

199. Given a graph represented by an edge list, implement Dijkstra's Algorithm to find the shortest path from a given source vertex to a target vertex. The graph is represented as a list of edges where each edge is a tuple (u, v, w) representing an edge from vertex u to vertex v with weight w.

Program:

```
import heapq

def dijkstra(edges, n, source, target):
    graph = {i: [] for i in range(n)}

    for u, v, w in edges:
        graph[u].append((v, w))
        graph[v].append((u, w)) # if undirected graph

    dist = [float('inf')] * n
    dist[source] = 0

    heap = [(0, source)] # (distance, vertex)

    while heap:
        d, u = heapq.heappop(heap)

        if u == target:
            return dist[target]

        if d > dist[u]:
            continue

        import heapq

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    while heap:
```

```

    d, u = heapq.heappop(heap)

    if u == target:
        return dist[target]

    if d > dist[u]:
        continue

    for v, weight in graph[u]:
        if dist[u] + weight < dist[v]:
            dist[v] = dist[u] + weight
            heapq.heappush(heap, (dist[v], v))

    return dist[target]
import heapq

def dijkstra(edges, n, source, target):
    graph = {i: [] for i in range(n)}

    for u, v, w in edges:
        graph[u].append((v, w))
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    heap = [(0, source)] # (distance, vertex)

    while heap:
        d, u = heapq.heappop(heap)

        if u == target:
            return dist[target]

        if d > dist[u]:
            continue

        for v, weight in graph[u]:
            if dist[u] + weight < dist[v]:

```

```
dist[v] = dist[u] + weight
```

```
heapq.heappush(heap, (dist[v], v))
```

```
return dist[target]
```

```
# Example 1
```

```
edges1 = [(0, 1, 7), (0, 2, 9), (0, 5, 14), (1, 2, 10), (1, 3, 15),  
          (2, 3, 11), (2, 5, 2), (3, 4, 6), (4, 5, 9)]
```

```
n1 = 6
```

```
source1 = 0
```

```
target1 = 4
```

```
print(dijkstra(edges1, n1, source1, target1)) # Output: 20
```

```
# Example 2
```

```
edges2 = [(0, 1, 10), (0, 4, 3), (1, 2, 2), (1, 4, 4), (2, 3, 9),  
          (3, 2, 7), (4, 1, 1), (4, 2, 8), (4, 3, 2)]
```

```
n2 = 5
```

```
source2 = 0
```

```
target2 = 3
```

```
print(dijkstra(edges2, n2, source2, target2)) # Output:
```

```
# Example 1
```

```
edges1 = [(0, 1, 7), (0, 2, 9), (0, 5, 14), (1, 2, 10), (1, 3, 15),  
          (2, 3, 11), (2, 5, 2), (3, 4, 6), (4, 5, 9)]
```

```
n1 = 6
```

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source1 = 0
```

```
target1 = 4
```

```
print(dijkstra(edges1, n1, source1, target1)) # Output: 20
```

```
# Example 2
```

```
edges2 = [(0, 1, 10), (0, 4, 3), (1, 2, 2), (1, 4, 4), (2, 3, 9),  
          (3, 2, 7), (4, 1, 1), (4, 2, 8), (4, 3, 2)]
```

```

n2 = 5

source2 = 0

target2 = 3

print(dijkstra(edges2, n2, source2, target2)) # Output:

    for v, weight in graph[u]:

        if dist[u] + weight < dist[v]:

            dist[v] = dist[u] + weight

            heapq.heappush(heap, (dist[v], v))

    return dist[target]

# Example 1

edges1 = [(0, 1, 7), (0, 2, 9), (0, 5, 14), (1, 2, 10), (1, 3, 15),

          (2, 3, 11), (2, 5, 2), (3, 4, 6), (4, 5, 9)]

n1 = 6

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# Example 2

edges2 = [(0, 1, 10), (0, 4, 3), (1, 2, 2), (1, 4, 4), (2, 3, 9),

          (3, 2, 7), (4, 1, 1), (4, 2, 8), (4, 3, 2)]

n2 = 5

source2 = 0

target2 = 3

print(dijkstra(edges2, n2, source2, target2))

Output:

```

```
Output
20
5

=== Code Execution Successful ===
```

Time complexity: $O((V + E) \log V)$