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module Stack where

import Lib (CanBeEmpty (..), FromList(..), ToList(..))

-- Definition des Stack-DatenTyps
data Stack a = Stack a (Stack a)
              | EmptyStack

-- Show-Instanz für Stack
instance Show a => Show (Stack a) where
  show EmptyStack = "EmptyStack" -- "===="
  show (Stack a rest) = show a ++ " -> " ++ show rest

-- FromList-Instanz für Stack
-- {-# MINIMAL fromList #-}
instance FromList Stack where
  fromList = foldr Stack EmptyStack

-- ToList-Instanz für Stack
-- {-# MINIMAL toList #-}
instance ToList Stack where
  toList = foldr (:) []

-- Functor-Instanz für Stack
-- {-# MINIMAL fmap #-}
instance Functor Stack where
  fmap _ EmptyStack = EmptyStack
  fmap f (Stack x rest) = Stack (f x) (fmap f rest)
  -- (<$) ist nicht unbedingt notwendig, weil es in Functor bereitgestellt
  wird,
  -- aber wir können es für Vollständigkeit auch einfügen.
  (<$) :: b -> Stack a -> Stack b
  (<$) x EmptyStack = EmptyStack
  (<$) x (Stack _ rest) = Stack x (x <$ rest)

-- CanBeEmpty-Instanz für Stack
-- {-# MINIMAL isEmpty #-}
instance CanBeEmpty (Stack a) where
  isEmpty EmptyStack = True
  isEmpty _ = False

-- Semigroup-Instanz für Stack
-- {-# MINIMAL (<>) #-}
instance Semigroup (Stack a) where
  EmptyStack <> stack = stack
  stack <> EmptyStack = stack
  Stack x rest <> stack = Stack x (rest <> stack)

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-- Foldable-Instanz für Stack
-- {-# MINIMAL foldMap | foldr #-}
instance Foldable Stack where
    foldr _ z EmptyStack = z
    foldr f z (Stack x rest) = f x (foldr f z rest)
    foldl _ z EmptyStack = z
    foldl f z (Stack x rest) = foldl f (f z x) rest
    foldMap _ EmptyStack = mempty
    foldMap f (Stack x rest) = f x `mappend` foldMap f rest
    foldr1 _ EmptyStack = error "foldr1: empty structure"
    foldr1 f (Stack x rest) = foldr f x rest
    foldl1 _ EmptyStack = error "foldl1: empty structure"
    foldl1 f (Stack x rest) = foldl f x rest
    null EmptyStack = True
    null _ = False
    length EmptyStack = 0
    length (Stack _ rest) = 1 + length rest
    elem _ EmptyStack = False
    elem e (Stack x rest) = (e == x) || elem e rest
    maximum EmptyStack = error "maximum: empty structure"
    maximum (Stack x rest) = foldl max x rest
    minimum EmptyStack = error "minimum: empty structure"
    minimum (Stack x rest) = foldl min x rest
    sum EmptyStack = 0
    sum (Stack x rest) = foldl (+) x rest
    product EmptyStack = 1
    product (Stack x rest) = foldl (*) x rest

-- Monoid-Instanz für Stack
-- {-# MINIMAL mempty #-}
instance Monoid (Stack a) where
    mempty = EmptyStack
    mappend = (<*)
    mconcat = foldr mappend mempty

-- Applicative-Instanz für Stack
-- {-# MINIMAL pure, (<*) #-}
instance Applicative Stack where
    pure x = Stack x EmptyStack
    EmptyStack <*> _ = EmptyStack
    _ <*> EmptyStack = EmptyStack
    (<*>) (Stack f restF) (Stack x restX) = Stack (f x) (restF <*> Stack x
restX)
    (*>) EmptyStack _ = EmptyStack
    (*>) _ EmptyStack = EmptyStack
    (*>) (Stack _ restF) stackX = restF *> stackX
    (<*) EmptyStack _ = EmptyStack
    (<*) _ EmptyStack = EmptyStack
    (<*) stackX@(Stack x restX) stackY = stackX <*> stackY

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-- Monad-Instanz für Stack
-- {-# MINIMAL (>=) #-}
instance Monad Stack where
    EmptyStack >= _ = EmptyStack
    (Stack x rest) >= f = (f x) <> (rest >= f)
    EmptyStack >> _ = EmptyStack
    stack >> EmptyStack = EmptyStack
    stack >> (Stack y rest) = rest
    return = pure

-- Hilfsfunktionen für Stack
-- ein element hinzufügen
push :: a -> Stack a -> Stack a
push x stack = Stack x stack

-- element entfernen
pop :: Stack a -> Stack a
pop EmptyStack = EmptyStack
pop (Stack _ rest) = rest

top :: Stack a -> a
top EmptyStack = error "Empty stack has no top element"
top (Stack x _) = x

-- Beispiel-Stacks
exampleStack :: Stack Int
exampleStack = push 1 (push 2 (push 3 EmptyStack))

sf = Stack (+1) (Stack (*2) EmptyStack) :: Stack (Int -> Int)
sx = Stack 1 (Stack 2 (Stack 3 EmptyStack)) :: Stack Int

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