STAI30 - Class #2:

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Today's Class

- Histograms and density functions
- Statistical data
- Data wrangling
- Tidy data

Histograms and Density Functions

Histograms and Density Functions

- The histogram of a variable is a graphical method to vizualize the distribution of a single variable.
- To construct a basic histogram:
 - I. Divide the data into intervals (called bins).
 - 2. Count the number of observations that are contained in the bin.
 - 3. Plot rectangles with height equal to the count from (2) and width equal to the width of the bin.

Histograms and Density Functions

Different bin width will yield different histograms

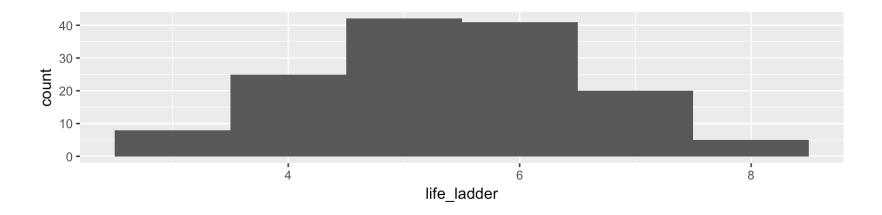
```
p1 <- ggplot(data = happinessdata2016, aes(x = life_ladder)) +
    geom_histogram(binwidth = 0.1)
p2 <- ggplot(data = happinessdata2016, aes(x = life_ladder)) +
    geom_histogram(binwidth = 1.0)

ggplot_build(p2)</pre>
```

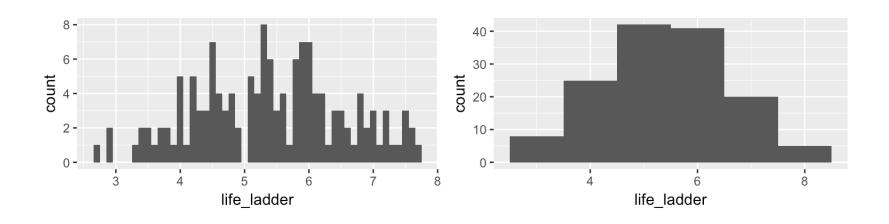
```
## $data
## $data[[1]]
     y count x xmin xmax
                             density
                                        ncount ndensity PANEL group ymin
           8 3 2.5 3.5 0.05673759 0.1904762 26.85714
                                                                  -1
           25 4
                3.5 4.5 0.17730496 0.5952381
                                                83.92857
           42 5
                     5.5 0.29787234 1.0000000 141.00000
                                                                  -1
                     6.5 0.29078014 0.9761905 137.64286
                                                                  -1
           41 6
## 5 20
           20 7
                     7.5 0.14184397 0.4761905 67.14286
                                                                  -1
                 6.5
                7.5 8.5 0.03546099 0.1190476 16.78571
                                                                  -1
                  fill size linetype alpha
     ymax colour
       8
             NA grey35
## 1
                        0.5
                                         NA
             NA grey35
      25
                        0.5
                                         NA
      42
             NA grey35
                       0.5
                                         NA
             NA grey35 0.5
      41
                                         NA
             NA grey35 0.5
## 5
      20
                                         NA
             NA grey35 0.5
## 6
        5
                                         NA
##
##
## $layout
## <qqproto object: Class Layout>
```

```
##
       facet: <ggproto object: Class FacetNull, Facet>
##
           compute layout: function
##
           draw back: function
##
           draw front: function
##
           draw labels: function
##
           draw panels: function
##
           finish data: function
##
           init scales: function
##
           map: function
##
           map data: function
##
           params: list
##
           render back: function
##
           render front: function
##
           render panels: function
##
           setup data: function
##
           setup params: function
##
           shrink: TRUE
##
           train: function
##
           train positions: function
##
           train scales: function
##
           vars: function
##
           super: <ggproto object: Class FacetNull, Facet>
##
       finish data: function
##
       get scales: function
##
       map: function
##
       map position: function
##
       panel layout: data.frame
##
       panel ranges: list
##
       panel scales: list
##
       render: function
##
       render labels: function
##
       reset scales: function
##
       setup: function
##
       train position: function
       train ranges: function
##
##
       xlabel: function
```

```
## ylabel: function
## super: <ggproto object: Class Layout>
##
## $plot
```



grid.arrange(p1,p2,nrow = 1)



Mathematical Definition of Histogram

■ The bins of the histogram are the intervals:

$$[x_0 + mh, x_0 + (m+1)h).$$

 x_0 is the origin, $m = \dots, -1, 0, 1, \dots$ indexes the bins, and $h = (x_0 + (m+1)h) - (x_0 + mh)$ is the bin width.

Example - Mathematical Definition of Histogram

```
dat <- data_frame(x = c(1,2,2.5,3,7))
dat$x
```

```
[1] 1.0 2.0 2.5 3.0 7.0
```

```
Let x_0 = 0.5, h = 0.25, m = 1, ..., 29
```

```
seq(0.5,7.5,by = 0.25)
```

```
[1] 0.50 0.75 1.00 1.25 1.50 1.75 2.00 2.25 2.50 2.75 3.00 3.25 3.50 3.75 [15] 4.00 4.25 4.50 4.75 5.00 5.25 5.50 5.75 6.00 6.25 6.50 6.75 7.00 7.25 [29] 7.50
```

The bins are: $[0.50, 0.75), [0.75, 1.00), [1.00, 1.25), \dots, [7.25, 7.50).$

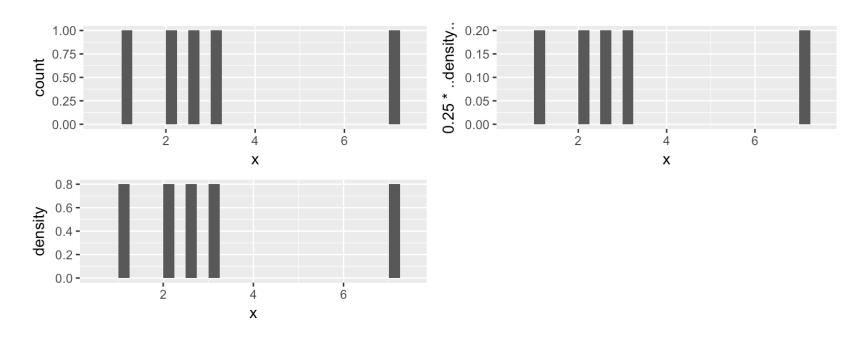
Example - Mathematical Definition of Histogram

- The bins can be used to construct rectangles with width h=0.25 and height y.
- y will be called density.
- The area of these rectangles is hy.
- We would like the area of these rectangles, hy, to be the same as the proportion of data in the bin. This will make the sum of all areas equal 1.
- Let n be the number of observations. Then,

$$hy = \frac{\#\{X_i \text{ in bin}\}}{n}$$

■ In this example, n = 5, and $X_1 = 1, X_2 = 2, X_3 = 2.5, X_4 = 3, X_5 = 7$.

Example - Mathematical Definition of Histogram



Mathematical Definition of Histogram

$$\hat{f}(x) = \frac{1}{hn} \#\{X_i \text{ in same bin as } x\}$$

is called the **histogram estimator**.

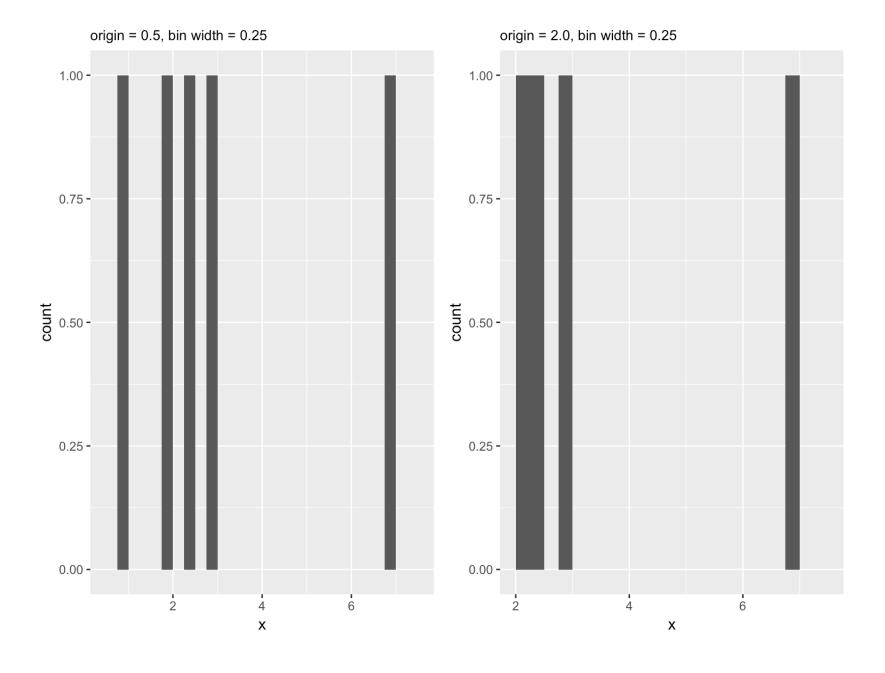
 $\hat{f}(x)$ is an estimate of the density at a point x.

To construct the histogram we have to choose an origin x_0 and bin width h.

Choosing Origin and Bin Width in R

Same bin width but different origin

```
dat <- data_frame(x = c(1,2,2.5,3,7))
p0.5 <- ggplot(data = dat, aes(x = x)) +
    geom_histogram(breaks = seq(0.5,7.5,.25)) +
    labs(subtitle = "origin = 0.5, bin width = 0.25")
p2 <- ggplot(data = dat, aes(x = x)) +
    geom_histogram(breaks = seq(2,7.5,.25)) +
    labs(subtitle = "origin = 2.0, bin width = 0.25")
grid.arrange(p0.5,p2,nrow = 1)</pre>
```



Statistical data

What is statistical data?

- Statistical data is obtained by observing (random) variables.
- A random variable can be given a precise mathematical definition that we will cover later in the course.
- In this class we will discuss examples.

Observing a few variables on STA130 students

- What is your height?
- How many years have been at UofT?
- What is your sex (male or female)?

Collecting this data will generate three variables: height, years, and sex.

Enter variables on STA 130 students

```
height <- c()
years <- c()
sex <- c()
```

Put the variables into an R data frame.

NB: data_frame is the tidyverse version of base R data.frame.

```
sta130_dat <- data_frame(height, years, sex)
```

We could have entred this in a spreadsheet program like MS Excel, saved it as a CSV file, then imported the file into R.

Tidy data

Tidy data

There are three interrelated rules which make a dataset tidy:

- I. Each variable must have its own column.
- 2. Each observation must have its own row.
- 3. Each value must have its own cell.

```
## # A tibble: 6 x 4
## country year cases population
## <chr> <int> <int> <int> <int>
## 1 Afghanistan 1999 745 19987071
## 2 Afghanistan 2000 2666 20595360
## 3 Brazil 1999 37737 172006362
## 4 Brazil 2000 80488 174504898
## 5 China 1999 212258 1272915272
## 6 China 2000 213766 1280428583
```

```
## # A tibble: 6 x 3

## country year rate

## * <chr> <int> <chr>
## 1 Afghanistan 1999 745/19987071

## 2 Afghanistan 2000 2666/20595360

## 3 Brazil 1999 37737/172006362

## 4 Brazil 2000 80488/174504898

## 5 China 1999 212258/1272915272

## 6 China 2000 213766/1280428583
```

Tidy data

"For a given dataset, it is usually easy to figure out what are observations and what are variables, but it is surprisingly difficult to precisely define variables and observations in general." (Wickham, 2014)

A general rule of thumb:

- It is easier to describe functional relationships between variables (e.g., z is a linear combination of x and y, density is the ratio of weight to volume) than between rows.
- It is easier to make comparisons between groups of observations (e.g., average of group a vs. average of group b) than between groups of columns.

(Wickham, 2014)

Data wrangling

Data wrangling

- The ggplot library implements a grammer of graphics.
- Similarily the dplyr library presents a grammer for data wrangling.

The Economic Guide to Picking a Major

FiveThirtyEight

Politics Sports

Science & Health

Economics

Culture

SEP. 12, 2014 AT 7:37 AM

The Economic Guide To Picking A College Major

By Ben Casselman

Filed under <u>Higher Education</u>
Get the data on **GitHub**





Students walk across the campus of UCLA in Los Angeles. KEVORK DJANSEZIAN / GETTY IMAGES

"...A college degree is no guarantee of economic success. But through their choice of major, they can take at least some steps toward boosting their odds."

The Economic Guide to Picking a Major

- The data used in the article is from the American Community Survey 2010-2012 Public Use Microdata Series.
- We can use the fivethirtyeight library in R.

Data behind the article

```
# uncomment this next line if fivethirtyeight lib is not installed
# install.packages("fivethirtyeight")
library(fivethirtyeight) # load the library
glimpse(college_recent_grads)
```

```
## Observations: 173
## Variables: 21
                                 <int> 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11,...
## $ rank
## $ major code
                                 <int> 2419, 2416, 2415, 2417, 2405, 2418...
                                 <chr> "Petroleum Engineering", "Mining A...
## $ major
## $ major category
                                 <chr> "Engineering", "Engineering", "Eng...
                                 <int> 2339, 756, 856, 1258, 32260, 2573,...
## $ total
                                 <int> 36, 7, 3, 16, 289, 17, 51, 10, 102...
## $ sample size
## $ men
                                 <int> 2057, 679, 725, 1123, 21239, 2200,...
                                 <int> 282, 77, 131, 135, 11021, 373, 960...
## $ women
## $ sharewomen
                                 <dbl> 0.1205643, 0.1018519, 0.1530374, 0...
## $ employed
                                 <int> 1976, 640, 648, 758, 25694, 1857, ...
## $ employed fulltime
                                 <int> 1849, 556, 558, 1069, 23170, 2038,...
## $ employed parttime
                                 <int> 270, 170, 133, 150, 5180, 264, 296...
## $ employed fulltime yearround <int> 1207, 388, 340, 692, 16697, 1449, ...
## $ unemployed
                                 <int> 37, 85, 16, 40, 1672, 400, 308, 33...
## $ unemployment rate
                                 <dbl> 0.018380527, 0.117241379, 0.024096...
## $ p25th
                                 <dbl> 95000, 55000, 50000, 43000, 50000,...
                                 <dbl> 110000, 75000, 73000, 70000, 65000...
## $ median
                                 <dbl> 125000, 90000, 105000, 80000, 7500...
## $ p75th
## $ college jobs
                                 <int> 1534, 350, 456, 529, 18314, 1142, ...
                                 <int> 364, 257, 176, 102, 4440, 657, 314...
## $ non college jobs
## $ low wage jobs
                                 <int> 193, 50, 0, 0, 972, 244, 259, 220,...
```

Select variables/columns using select()

To retrieve a data frame with only major, number of male and female graduates we use the select() function in the dplyr library.

```
select(college_recent_grads,major, men,women)
```

```
# A tibble: 173 x 3
##
                                          major
                                                   men women
##
                                          <chr> <int> <int>
                          Petroleum Engineering
                                                  2057
                                                         282
                 Mining And Mineral Engineering
                                                  679
                                                         77
                      Metallurgical Engineering
                                                  725
                                                         131
    4 Naval Architecture And Marine Engineering
                                                  1123
                                                         135
                           Chemical Engineering 21239 11021
##
    5
##
                            Nuclear Engineering
                                                 2200
                                                         373
                              Actuarial Science
                                                   832
                                                         960
                     Astronomy And Astrophysics
                                                  2110
                                                       1667
                         Mechanical Engineering 12953
                                                        2105
                         Electrical Engineering
                                                 8407
                                                        6548
     ... with 163 more rows
```

Select observations/rows using filter()

If we want to retrieve only those observations (rows) that pertain to engineering majors then we need to specify that the value of the major variable is Electrical Engineering.

```
EE <- filter(college_recent_grads, major == "Electrical Engineering")
glimpse(EE)</pre>
```

```
## Observations: 1
## Variables: 21
## $ rank
                                 <int> 10
## $ major code
                                 <int> 2408
## $ major
                                 <chr> "Electrical Engineering"
## $ major category
                                 <chr> "Engineering"
## $ total
                                 <int> 81527
## $ sample size
                                 <int> 631
## S men
                                 <int> 8407
                                 <int> 6548
## $ women
## $ sharewomen
                                 <dbl> 0.4378469
## $ employed
                                 <int> 61928
## $ employed fulltime
                                 <int> 55450
## $ employed parttime
                                 <int> 12695
## $ employed fulltime yearround <int> 41413
## $ unemployed
                                <int> 3895
## $ unemployment rate
                                 <dbl> 0.05917385
## $ p25th
                                 <db1> 45000
## $ median
                                 <dbl> 60000
## $ p75th
                                 <db1> 72000
```

NB: == is a test for equality and is different than =.

Combine select() and filter()

- We can drill down to get certain pieces of information using filter() and select() together.
- The median variable is median salary.

select(filter(college_recent_grads, median >= 60000), major, men, women)

(1) Which students, and (2) variables are in this data frame?

Respond at **PollEv.com/nathantaback**

Text NATHANTABACK to 37607 once to join, then A, B, C, D, or E

(1) All students in the original data set; (2) all variables in the data set.

(1) All students in the original data set in a major where the median

salary is at most than 60,000; (2) all variables in the data set.

(1) All students in the original data set in a major where the median salary is at least than 60,000; (2) all variables in the data set.

(1) All students in the original data set in a major where the median salary is at least than 60,000; (2) three variables: major, men, women

(1) All students in the original data set in a major where the median salary is at least than 60,000; (2) all variables in the data set.

E

The pipe operator %>%

In the code:

```
select(filter(college_recent_grads, median >= 60000), major,men,women)
```

filter is nested inside select.

The pipe operator allows is an alternative to nesting and yields easier to read code. The same expression can be written with the pipe operator

```
college_recent_grads %>%
  filter(median >= 60000) %>%
  select(major, men, women)
```

Create new variables from existing variables using mutate()

What percentage of graduates from each major where the median earnings is at least \$60,000 are men?

```
college_recent_grads %>%
  filter(median >= 60000) %>%
  select(major, men, women) %>%
  mutate(total = men + women, pct_male = round((men / total)*100, 2))
```

Compare to nested code:

Create new variables from existing variables using mutate()

major	men	women	total	pct_male
Petroleum Engineering	2057	282	2339	87.94
Mining And Mineral Engineering	679	77	756	89.81
Metallurgical Engineering	725	131	856	84.70
Naval Architecture And Marine Engineering	1123	135	1258	89.27
Chemical Engineering	21239	11021	32260	65.84
Nuclear Engineering	2200	373	2573	85.50
Actuarial Science	832	960	1792	46.43
Astronomy And Astrophysics	2110	1667	3777	55.86
Mechanical Engineering	12953	2105	15058	86.02
Electrical Engineering	8407	6548	14955	56.22
Computer Engineering	33258	8284	41542	80.06

Aerospace Engineering	65511	16016 81527	80.35
Biomedical Engineering	80320	10907 91227	88.04
Materials Science	2949	1330 4279	68.92

Create new variables from existing variables using mutate()

- Suppose that we would like to create a categorical variable to identify majors with 45% and 55% women (ie., approximately equal numbers of males and females).
- We can use ifelse() in a mutate() statement.

```
college_recent_grads %>%
  select(major, men, women) %>%
  mutate(total = men + women, pct_female = round((women / total)*100, 2),
       male.bias = ifelse(pct_female >= 45 & pct_female <= 55, "No", "Yes")) %>%
  select(major,male.bias)
```

```
# A tibble: 173 x 2
##
                                           major male.bias
##
                                           <chr>>
                                                      <chr>
                           Petroleum Engineering
                                                        Yes
                 Mining And Mineral Engineering
                                                        Yes
##
                      Metallurgical Engineering
                                                        Yes
##
    4 Naval Architecture And Marine Engineering
                                                        Yes
                            Chemical Engineering
    5
                                                        Yes
                             Nuclear Engineering
                                                        Yes
                               Actuarial Science
                                                         No
                     Astronomy And Astrophysics
                                                        Yes
                         Mechanical Engineering
                                                        Yes
                         Electrical Engineering
                                                        Yes
```

Rename variables using rename ()

- It's considered bad practice in R to use periods in variable names.
- We can use rename() to change the name of sex.equal to sex_equal.

Sort a data frame using arrange()

```
my_college_dat %>%
  arrange(salary_median) %>%
  select(major, salary_median) %>%
  arrange(desc(salary_median))
```

```
## # A tibble: 173 x 2
##
                                           major salary median
##
                                           <chr>>
                                                          <db1>
##
                          Petroleum Engineering
                                                         110000
##
                 Mining And Mineral Engineering
                                                          75000
##
                      Metallurgical Engineering
                                                          73000
   4 Naval Architecture And Marine Engineering
                                                          70000
##
                           Chemical Engineering
                                                          65000
##
                             Nuclear Engineering
                                                          65000
                               Actuarial Science
                                                          62000
                     Astronomy And Astrophysics
                                                          62000
##
                         Mechanical Engineering
                                                          60000
                         Electrical Engineering
  10
                                                          60000
     ... with 163 more rows
```

Summarize a data frame using summarize()

The average number of female grads and the total number of majors in the data set.

```
college_recent_grads %>%
  select(major, men, women) %>%
  summarise(femgrad_mean = mean(women), N = n())
```

```
## # A tibble: 1 x 2
## femgrad_mean N
## <dbl> <int>
## 1 22530.36 173
```

Summarize groups in a data frame using summarize() and group_by()

The median salary in majors with 45%-55% female students.

```
my_college_dat %>%
  group_by(sex_equal) %>%
  summarise(median(salary_median))
```

Combining Multiple Tables

Sentiment of Trump's Tweets

- Donald Trump likes to tweet a lot.
- Some tweets have an angry sentiment or contain insults, and some are not.
- Trump supposedly used to send tweets from a Samsung Galaxy when he is insulting people, places, and things, from other devices such as an iPhone when he is not.
- Trump's last tweet from Android were March 25, 2017



Is Trump Still Tweeting From His Unsecured Android Phone?

If so, he's extremely vulnerable to being hacked.

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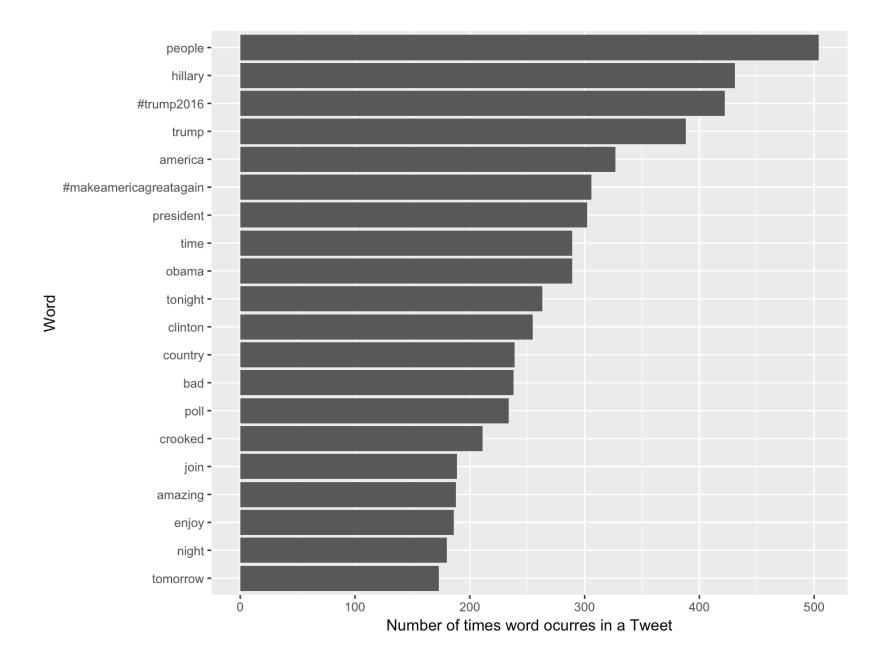
Trump's Tweets

A data frame with Trump's Tweets.

```
trumptweets <- read_csv("trumptweets.csv") #import from csv file
glimpse(trumptweets)</pre>
```

Trump's tweets

```
trumptweets %>%
  count(word) %>%
  mutate(word = reorder(word,n)) %>%
  top_n(20) %>%
  ggplot(aes(word, n)) + geom_col() + coord_flip() +
  labs(x = "Word",y = "Number of times word ocurres in a Tweet")
```



Sentiment Lexicon

- Several lexicons (dictionaries) have been developed that categorize words according to sentiment (feeling or emotion).
- The tidytext library contains several lexicons.

```
library(tidytext)
sentiments
```

```
# A tibble: 27,314 x 4
             word sentiment lexicon score
            <chr>
                      <chr>
                               <chr> <int>
           abacus
                      trust
                                 nrc
                                        NA
          abandon
                       fear
                                        NA
                                 nrc
      abandon
                   negative
                                        NA
                                 nrc
        abandon
                    sadness
                                 nrc
                                        NA
        abandoned
                                        NA
                      anger
                                 nrc
        abandoned
                       fear
                                 nrc
                                        NA
                   negative
        abandoned
                                 nrc
                                        NA
        abandoned
                    sadness
                                 nrc
                                        NA
    9 abandonment
                      anger
                                        NA
                                 nrc
  10 abandonment
                       fear
                                        NA
                                 nrc
## # ... with 27,304 more rows
```

NRC Lexicon

- The nrc lexicon categorizes words in a binary fashion ("yes"/"no") into categories of positive, negative, anger, anticipation, disgust, fear, joy, sadness, surprise, and trust.
- The getsentiments() function provides a way to get specific sentiment lexicons without the columns that are not used in that lexicon.

NRC Lexicon

```
get_sentiments("nrc")
```

```
## # A tibble: 13,901 x 2
            word sentiment
           <chr>
                     <chr>
          abacus
                     trust
      abandon
                      fear
      abandon
                  negative
        abandon
                   sadness
       abandoned
                     anger
       abandoned
                      fear
       abandoned
                  negative
       abandoned
##
                   sadness
   9 abandonment
                     anger
## 10 abandonment
                      fear
## # ... with 13,891 more rows
```

Sentiment of Words used in Tweets

- To examine the sentiment of the words Trump used in tweets we need to join the data frame containing the NRC lexicon and the data frame of Trump's words used in tweets.
- inner_join(x,y): return all rows from x where there are matching values in y, and all columns from x and y. If there are multiple matches between x and y, all combination of the matches are returned.

```
trumptweets %>% inner_join(get_sentiments("nrc"))
```

```
# A tibble: 33,043 x 5
                                      id str
                                                   word sentiment
    source
                     created at
     <chr>
                                       <db1>
                                                  <chr>>
                         <dttm>
                                                            <chr>
                                               terrific
 1 Android 2013-02-06 01:53:40 2.989727e+17
                                                          sadness
                                                    sky positive
 2 Android 2013-02-18 23:36:36 3.036492e+17
 3 Android 2013-02-18 23:36:36 3.036492e+17
                                                 rocket
                                                            anger
 4 Android 2013-02-18 23:36:36 3.036492e+17
                                               payback
                                                            anger
                                               payback
                                                        negative
 5 Android 2013-02-18 23:36:36 3.036492e+17
 6 Android 2013-02-19 00:25:48 3.036616e+17 surprised
                                                         surprise
 7 Android 2013-02-19 12:36:19 3.038455e+17
                                                   buss
                                                              iov
 8 Android 2013-02-19 12:36:19 3.038455e+17
                                                   buss
                                                         positive
```

```
## 9 Android 2013-02-19 12:36:19 3.038455e+17 friend joy
## 10 Android 2013-02-19 12:36:19 3.038455e+17 friend positive
## # ... with 33,033 more rows
```

Sentiment of Words used in Tweets

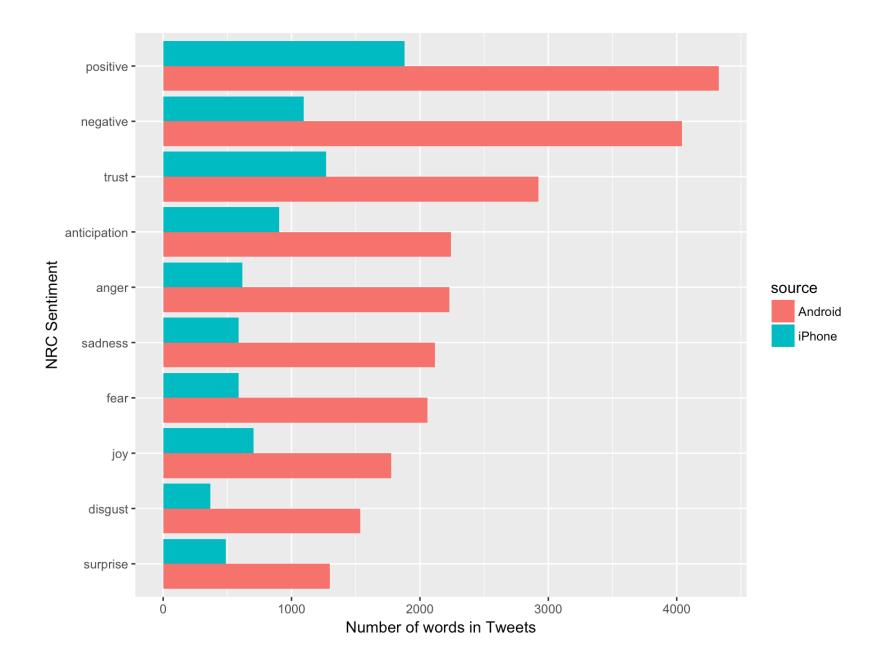
```
## Joining, by = "word"
```

```
\# A tibble: 20 x 4
## # Groups:
              sentiment [10]
##
         sentiment
                    source
                               n
                                   pct
             <chr>
                     <chr> <int> <dbl>
          disgust Android 1537 80.68
##
         negative Android
                           4040 78.68
##
           sadness Android
                          2117 78.32
##
             anger Android 2228 78.31
##
              fear Android 2057 77.80
##
          surprise Android 1297 72.70
##
               joy Android 1777 71.65
    8 anticipation Android
                           2240 71.25
##
          positive Android
                          4328 69.72
## 10
             trust Android
                           2924 69.70
## 11
             trust iPhone
                          1271 30.30
## 12
          positive iPhone 1880 30.28
  13 anticipation iPhone
                           904 28.75
## 14
                   iPhone
               joy
                           703 28.35
          surprise iPhone
                             487 27.30
## 15
## 16
              fear
                   iPhone
                             587 22.20
                          617 21.69
## 17
                   iPhone
             anger
## 18
           sadness
                  iPhone
                             586 21.68
## 19
          negative iPhone 1095 21.32
## 20
           disgust iPhone
                             368 19.32
```

Sentiment of Words used in Tweets

Now let's plot our results

```
trumptweets %>%
  inner_join(get_sentiments("nrc")) %>%
  group_by(sentiment, source) %>%
  count(sentiment) %>%
  ungroup() %>%
  mutate(sentiment = reorder(sentiment,n)) %>%
  group_by(sentiment, source) %>%
  ggplot(aes(sentiment,n)) + geom_col(aes(fill = source), position = "dodge") + coord_flip() +
  labs(y = "Number of words in Tweets",x = "NRC Sentiment")
```



Join two tables together

In the dplyr library there are several other ways to join tables: left_join(),right_join(),full_join(),semi_join(), anti_join().

See dplyr documentation.

Transforming data

Statistical Transformations

- In statistical analysis it's often necessary to transform data.
- Transforming data takes each value of a variable x_i and transforms it into $f(x_i)$:

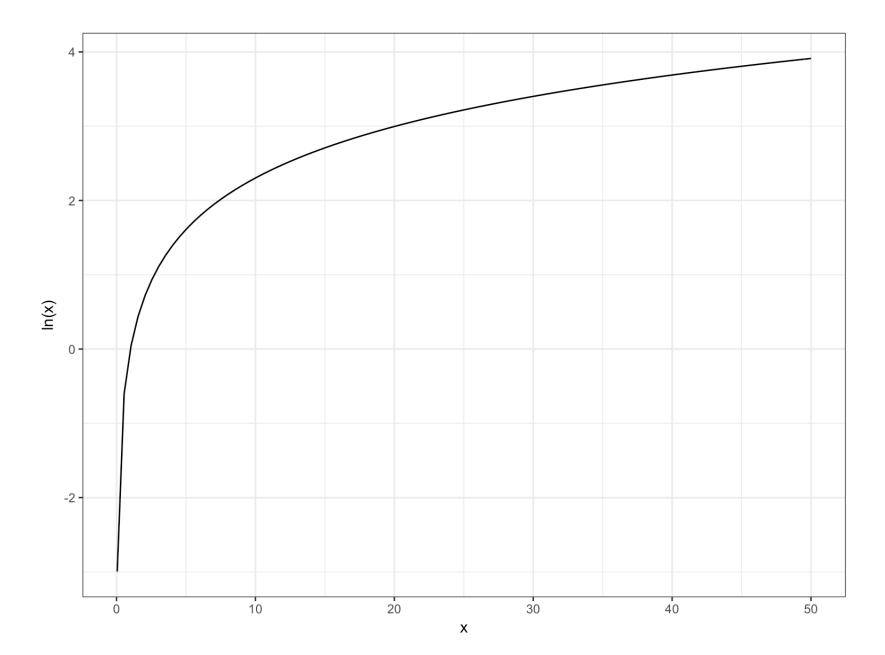
$$x_i \mapsto f(x_i)$$
.

- Common transformations include: $f(x) = \ln(x)$, and $f(x) = x^p$, $p \in \mathbb{R}$. For example, if p = 1/2 then f is the square-root transformation.

Logarithmic transformation

Logarithmic transformation refers to the natural logarithm:

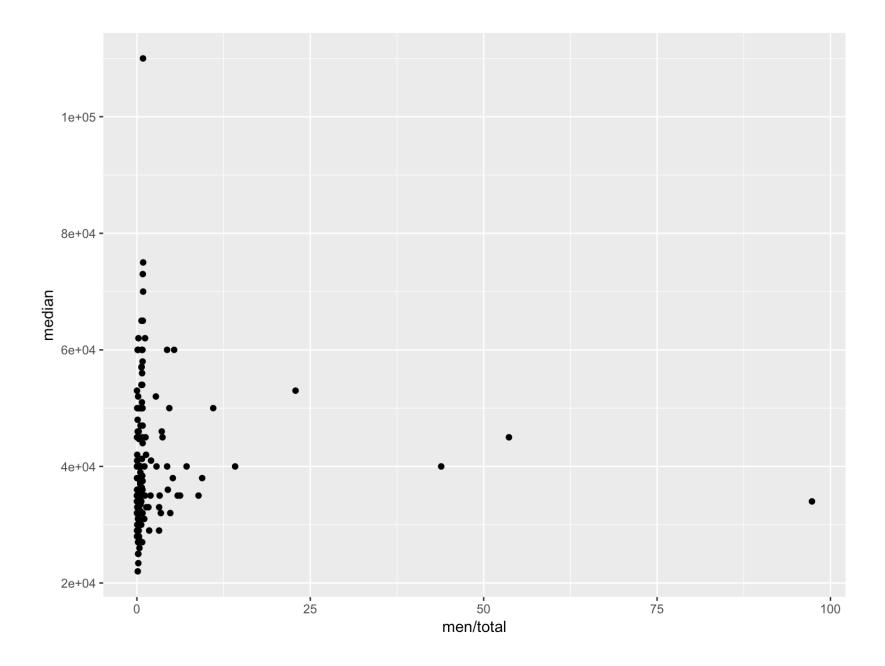
$$y = \log_e(x) \iff \exp(y) = e^y = x$$



Transforming Variables in R

The relationship between Salary (median) and percentage of male graduates.

```
college_recent_grads %>%
  ggplot(aes(x = men / total, y = median)) + geom_point()
```



```
college_recent_grads %>%
  mutate(log_men = log(men / total), log_salary = log(median)) %>%
  ggplot(aes(x = log_men, y = log_salary)) + geom_point()
```

