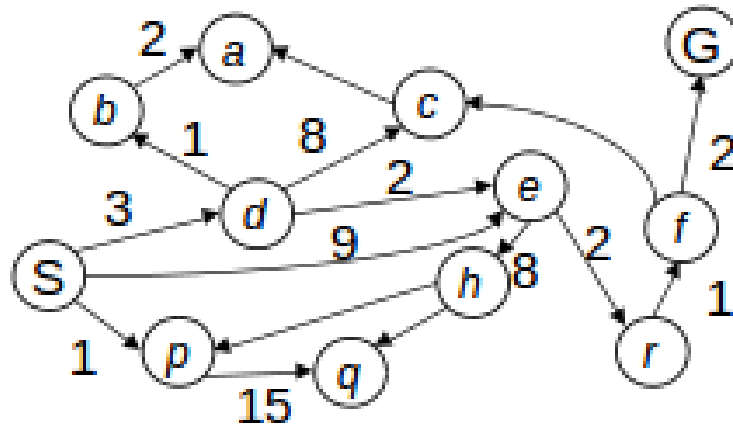
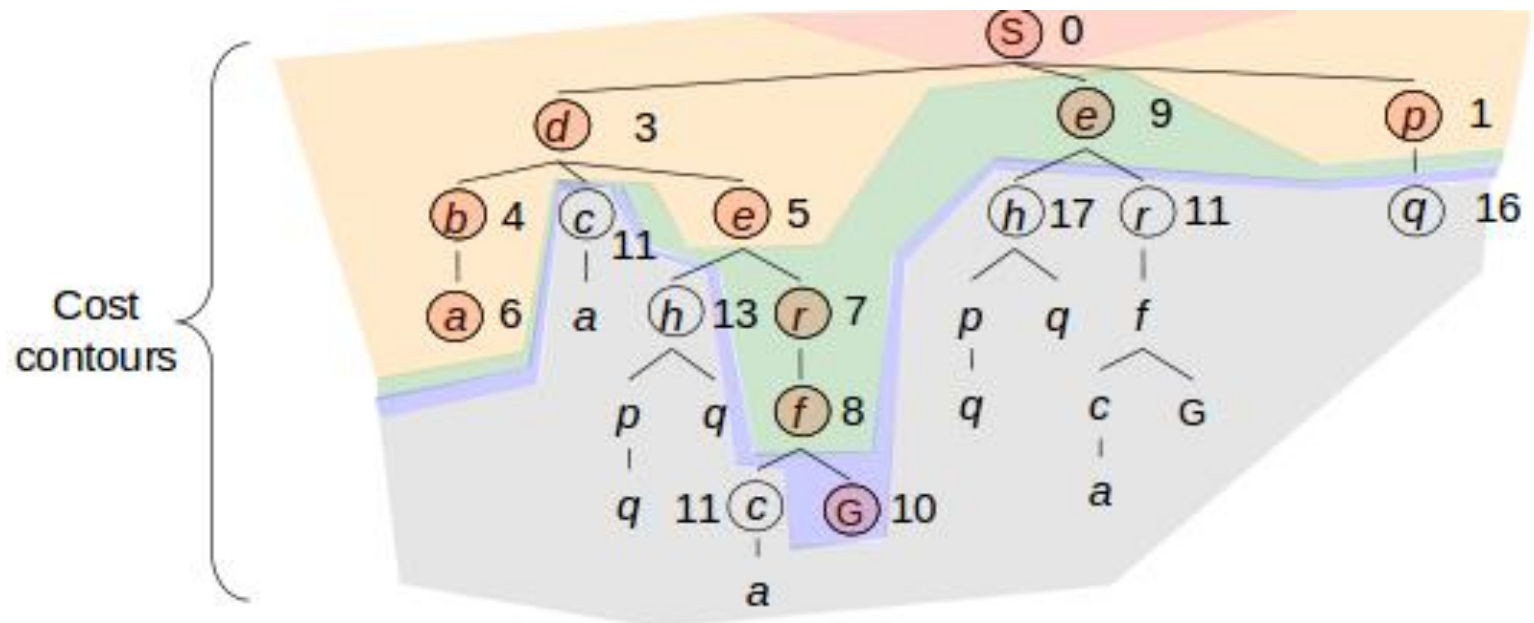


# Uniform Cost Search



- Strategy: Expand cheapest node first.
- Data structure: ?



# Uniform Cost Search: Algorithm

- Insert the root node into the priority queue
- *Repeat while the queue is not empty:*
  - Remove the element with the highest priority
  - If the removed node is the destination,*
    - print total cost and stop the algorithm
  - Else,*
    - enqueue all the children of the current node to the priority queue, with their cumulative cost from the root as priority.

# Heuristic Search

# Outline

- Best-first search
- Greedy best-first search
- $A^*$  search
- Heuristics
- Local search algorithms
- Hill-climbing search

# Heuristic Search

- Heuristics are criteria for deciding which among several alternatives be the most effective in order to achieve some goal.
- Heuristic is a technique that
  - improves the efficiency of a search process possibly by sacrificing claims of systematicity and completeness.
  - It no longer guarantees to find the best answer but almost always finds a very good answer.

# Heuristic Search – Contd..

- Using good heuristics, we can hope to get good solution to hard problems in less than exponential time.
- There are **general-purpose** heuristics that are useful in a wide variety of problem domains.
- We can also construct **special purpose** heuristics, which are domain specific.

# General Purpose Heuristics

- A general-purpose heuristics for combinatorial problem is
  - **Nearest neighbor algorithms** which works by selecting the locally superior alternative.
- In many AI problems,
  - it is often hard to measure precisely the goodness of a particular solution.
  - But still it is important to keep performance question in mind while designing algorithm.

# Contd...

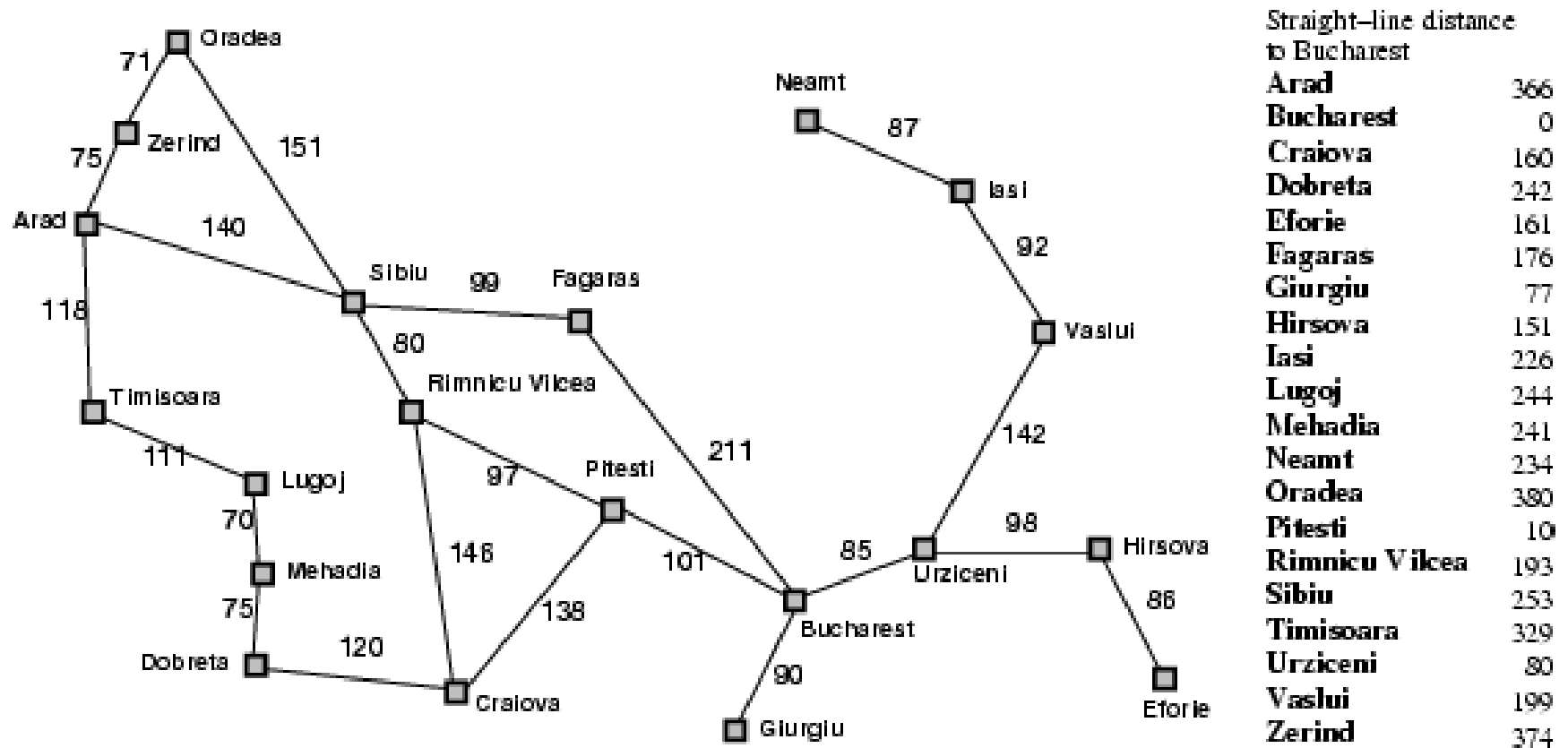
- For real world problems,
  - it is often useful to introduce heuristics based on relatively unstructured knowledge.
  - It is impossible to define this knowledge in such a way that mathematical analysis can be performed.
- In AI approaches,
  - behavior of algorithms are analyzed by running them on computer as contrast to analyzing algorithm mathematically.



# Best-first search

- Idea: use an **evaluation function**  $f(n)$  for each node
  - estimate of "desirability"
  - Expand most desirable unexpanded node
- Implementation:  
Order the nodes in fringe in decreasing order of desirability
- Special cases:
  - greedy best-first search
  - A\* search

# Romania with step costs in km



# Greedy best-first search

- Evaluation function  $f(n) = h(n)$  (**h**euristic)
- = estimate of cost from  $n$  to *goal*
- e.g.,  $h_{SLD}(n)$  = straight-line distance from  $n$  to Bucharest
- Greedy best-first search expands the node that **appears** to be closest to goal

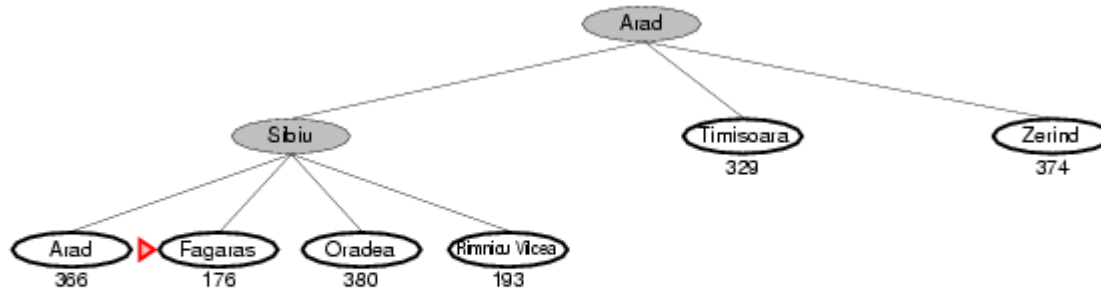
# Greedy best-first search example



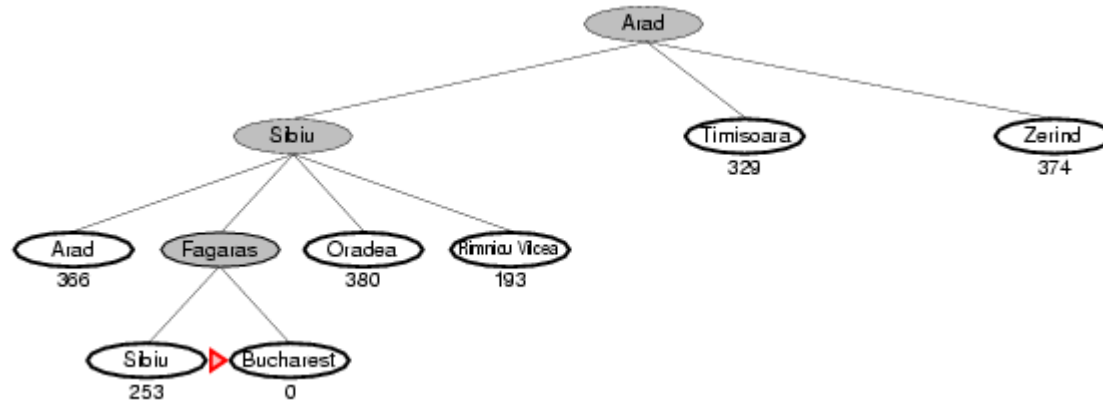
# Greedy best-first search example



# Greedy best-first search example



# Greedy best-first search example



# Properties of greedy best-first search

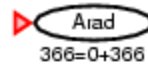
- Complete?
- No – can get stuck in loops, e.g., lasi → Neamt → lasi → Neamt →
- Time?
- $O(b^m)$ , but a good heuristic can give dramatic improvement
- Space?
- $O(b^m)$  -- keeps all nodes in memory
- Optimal?



# A\* search

- Idea: avoid expanding paths that are already expensive
- Evaluation function  $f(n) = g(n) + h(n)$
- $g(n)$  = cost so far to reach  $n$
- $h(n)$  = estimated cost from  $n$  to goal
- $f(n)$  = estimated total cost of path through  $n$  to goal

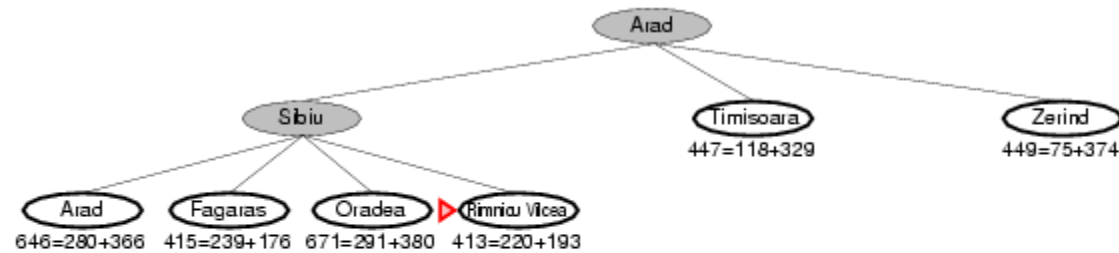
# A\* search example



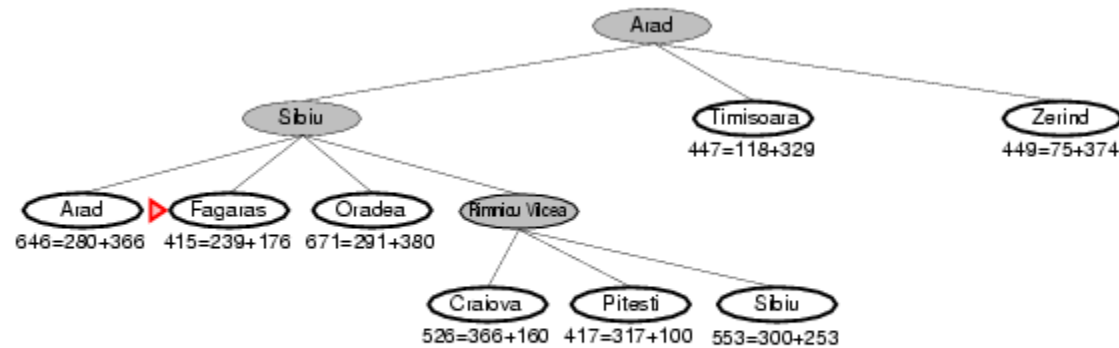
# A\* search example



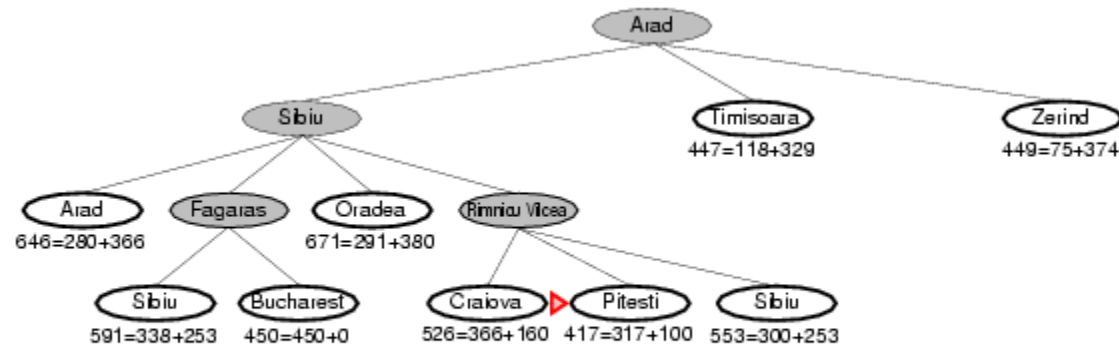
# A\* search example



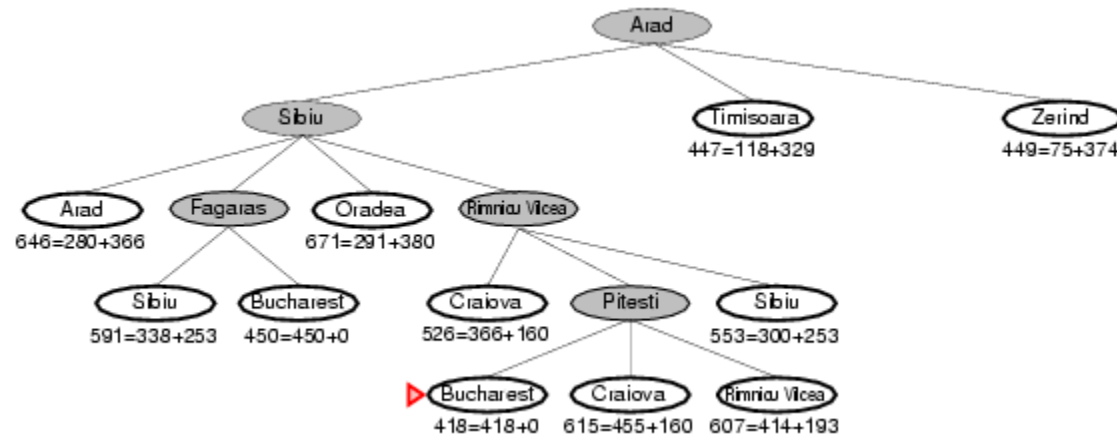
# A\* search example



# A\* search example



# A\* search example



# Admissible heuristics

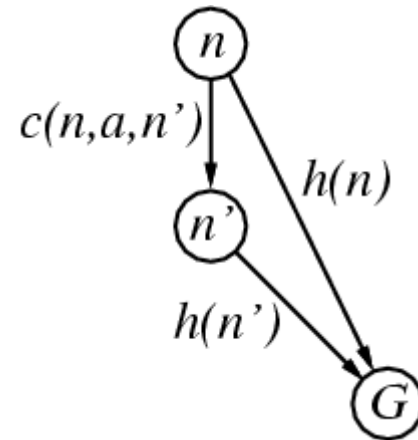
- A heuristic  $h(n)$  is **admissible** if for every node  $n$ ,  $h(n) \leq h^*(n)$ , where  $h^*(n)$  is the **true** cost to reach the goal state from  $n$ .
- An admissible heuristic **never overestimates** the cost to reach the goal, i.e., it is **optimistic**
- Example:  $h_{SLD}(n)$  (never overestimates the actual road distance)



# Consistent heuristics

- A heuristic is **consistent** if for every node  $n$ , every successor  $n'$  of  $n$  generated by any action  $a$ ,

$$h(n) \leq c(n,a,n') + h(n')$$



# Properties of $A^*$

- Complete?
- Yes (unless there are infinitely many nodes with  $f \leq f(G)$  )
- Time?
- Exponential
- Space?
- Keeps all nodes in memory
- Optimal?
- Yes

# Dominance

- If  $h_2(n) \geq h_1(n)$  for all  $n$  (both admissible)
- then  $h_2$  **dominates**  $h_1$
- $h_2$  is better for search
- Typical search costs (average number of nodes expanded):
  - $d=12$       IDS = 3,644,035 nodes  
     $A^*(h_1) = 227$  nodes  
     $A^*(h_2) = 73$  nodes
  - $d=24$       IDS = too many nodes  
     $A^*(h_1) = 39,135$  nodes  
     $A^*(h_2) = 1,641$  nodes
  -

# Relaxed problems

- A problem with fewer restrictions on the actions is called a **relaxed problem**
- The cost of an optimal solution to a relaxed problem is an admissible heuristic for the original problem
- If the rules of the 8-puzzle are relaxed so that a tile can move **anywhere**, then  $h_1(n)$  gives the shortest solution
- If the rules are relaxed so that a tile can move to **any adjacent square**, then  $h_2(n)$  gives the shortest solution

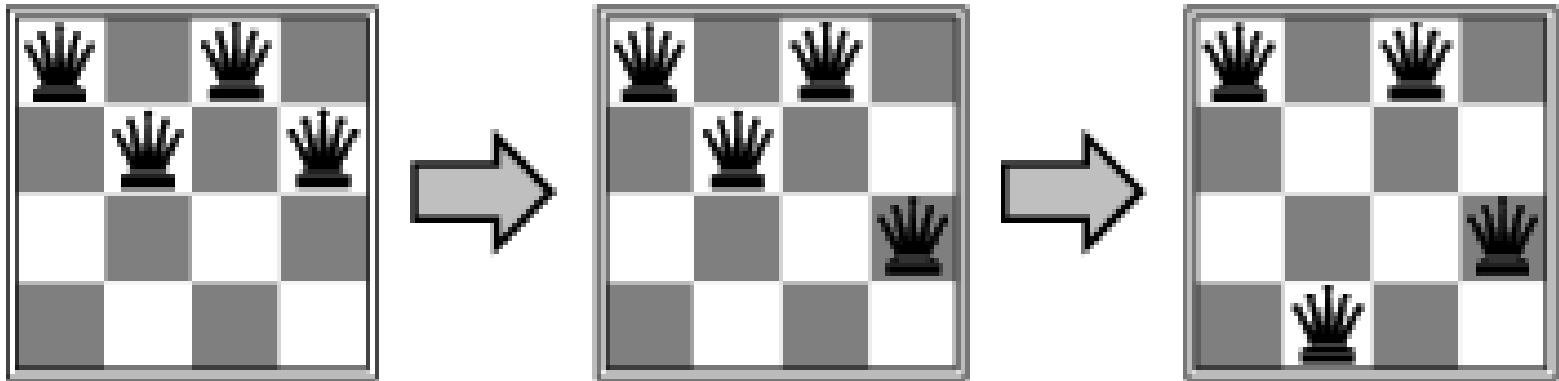
# Local search algorithms

- In many optimization problems, the **path** to the goal is irrelevant; the goal state itself is the solution
- State space = set of "complete" configurations
- Find configuration satisfying constraints, e.g., n-queens
- In such cases, we can use **local search algorithms**
- keep a single "current" state, try to improve it

# Example: $n$ -queens

- Put  $n$  queens on an  $n \times n$  board with no two queens on the same row, column, or diagonal

- 



# Hill Climbing- Algorithm

## **Generate and Test *Algorithm***

### ***Start***

- Generate a possible solution
- Test to see, if it is goal.
- If not go to start else quit

### ***End***

# Hill Climbing- (Variant of generate and test strategy)

- Search efficiency may be improved if there is some way of ordering the choices so that the most promising node is explored first.
- Moving through a tree of paths, hill climbing proceeds
  - in depth-first order but the choices are ordered according to some **heuristic** value (i.e, measure of remaining cost from current to goal state).



# Example of heuristic function

- Straight line (as the crow flies) distance between two cities may be a heuristic measure of remaining distance in traveling salesman problem .

# Hill climbing : Algorithm

- Store initially, the root node in a OPEN list (maintained as stack) ;     Found = false;
- While ( OPEN  $\neq$  empty and Found = false)    Do  
{
  - Remove the top element from OPEN list and call it NODE;
  - If NODE is the goal node, then **Found = true** else find SUCCs, of NODE, if any, and **sort SUCCs** by estimated cost from NODE to goal state and add them to the front of OPEN list.
- } /\* end while \*/
- If **Found = true** then return **Yes** otherwise return **No**
- Stop

# Problems in hill climbing

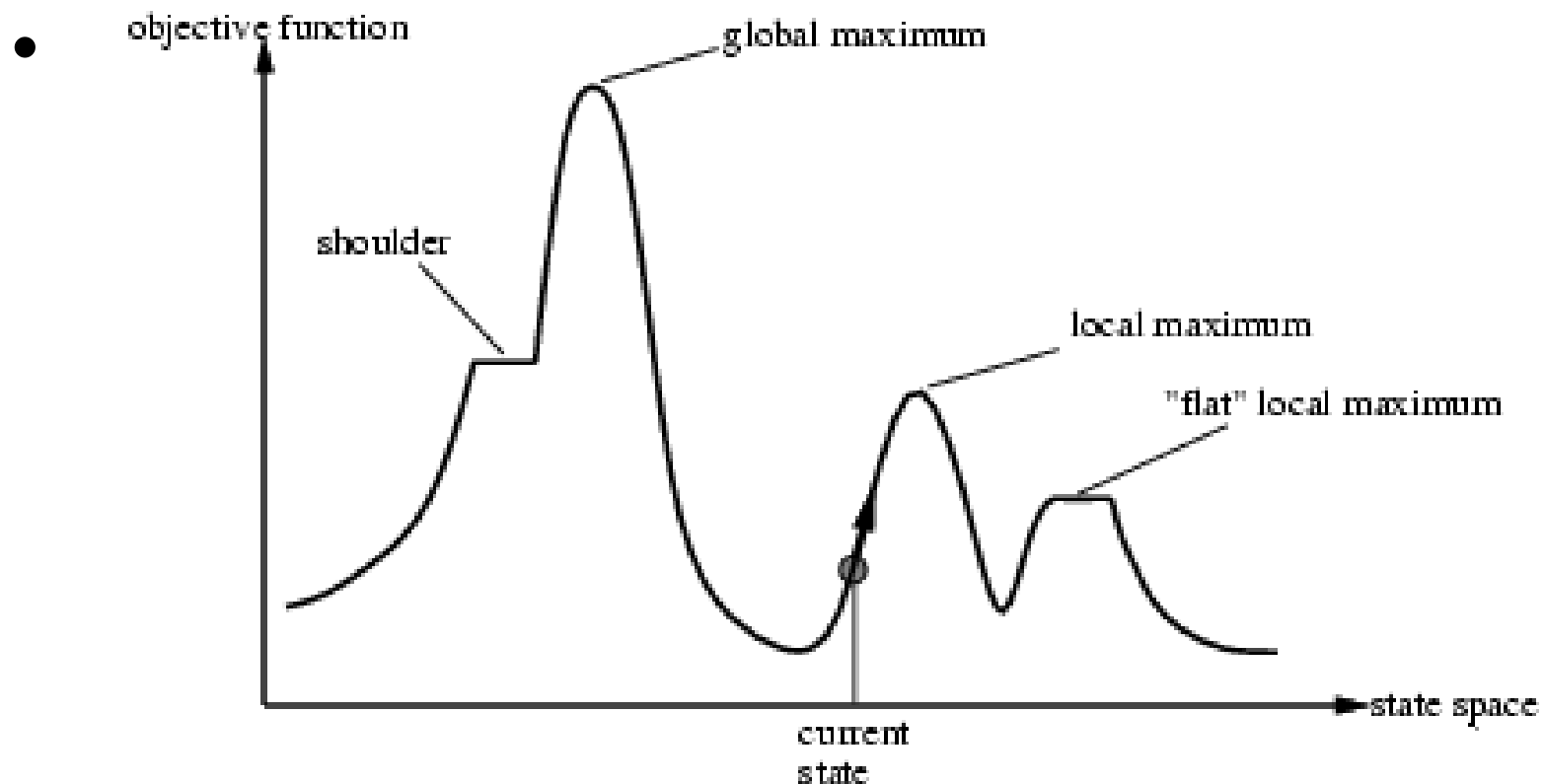
- There might be a position that is not a solution but from there no move improves situations?
- This will happen if we have reached a *Local maximum*, a *plateau* or a *ridge*.
  - **Local maximum:** It is a state that is better than all its neighbors but is not better than some other states farther away. All moves appear to be worse.
    - *Solution to this is to backtrack to some earlier state and try going in different direction.*

# Contd...

- **Plateau:** It is a flat area of the search space in which, a whole set of neighboring states have the same value. It is not possible to determine the best direction.
  - *Here make a big jump to some direction and try to get to new section of the search space.*
  - *Here apply two or more rules before doing the test i.e., moving in several directions at once.*

# Hill-climbing search

- Problem: depending on initial state, can get stuck in local maxima



# Hill-climbing search: 8-queens problem

18	12	14	13	13	12	14	14
14	16	13	15	12	14	12	16
14	12	18	13	15	12	14	14
15	14	14	♚	13	16	13	16
♚	14	17	15	♚	14	16	16
17	♚	16	18	15	♚	15	♚
18	14	♚	15	15	14	♚	16
14	14	13	17	12	14	12	18

- $h$  = number of pairs of queens that are attacking each other, either directly or indirectly
- $h = 17$  for the above state
-

# Hill-climbing search: 8-queens problem

