_0 + \beta_1 X_1 + \beta_2 X_2 + \dots + \beta_n X_n$$

$$RSS = \sum_{i=1}^{n} \left( y_i - \beta_0 - \sum_{j=1}^{p} \beta_j x_{ij} \right)^2 + PenaltyTerm$$

L1 / L2 regularization

Lasso regression (L1 regularization)

- Least Absolute Shrinkage and Selection Operator
- Adds absolute value of magnitude of coefficient
- Penalizes high coefficients, sets to zero

Ridge regression (L2 regularization)

- Adds squared coefficients to cost function
- High coefficients very costly
- Coefficients never zero

Minimize Cost Function

$$RSS + \lambda \sum_{j=1}^{p} |\beta_j|$$

$$RSS + \lambda \sum_{j=1}^{p} \beta_j^2$$

Difference Lasso / Ridge Regression

#### **Lasso Regression**

- better, if useless variables existent
- better, if few variables have high coefficients and other variables coefficients close to zero
- removes features from model
- → acts like feature selection

#### Ridge Regression

- minimizes coefficients
- Reduces coefficients asymptotically close to zero
- Performs better, if there are many variables with similar coefficient values
- Ridge better, if most variables useful

Penalty Factor Lambda

- Lambda Range: 0 to +∞
- Shrinkage penalty increases with lambda

