



UNIVERSITAT DE  
BARCELONA

# CAUSAL INFERENCE AND MACHINE LEARNING

# About the course

The relationship between causality and artificial intelligence can be seen from two points of view: how causality can help solve some of the current problems of AI and how causal inference can leverage machine learning techniques. In this course we will review the two points of view with special emphasis on examples and practical cases.

- 01**  
Jordi | **Introduction**  
Observational and Interventional Distributions. Causal Thinking.
- 02**  
Roger | **Potential Outcomes**  
Fundamental Problem of Causal Inference
- 03**  
Jordi | **Causal Graphs**  
Do Calculus

- 04**  
Roger | **Estimand-based Estimation**  
Metalearners
  - 05**  
Jordi | **Estimand-agnostic Estimation**  
Counterfactuals
  - 06**  
Jordi & Enrique | **Causal Machine Learning**  
Supervised and Reinforcement Learning
  - 07**  
Enrique | **Practical Causal Inference**  
Exercises
- 17:30 End**

# Causal Machine Learning

Supervised Learning

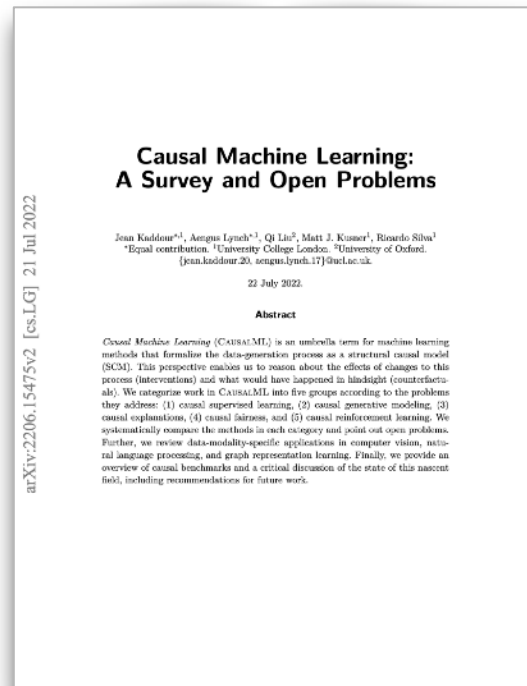
Jordi Vitrià  
jordi.vitria@ub.edu



# Causal Machine Learning

Causal Machine Learning (CausalML) is an umbrella term for **machine learning methods** that formalize the data-generation process as a structural causal model (SCM).

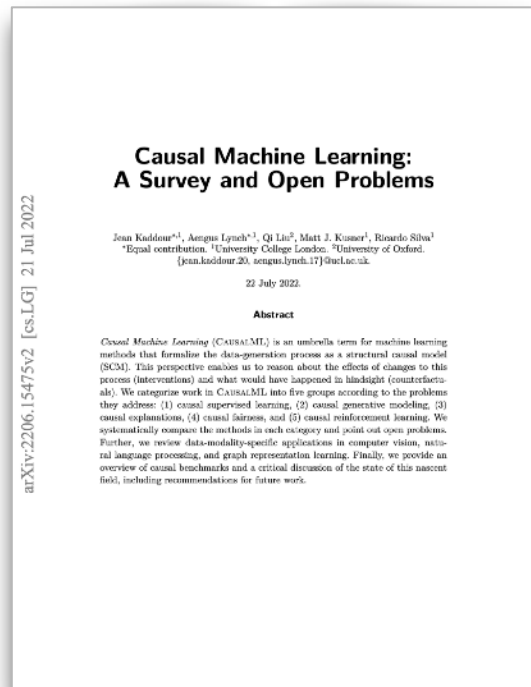
This perspective enables us to reason about the effects of changes to this process (interventions) and what would have happened in hindsight (counterfactuals).



<https://arxiv.org/pdf/2206.15475.pdf>

# Causal Machine Learning

We can categorize work in CausalML into five groups according to the problems they address: (1) **causal supervised learning**, (2) causal generative modeling, (3) causal explanations, (4) causal fairness, and (5) **causal reinforcement learning**.



<https://arxiv.org/pdf/2206.15475.pdf>

# Causal Supervised Learning

The goal of supervised learning is to learn the conditional distribution  $P(Y | X)$  by training on data of the form  $D = \{(x_i, y_i)\}_{i=1}^N$ , where  $X$  and  $Y$  denote covariates and label, respectively.

One of the most fundamental principles in supervised learning is to assume that our data  $D$  is independent and identically distributed (i.i.d.).

The validity of this assumption has been challenged; it has been famously called “*the big lie in machine learning*”.

# Causal Supervised Learning

As an alternative to the i.i.d. assumption, we can assume that our data is sampled from interventional distributions governed by an SCM.

For a given dataset generated across a set of environments  $\mathcal{E}$ ,  $\{(x_i^e, y_i^e)_{i=1}^N\}_{e \in \mathcal{E}}$ , we view each environment  $e \in \mathcal{E}$  as being sampled from a separate interventional distribution.

How can we estimate  $P(Y | X)$  in a principled manner?

# Invariant Feature Learning

**Invariant feature learning** (IFL) is the task of identifying features of our data  $X, X_c$ , that are predictive of  $Y$  across a range of environments  $\mathcal{E}$ .

From a causal perspective, the causal parents  $Pa(Y)$  are always predictive of  $Y$  under any interventional distribution except where  $Y$  itself has been intervened upon.

IFL methods often simplify the governing SCM to focus on identifying the causal parents of  $Y$ , which are often only implicit in data.

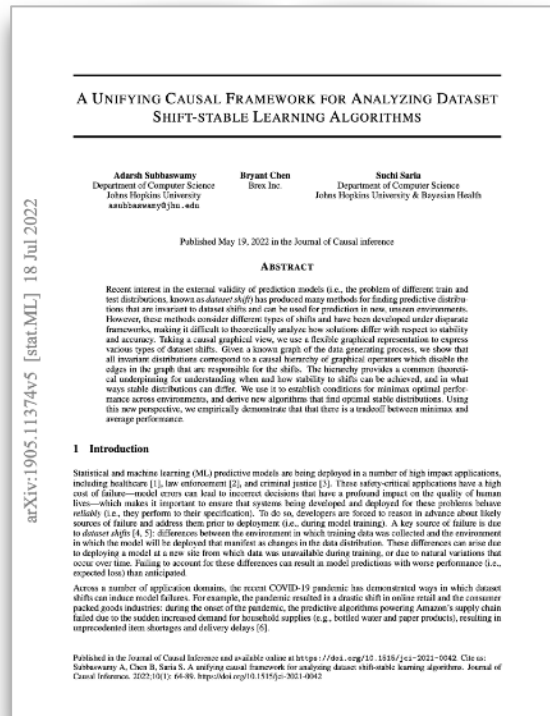


# Distribution Shifts

In this paper, authors provide a unifying framework for **specifying dataset shifts** that can occur, analyzing model stability to these shifts, and determining conditions for achieving the lowest worst-case error across environments produced by these shifts.

This provides common ground so that we can begin to answer fundamental questions such as:

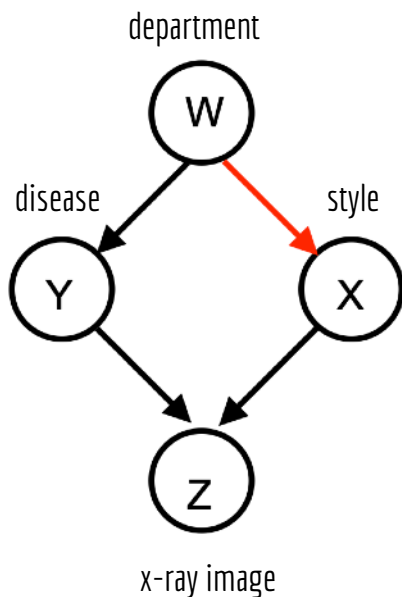
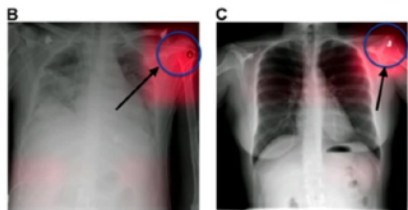
- **To what dataset shifts are the model's predictions stable vs unstable?** (Stability of the data generating model)
- **How will the model's performance be affected by these shifts?**



<https://arxiv.org/pdf/1905.11374.pdf>

# Distribution Shifts

**Example:** The goal is to diagnose pneumonia  $Y$  from chest x-rays  $Z$  and stylistic features of the image  $X$  (i.e., orientation and coloring). The latent variable  $W$  represents the hospital department the patient visited.

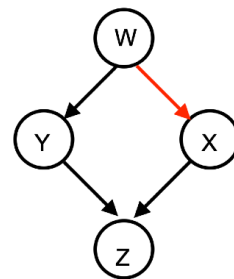


In the pneumonia example, each department has its own protocols and equipment, so the style preferences  $P(X | W)$  vary across departments.

# Distribution Shifts

Each environment is a different instantiation of that graph such that certain mechanisms differ.

Thus, the **factorization of the data distribution is the same in each environment**, but the **terms in the factorization corresponding to shifts will vary across environments**.



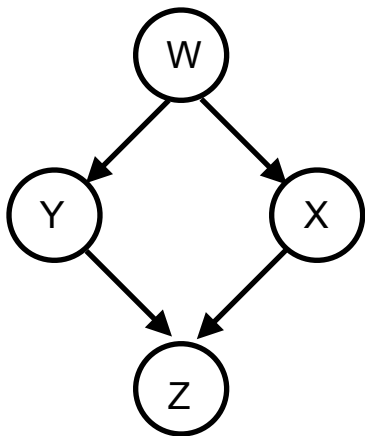
$$E = \{P(Z | Y, X)P(Y | W)P(X | W)P(W)\}$$

# Distribution Shifts

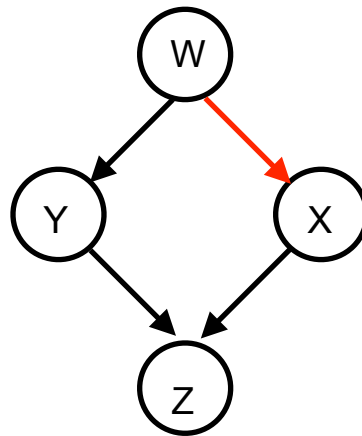
**Key Result:** Distribution shifts can be expressed in terms of edges.

# Distribution Shifts

A graph and a set of edges which are marked as unstable defines an uncertainty set of environments whose distributions differ in the unstable factors.



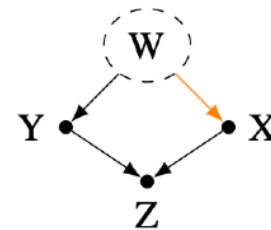
$$P(Z | Y, X)P(Y | W)P(X | W)P(W)$$



$$E = \{P(Z | Y, X)P(Y | W)P(X | W)P(W)\}$$

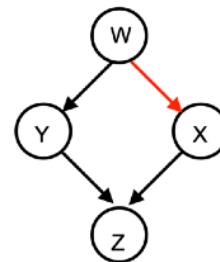
# Distribution Shifts

In this pneumonia example, because  $W$  is unobserved, a model of  $P(Y|X, Z)$  will learn an association between  $Y$  and  $X$  through  $W$ . Thus,  $P(Y|X, Z)$  contains an **unstable** path, and this distribution is **unstable** to shifts in the style mechanism. This means that  $P(Y|X, Z)$  is different in each environment.



By contrast, if  $W$  were observed and we could condition on it, then  $P(Y|X, Z, W)$  is **stable** to shifts in the style mechanism because all paths containing the unstable edge are blocked by  $W$ . Thus,  $P(Y|X, Z, W)$  is invariant across environments.

$P(Y|X, Z)$  is **unstable** because of the backdoor path.



# Distribution Shifts

In order to achieve stable distributions to shifts we can

- find the maximal set of features to **condition** on so that the resulting model is stable with respect to the foreseen shifts,
- **intervene** ( $do(\cdot)$ ) in variables with a shifted mechanism,
- compute **counterfactuals**.

