Problem Sheet 4

1. It a vandom variable X has the pdf $f_X(x) = \begin{cases} R x/2 & 0 \le x \le 2 \\ 0 & \text{otherwise} \end{cases}$

find the value of h. Also determine its

2. Let x let y = g(x) where $g(x) = \begin{cases} 1 & \text{if } x \leq \frac{y_3}{3} \\ 2 & \text{if } x > \frac{y_3}{3} \end{cases}$.

Find ECYJ.

3. Let X Rave the CDF $F_X(x) = \begin{cases} \frac{0}{2} & \text{if } x < -1 \\ \frac{1}{2} & \text{if } -1 \leq x < 1 \end{cases}$ Show that its variance is $\frac{1}{3}$.

4. Let X and Y be two normal Trandom variables With mean o and I, respectively and variance I and 4, respectively.

ag Show mati) P(x = 1.5) = 0.933.2

in) P(x = -1) = 0.1587

Di) Show that $\frac{\gamma-1}{2}$ is 18td. normal

c) P(-1=y=1)=0.3413

- Let X ~ N(0,1). Using normal table, find x in the following cases.
 -) P(x4x) = 0.6406

 - (ii) P(X > x) = 0.0606 iii) P(0 < X < x) = 0.4783
 - iv) P(-1.54 X4x) = 0.2313
 - V) P(- x < x < x) = 0.5467
- het X~ N(10; %). Find he values of 1) P(X 510) and (ii) P(8 5 X 5 14)
- The germination success rate for certain seeds is 60 %. In a package of 200 Reeds, Use normal approx. to find the probability that one Ralf of them germinate. (Ams. 0.9975)
- Let X N Exp(2) and Y = 2 + 3 XShow . Mat i) P (x>2) = :e-4.
 - ii) Van(y) = 9/4iii) $P(x>2|y=11) = \frac{e^{-4} e^{-6}}{1 e^{-6}}$
- A real number is chosen at rendom on the interval C2, 6]. Let X be the chosen number. Find Fx(x). (CDF) of X and ECXJ.