

Biological Vision and Applications

Module 05-04: Probabilistic models

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Information theoretic model

- Challenges à-prior defined features for attention in Cognitive models
- Based on Shannon's information theory:
 - ▶ The event that is least likely to occur has the maximum information value
 - ▶ Self-information of an event x : $-\log P(x)$
- Image region that is least likely to occur in an image is the most salient one
- How to decide what is least likely to occur?

Shannon's Information theory

A generative model of an image

Independent Component Analysis

- An image region (signal) is a manifestation of some underlying hidden processes
- It is a weighted sum of contributions from each process
 - ▶ The processes are independent of each other
 - ▶ The processes are hidden
 - ▶ The weights are unknown
- We resort to Natural Scene Statistics
 - ▶ Observe a large number of images
 - ▶ Learn the processes and the weights
- Given a new image, we would expect each region to be a weighted sum of contributions from some of these features

Independent Component Analysis

What is unexpected ?

- Model a new image with the learned features
 - ▶ Select features for best fit over all image regions
- There will be some outlier regions, which do not fit
 - ▶ Has least probability to occur
 - ▶ Has most information value
- These image regions are the salient ones
 - ▶ Lower is the probability, the higher is the saliency
- Bruce. Features that draw visual attention: ...
- Bruce & Tsotsos. Saliency Based on Information Maximization (2006)

Bayesian model

Based on “surprise” – brings in exponential factor

- Image regions (observed data) are caused by some hidden states (features)
- Bayesian definition of surprise
 - ▶ M : a continuous range of states (features that manifests as image regions)
 - ▶ $p(m)$: the prior pdf for states (characterizes alternate models)
 - ▶ $p(m | D)$: the posterior pdf for the states, after experiencing some data D
- The surprise factor of the data D is defined as
 - ▶ The difference between the posterior and the prior pdfs for M
 - ▶ $S(D) = KLD(p(m), p(m | D)) = \int_m p(m) \cdot \log \frac{p(m)}{p(m|D)} \cdot dm$

Surprise

... contd.

- The surprise factor of the data D : $S(D) = \int_m p(m) \cdot \log \frac{p(m)}{p(m|D)} \cdot dm$
- Baye's Theorem: $p(m | D) = \frac{p(m)P(D|m)}{P(D)}$
- Using Baye's Theorem and simplifying [$\int_m p(m) = 1$]
 - ▶ $S(D) = \log P(D) - \int_m \log P(D | m) \cdot dm$
- The model of the environment builds incrementally as the agent observes
 - ▶ For repeated observations, posterior of one observation is the prior for the next
 - ▶ Leads to change awareness

Itti & Baldi. Bayesian Surprise Attracts Human Attention (2005)

Outlier and surprise

Criticism to information theoretic model

- Outlier D : $P(D \mid M_{\text{best}})$ to have low value
- Suppose $P(D \mid M')$ is low for all possible alternate models M'
- D has little informative value for discriminating the models for best explanation of the observation
- Cannot be treated as “surprise” and cannot be considered to be a guiding factor for attention

Eye movement ?

- Fixations and saccades are guided by WTA and RL policies as in Cognitive models

Quiz 05-04

End of Module 05-04