# momentuHMM: R package for analysis of telemetry data using generalized multivariate hidden Markov models of animal movement

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#### 1 Summary

1. Discrete-time hidden Markov models (HMMs) have become an immensely popular tool for inferring latent animal behaviors from telemetry data, largely because they are relatively fast and easy to implement when data streams are observed without error and at regular time intervals. While movement HMMs typically rely solely on location data, auxiliary biotelemetry and environmental data are powerful and readily-available resources for incorporating much more behavioral realism and inferring ecological relationships that would otherwise be difficult or impossible to infer from location data alone. However, there is a paucity of generalized user-friendly software available for implementing (multivariate) HMMs of animal movement. Furthermore, location measurement error, temporal irregularity, and other forms of missing data are often pervasive in telemetry studies (particularly in marine systems). 12 2. Here we introduce an open-source R package, momentuHMM, that addresses many of the deficiencies in existing software. Features for multivariate HMMs in momentuHMM include: 1) tools for data pre-processing and visualization; 2) user-specified probability distributions for an unlimited number of data streams, such as those based on location (e.g., step length, turning angle) and auxiliary biotelemetry data (e.g., from 17 pressure, conductivity, heart rate, or motion sensors); 3) user-specified design matri-18 ces and constraints for covariate modelling of state transition probability and probability distribution parameters using linear model formulas familiar to most R users; 20 4) multiple imputation methods that account for observation error attributable to measurement error and temporally-irregular or missing data; 5) seamless integration of spatio-temporal environmental covariate data (e.g., wind direction, forest cover,

- sea ice concentration) using rasters; 6) incorporation of "activity center" effects on
  parameters (e.g., areas associated with attractive or repulsive forces); 7) circularcircular regression models for angular probability distributions; 8) cosinor and spline
  regression formulas for cyclical (e.g., daily, seasonal) and other complicated patterns;
  and 9) data simulation capabilities for power analyses and assessing model performance, including simulation of location data subject to temporal irregularity and/or
  measurement error.
- 31 3. After providing a brief introduction to (multivariate) HMMs for telemetry data,
  32 we demonstrate some of the capabilities of momentuHMM using real-world examples.
  33 This brief tutorial includes workflows for data formatting, model specification, model
  34 fitting, and diagnostics.
- <sup>35</sup> **4.** While many of the features of momentuHMM were motivated by animal movement data, the package can be used for analyzing any type of data that is amenable to (multivariate) HMMs. Practitioners interested in additional features for momentuHMM are encouraged to contact the authors.

Key-words biologging, biotelemetry, crawl, moveHMM, state-space model, stateswitching

# 1 Introduction

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Discrete-time hidden Markov models (HMMs) have become immensely popular for the analysis of animal telemetry data (e.g. Morales *et al.* 2004; Jonsen *et al.* 2005; Langrock *et al.* 2012; McClintock *et al.* 2012). In short, an HMM is a time series model composed of one or more observable data streams  $(\mathbf{Z}_1, \ldots, \mathbf{Z}_T)$ , each of which is generated by N state-dependent probability distributions, where the unobservable (hidden) state sequence  $(S_t \in \{1, ..., N\}, t = 1, ..., T)$  is assumed to be a Markov chain. The state sequence of the Markov chain is governed by (typically first-order) state transition probabilities,  $\gamma_{ij}^{(t)} = \Pr(S_{t+1} = j \mid S_t = i)$  for i, j = 1, ..., N, and an initial distribution  $\boldsymbol{\delta}^{(0)}$ . The likelihood of an HMM can be succinctly expressed using the forward algorithm:

$$\mathcal{L} = \boldsymbol{\delta}^{(0)} \boldsymbol{\Gamma}^{(1)} \mathbf{P}(\mathbf{z}_1) \boldsymbol{\Gamma}^{(2)} \mathbf{P}(\mathbf{z}_2) \boldsymbol{\Gamma}^{(3)} \cdots \boldsymbol{\Gamma}^{(T-1)} \mathbf{P}(\mathbf{z}_{T-1}) \boldsymbol{\Gamma}^{(T)} \mathbf{P}(\mathbf{z}_T) \mathbf{1}^N$$
(1)

where  $\mathbf{\Gamma}^{(t)} = \left(\gamma_{ij}^{(t)}\right)$  is the  $N \times N$  transition probability matrix,  $\mathbf{P}(\mathbf{z}_t) = \text{diag}(p_1(\mathbf{z}_t), \dots, p_N(\mathbf{z}_t))$ ,  $p_s(\mathbf{z}_t)$  is the conditional probability density of  $\mathbf{Z}_t$  given  $S_t = s$ , and  $\mathbf{1}^N$  is a N-vector of ones (for a thorough introduction to HMMs see Zucchini et al. 2016). One of the most common discrete-time animal movement HMMs for telemetry 56 location data is composed of two data streams, step length and turning angle (or bear-57 ing), which are calculated for each of the T time steps from the temporally-regular ob-58 servations of an animal's position,  $(x_t, y_t)$ , for  $t = 1, \dots, T+1$  (e.g. Morales et al. 2004; 59 Langrock et al. 2012; McClintock et al. 2012). Step length  $(l_t)$  is typically calculated as the Euclidean distance between the locations  $(x_t, y_t)$  and  $(x_{t+1}, y_{t+1})$ , while turn-61 ing angle  $(\phi_t)$  is calculated as the change in bearing  $(b_t = \operatorname{atan2}(y_{t+1} - y_t, x_{t+1} - x_t))$ 62 between the intervals [t-1,t] and [t,t+1] (e.g.  $\phi_t=0$  if  $b_{t-1}=b_t$ ). For this HMM composed of 2 data streams,  $\mathbf{z}_t = (l_t, \phi_t)$ , and, conditional on the latent state  $S_t$ , independent probability distributions are typically assumed for each stream, e.g.,  $p_s(\mathbf{z}_t) = p_s(l_t)p_s(\phi_t)$ . Some common probability distributions for the step length data stream are the Gamma or Weibull distributions, while the wrapped Cauchy or von Mises distributions are often employed for turning angle or bearing.

While HMMs for animal movement based solely on location data are somewhat 69 limited in the number and type of biologically-meaningful movement behavior states 70 they are able to accurately identify, advances in biologging technology are now allowing the collection of valuable auxiliary biotelemetry data (e.g., dive activity, accelerometer, heart rate, stomach temperature), which, when combined with location data, allow for multivariate HMMs that can incorporate much more behavioral realism and facilitate inferences about complex ecological relationships that would otherwise be difficult or impossible to infer from location data alone (e.g. McClintock et al. 2013; DeRuiter et al. 2017; McClintock et al. 2017). Multivariate HMMs 77 that utilize both location and auxiliary biotelemetry data can facilitate the identification of additional states that go beyond the N=2 state approaches that are 79 most frequently used by practitioners. For example, the most widely used 2-state 80 HMMs for animal movement include "encamped" (or "foraging") and "exploratory" 81 (or "transit") states characterized by area-restricted-search-type movements (shorter 82 step lengths with little to no directional persistence) and migratory-type movements 83 (longer step lengths with high directional persistence), respectively (Morales et al. 2004; Jonsen et al. 2005). However, very different behaviors can exhibit similar hori-85 zontal trajectories. For example, for herbivores such as North American elk (Morales 86 et al. 2004) or central-place foragers such as harbour seals (McClintock et al. 2013), 87 the horizontal trajectories of "resting" and "foraging" movements can be very difficult to distinguish. Standard 2-state HMMs based solely on horizontal trajectory will tend to lump these behaviors together, and this could have unintended consequences if, for example, one intends to use the estimated state sequences to identify foraging habitat. In order to tweeze apart distinct behaviors with similar horizontal trajectories, additional states informed by auxiliary information (such as mandible accelerometer or dive data) must often be incorporated as additional data stream(s) in a multivariate HMM.

When data streams are observed without error and at regular time intervals, a major advantage of HMMs is the relatively fast and efficient maximization of the likelihood using the forward algorithm (Eq. 1). However, location measurement error is rarely non-existent in animal-borne telemetry studies and depends on both the device and the system under study. For example, GPS errors are typically less 100 than 50m, but Argos errors can exceed 10km (e.g. Costa et al. 2010). An extreme 101 case of missing data can arise when location data are obtained with little or no tem-102 poral regularity, as in many marine mammal telemetry studies (e.g. Jonsen et al. 103 2005), such that few (if any) observations align with the regular time steps required 104 by discrete-time HMMs. When explicitly accounting for uncertainty attributable 105 to location measurement error, temporally-irregular observations, or other forms of 106 missing data, one must typically fit (multivariate) HMMs using computationally-107 intensive (and often time-consuming) model fitting techniques such as Markov chain 108 Monte Carlo (Jonsen et al. 2005; McClintock et al. 2012). However, complex analy-109 ses requiring novel statistical methods and custom model-fitting algorithms are not 110 practical for many practitioners. 111

While statisticians have been applying HMMs to telemetry data for decades, R (R Core Team 2016) packages such as bsam (Jonsen et al. 2005), moveHMM (Michelot et al. 2016), and swim (Whoriskey et al. 2017) have recently helped make these models of animal movement behavior more accessible to the practitioners that are actually conducting telemetry studies. These advances represent important steps

toward making HMMs of animal movement more accessible, but the models that 117 can currently be implemented using existing software remain limited in many key 118 respects. For example, existing HMM software for animal movement is limited to 119 two data streams based solely on location data (e.g. step length and turning an-120 gle), and while moveHMM allows for a user-specified number of latent behavioral states 121 (bsam and swim are limited to N=2 states), it is typically difficult to identify 122 >2 biologically-meaningful behavior states from only 2 data streams (e.g. Morales et al. 2004; Beyer et al. 2013; McClintock et al. 2014). Both moveHMM and swim 124 are designed for temporally-regular (or linearly-interpolated) location data with neg-125 ligible measurement error, but the realities of animal-borne telemetry often yield 126 temporally-irregular location data subject to error (particularly in aquatic environ-127 ments). Other notable deficiencies of existing software include limited abilities to 128 incorporate spatio-temporal environmental or individual covariates on parameters, 129 biased (or directed) movements in response to attractive or repulsive forces (e.g. Mc-130 Clintock et al. 2012; Langrock et al. 2014), cyclical (e.g. daily, seasonal) and other 131 more complicated behavioral patterns, or constraints on parameters. 132

To address these defeciencies in existing software, we introduce a new user-friendly
R package, momentuHMM (Maximum likelihood analysis Of animal MovemENT behavior Using multivariate Hidden Markov Models), intended for practitioners wishing
to implement more flexible and realistic (multivariate) HMM analyses of animal
movement while accounting for common challenges associated with telemetry data.
Features for multivariate HMM analyses in momentuHMM include: 1) tools for data
pre-processing and visualization; 2) user-specified probability distributions for an unlimited number of data streams and latent behavior states; 3) user-specified design

matrices and constraints for covariate modelling of state transition probability and probability distribution parameters using linear model formulas familiar to most R 142 users; 4) multiple imputation methods that account for observation error attributable 143 to measurement error and temporally-irregular or missing data (Hooten et al. 2017; McClintock 2017); 5) seamless integration of spatio-temporal environmental covari-145 ate data (e.g., wind direction, forest cover, sea ice concentration) using the raster package (Hijmans 2016); 6) incorporation of "activity center" effects (e.g., areas asso-147 ciated with attractive or repulsive forces); 7) circular-circular regression models for 148 angular probability distributions (Duchesne et al. 2015); 8) cosinor (e.g. Cornelissen 149 2014) and spline regression formulas for cyclical and other complicated behavioral 150 patterns; and 9) data simulation capabilities for power analyses and assessing model 151 performance, including simulation of location data subject to temporal irregularity 152 and/or measurement error. 153

In the following tutorial, we demonstrate some of the capabilities of momentuHMM 154 using real-world examples, including an example of periodic cycles in African elephant 155 movement, a 3-state ("resting", "foraging", "transit") northern fur seal example in-156 corporating auxiliary dive activity data (McClintock et al. 2014), a loggerhead turtle 157 example relating "foraging" and "transit" movements to ocean surface currents, and 158 a 5-state grey seal example incorporating biased movements toward haul-out and 159 foraging locations (McClintock et al. 2012). This brief tutorial includes workflows 160 for data formatting, model specification, model fitting, and diagnostics. While many 161 of the features of momentuHMM were motivated by animal movement data, the pack-162 age can be used for analyzing any type of data that is amenable to (multivariate) 163 HMMs. Additional information, including help files, data, examples, and package usage is available by downloading the momentuHMM package from CRAN (http://cran.r-project.org) or github (https://github.com/bmcclintock/momentuHMM). This article describes momentuHMM version 1.0.0.

# <sup>168</sup> 2 momentuHMM overview

Before delving into some of the finer details, we will first provide an overview of the 169 main features and functions of the package. While space is limited in this tutorial, 170 further details on implementation can be found in the package's documentation and 171 vignette. The workhorse functions of momentuHMM are listed in Table 1. Usage of 172 several of these functions (e.g. fitHMM, prepData, simData) is deliberately very sim-173 ilar to equivalent functions in moveHMM (Michelot et al. 2016), but the momentuHMM 174 arguments for these functions have been generalized and expanded to accommodate 175 a more flexible framework for data pre-processing, model specification, parameteri-176 zation, and simulation. R users already familiar with moveHMM will therefore likely 177 find it easy to immediately begin using momentuHMM.

One of the key features of momentuHMM is the ability to specify an unlimited 179 number of HMM data streams from a broad range of commonly used probability 180 distributions. Any of the probability distribution parameters (as well as the state 181 transition probabilities) can be modelled as a function of environmental and indi-182 vidual covariates using link functions (Table 2). For any given "natural scale" (or 183 "real scale") probability distribution parameter  $\theta$ , all of the link functions (q) in 184 momentuHMM are of the general form  $g(\boldsymbol{\theta}) = \mathbf{X}_{\theta} \boldsymbol{\beta}_{\theta}$ , where  $\mathbf{X}_{\theta}$  is the  $T \times k$  design 185 matrix (composed of k covariates) and  $\beta_{\theta}$  is the corresponding k-vector of "working 186 scale" (or "beta scale") parameters for  $\theta$ . For example, suppose step length is as-

**Table 1.** Workhorse functions for the R package momentuHMM.

Function	Description		
crawlMerge	Merge crawlWrap output with additional data streams or covariates		
crawlWrap	Fit crawl models and predict temporally-regular locations		
fitHMM	Fit a (multivariate) HMM to the data		
MIfitHMM	Fit (multivariate) HMMs to multiple imputation data		
MIpool	Pool momentuHMM model results across multiple imputations		
plot.crwData	Plot crawlWrap output		
plot.miSum	Plot summaries of multiple imputation momentuHMM models		
<pre>plot.momentuHMM</pre>	Plot summaries of momentuHMM models		
<pre>plot.momentuHMMData</pre>	Plot summaries of selected data streams and covariates		
plotPR	Plot time series, qq-plots and sample ACFs of pseudo-residuals		
plotSat	Plot locations on satellite image		
plotSpatialCov	Plot locations on raster image		
plotStates	Plot the (Viterbi-)decoded states and state probabilities		
prepData	Pre-process data streams and covariates		
pseudoRes	Calculate pseudo-residuals for momentuHMM models		
simData	Simulate movement data using a (multivariate) HMM		
stateProbs	State probabilities for each time step		
viterbi	Most likely state sequence (using the Viterbi algorithm)		

sumed to have a Gamma distribution,  $l_t \mid S_t = s \sim \text{Gamma}(\mu_s, \sigma_s)$ . In momentuHMM, the natural scale parameters for the Gamma distribution are the (state-dependent) step length mean  $(\mu_s > 0)$  and standard deviation  $(\sigma_s > 0)$ . Because both of these parameters must be positive, the log link function is a natural choice for modelling these parameters as a function of covariates, e.g.,  $\log(\mu) = \mathbf{X}_{\mu}\boldsymbol{\beta}_{\mu}$ .

## $_{\scriptscriptstyle 3}$ 2.1 Data preparation and visualization

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- For temporally-regular location data with negligible measurement error, the prepData function is used to create a momentuHMMData object that can be used for data visualization and further analysis. The arguments for prepData include:
- Data A data frame with T+1 rows including optionally a field 'ID' (identifiers for different individuals), coordinates from which step length ('step') and turning angle ('angle') data streams are to be calculated, any additional data streams, and any covariates identified in the covNames and angleCovs arguments. Altervatively, Data can be a crwData object returned by crawlWrap.
  - type Coordinate type; 'UTM' if easting-northing or 'LL' if longitude-latitude.
- coordNames Names of the two coordinate columns in Data. If coordNames=NULL
  then step lengths, turning angles, and any location-based covariates (i.e., those
  specified by spatialCovs, centers, and angleCovs) are not calculated.
  - covNames Character vector indicating the names of any covariates in Data.

    Any variables in Data (other than "ID") that are not identified in covNames or angleCovs are assumed to be data streams.

Table 2. Data stream (z) probability distributions, natural parameters, and default link functions for covariate modelling. Probability distributions with positive support can be zero-inflated (with additional zero-mass parameters), while the Beta distribution can be zero- and one-inflated (with additional one-mass parameters). If user-specified bounds are provided, then custom link functions are used instead of the defaults (see package documentation for further details). If circular-circular regression is specified for the mean of angular distributions ("vm" and "wrpcauchy"), then the link function described in Duchesne  $et\ al.\ (2015)$  is used. Users seeking additional probability distributions are encouraged to contact the authors.

Distribution	Support	Parameters	Link function
Beta ("beta")	$z_t \in (0,1)$	$\mathtt{shape1} > 0$	log
		$\mathtt{shape2} > 0$	$\log$
		$\texttt{zero-mass} \in (0,1)$	logit
		$\mathtt{one\text{-}mass} \in (0,1)$	logit
Exponential ("exp")	$z_t > 0$	$\mathtt{rate} > 0$	$\log$
		$\texttt{zero-mass} \in (0,1)$	logit
Gamma ("gamma")	$z_t > 0$	$\mathtt{mean} > 0$	$\log$
		$\operatorname{sd} > 0$	$\log$
		$\texttt{zero-mass} \in (0,1)$	logit
Log normal ("lnorm")	$z_t > 0$	${\tt location} \in {\rm I\!R}$	identity
		scale > 0	$\log$
		$\texttt{zero-mass} \in (0,1)$	logit
Poisson ("pois")	$z_t \in \{0, 1, \ldots\}$	${\tt lambda} > 0$	$\log$
Von Mises ("vm")	$z_t \in (-\pi, \pi]$	$\mathtt{mean} \in (-\pi,\pi]$	$\tan(\mathtt{mean}/2)$
		${\tt concentration} > 0$	$\log$
Weibull ("weibull")	$z_t > 0$	$\mathtt{shape} > 0$	$\log$
		$\mathtt{scale} > 0$	$\log$
Wrapped Cauchy ("wrpcauchy")	$z_t \in (-\pi, \pi]$	$\mathtt{mean} \in (-\pi,\pi]$	$\tan(\mathtt{mean}/2)$
		$\mathtt{concentration} \in (0,1)$	logit

• spatialCovs List of Raster-class objects (Hijmans 2016) containing spatiotemporally referenced covariates. Covariates specified by spatialCovs are extracted from the raster layer(s) based on the location data. Raster stacks may also be included, in which case the appropriate z values (e.g. time, date) must also be included in Data.

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- centers 2-column matrix providing the coordinates for any activity centers (e.g., potential centers of attraction or repulsion) from which distance and angle covariates will be calculated based on the location data and returned in the momentuHMMData object.
- angleCovs Character vector indicating the names of any circular-circular regression angular covariates in Data or spatialCovs that need conversion from standard direction (in radians relative to the x-axis) to turning angle (relative to previous movement direction).
- Summary plots of the momentuHMMData object returned by prepData can be created for any data stream or covariate using the generic plot function.
- If location data are temporally-irregular or subject to measurement error, then
  they are not suitable for prepData. In this case, momentuHMM can be used to perform a
  2-stage multiple imputation approach (McClintock 2017). We discuss this pragmatic
  approach to incorporating uncertainty attributable to observation error and temporal
  irreglarity into multivariate HMM analyses in section 2.3.

### 2.2 HMM specification and fitting

- Once a momentuHMMData object has been created using prepData, then the data are ready to be passed to the generalized multivariate HMM-fitting function fitHMM.

  There are many different options for specifying HMMs using fitHMM, so here we will only focus on several of the most important and useful features (further details of all fitHMM arguments are in the package documentation). The bare essentials of fitHMM include the arguments:
- data A momentuHMMData object
- nbStates Number of latent states (N)
- dist A named list indicating the probability distributions of the data streams.
- estAngleMean An optional named list indicating whether or not to estimate
  the angle mean for data streams with angular distributions (e.g. turning angle).

  If not estimated (the default), the angle mean is fixed to 0.
- formula Regression formula for the transition probability covariates
- stationary Logical indicating whether or not the initial distribution is considered equal to the stationary distribution (must be FALSE if formula includes covariates)
- Par0 A named list containing vectors of starting values for the state-dependent probability distribution parameters of each data stream
- These seven arguments are all that are needed in order to fit the HMMs currently supported in moveHMM (Michelot et al. 2016). For example, here is how the analysis

of 15 "wild haggis" tracks described in Michelot *et al.* (2016) would be implemented using momentuHMM:

```
> library(momentuHMM)
> ### Load raw data
> rawHaggis<-read.csv("rawHaggises.csv")</pre>
> ### Process data
> processedHaggis<-prepData(data=rawHaggis,covNames=c("slope","temp"))</pre>
> ### Fit HMM
> # initial step distribution natural scale parameters
> stepPar0 <- c(1,5,0.5,3) \# (mu_1,mu_2,sd_1,sd_2)
> # initial angle distribution natural scale parameters
> anglePar0 < c(0,0,1,8) # (mean_1,mean_2,concentration_1,concentration_2)
> fitHaggis <- fitHMM(data = processedHaggis, nbStates = 2,</pre>
                       dist = list(step = "gamma", angle = "vm"),
                       Par0 = list(step = stepPar0, angle = anglePar0),
                       formula = ~ slope + I(slope^2),
+
                       estAngleMean = list(angle=TRUE))
```

Note that many of the arguments in fitHMM are lists, with each element of the list corresponding to a data stream. The list names provided in dist, ParO, and estAngleMean (e.g. 'step' and 'angle') must therefore have a corresponding column in data with the same name. Additional data streams can be added to the model by simply adding the additional elements to these list arguments (see example in section 3.2).

As seen above, the formula argument can include many of the functions and operators commonly used to construct terms in R linear model formulas (e.g. a\*b, a:b, cos(a)). Unique to momentuHMM, the formula argument can also be used to specify transition probability matrix models that incorporate cyclical patterns (using the cosinor special function; see example in section 3.1), splines for explaining other more complicated patterns (e.g., bs and ns functions in the R base package splines), and factor variables (e.g., formula=~ID for individual-level effects). By

default the formula argument applies to all state transition probabilities, but the
special functions state and betaCol allow for state- and parameter-specific formulas
to be specified. Specific state transition probabilities can also be fixed to zero (or
any other value) using the fixPar argument, which can be useful for incorporating
more behavioral realism. For example, fixPar can be used to prohibit or enforce
switching from one particular state to another (possibly as a function of spatiotemporal covariates).

Similar to the formula argument for state transition probability modelling, it is
through the DM argument of fitHMM that models are specified for the state-dependent
probability distribution parameters for each data stream. DM is a list argument containing an element for each data stream, but each element itself is also a list specifying
the design matrix formulas for each parameter. For example, the following fits the
exact same wild haggis model as above, but employs a user-specified (intercept-only)
design matrix for the step length data stream:

Note that when DM is specified for a data stream, the initial parameter values (ParO) for that data stream now correspond to columns of the resulting design matrix and must be on the working scale instead of the natural scale. In this case, because the log link is used for the natural parameters of the Gamma distribution, ParO\$step was specified on the log scale. The functions getParO and getParDM are designed to

assist users in the specification of design matrices and corresponding initial values
on the working scale for any given model (see package documentation for further
details). DM formulas are just as flexible as the formula argument and, in addition
to common linear model formula functions and operators, can also include cyclical
cosinor models, splines, factor variables, and state-specific probability distribution
parameter formulas (see examples in sections 3.3 and 3.4). As with the state transition probabilities, working parameters for probability distributions can also be fixed
to user-specified values using the fixPar argument.

Specification of design matrices using DM is not limited to formulas. Alternatively,

"pseudo-design" matrices can be specified, using an R matrix with rows corresponding

to the natural parameters and columns corresponding to the working parameters.

The elements in the matrix may be numeric or character strings containing model

formula terms (see examples in sections 3.2 and 3.4). Using a pseudo-design matrix

for step length, the following is yet another way to implement the exact same wild

haggis model:

```
> stepDMp <- matrix(c(1,0,0,0,
                      0,1,0,0,
+
                      0,0,1,0,
                      0,0,0,1),4,4,byrow=TRUE)
> rownames(stepDMp) <- c("mean_1", "mean_2", "sd_1", "sd_2")</pre>
  colnames(stepDMp) <- c("mean_1:(Intercept)", "mean_2:(Intercept)",</pre>
                         "sd_1:(Intercept)","sd_2:(Intercept)")
> ### Fit HMM
                      using user-specified DM
  fitHaggisDMp <- fitHMM(data = processedHaggis, nbStates = 2,
                          dist = list(step = "gamma", angle = "vm"),
                          DM = list(step = stepDMp),
                          Par0 = list(step = log(stepPar0), angle = anglePar0),
                          formula = ~ slope + I(slope^2),
                          estAngleMean = list(angle=TRUE))
```

(note that column and rownames for pseudo-design matrices are not required but can be useful). Pseudo-design matrices allow for the sharing of common working parameters (such as intercept terms) among natural scale parameters, and this can be used to constrain natural scale parameters (e.g.,  $\mu_1 \leq \mu_2$ ) when used in tandem with the cons argument. This is particularly useful for preventing state label switching when repeatedly fitting the same HMM using multiple imputation methods (see section 2.3).

Another noteworthy fitHMM argument, circularAngleMean, is a list argument that enables users to specify circular-circular regression models for the mean  $(\mu)$  parameter of angular distributions, such as the wrapped Cauchy and von Mises, instead of circular-linear models based on the tangent link function (Table 2). When circularAngleMean is specified as TRUE for any given angular data stream (e.g. turning angle), then a special link function based on Duchesne et al. (2015) is used:

$$\boldsymbol{\mu} = \operatorname{atan2}(\sin(\mathbf{X}_{\mu})\boldsymbol{\beta}_{\mu}, 1 + \cos(\mathbf{X}_{\mu})\boldsymbol{\beta}_{\mu}), \tag{2}$$

where  $\mathbf{X}_{\mu}$  is a  $T \times k$  matrix composed of the turning angles between k angular covariates (e.g., wind direction, sea surface currents) and the bearing of movement during the previous time step, i.e., each element  $x_{t,i} = \operatorname{atan2}(\sin(r_{t,i} - b_{t-1}), \cos(r_{t,i} - b_{t-1}))$  for angular covariate  $r_{t,i}$  and  $i = 1, \dots, k$  (note that prepData calculates  $\mathbf{X}_{\mu}$  based on the angleCovs argument so users need not bother). Because this link function is designed for turning angles, a turning angle of 0 is provided as the reference angle (hence the "1+" preceding the cosine term in Eq. 2). Thus as a trade-off between biased and correlated movements, the working parameters  $(\boldsymbol{\beta}_{\mu})$  for the expected turning angle at time t weight the attractive (or repulsive) strengths of

the angular covariates relative to directional persistence. When all  $\beta_{\mu} = 0$ , the model reduces to a correlated random walk, but an increasingly biased random walk results as  $\beta_{\mu}$  gets larger (or smaller). Many interesting hypotheses about animal movement can be addressed using circular-circular regression on movement direction, including the effects of wind, sea surface currents (see example in section 3.3), and centers of attraction or repulsion (see example in section 3.4)

#### <sub>7</sub> 2.3 Multiple imputation

When location data are temporally-irregular or subject to measurement error, then they are not suitable for standard maximum-likelihood HMM analyses based on the 329 forward algorithm (Eq. 1). In this case, momentuHMM can be used to perform the 330 2-stage multiple imputation approach of McClintock (2017). The basic concept is 331 to first employ a single-state (i.e., N=1) movement model that is relatively easy 332 to fit but can accommodate location measurement error and temporally-irregular or 333 missing observations (e.g. Johnson et al. 2008). The second stage involves repeatedly 334 fitting the desired HMM to m temporally-regular realizations of the position process 335 drawn from the model output of the first stage. Data streams or covariates that are 336 dependent on location (e.g., step length, turning angle, habitat type, snow depth, 337 sea surface temperature) will of course vary among the m realizations of the position 338 process, and the pooled inferences across the HMM analyses therefore reflect location 339 uncertainty. 340

There are three primary functions (MIfitHMM, MIpool, and crawlWrap) for performing multiple imputation HMM analyses in momentuHMM, and all rely on parallel processing to speed up computations. crawlWrap is a wrapper function for fitting the

continuous-time correlated random walk (CTCRW) model of Johnson et al. (2008) to one or more tracks (subject to location measurement error and/or temporal ir-345 regularity) and then predicting temporally-regular tracks of the user's choosing (e.g. 346 15 min, hourly, daily) based on the CTCRW model output. crawlWrap returns a crwData object that can be used to draw m realization of the position process within the MIfitHMM function. MIfitHMM is essentially a wrapper function for fitHMM that 349 repeatedly fits the same user-specified HMM to m imputed data sets and stores the 350 output from each of the m model fits. If a crwData object is provided, then MIfitHMM 351 will first draw m imputations based on the crwData output and then fit the speci-352 fied HMM to each imputed data set. If users wish to use a movement model other 353 than the CTCRW to account for measurement error and temporal irregularity (e.g. 354 Calabrese et al. 2016; Gurarie et al. 2017), or if other observation error processes 355 (e.g. missing data) are to be accounted for in the imputation step, MIfitHMM can 356 also be used for analysis of a list of m momentuHMMData objects that were imputed 357 by the user. Based on the m model fits, the MIpool function calculates pooled es-358 timates, standard errors, and confidence intervals for the working scale parameters, 359 natural scale parameters (based on transformations of the pooled working param-360 eters and mean or user-specified values for any covariates), state sequences, state 361 probabilities, and activity budgets (i.e. the proportion of the T times step assigned 362 to each state) using standard multiple imputation formulae (Rubin & Schenker 1986; 363 McClintock 2017). MIpool can be called separately or within MIfitHMM (using the poolEstimates argument), and the function returns a miSum object containing the pooled output across all imputatons. See sections 3.2, 3.3, and 3.4 for example HMM analyses that use multiple imputation to account for location measurement error and 368 temporally irregularity.

function.

390

#### <sup>369</sup> 2.4 Model visualization and diagnostics

The generic plot functions for momentuHMM models (plot.momentuHMM and plot.miSum) 370 plot the data stream histograms along with their corresponding estimated probability 371 distributions, the estimated natural parameters and state transition probabilities as 372 a function of any covariates included in the model, and the tracks of all individuals (color-coded by the most likely state sequence). By default, the probability distributions are plotted based on the means of any covariate values, but user-specified 375 covariate values for the plots can be provided using the covs argument. When the ar-376 gument plotCI=TRUE, then confidence intervals for the natural parameters and state 377 transition probabilities are also plotted. Confidence intervals are calculated from the 378 working parameter estimates based on the delta method and finite-difference approxi-379 mations of the first derivative for the transformation using the numDeriv::grad func-380 tion (Gilbert & Varadhan 2016). For multiple imputation analyses (plot.miSum), all 381 plots are based on the pooled parameter estimates and the means of any covariates 382 (if not provided by the covs argument) across each imputation. Using the argument 383 errorEllipse, plot.miSum will include estimated location error ellipses in the plots 384 of individual tracks. The functions plotSat, plotSpatialCov, and plotStates (Ta-385 ble 1) provide further methods for visualizing model results. 386 Diagnostic tools include the calculation and plotting of pseudo-residuals (Zucchini 387 et al. 2016) using the pseudoRes and plotPR functions, respectively. Akaike's Infor-388 mation Criterion can be calculated for one or more models using the AIC.momentuHMM 389

#### 2.5 Simulation

The function simData can be used to simulate multivariate HMM data from scratch 392 or based on the estimated parameters of existing momentuHMM or miSum models. The 393 simData arguments are very similar to those used for model specification in fitHMM 394 (e.g., dist, DM) and data preparation in prepData (e.g., spatialCovs, centers), 395 but they include additional arguments, lambda and errorEllipse, for simulating location data subject to temporal irregularity and measurement error, respectively. 397 The spatialCovs argument allows for rasters of spatio-temporal covariate values to be utilized in simulation models, while the centers argument allows activity centers 399 to be incorporated. Thus simData can be used to simulate more ecologically-realistic 400 tracks (potentially subject to observation error) that can be useful for study design, 401 power analyses, and assessing model performance. 402

# 403 3 Examples

We will now demonstrate some of the capabilities of momentuHMM using real telemetry
data. These examples are intended for demonstration purposes only, and we do
not claim these example analyses represent improvements relative to previous or
alternative analyses for these data sets. While only some of the key workflow elements
are included here, complete R code and further details for these analyses can be found
in the online Supplementary Material.

# 3.1 African elephant

As our first example, we use an African elephant (*Loxodonta africana*) bull track described in Wall *et al.* (2014) and publicly available from the movebank.org data

```
repository. In addition to hourly locations, the tag also collected external tempera-
   ture data. Location measurement error is negligible for these terrestrial GPS data,
414
   although about 1% of the hourly observations collected between 22 March 2008 and
415
   30 September 2010 are missing. Instead of simply ignoring these missing data, we
   can employ crawlWrap to predict the missing locations based on the CTCRW model
   of Johnson et al. (2008) prior to conducting our HMM analysis:
   > crwOut <- crawlWrap(obsData = elephantData, timeStep = "hour",
                           initial.state = inits, theta = c(4,-10), fixPar = c(NA,NA))
   Here the desired time step is specified by the timeStep argument, and the initial.state,
   theta, and fixPar arguments are the same as for crawl::crwMLE (Johnson 2017).
420
   Now that we have our complete set of temporally-regular location data, we can begin
421
   fitting HMMs using fitHMM.
422
       During preliminary exploratory data analysis, autocorrelation function estimates
423
   suggested there are 24-hour cycles in the step length data (see Figure 1), and this
424
   presents an opporunity to demonstrate the use of the cosinor function for incorpo-
   rating cyclical behavior in model parameters using momentuHMM. But first we must
   create a momentuHMMData object and the 24-hour cosinor model covariate:
   > ### create momentuHMMData object from crwData object
   > dataHMM <- prepData(crwOut,covNames="temp")</pre>
   > ### add cosinor covariate based on hour of day
   > dataHMM$hour <- as.integer(strftime(dataHMM$time, format = "%H", tz="GMT"))</pre>
   As seen here, the function prepData can also be used for pre-processing the best pre-
   dicted track data from crawlWrap output. The 24-hour cosinor covariate ("hour")
429
   is simply a set of integers (0, 1, \ldots, 23) indicating the hour of day for each obser-
430
```

vation. Now that the data have been pre-processed and the cosinor covariate has

been created, we're ready to fit a 2-state HMM to the elephant track that includes temperature effects on the turning angle concentration parameters and cycling temperature effects (with a 24-hour periodicity) on the step length and state transition probability parameters:

The function getParO was used to extract parameters from an existing model and organize the starting values for the data stream (ParO) and state transition probability (betaO) working parameters in the correct format based on DM and formula, respectively.

The above model identifed an "encamped" (0.74 of time steps) and "exploratory" (0.26 of time steps) state (Figure 1), and was overwhelmingly supported by AIC when compared to alternative models with fewer covariates. Interestingly, this model suggests step lengths and directional persistence for the "encamped" state decreased as temperature increased, step lengths for both states tended to decrease in the late evening and early morning, and transition probabilities from the "encamped" to "exploratory" state decreased as temperature increased (Figure 2). Autocorrelation function plots of the pseudo-residuals (Figure 1) indicate this model explained much of the periodicity in step length, although there does still appear to be some room for improvement.

#### 3.2 Northern fur seal

In our second example, we use the northern fur seal (Callorhinus ursinus) example 451 from McClintock et al. (2014) to demonstrate the use of additional data streams for 452 distinguishing behaviors with similar horizontal trajectories in a multivariate HMM. 453 The data consist of 241 temporally-irregular Fastloc GPS locations obtained during 454 a foraging trip of a nursing female near the Pribilof Islands of Alaska, USA, from 455 10-17 October 2007. The tag included time-depth recording capabilities, and the 456 dive activity data were summarized as the number of foraging dives over T=228457 temporally-regular 1 hr time steps. To fit the Z=3 state (1="resting", 2="foraging", 458 3="transit") of McClintock et al. (2014) using momentuHMM, we first used crawlWrap 459 to predict temporally-regular locations at 1 hr time steps assuming a bivariate normal 460 measurement error model and merged the results with the foraging dive data using 461 the crawlMerge function (see Supplementary Material). Then multiple imputation 462 was used to account for location measurement error by repeatedly fitting the HMM 463 to nSims realizations of the position process using MIfitHMM:

Here we specified a gamma distribution for step length ('step'), wrapped Cauchy distribution for turning angle ('angle'), and Poisson distribution for the number of 466 foraging dives ('dive'). The function getParDM was used to organize the starting 467 values for the data stream working parameters (Par0) in the correct format based on DM, cons, and estimates of the natural parameters (Par) from McClintock et al. (2014). As detailed in Supplementary Material, the DM and cons arguments were 470 specified to avoid label switching among the nSims imputed data model fits and 471 enforce similar state-dependent probability distribution constraints as McClintock 472 et al. (2014), e.g., constraining the Poisson rate parameters such that the "foraging" 473 state tends to have higher numbers of foraging dives than the "transit" state ( $\lambda_2$ ) 474  $\lambda_3$ ). To prohibit foraging dives for the "resting" state, we used the fixPar argument 475 to effectively fix the Poisson rate parameter to zero on the natural scale (i.e.  $\lambda_1 \approx$ 476 0). To help deal with the problem of convergence to local maxima, the retryFits 477 argument allows users to specify the number of times to attempt to re-fit each model 478 using random perturbations of the parameter estimates as the starting values for 470 optimization. 480

The results are very similar to those of the discrete-time model of McClintock et al. (2014), with periods of foraging often followed by resting (Figure 3). The "activity budgets" (i.e. the proportion of time steps allocated to each state) calculated by MIpool based on the estimated state sequences for each imputation were 0.3 (95% CI: 0.22-0.39) for "resting", 0.29 (95% CI: 0.22-0.36) for "foraging", and 0.41 (95% CI: 0.32-0.52) for "transit".

### 3.3 Loggerhead turtle

487

For our third example, we demonstrate how to model movement direction and step 488 length as a function of angular covariates using hitherto unpublished loggerhead 489 turtle (Caretta caretta) data for a captive-raised juvenile released in 2012 on the coast 490 of North Carolina, USA. The data consist of 165 temporally-irregular Argos locations 491 subject to measurement error and rasters of daily ocean surface currents collected 492 between 20 November and 19 December 2012. Assuming a gamma distribution for 493 step length  $(l_t)$  and a wrapped Cauchy distribution for turning angle  $(\phi_t)$ , we model 494 the mean step length parameter  $(\mu_t^l)$  as a function of ocean surface current speed 495  $(w_t)$  and direction  $(r_t)$  relative to the bearing of movement  $(b_t)$ :

$$\mu_t^l = \exp(\beta_0^l + \beta_1^l w_t \cos(b_t - r_t)),$$
(3)

and the turning angle mean parameter  $(\mu_t^{\phi})$  as a trade-off between short-term directional persistence and bias in the direction of ocean surface currents using the circular-circular regression link function:

$$\mu_t^{\phi} = \operatorname{atan2}(\sin(d_t)\beta^{\phi}, 1 + \cos(d_t)\beta^{\phi}), \tag{4}$$

where  $d_t = \text{atan2}(\sin(r_t - b_{t-1}), \cos(r_t - b_{t-1})).$ 

We wish to fit a 2-state HMM to the turtle data, with a "foraging" state unaffected by currents and a "transit" state potentially influenced by ocean surface currents as in Eqs. 3 and 4. We used crawlWrap to predict T=350 temporally-regular locations at 2 hr time steps assuming a bivariate normal measurement error model that accounts for the Argos location quality class (i.e. 3,2,1,0,A,B) of each observation (see Supplementary Material). We then again used multiple imputation to account

```
for location uncertainty by repeatedly fitting the HMM to nSims realizations of the
   position process using MIfitHMM. We first draw nSims realizations of the position
508
   process and extract the corresponding spatial covariates from the raster bricks for
   ocean surface current speed ("speedBrick") and direction ("dirBrick") using MIfitHMM
   with fit=FALSE:
   > miTurtleData <- MIfitHMM(crwOut, nSims = 100, fit=FALSE,
                         spatialCovs = list(w = speedBrick, d = dirBrick, r = dirBrick),
   +
                         angleCovs = "d")
   When the fit argument is FALSE, MIfitHMM returns a list of length nSims composed
   of momentuHMMData objects (miData). For convenience and ease of interpretation,
   we manually added an additional covariate (angle\_osc = cos(b_t - r_t)) to each of the
   imputed data sets and fitted the 2-state HMM using Eqs. 3 and 4 for state 2 ("tran-
   sit"):
516
   > nbStates<-2
   > dist <- list(step = "gamma", angle = "wrpcauchy")</pre>
   > DM <- list(step = list(mean = ~state2(w:angle_osc), sd = ~1),
                  angle = list(mean = ~state2(d), concentration= ~1))
   > turtleFits <- MIfitHMM(miTurtleData$miData, nbStates = nbStates, dist = dist,
                                Par0 = Par0, DM = DM,
   +
   +
                                estAngleMean = list(angle = TRUE),
                                circularAngleMean = list(angle = TRUE))
   > plot(turtleFits, plotCI = TRUE, covs = data.frame(angle_osc = cos(0)))
   Note that the state2 special function in DM indicates the covariate formulas are
   specific to state 2 ("transit") and the circular Angle Mean argument indicates that
   circular-circular regression link function is to be used on the mean turning angle
   parameter as in Eq. 4.
520
      For the "transit" state, pooled parameter estimates indicated step lengths in-
521
```

creased with ocean surface current speed and as the bearing of movement aligned

with ocean surface current direction ( $\beta_1^l = 0.43, 95\%$  CI: 0.1 - 0.77; Figure 4). The estimated wrapped Cauchy distribution for turning angle had mean angles  $(\mu_t^{\phi})$ 524 biased towards the direction of ocean surface currents for each time step ( $\beta^{\phi}$ 525 0.24, 95% CI: -0.01-0.5), with concentration parameter  $\rho_2^{\phi}=0.85$  (95% CI: 526 0.77-0.92) indicating turning angles were concentrated at  $\mu_t^{\phi}$ . Thus movement 527 during the "transit" state appears to strongly follow ocean surface currents (mean  $angle\_osc = 0.87, SD = 0.23$ ), while movement during the "foraging" state exhibited 529 shorter step lengths ( $\mu_1^l=2996\mathrm{m},95\%$  CI: 1791 -4202) perpendicular to ocean sur-530 face currents (mean  $angle\_osc = 0.07, SD = 0.26$ ), with no directional persistence 531  $(\rho_1^{\phi}=0.03)$ . The turtle spent 0.53 (95% CI: 0.34–0.71) of the 2 hr time steps in 532 the "foraging" state and 0.47 (95% CI: 0.29-0.66) of time steps in the "transit" state 533 as it travelled northeast along a predominant current until it (presumably) found an 534 attractive foraging patch (Figure 4). 535

## 536 3.4 Grey seal

For our last example, we perform a similar analysis of a grey seal (Halichoerus grypus) track that was originally conducted by McClintock et al. (2012) using Bayesian
methods and (computationally-intensive) Markov chain Monte Carlo. The data consist of 1045 temporally-irregular Fastloc GPS locations collected in the North Sea
between 9 April and 11 August 2008. Because the seal repeatedly visited the same
haulout and foraging locations, it provides a nice example for demonstrating how
to implement biased movements relative to activity centers using momentuHMM. McClintock et al. (2012) fitted a 5-state model to these data that included three center
of attraction states, with movement biased towards two haulout sites ("Abertay"

and "Farne Islands") and a foraging area ("Dogger Bank"), and two "exploratory" states ("low speed", "high speed") that were unassociated with an activity center. 547 After using crawlWrap to predict T = 1515 temporally-regular locations at 2 hr 548 time steps including a bivariate normal measurement error model (see Supplementary Material), we can perform a very similar analysis to McClintock et al. (2012) 550 in momentuHMM by using the centers argument and state-specific functions for the probability distribution parameters. A cluster analysis on the observed locations 552 using the R package dtwclust (Sarda-Espinosa 2017) identified three centroids with 553 coordinates that were nearly identical to the three activity centers ("Abertay", "Farne 554 Islands", and "Dogger Bank") identified by McClintock et al. (2012). We use these 555 coordinates derive covariates relative to the activity centers when drawing nSims realizations of the position process:

```
> crwSim <- MIfitHMM(crwOut, nSims = 100, fit=FALSE,
+ center = centers)</pre>
```

Specifying the **centers** argument results in the calculation of two covariates for each activity center: the distance (with '.dist' suffix) and angle (with '.angle' suffix) from each location at time t. These covariates can then be used to model parameters as a function of the distance and angle to activity centers for each time step:

562 Similar to McClintock et al. (2012), we assume a Weibull distribution for step length

where both the shape and scale parameter depend on the distance from the location at time t to each activity center. For the activity centers on land ("Abertay" and 564 "Farne"), we allow the (state-dependent) step length parameters to change when the 565 seal is beyond 2500m of the haulout. For the "Dogger" activity center, we allow the parameters to change when the seal is beyond 15000m of this (presumably) foraging area. We thus allow the movement behavior to change within these activity center states upon entering or leaving the viscinity of these sites. We assume a wrapped 569 Cauchy distribution for turning angle with (state-dependent) mean angle derived 570 from the direction to each activity center at time t, and the concentration parameter 571 is modeled similarly to the step length parameters. For the two "exploratory" states, 572 we assumed they are simple random walks unaffected by proximity to activity centers. 573 To complete our model specification, we use the knownStates argument to assign 574 the seal to the corresponding activity center state whenever it was within the 2500m 575 (haulout area) or 15000m (foraging area) thresholds for each imputed data set: 576

As with the step length and turning angle concentration parameters, the state transition probabilities are also allowed to change as a function of distance to activity centers (as specified by the formula argument). The starting values (ParO and betaO)
for each imputation were extracted from a single HMM fitted to the best predicted
locations from crawlWrap, and fixPar was used to remove short-term directional

persistence (and thus formulate the model as a mixture of biased and simple random walks; see Supplementary Material for these finer details).

Estimated activity budgets for the 5 states of this multiple imputation HMM 584 were 0.28 (0.27 - 0.3) for the "Abertay" haul-out state, 0.12 (0.11 - 0.14) for the "Farne Islands" haul-out state, 0.37 (0.35 - 0.38) for the "Dogger Bank" foraging 586 state, 0.09 (0.03 - 0.2) for a low-speed "exploratory" state, and 0.14 (0.08 - 0.23) for a high-speed "exploratory" state. All three activity center states exhibited shorter 588 step lengths and less biased movements when within the viscinity of these targets 589 (Figure 5). Results from this analysis were thus very similar to those of McClintock 590 et al. (2012), but this implementation required far less computation time and no 591 custom model-fitting algorithms. 592

The simData function can be used to simulate tracks from a fitted model:

```
> greySealSim<-simData(model = greySealFits, centers = centers,
+ initialPosition = centers[1,],
+ obsPerAnimal = 1515)</pre>
```

A simulated track is presented along with the fitted track in Figure 6. While potentially useful for study design, power analysis, and prediction, the simData function can also be helpful in assessing goodness of fit by repeatedly drawing simulated data sets from a fitted model and comparing them to observed properties of the data (e.g. Morales et al. 2004).

## 4 Discussion

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Here we have introduced version 1.0.0 of the R package momentuHMM and demonstrated some of its capabilities for conducting multivariate HMM analyses with animal location, auxiliary biotelemetry, and environmental data. The package allows for

fitting (and simulating from) a suite of biased and correlated random walk movement 603 process models (e.g. McClintock et al. 2012), can be used for an unlimited number of 604 data streams and latent behavior states, includes multiple imputation methods to ac-605 count for measurement error, temporal irregularity, and other forms of missing data that would otherwise be prohibitive to maximum likelihood analysis, and integrates 607 seamlessly with rasters to facilitate spatio-temporal covariate modelling. Because 608 the package incorporates biased random walks, it can also be used to implement 609 group dynamic models (e.g. Langrock et al. 2014). The package therefore greatly 610 expands on available software and facilitates the incoporation of more ecological and 611 behavioral realism for hypothesis-driven analyses of animal movement that account 612 for many of the challenges commonly associated with telemetry data. While many of 613 the features of momentuHMM were motivated by animal movement data, we note that 614 the package is not limited to location data and can be used for analyzing any type 615 of data that is amenable to (multivariate) HMMs. 616

Model fitting in momentum is relatively fast because the forward algorithm (Eq. 617 1) is coded in C++. Because multiple imputations are completely parallelizable, 618 with sufficient processing power computation times for analyses that account for 619 measurement error, temporal irregularity, or other forms of missing data need not 620 be longer than that required to fit a single HMM. However, computation times will 621 necessarily be slower as the number of states and/or parameters increase. For exam-622 ple, momentum required about 1 hr to fit a single HMM with N=6 states, seven 623 data streams, and T = 7414 time steps (McClintock 2017). 624

As in any maximum likelihood analysis based on numerical optimization, computation times will also depend on the starting values (Par0 and beta0). Specifying

"good" starting values is arguably the most challenging aspect of model fitting in 627 momentuHMM, particularly for the working scale coefficients when using covariates. 628 The getPar, getPar0, and getParDM functions are designed to help with the speci-629 fication of starting values, and the retryFits argument in crawlWrap, fitHMM, and 630 MIfitHMM will re-optimize based on random perturbations of the parameters to help 631 explore the likelihood surface and diagnose convergence to local maxima. Optimiza-632 tion for the circular-linear regression link function (tan(mean/2); see Table 2) in 633 particular can be prone to local minima, so users are encouraged to explore a range 634 of starting values when fitting these models. 635

While momentuHMM includes functions for drawing realizations of the position pro-636 cess based on the CTCRW model of Johnson et al. (2008), this is but one of many 637 methods for performing the first stage of multiple imputation. Realizations of the 638 position process from any movement model that accounts for measurement error 639 and/or temporal irregularity (e.g. Calabrese et al. 2016; Gurarie et al. 2017) could 640 be passed to MIfitHMM for HMM-type analyses in the second stage. Multiple im-641 putation methods also need not be limited to these telemetry error scenarios. For 642 example, conventional missing data could also be imputed using standard techniques 643 (Rubin & Schenker 1986), thereby allowing the investigation of non-random mecha-644 nisms for missingness that can be problematic if left unaccounted for in HMMs. 645

There remain many potential avenues for refining and extending the capabilities 646 of momentum. Computation times could likely be improved by further optimizing the R and C++ code for speed. Notable extensions include hidden semi-Markov models and random effects on data stream probability distribution and state transition probability parameters (Zucchini et al. 2016). We would also like to incorporate

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additional parameters for change-point thresholds and the locations of activity centers instead of requiring that they be pre-specified (and potentially compared using AIC or other model selection criteria) as in grey seal example. Lastly, it is relatively straightforward to add additional probability distributions, and we are pleased to do so upon request. Practitioners interested in additional features for momentuHMM are

encouraged to contact the authors.

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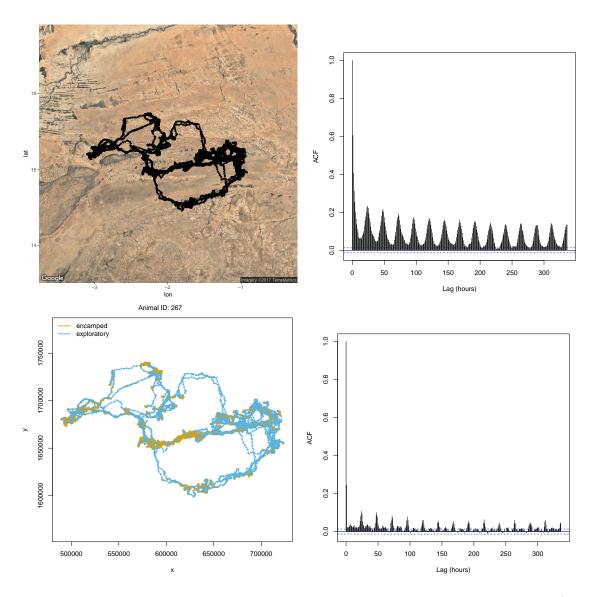


Figure 1. Plot of the elephant track produced using the 'plotSat' function (top-left panel), autocorrelation function (ACF) plot of the corresponding step length data (top-right panel), plot of the Viterbi-decoded state sequence for the 2-state ("encamped" and "exploratory") model generated using the generic 'plot' function (bottom-left panel), and the step length pseudo-residual ACF plot for this model using the 'plotPR' function (bottom-right panel).

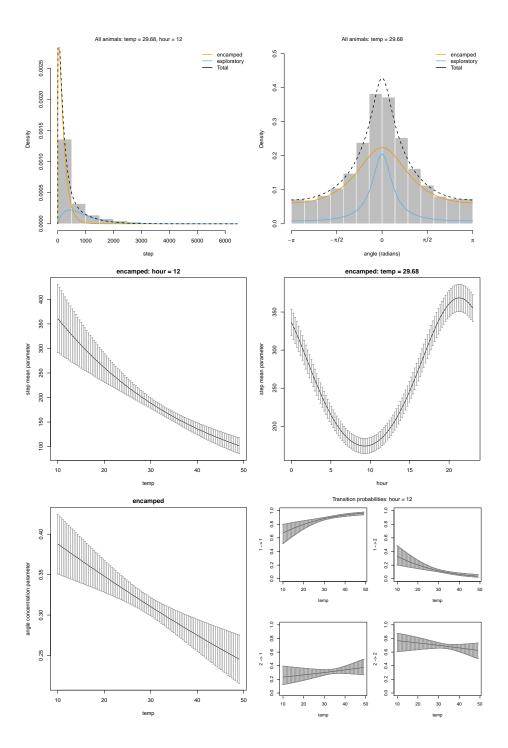


Figure 2. Selected plots for the 2-state ("encamped" and "exploratory") African elephant example generated using the generic 'plot' function. Top panels present histograms of the step length (top-left) and turning angle (top-right) data along with the estimated state-dependent probability distributions based on the mean temperature (temp = 29.7 degrees celsius) at 12:00 GMT (hour = 12). Middle panels present estimates (and 95% confidence intervals) for the step length mean parameter of the "encamped" state as a function of temperature and hour of day. Bottom-left panel presents estimates for the turning angle concentration parameter of the "encamped" state as a function of temperature. Bottom-right panel presents estimated state transition probabilities (1 = "encampled", 2 = "exploratory") as a function of temperature at 12:00 GMT.

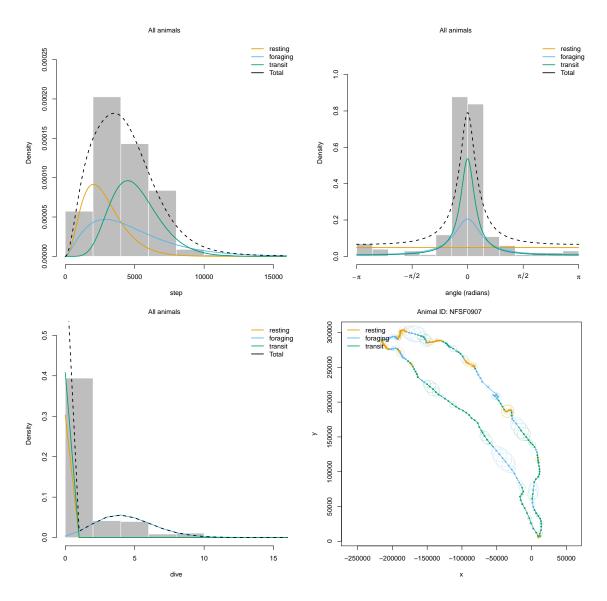


Figure 3. Plots of the northern fur seal example results generated using the generic 'plot' function. The estimated probability distributions for step length (top-left panel), turning angle (top-right panel), and number of foraging dives (bottom-left panel) for the 3-state ("resting", "foraging", and "transit") model are plotted along with histograms of these data streams. The temporally-regular predicted locations (and 95% ellipsoidal confidence bands) and estimated states are plotted in the bottom-right panel. All estimates are pooled across multiple imputations of the position process and thus reflect uncertainty attributable to location measurement error and temporally-irregular observations.

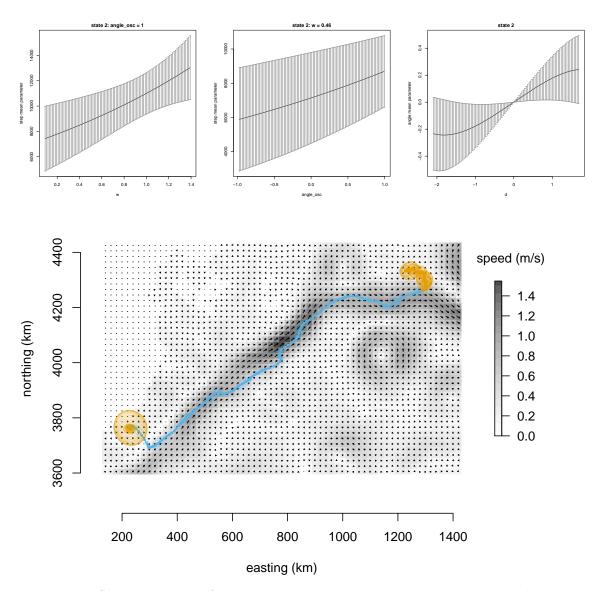


Figure 4. Selected results from the loggerhead turtle example. Top panels include estimates and 95% confidence intervals for the mean step length parameter as a function of ocean surface current speed (w) when ocean surface current direction  $(r_t)$  is the same as the bearing  $(b_t)$  of movement (i.e.  $angle\_osc = cos(b_t - r_t) = 1$ ; top-left panel), mean step length parameter as a function of  $angle\_osc$  at the mean ocean surface current speed (w = 0.46 m/s; top-middle panel), and mean turning angle parameter as a function of  $d_t = atan2(\sin(r_t - b_{t-1}), \cos(r_t - b_{t-1}))$  (top-right panel). Bottom panel plots the pooled track, 95% error ellipse confidence bands, and state (orange = "foraging", blue = "transit") estimates based on multiple imputations of the position process relative to ocean surface current speed (m/s) and direction on 2 December 2012.

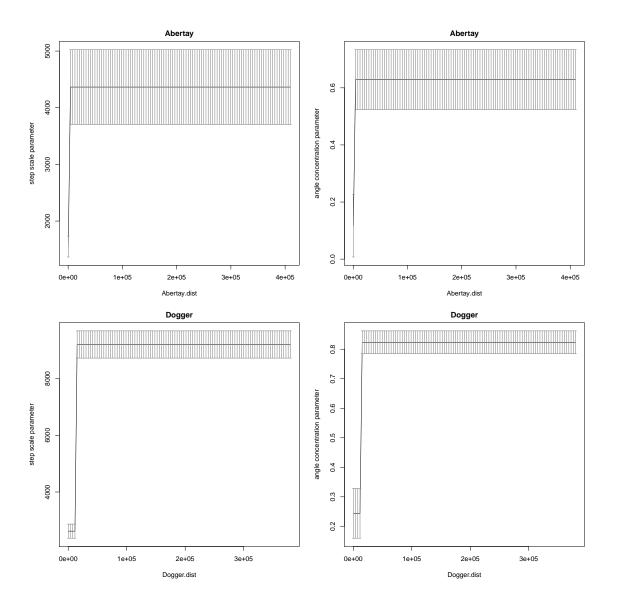
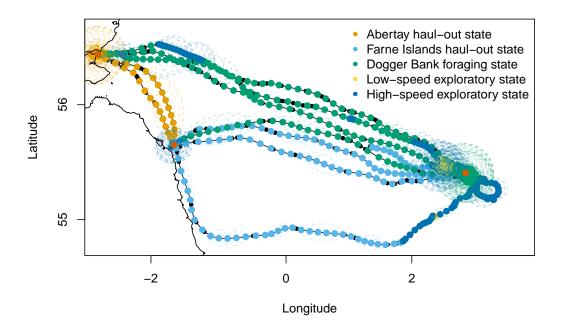


Figure 5. Selected results from the grey seal example. Panels include estimates and 95% confidence intervals for the "Abertay" haul-out state step length scale parameter as a function of distance in meters ('Abertay.dist'; top-left panel), "Abertay" haul-out state turning angle concentration parameter as a function of distance (top-right panel), "Dogger Bank" foraging state step length scale parameter as a function of distance ('Dogger.dist'; bottom-left panel), and the "Dogger Bank" foraging state turning angle concentration parameter as a function of distance (bottom-right panel).



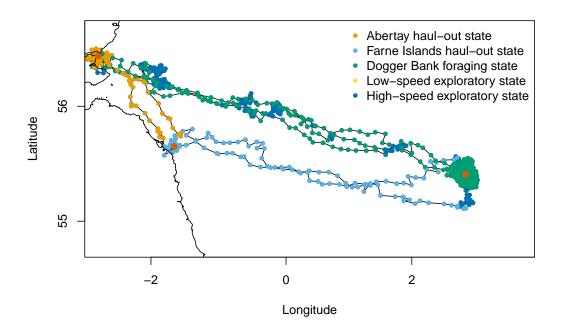


Figure 6. Fitted and simulated tracks from the grey seal example. This seal tended to move in a clockwise fashion between two haul-out locations ("Abertay" and "Farne Islands") and a foraging area ("Dogger Bank") in the North Sea. Top panel plots the pooled track, 95% error ellipse confidence bands, and state estimates based on the 5-state HMM fitted to multiple imputations of the position process. Red points indicate the locations of the three activity centers. Black points indicate the (temporally-irregular) observed locations. Bottom panel presents the locations and states for a track simulated from the fitted model using the 'simData' function.