

$$R_0 = Q_0 + C_0$$

$$Q_0 = B_0 + \sum_{V_j, P_j < P_0} \left\lceil \frac{Q_0 + 0.1}{T_j} \right\rceil C_j$$

Since  $P_0$  is the smallest,  $\sum_{V_j, P_j < P_0} \left\lceil \frac{Q_0 + 0.1}{T_j} \right\rceil C_j = 0$

$$\Rightarrow R_0 = B_0 + C_0 = 30 + 10 = 40$$

Iteration	LHS ( $Q_0$ )	$B_0$	RHS	Stop?
1	30	30	30	yes

2.

Iteration	LHS ( $Q_1$ )	$B_1$	$j$	$Q_1 + \tau$	$T_j$	$\left\lceil \frac{Q_1 + \tau}{T_j} \right\rceil$	$C_j$	RHS	Stop?
1	30	30	0	30.1	50	1	10	40	no
2	40	30	0	40.1	50	1	10	40	yes

Based on the above table,

$$R_1 = Q_1 + C_1 = 40 + 30 = 70$$

3.

Iteration	LHS ( $Q_2$ )	$B_2$	$j$	$Q_2 + \tau$	$T_j$	$\left\lceil \frac{Q_2 + \tau}{T_j} \right\rceil$	$C_j$	RHS	Stop?
1	20	20	0 1	20.1 20	50 200	1 1	10 30	60	no
2	60	20	0 1	60.1 20	50 200	2 1	10 30	70	no
3	70	20	0 1	70.1 20	50 200	2 1	10 30	70	yes

Based on the above table,

$$R_2 = Q_2 + C_2 = 70 + 20 = 90$$

```

/*
1.44
2.04
2.56
3.16
3.68
4.28
5.2
8.4
9
9.68
10.2
19.36
19.8
20.32
29.4
29.76
30.28
*/

#include <bits/stdc++.h>
using namespace std;

int main()
{
    ios_base::sync_with_stdio(false);
    cin.tie(NULL);

    double n, tau;
    cin >> n >> tau; // n = number of messages, tau = time doubleerval
    vector<double> priority(n), transmission_time(n), period(n), response_time(n, 0);

    for (int i = 0; i < n; i++)
        cin >> priority[i] >> transmission_time[i] >> period[i];

    for (int i = 0; i < n; i++)
    {
        double LHS = -1, RHS = transmission_time[i];
        while (LHS != RHS)
        {
            LHS = RHS;
            double blocking_time = 0, sigma = 0;
            for (int j = 0; j < n; j++)
            {
                if (priority[j] >= priority[i])
                    blocking_time = max(blocking_time, transmission_time[j]);
            }
            for (int j = 0; j < n; j++)
            {
                if (priority[j] < priority[i])
                    sigma += ceil((LHS + tau) / period[j]) * transmission_time[j];
            }
            RHS = blocking_time + sigma;
        }
        response_time[i] = RHS + transmission_time[i];
    }

    for (int i = 0; i < n; i++)
        cout << response_time[i] << "\n";

    return 0;
}

```

1.

Iteration	LHS ( $R_0$ )	$C_0$	RHS	Stop?
1	10	10	10	Yes

$R_0 = C_0 = 10.$

2.

Iteration	LHS ( $R_1$ )	$C_1$	$j$	$R_1$	$T_j$	$\left\lceil \frac{R_1}{T_j} \right\rceil$	$C_j$	RHS	Stop?
1	30	30	0	30	50	1	10	40	no
2	40	30	0	40	50	1	10	40	Yes

$R_1 = 40.$

3.

Iteration	LHS ( $R_2$ )	$C_2$	$j$	$R_2$	$T_j$	$\left\lceil \frac{R_2}{T_j} \right\rceil$	$C_j$	RHS	Stop?
1	20	20	0	20	50	1	10	60	no
			1		200	1	30		
2	60	20	0	60	50	2	10	70	no
			1		200	1	30		
3	70	20	0	70	50	2	10	70	Yes
			1		200	1	30		

$R_2 = 70.$

4.

The algorithm for  $M$  overestimates the worst case response time while the algorithm for  $P$  doesn't.

1.

$$(2, 5, 1, 2) \rightarrow (4, 10, 1, 2, 6, 7)$$

2.

$$(4, 10, 0, 3, 5, 6) \rightarrow (4, 10, 0, 3, 5, 6, 10, 13, 15, 16) \quad a$$

3.

$$(4, 10, 1, 2, 6, 7) \rightarrow (4, 10, 1, 2, 6, 7, 11, 12, 16, 17) \quad s$$

4.

$k$	$\max_{1 \leq j \leq n} (s_{j+k} - s_j)$	=	$\min_{1 \leq i \leq m} (a_{i+k-1} - a_i)$	=	(Column-3) - (Column-5)
1	$\max_{1 \leq j \leq 4} (s_{j+1} - s_j)$	4	$\min_{1 \leq i \leq 4} (a_i - a_i)$	0	4
2	$\max_{1 \leq j \leq 4} (s_{j+2} - s_j)$	5	$\min_{1 \leq i \leq 4} (a_{i+1} - a_i)$	1	4
3	$\max_{1 \leq j \leq 4} (s_{j+3} - s_j)$	9	$\min_{1 \leq i \leq 4} (a_{i+2} - a_i)$	3	6
4	$\max_{1 \leq j \leq 4} (s_{j+4} - s_j)$	10	$\min_{1 \leq i \leq 4} (a_{i+3} - a_i)$	6	4

5.

$$\text{worst case response time} = 1 + 6 = 7$$

1.

$\alpha$	$\beta$	$\gamma$	LHS	$\alpha + \beta - \gamma \leq 1$	$\alpha - \beta + \gamma \leq 1$	$-\alpha + \beta + \gamma \leq 1$	RHS	LHS=RHS?
0	0	0	T	T	T	T	T	T
0	0	1	T	T	T	T	T	T
0	1	0	T	T	T	T	T	T
0	1	1	F	T	T	F	F	T
1	0	0	T	T	T	T	T	T
1	0	1	F	T	F	T	F	T
1	1	0	F	F	T	T	F	T
1	1	1	T	T	T	T	T	T

2.

$\alpha$	$\beta$	$\gamma$	LHS	$\alpha + \beta - 1 \leq \gamma$	$\gamma \leq \alpha$	$\gamma \leq \beta$	RHS	LHS=RHS?
0	0	0	T	T	T	T	T	T
0	0	1	F	T	F	F	F	T
0	1	0	T	T	T	T	T	T
0	1	1	F	T	F	T	F	T
1	0	0	T	T	T	T	T	T
1	0	1	F	T	T	F	F	T
1	1	0	F	F	T	T	F	T
1	1	1	T	T	T	T	T	T

3.

$\beta$	LHS	$0 \leq y \leq x$	$x - M(1 - \beta) \leq y$	$y \leq M\beta$	RHS
0	$0 = y$	$0 \leq y \leq x$	$x - M \leq y$	$y \leq 0$	$x - M \leq y = 0 \leq x$
1	$x = y$	$0 \leq y \leq x$	$x \leq y$	$y \leq M$	$0 \leq y = x \leq M$

from the table, we can know

$$x - M \leq 0 \leq x \quad \Rightarrow \quad M \geq x \geq y \geq 0$$

$$0 \leq y = x \leq M$$

since  $x \leq 2022$ , we can select  $M$  as 2022.

1.

Yes.

To transmit  $\mu_0$ , we need  $8 + 44 + 3$  bits.

"  $\mu_1$ , "  $16 + 44 + 3$  "

"  $\mu_0'$ , "  $16 + 44 + 3$  "

We can save a lot bits if we use the new design.

2.

No.

The senders are not the same.

3.

Yes.

$$\mu_0' = (16 + 44 + 3) / 50 = 1.26 \text{ bpms}$$

$$\mu_2 = (16 + 44 + 3) / 50 = 1.26 \text{ bpms}$$

$$\mu_3 = (16 + 44 + 3) / 100 = 0.63 \text{ bpms}$$

Since the sender of  $\mu_0'$  and  $\mu_3$  are the same, we can concat  $\mu_3$  behind  $\mu_0'$ .

$$\mu_0'' = (32 + 44 + 3) / 50 = 1.58 < 1.26 + 0.63$$