

# ~ Genetic Algorithms ~

## In Search of the Missing Solution

Daive Carneiro

Press Start!

# \$ About

- \* PhD from the Universities of Minho, Aveiro and Porto (MAP-i)

- \* Interests/Teaching:

- Artificial Intelligence
- Data Science/Engineering
- Decision Support Systems

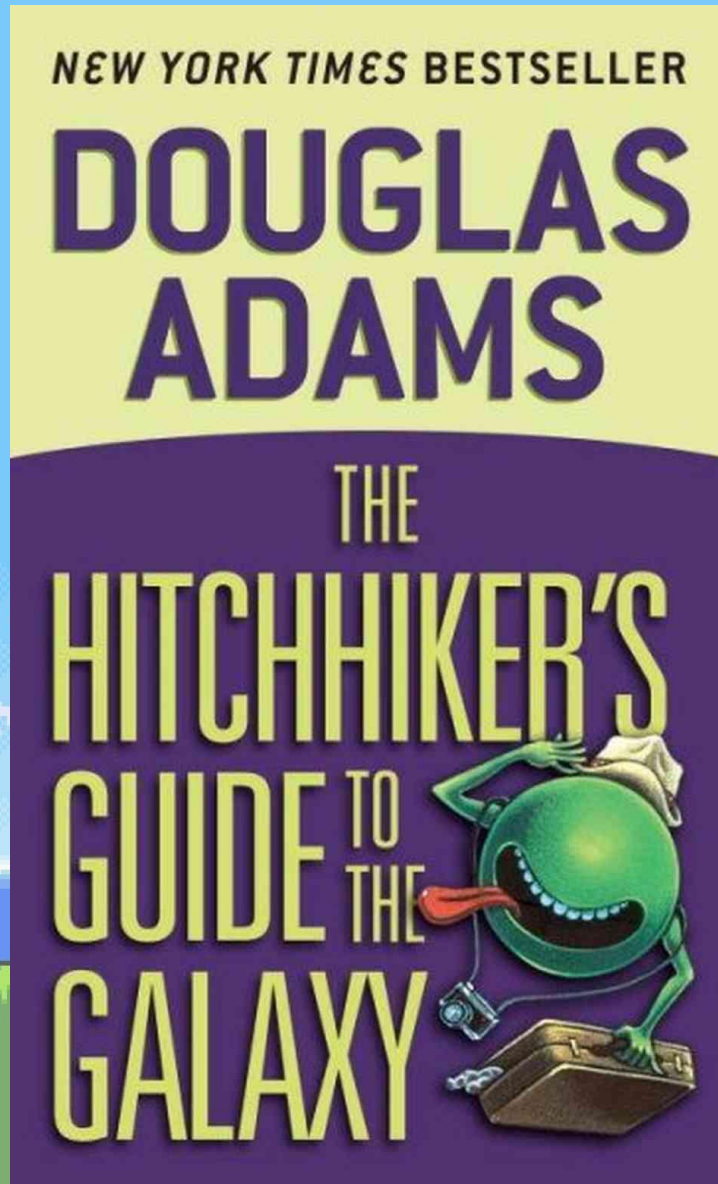
...

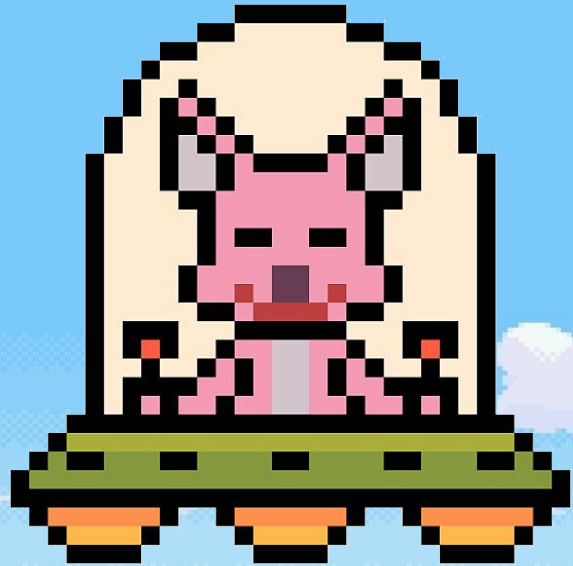
- \* Participation in Scientific Projects with real-life applications

# \$ About this









# What is the meaning of life?

input

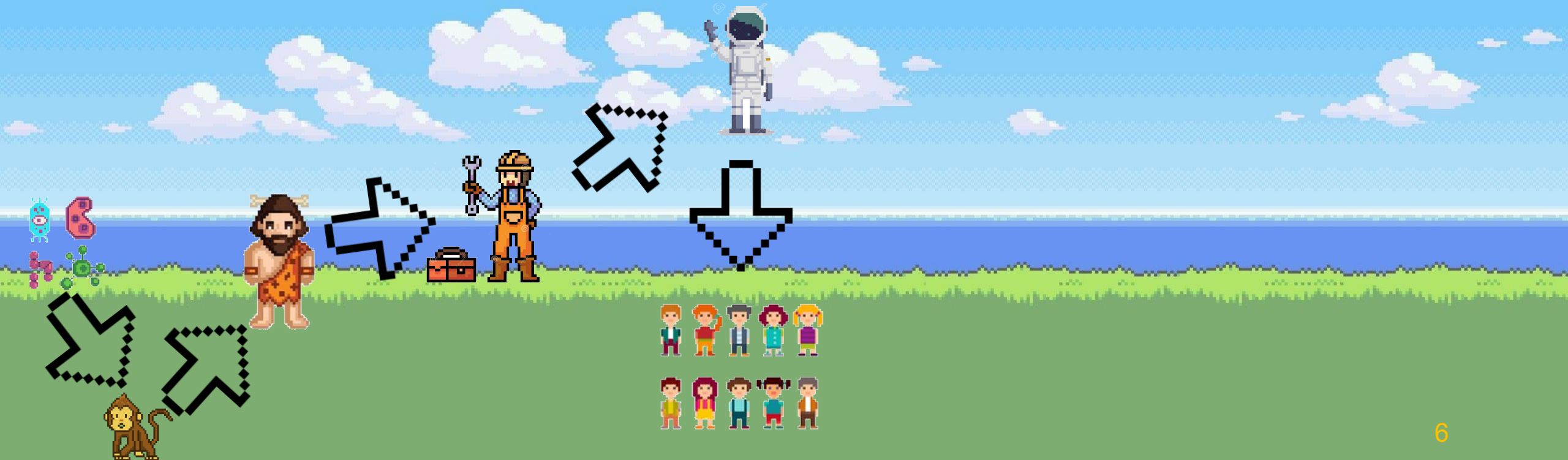


output





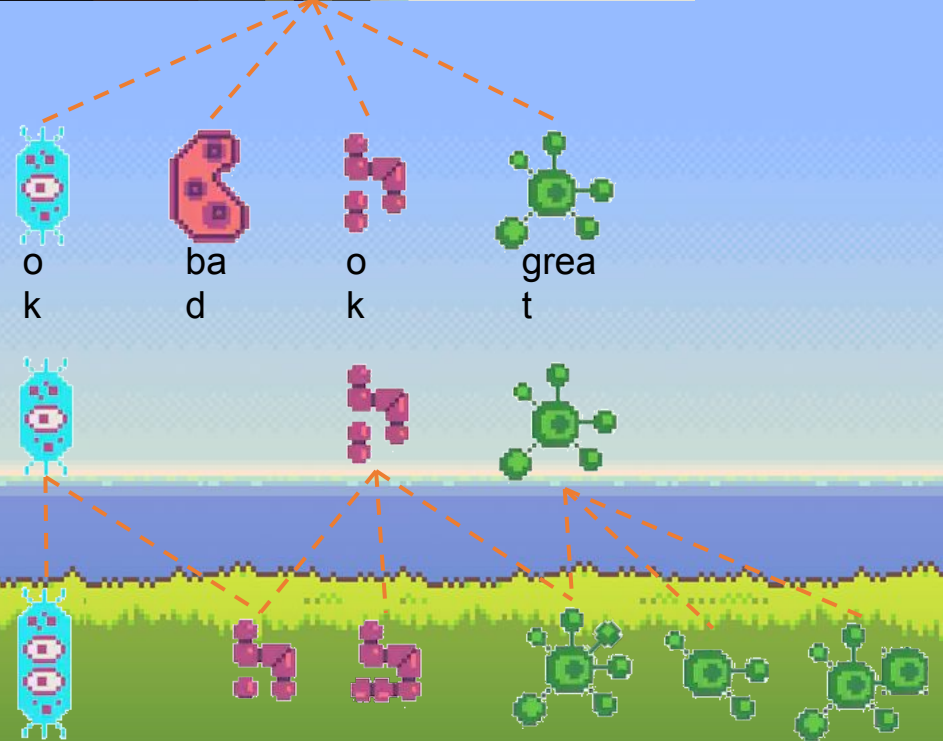
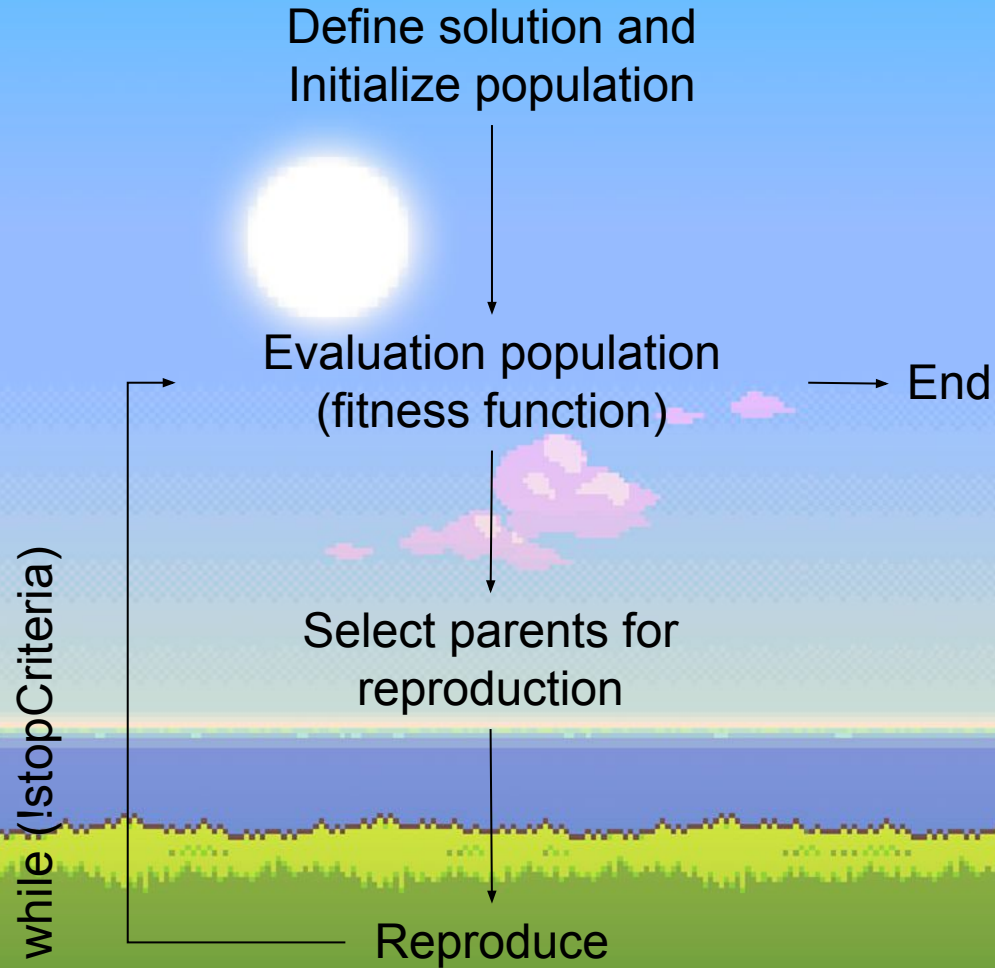
How does this computer work?  
How does it find a solution?  
What does the solution even look like?



# \$ What are GAs?

- \* **Search algorithms** inspired by the natural mechanics of biological evolution
- \* Are good at taking potentially large **multi-dimensional search spaces** and **navigating them**, looking for optimal solutions
- \* Ideal when the path towards a good solution is **not known** and/or when **brute-force** approaches are **not feasible**

# \$ Algorithm

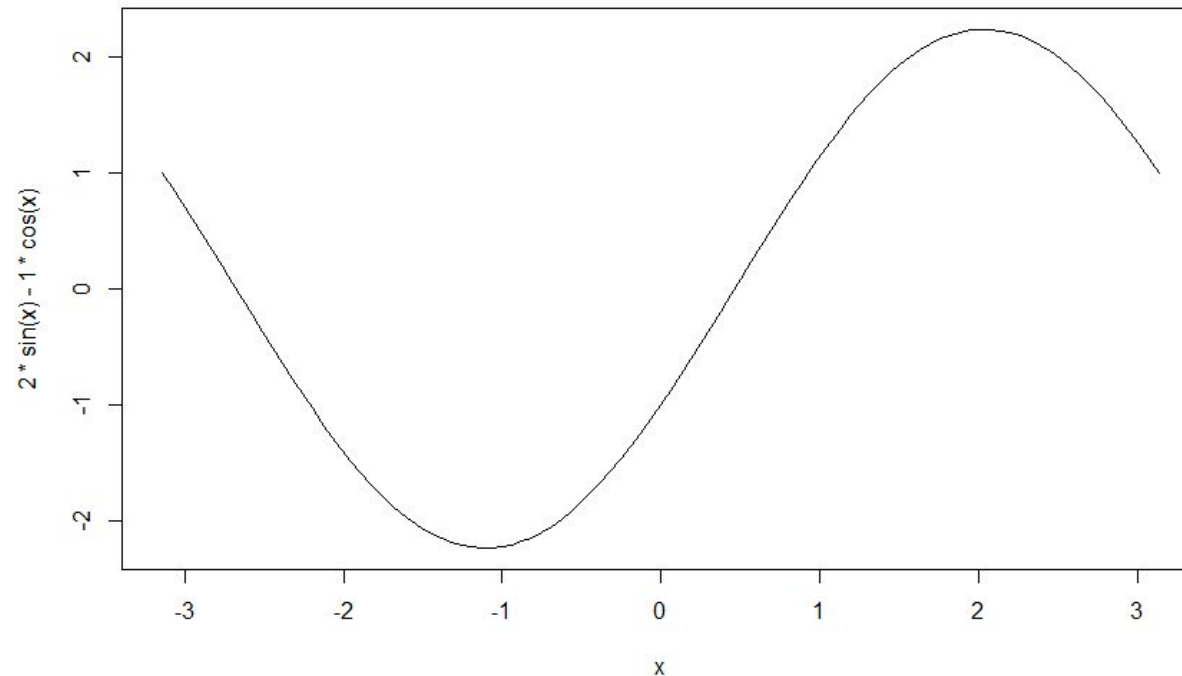




# \$ Quest #1

\* Find the minimum of  
between  $-\pi$  and  $\pi$

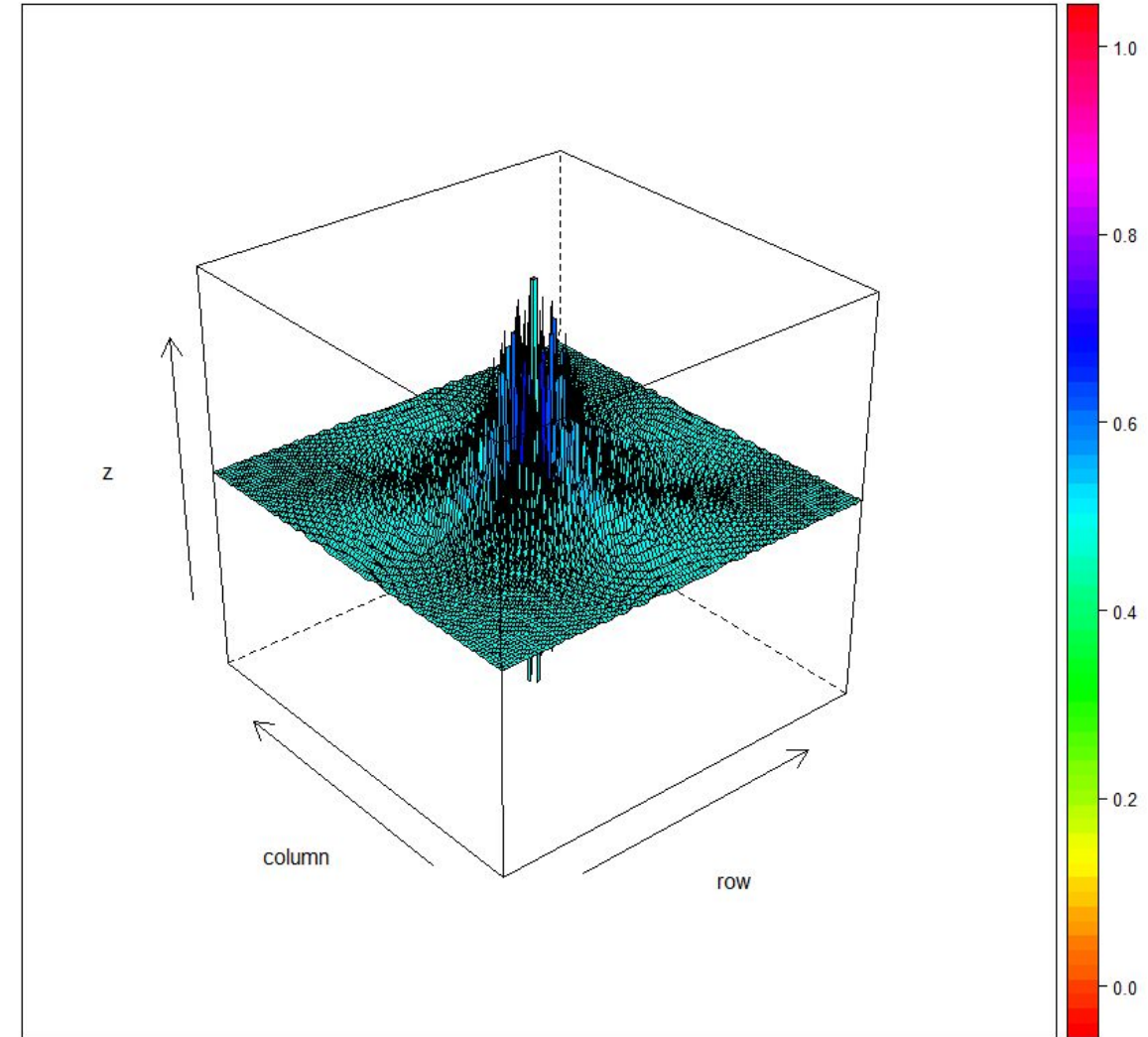
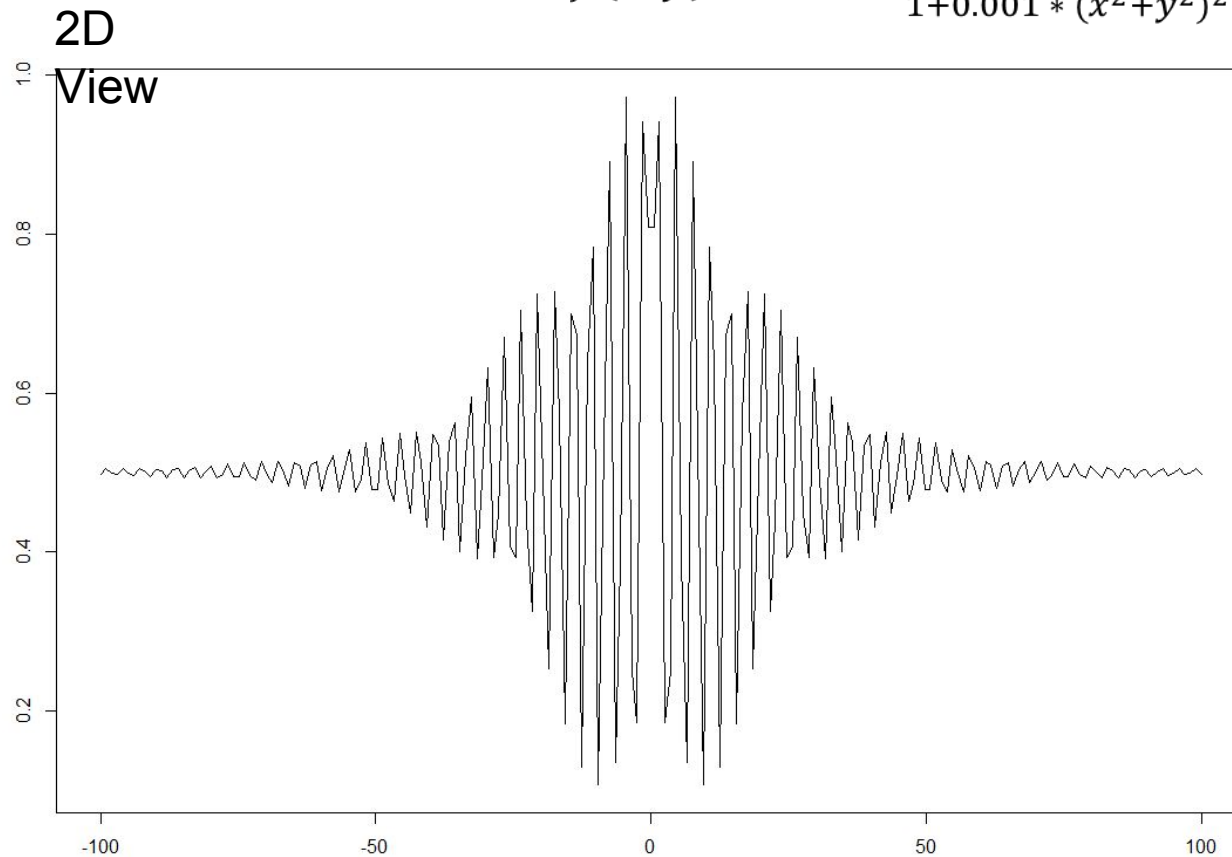
$$f(x) = 2 * \sin(x) - 1 * \cos(x)$$



# \$ Quest #2

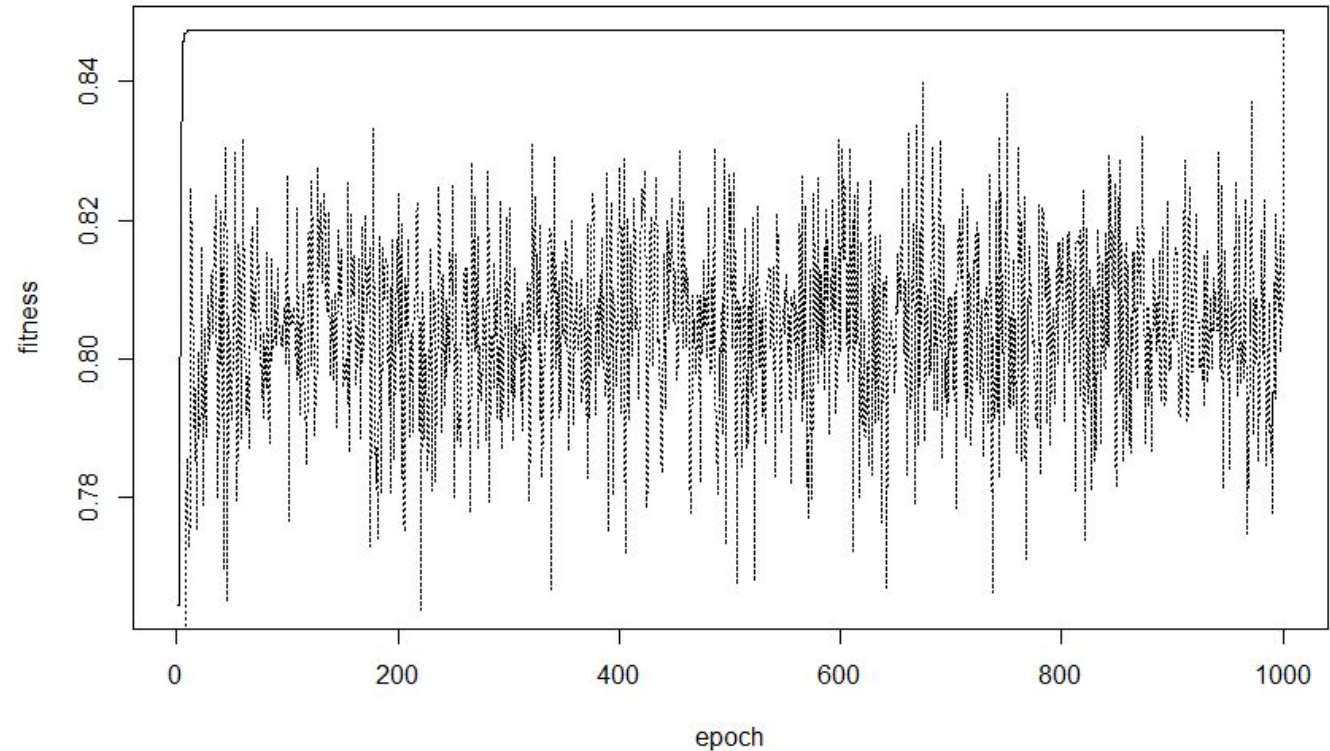
\* Find the maximum of

$$f(x, y) = 0.5 + \frac{\sin(\sqrt{x^2 + y^2})^2 - 0.5}{1 + 0.001 * (x^2 + y^2)^2}$$



# \$ Configuration #1

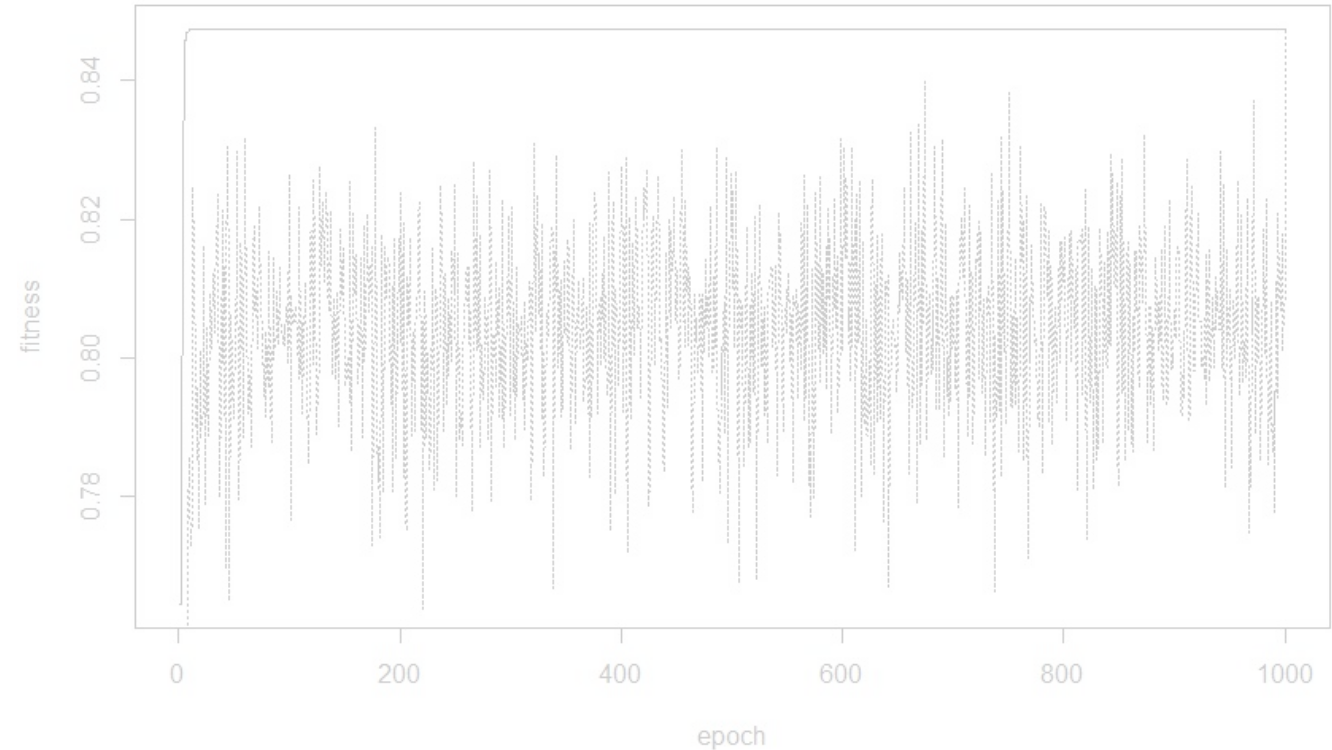
- \* Population size: 20
- \* heredityRate: 0
- \* crossoverRate: 0
- \* mutationRate: 0.75
- \* maxIterations: 1000
- \* DeltaMin: 0,0000001
- \* MutationFactor: 0.2
- \* Strategy: apply the genetic operators with the given probabilities to all solutions, select best afterwards





# \$ Configuration #1

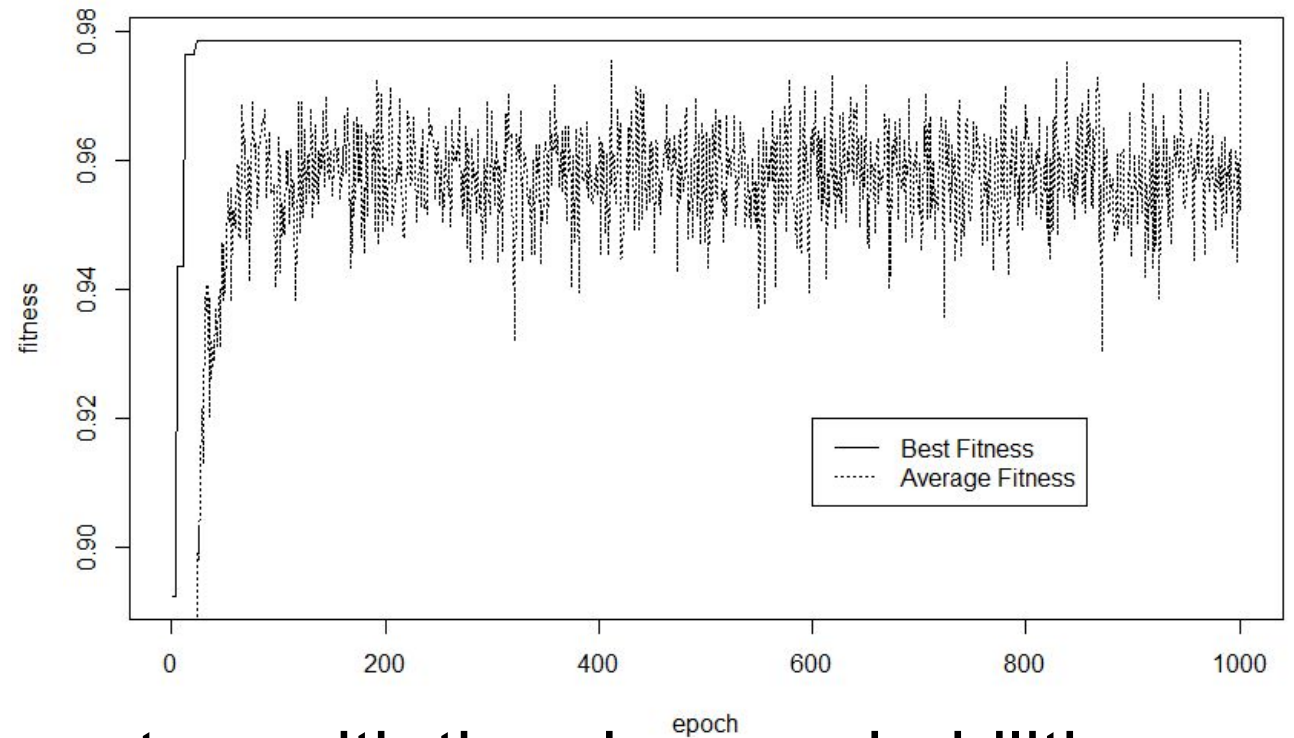
- \* Population
- \* heredityR
- \* crossover
- \* mutation
- \* maxIterat
- \* DeltaMin
- \* Mutation



- \* Strategy: apply the genetic operators with the given probabilities to all solutions, select best afterwards

# \$ Configuration #2

- \* Population size: 20
- \* heredityRate: 0.1
- \* crossoverRate: 0.25
- \* mutationRate: 0.25
- \* maxIterations: 1000
- \* DeltaMin: 0.0000001
- \* MutationFactor: 0.2
- \* Strategy: apply the genetic operators with the given probabilities to all solutions, select best afterwards



# \$ Configuration #2

- \* Population size: 20

- \* hereditarity

- \* crossover

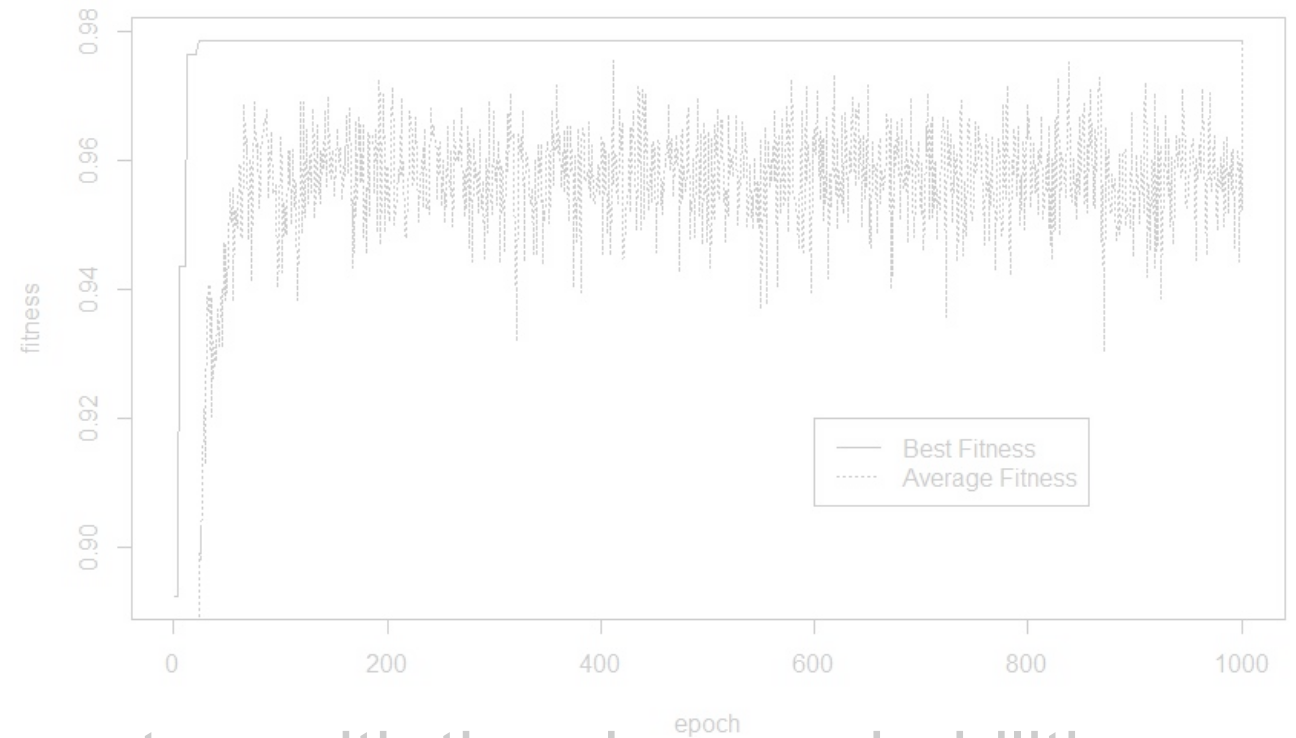
- \* mutation

- \* maxIterat

- \* DeltaMin

- \* Mutation

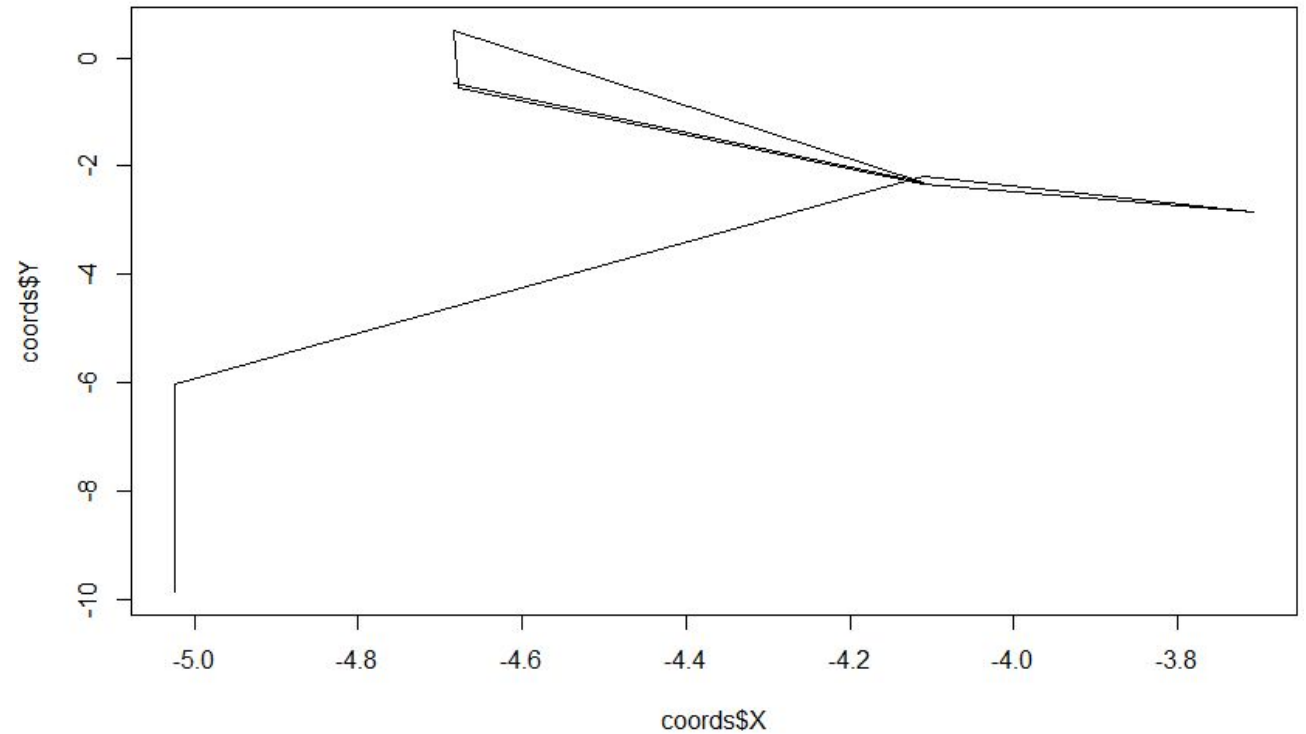
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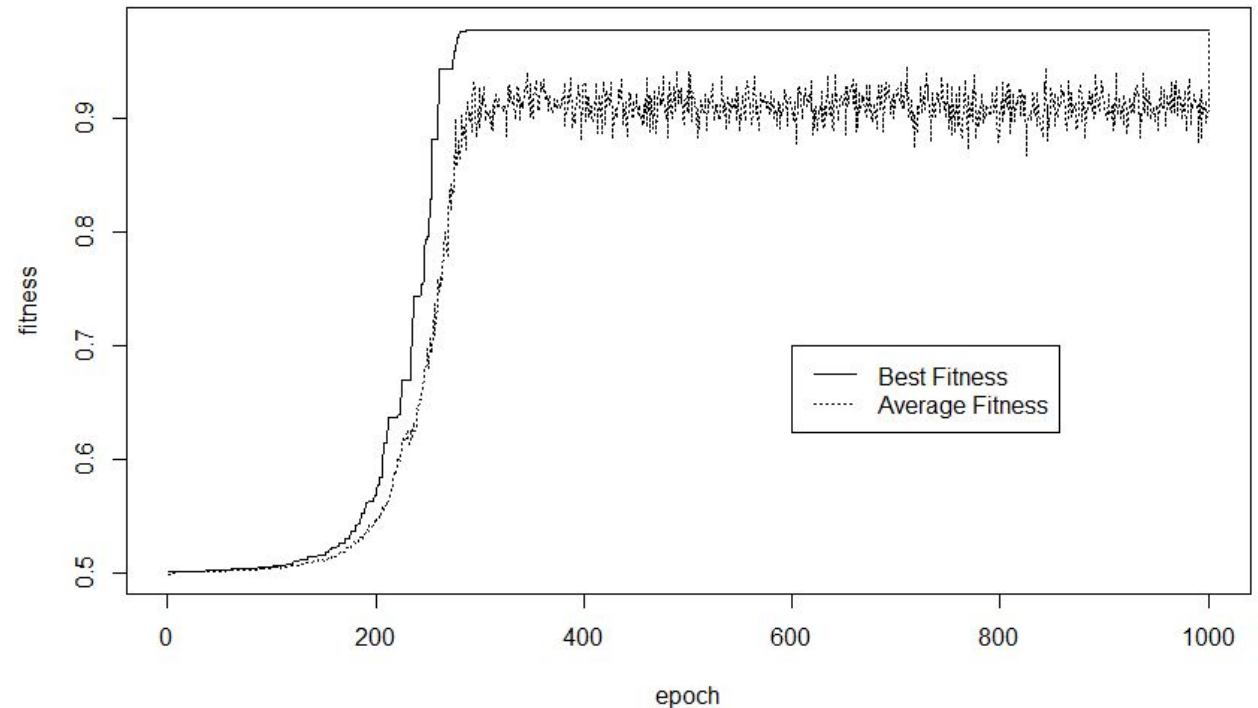
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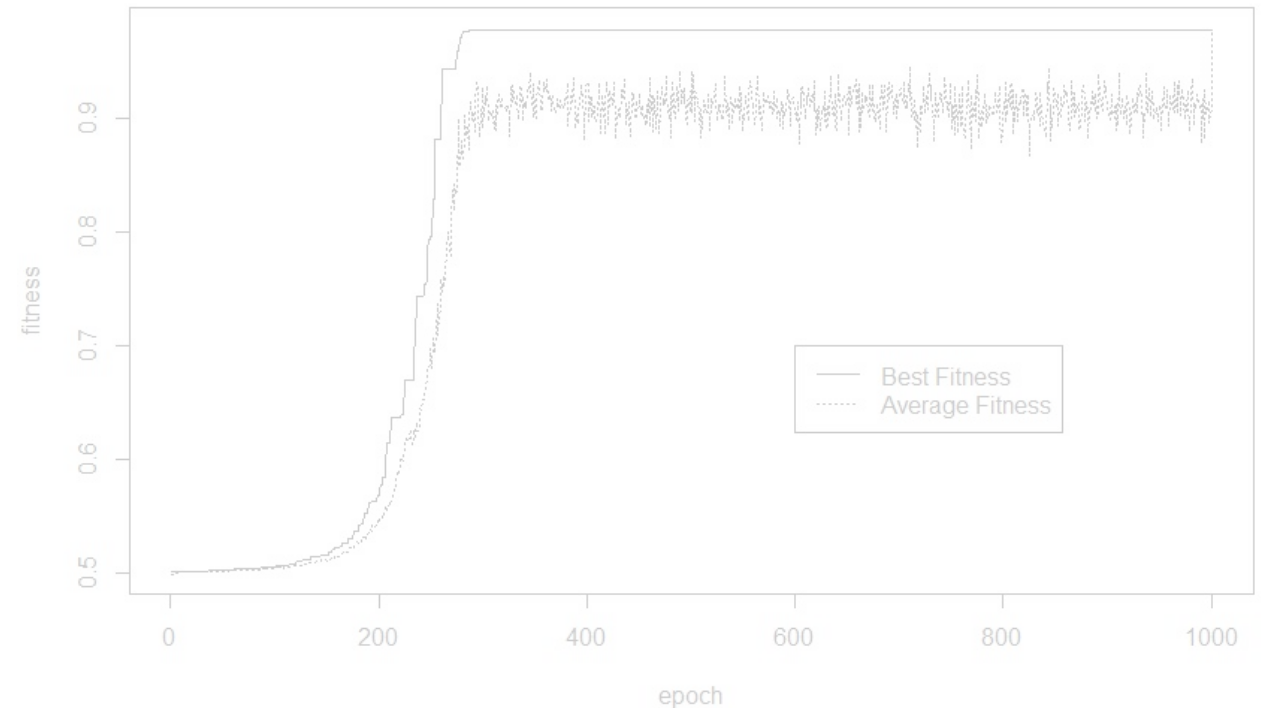
# \$ Configuration #3 – start at (-100, -100)

- \* Population size: 20
- \* heredityRate: 0.1
- \* crossoverRate: 0.25
- \* mutationRate: 0,25
- \* maxIterations: 1000
- \* DeltaMin: 0,00000001
- \* MutationFactor: 0,2
- \* Strategy: apply the genetic operators with the given probabilities to all solutions, select best afterwards



# \$ Configuration #3 – start at (-100, -100)

- \* Population size: 100
  - \* hereditability: 0.9
  - \* crossover: 0.9
  - \* mutation: 0.01
  - \* maxIter: 1000
  - \* DeltaMax: 0.001
  - \* Mutation: 0.01
- 

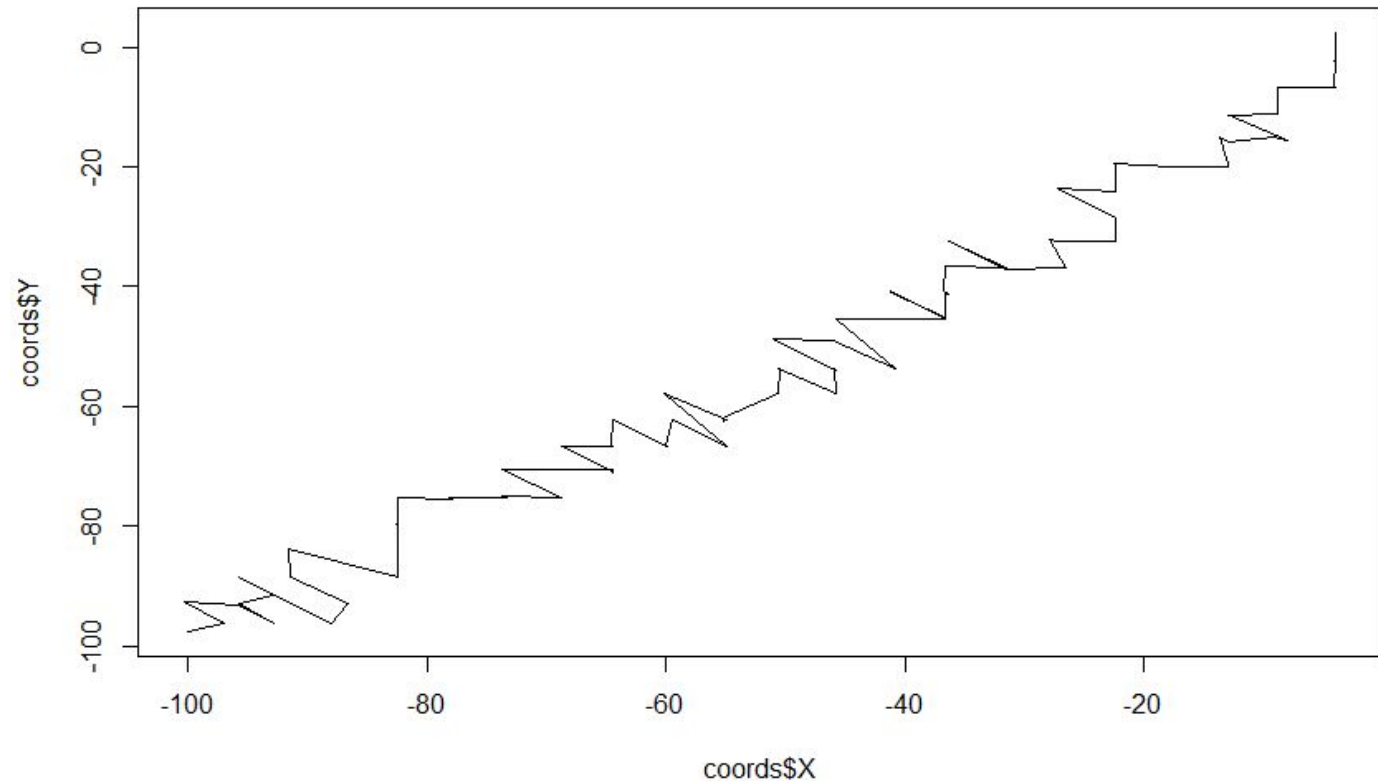


- \* Strategy: apply the genetic operators with the given probabilities to all solutions, select best afterwards



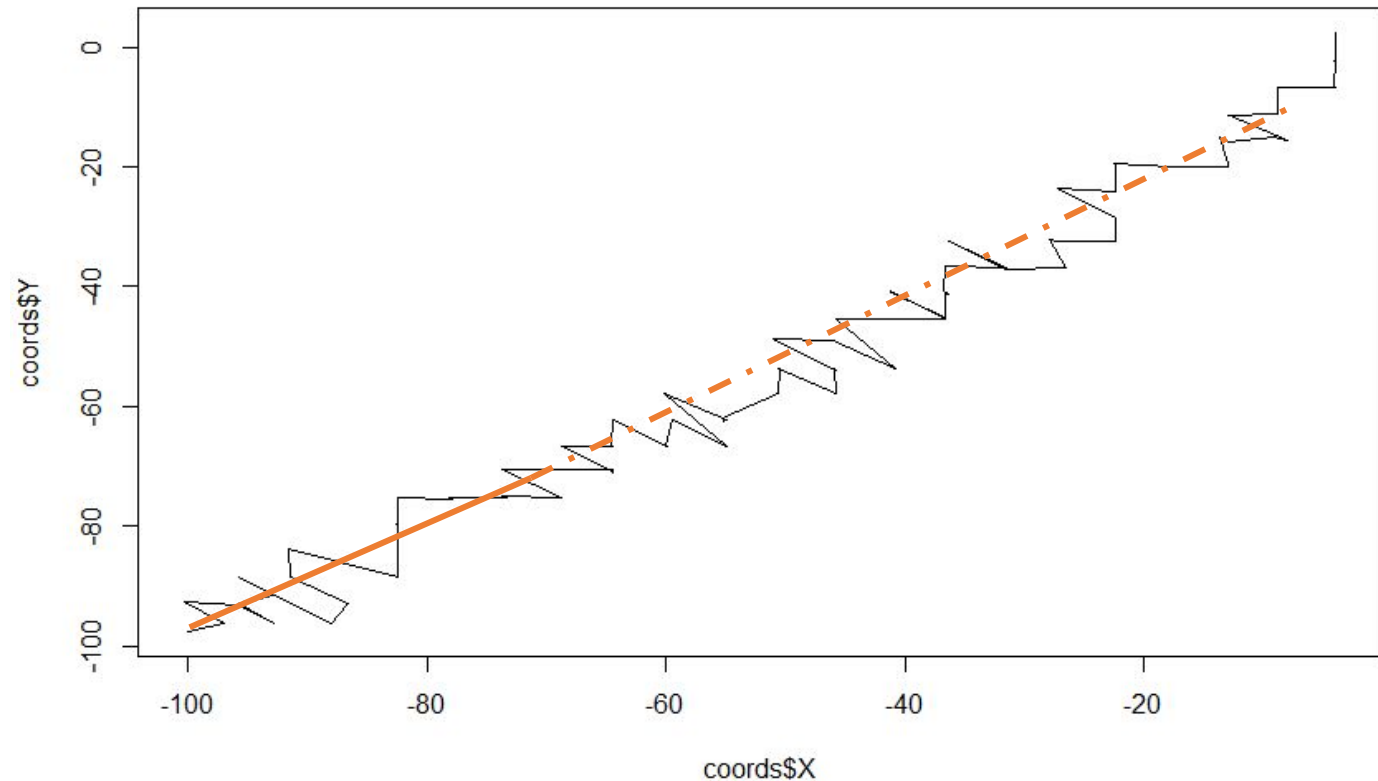
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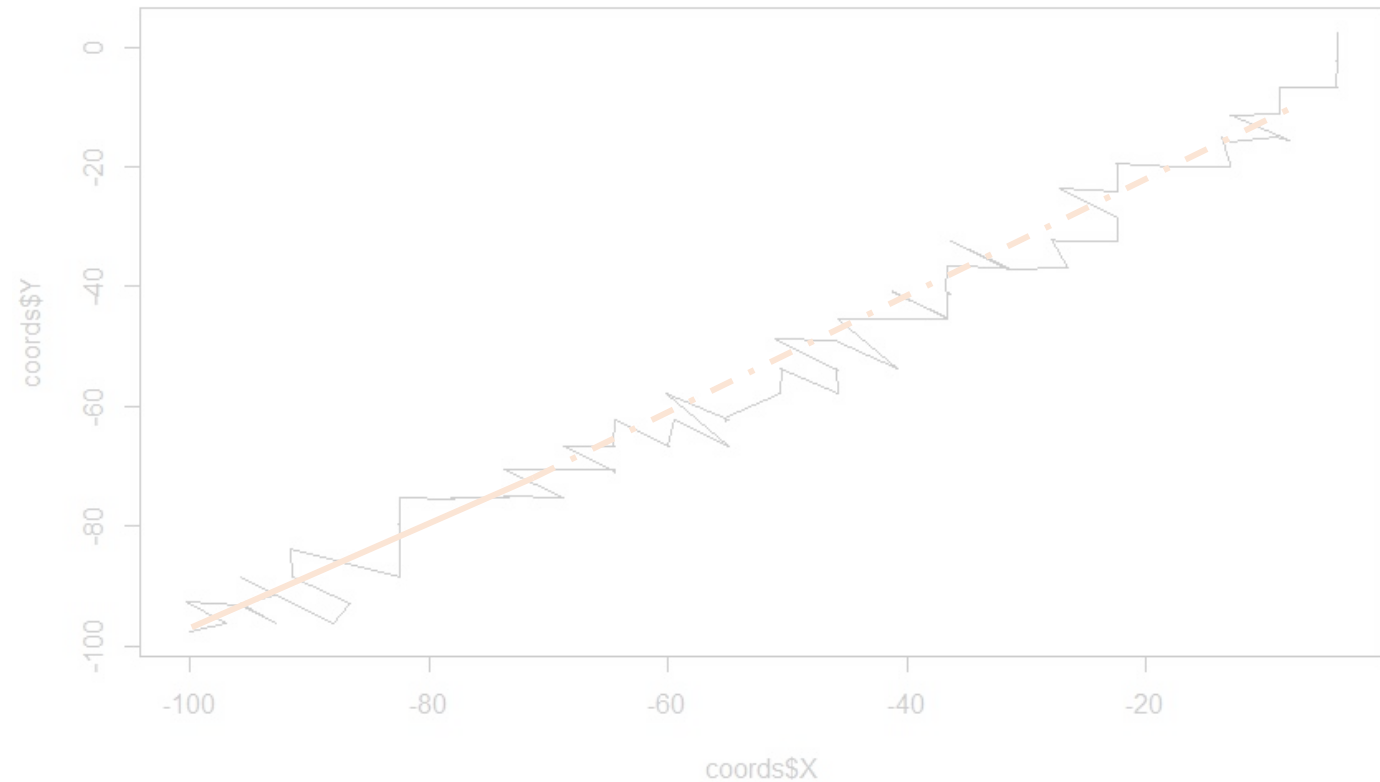
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- \* crossoverRate: 0.25
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- \* maxIterations: 1000
- \* DeltaMin: 0.00000001
- \* MutationFactor: 0.2
- \* Strategy: apply the genetic operators with the given probabilities to all solutions, select best afterwards



# \$ Configuration #3 – start at (-100, -100)

- \* Population size: 100
- \* Heredity: R1
- \* Crossover: 0.5
- \* Mutation: 0.2
- \* Max iterations: 1000
- \* Delta Mutation: 0.01
- \* Mutation Factor: 0.2



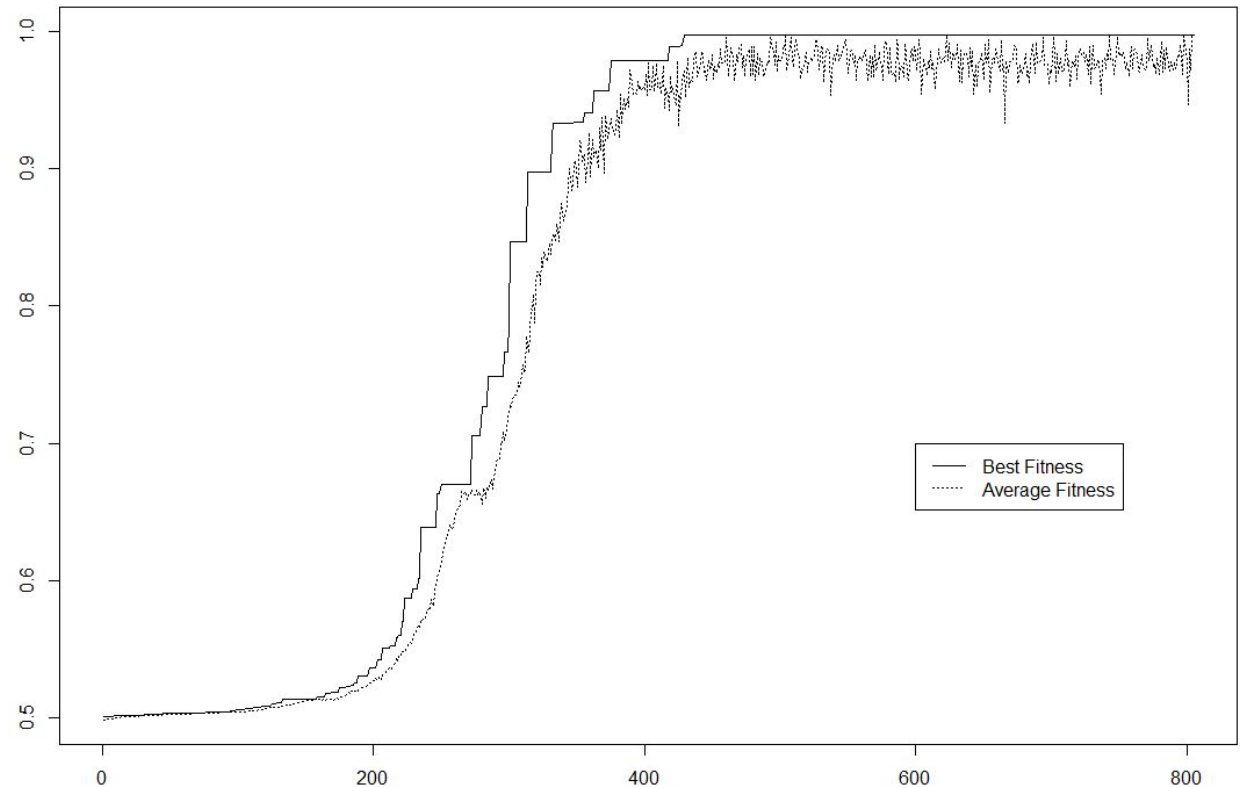
- \* Strategy: apply the genetic operators with the given probabilities to all solutions, select best afterwards



# \$ Configuration #4 – start at (-100, -100)

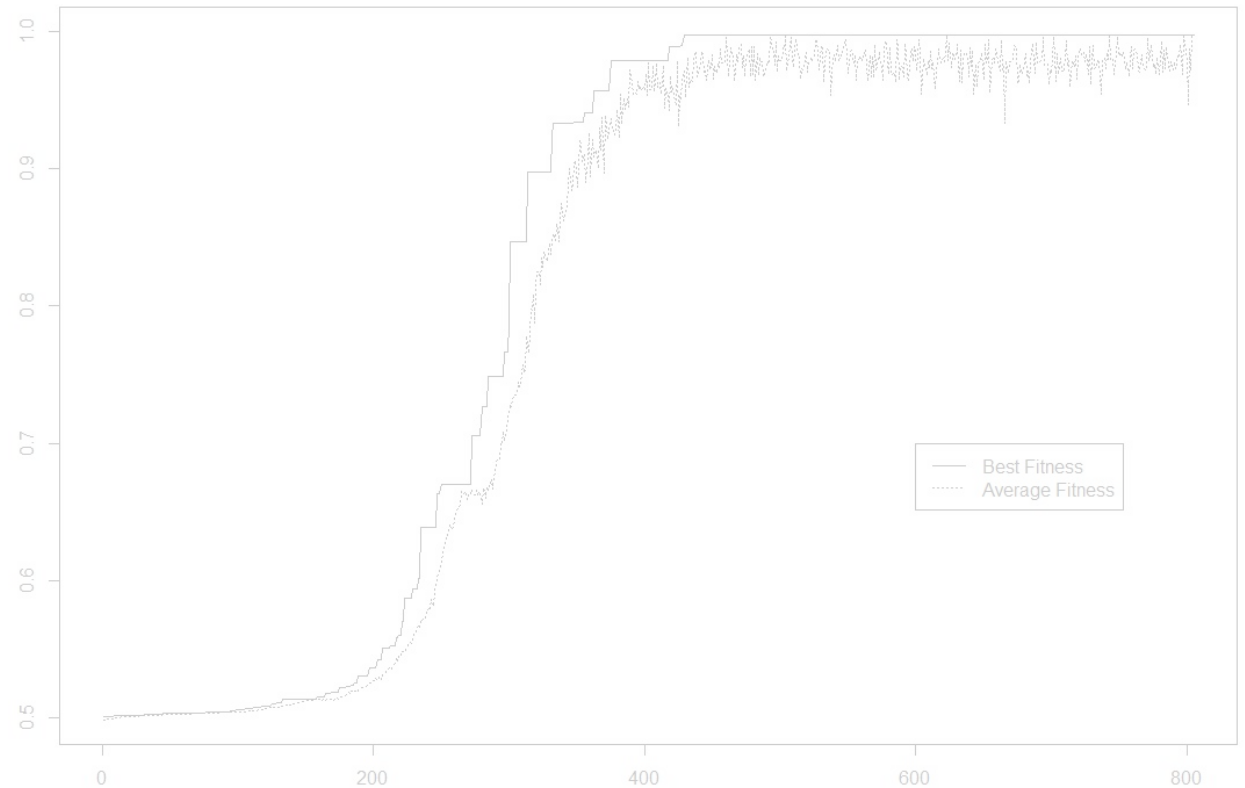
- \* Population size: 20
- \* heredityRate: 0.1
- \* crossoverRate: 0.25
- \* mutationRate: 0.25
- \* maxIterations: 1000
- \* DeltaMin: 0.0000001
- \* MutationFactor: 0.2

\* Strategy: apply the genetic operators with the given probabilities to the top 20% of solutions, select best



# \$ Configuration #4 – start at (-100, -100)

- \* PopulationSize: 100
- \* hereditarian: 0.5
- \* crossover: 0.5
- \* mutation: 0.001
- \* maxIterations: 1000
- \* DeltaMethod: DeltaMethod
- \* MutationFactor: 0.2

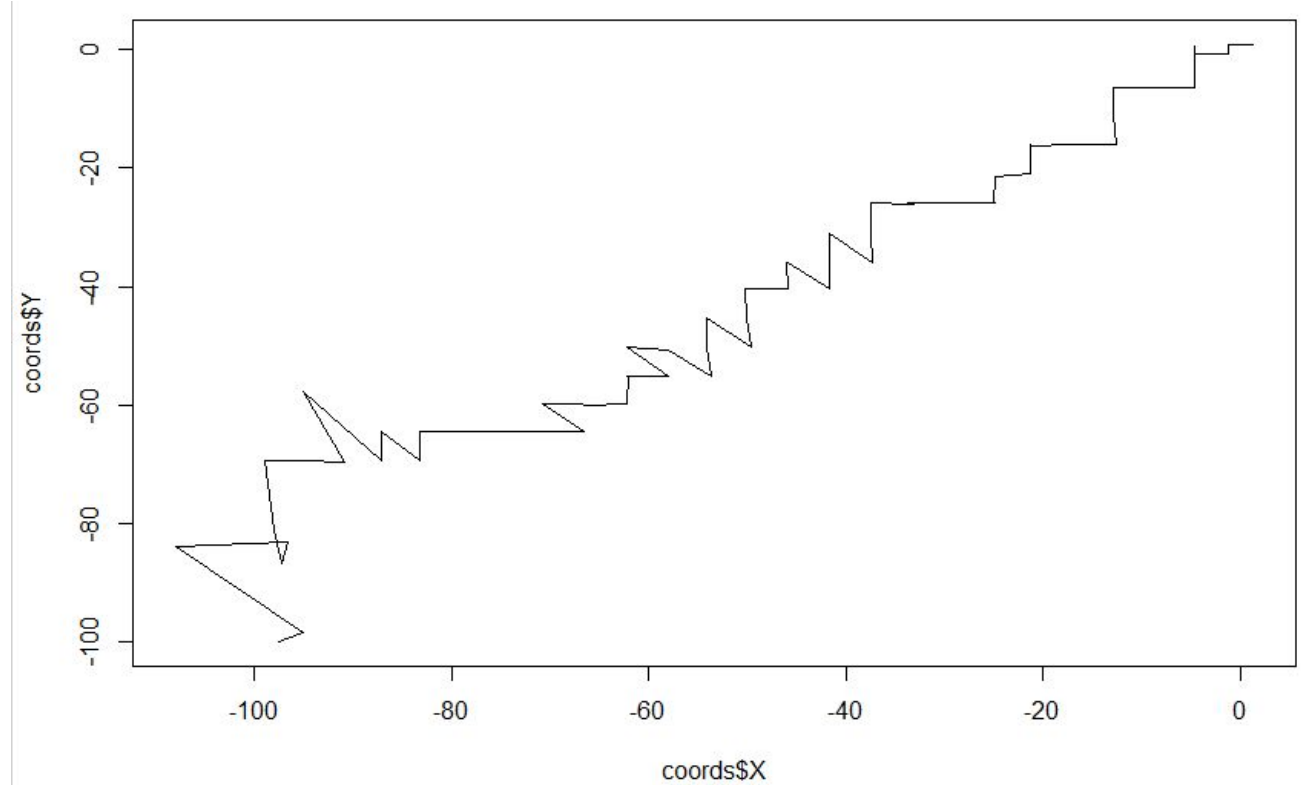


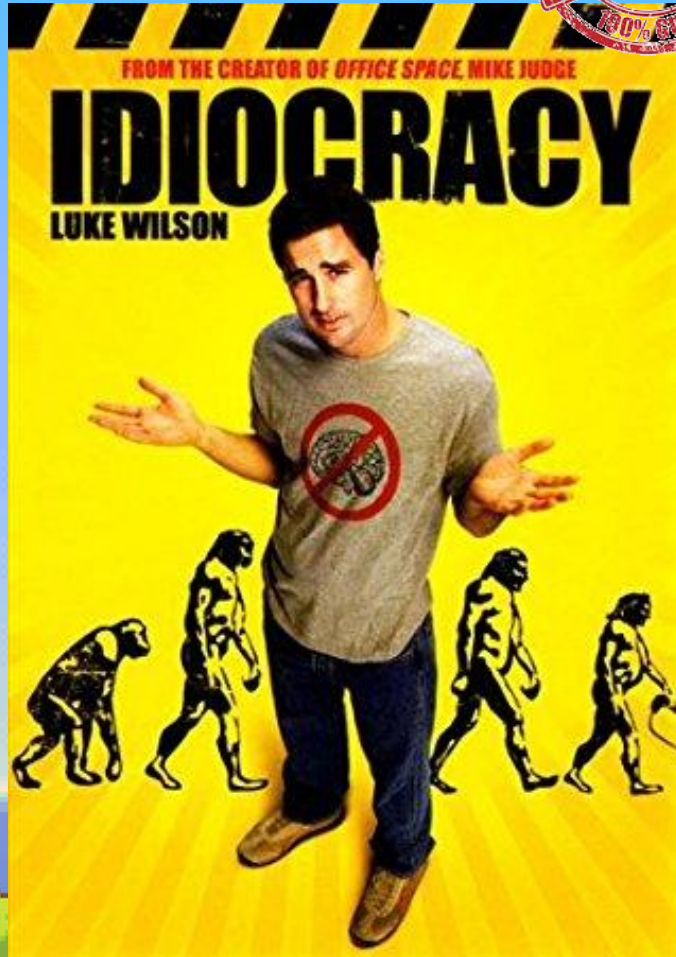
- \* Strategy: apply the genetic operators with the given probabilities to the top 20% of solutions, select best

# \$ Configuration #4 – start at (-100, -100)

- \* Population size: 20
- \* heredityRate: 0.1
- \* crossoverRate: 0.25
- \* mutationRate: 0,25
- \* maxIterations: 1000
- \* DeltaMin: 0,00000001
- \* MutationFactor: 0,2

\* Strategy: apply the genetic operators with the given probabilities to the top 20% of solutions, select best





“A very educational movie, addressing the importance of proper selection strategies and genetic diversity towards the successful evolution of species. And a wake up call to our own evolution!”

- *Davide Carneiro*





# \$ Quest #3

•

$$Ch = \begin{bmatrix} V_{1,1} & \cdots & V_{1,n} \\ \vdots & \ddots & \vdots \\ V_{m,1} & \cdots & V_{m,n} \end{bmatrix}$$

$$Ch = \begin{matrix} & \begin{matrix} P1 & & P2 \end{matrix} \\ \begin{matrix} P3 \\ 1 \\ 0,1 \end{matrix} & \begin{bmatrix} 0,2 & 0,3 & 0,5 \\ 1 & 0 & 0 \\ 0,1 & 0,8 & 0,1 \end{bmatrix} \end{matrix}$$



$$P = \left[ Ch_1 = \begin{bmatrix} V_{1,1} & \cdots & V_{1,n} \\ \vdots & \ddots & \vdots \\ V_{m,1} & \cdots & V_{m,n} \end{bmatrix} \quad Ch_2 = \begin{bmatrix} V_{1,1} & \cdots & V_{1,n} \\ \vdots & \ddots & \vdots \\ V_{m,1} & \cdots & V_{m,n} \end{bmatrix} \quad \dots \quad Ch_s = \begin{bmatrix} V_{1,1} & \cdots & V_{1,n} \\ \vdots & \ddots & \vdots \\ V_{m,1} & \cdots & V_{m,n} \end{bmatrix} \right]$$

$$\begin{aligned} V_{m,n} &\in A, \quad A = \{x \in \mathbb{R} \mid 0 \leq x \leq 1\} \\ \sum_{i=1}^n V_{m,i} &= 1, \forall m \in \{1, 2, \dots, m\} \\ R_n &= \sum_{i=1}^m V_{m,i} \\ V_{m,i} = 1 &\Rightarrow V_{m,x} = 0, \forall x \in \{1, 2, \dots, n\}, x \neq i \end{aligned}$$

# \$ Quest #3

•

$$Ch = \begin{bmatrix} V_{1,1} & \cdots & V_{1,n} \\ \vdots & \ddots & \vdots \\ V_{m,1} & \cdots & V_{m,n} \end{bmatrix} \quad Ch = \begin{bmatrix} P1 & P2 \\ 0,2 & 0,3 & 0,5 \\ 1 & 0 & 0 \\ 0,1 & 0,8 & 0,1 \end{bmatrix}$$



$$P = \begin{bmatrix} Ch_1 = \begin{bmatrix} V_{1,1} & \cdots & V_{1,n} \\ \vdots & \ddots & \vdots \\ V_{m,1} & \cdots & V_{m,n} \end{bmatrix} & Ch_2 = \begin{bmatrix} V_{1,1} & \cdots & V_{1,n} \\ \vdots & \ddots & \vdots \\ V_{m,1} & \cdots & V_{m,n} \end{bmatrix} & \cdots & Ch_s = \begin{bmatrix} V_{1,1} & \cdots & V_{1,n} \\ \vdots & \ddots & \vdots \\ V_{m,1} & \cdots & V_{m,n} \end{bmatrix} \end{bmatrix}$$

$$V_{m,n} \in A, \quad A = \{x \in \mathbb{R} \mid 0 \leq x \leq 1\}$$

$$\sum_{i=1}^n V_{m,n} = 1, \forall m \in \{1, 2, \dots, m\}$$

$$R_n = \sum_{i=1}^m V_{m,n}$$

$$V_{m,i} = 1 \Rightarrow V_{m,x} = 0, \forall x \in \{1, 2, \dots, n\}, x \neq i$$



# \$ Quest #3

GeNeg

**General Information**

Max Generations: 10

Population: 100

Best Individuals: 5

Species: 2

**Genetic Operators**

Crossover: 10 \* 2 = 20

Heredity: 10 \* 2 = 20

Mutation: 30 \* 2 = 60

Total: 100

**Issues**

☐ Use Default ☒ Use Custom

Issue Name:

Value:

☐ Indivisible

**Parties**

☐ Use Default ☒ Use Custom

PartyID:

**Preferences**

House  John   Points  Points Remaining: 100

**Options**

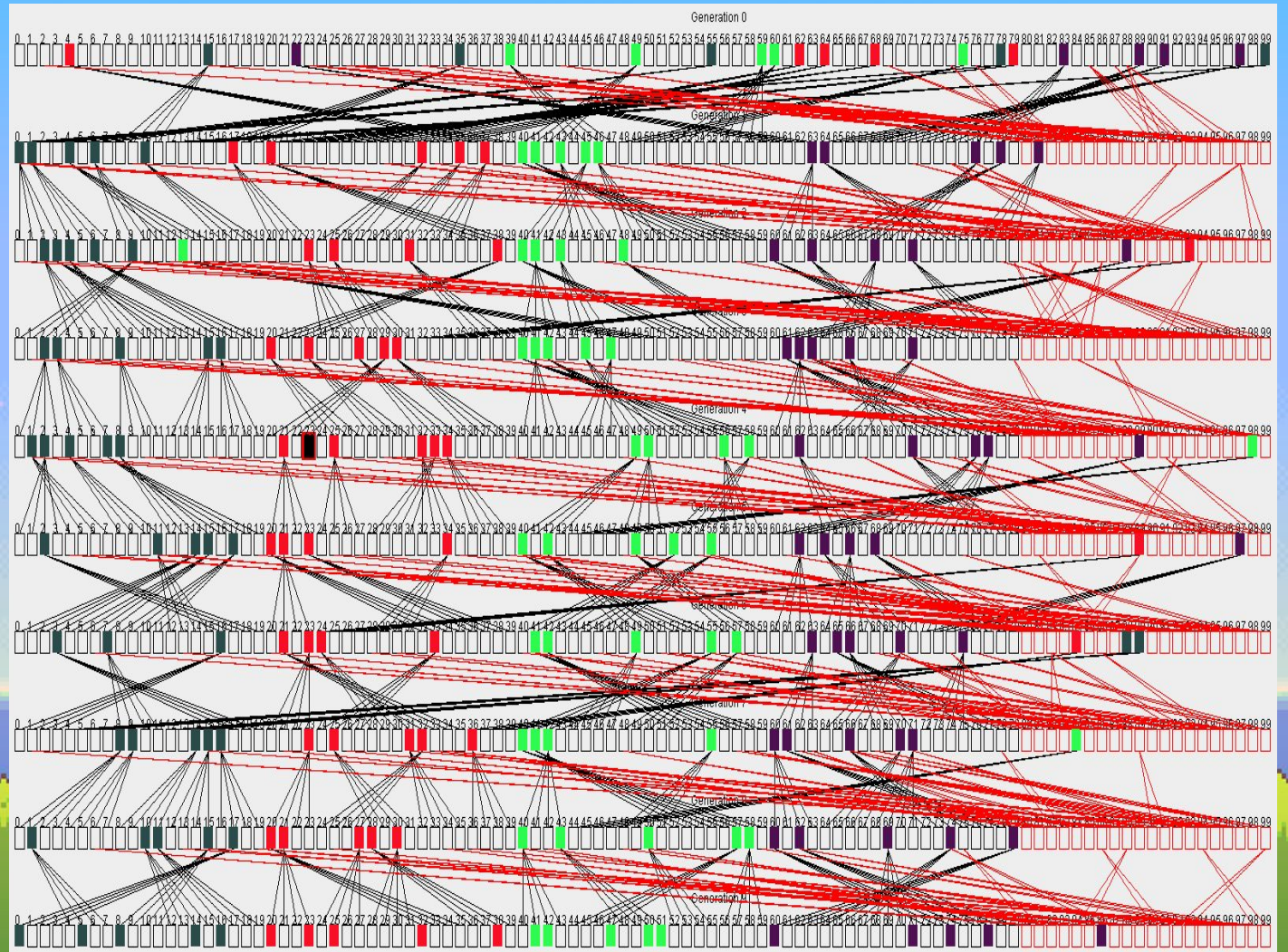
☒ Allow Inter Species

☒ Random Crossovers

☐ Verbose

**Fitness Function**

Personal Value  Monetary Value





# \$ Quest #3

GeNeg

**General Information**

Max Generations: 10

Population: 100

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**Genetic Operators**

Crossover: 10 \* 2 = 20

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Mutation: 30 \* 2 = 60

Total: 100

**Issues**

☐ Use Default ☒ Use Custom

Issue Name:

Value:

☐ Indivisible

**Parties**

☐ Use Default ☒ Use Custom

PartyID:

**Preferences**

House:  John:  Points:  Points Remaining: 100

**Options**

☒ Allow Inter Species

☒ Random Crossovers

☐ Verbose

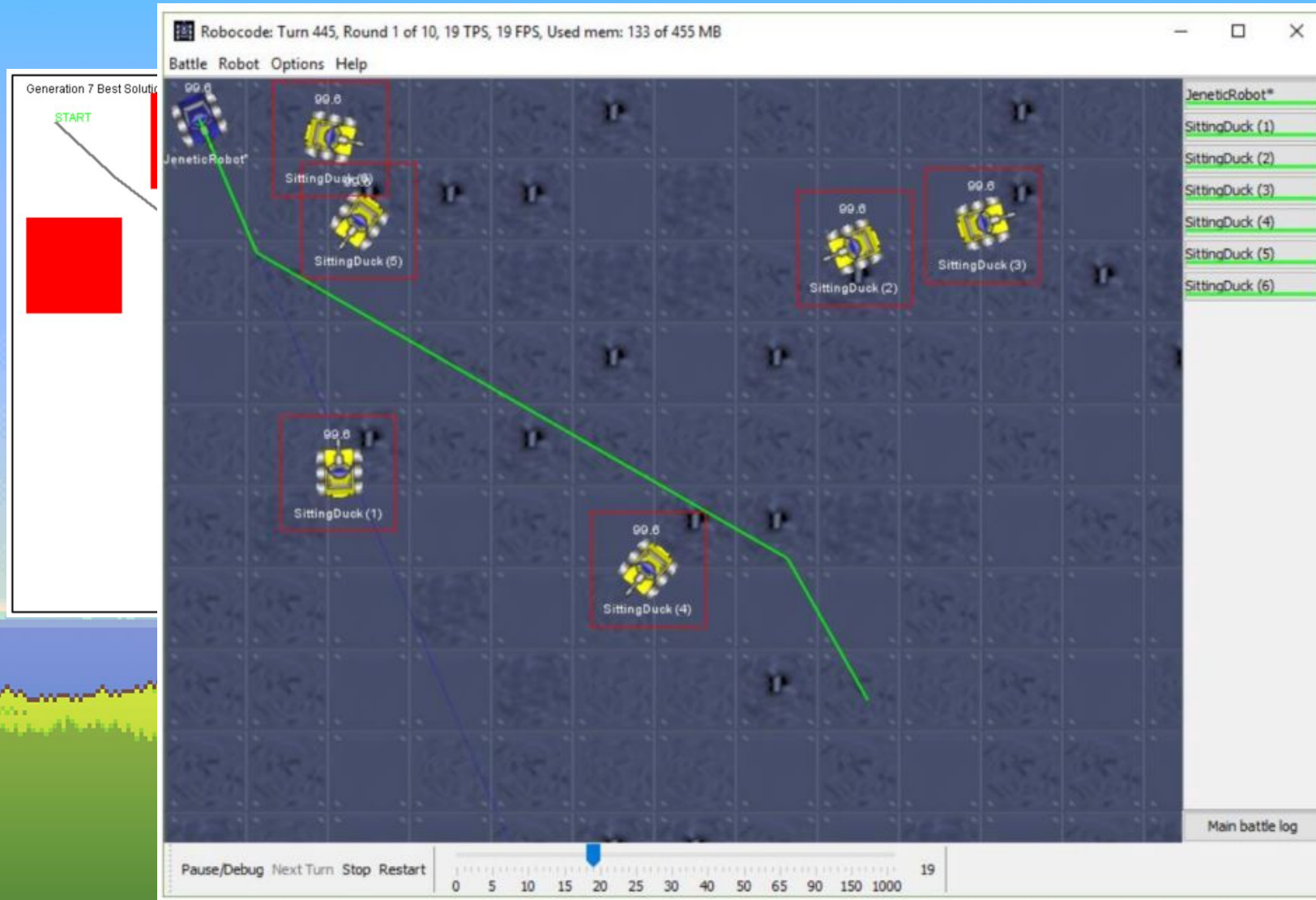
**Fitness Function**

Personal Value  Monetary Value

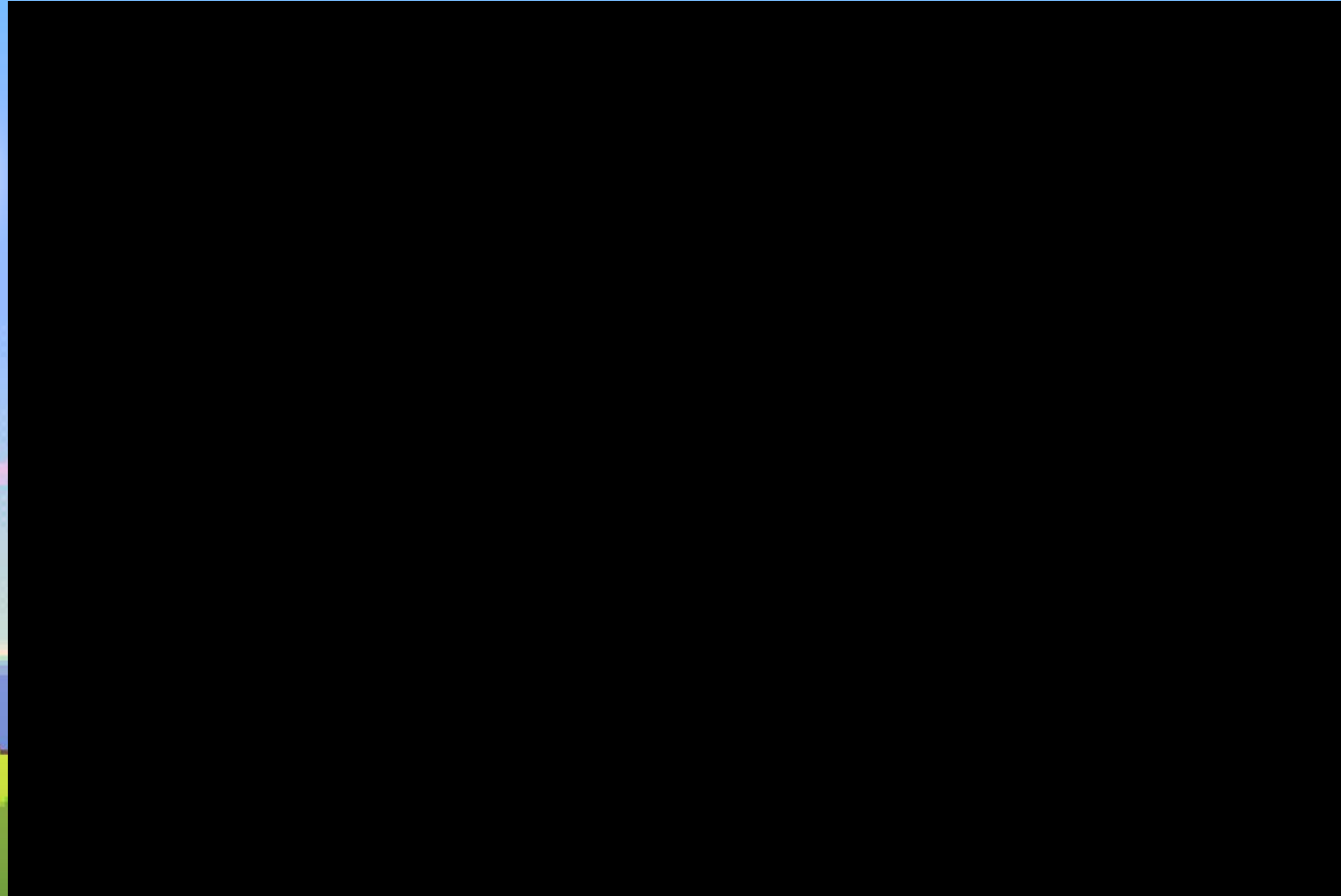




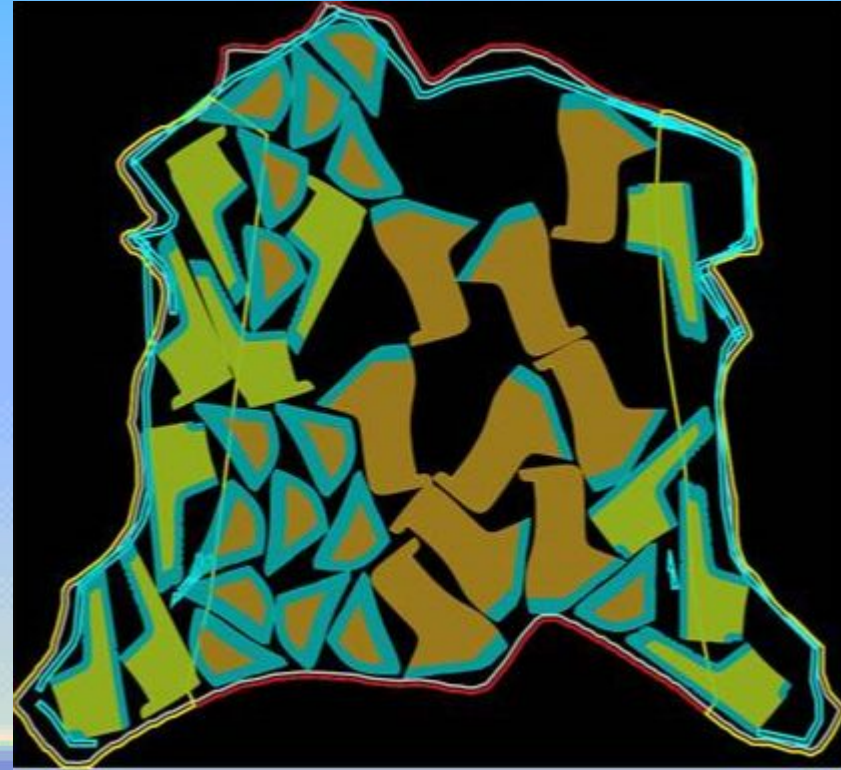
# \$ Quest #4



# \$ Quest #5



# \$ Quest #6





# \$ Quest #7



# TL;DR



- \* Does not need a lot of domain knowledge
- \* It's often faster and more efficient than traditional methods
- \* Is easily parallelized and/or distributed
- \* Optimizes both discrete and continuous functions
- \* Finds multiple “good” solutions
- \* Always finds a solution
- \* Useful when the search space is multi-dimensional and very large



- \* Cannot be applied to every problem
- \* Efficiency depends significantly on the fitness function
- \* Does not guarantee optimum solutions nor the quality of the solution found
- \* May not converge to the optimum solution
- \* Has the disadvantage of gradient search methods



# TL;DR



- \* Does not need a lot of domain knowledge
- \* It's **local optimum** more efficient than traditional methods

- \* Is easily parallelized and/or distributed

- \* Optimizes both discrete and continuous functions

- \* Finds multiple "good" solutions

- \* Always a solution

with sparse

by l

global optimum

- \* Cannot be applied to every problem

- \* Efficiency depends significantly on the fitness

- \* Does not guarantee optimum solution

- \* Quality of the solution depends on the optimum

- \* Gradient

start here!



# ~ Genetic Algorithms ~

## In Search of the Missing Solution

A row of pixel art clouds in white and light blue against a dark blue background.

Daide Carneiro

A row of pixel art grass in light green and dark green against a dark blue background.

Game Over!