

Biological Vision and Applications

Module 02-05: Motion Perception

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Rigid, Elastic and Fluid Motion

- **Rigid motion** is where the moving object does not change shape
- **Elastic motion** is where the moving object changes shape with some continuity
- **Fluid motion** is where the continuity is not there

- o Translation
- o Rotation
- o Scaling



Rigid Motion



Elastic Motion

What is the problem?

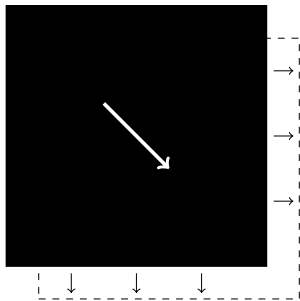
- An image is motion: $I(x, y, t)$
- The motion: $\vec{V}(x, y, t)$
- How to estimate $\vec{V}(x, y, t)$ from values of $I(x, y, t)$ observed over time
- Sometimes it is sufficient to detect motion
 - ▶ Measurement not necessary

Continuous and Discrete Motion

- Human observers can distinguish two types of motion
 - ▶ Continuous
 - ▶ Discrete
- To recognize continuous motion, an object need not move continuously over retinal field
 - ▶ Examples: Alternately blinking on of festive decoration lights, movie / TV
- There are two stages of motion recognition
 - ▶ Short range (60 - 100ms, 10 - 15' of visual arc): Based on local intensity changes
 - ▶ Local contrasts: early vision
 - ▶ Long range (400ms): Based on token matching
 - ▶ Object recognition: late vision

Intensity based scheme

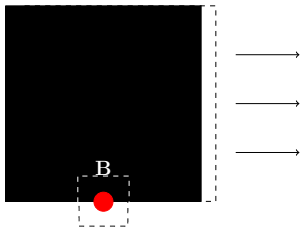
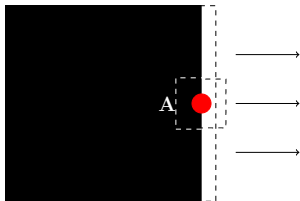
Basic Principle



- See the contour changing and infer motion
- Works well when there is significant intensity variation
 - ▶ Can be applied to object boundaries if there is a significant contrast between FG and BG

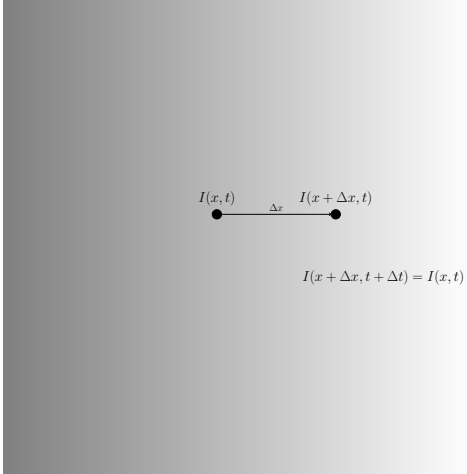
Estimating local motion

Aperture problem



- The motion can be perceived near point A
 - ▶ Intensity changes with time
- The motion cannot be perceived near point B
 - ▶ No intensity changes with time
 - ▶ Aperture problem

Gradient model of motion estimation



$I(x, t)$ $I(x + \Delta x, t)$

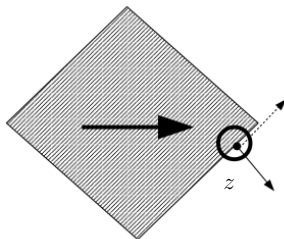
Δx

$$I(x + \Delta x, t + \Delta t) = I(x, t)$$

- $\Delta I = I(x + \Delta x, t) - I(x, t)$
- $\Delta x = \Delta I / \frac{\partial I}{\partial x}$
- $\Delta t = -\Delta I / \frac{\partial I}{\partial t}$
- $v = \frac{\Delta x}{\Delta t} = -\frac{\partial I / \partial t}{\partial I / \partial x}$

Gradient model of motion estimation

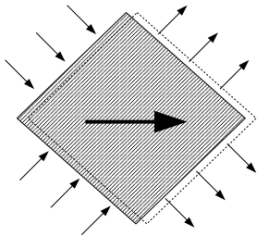
contd.



- Motion is estimated from the local gradients of the image intensity.
- The local velocity at z , in the direction of the spatial intensity gradient
- $v(z, t) \nabla I = -\frac{I_t(z, t)}{|\nabla I(z, t)|}$
 - ▶ where
 - ▶ $I_t(z, t)$ represents the temporal gradient for local illumination change
 - ▶ $|\nabla I(z, t)|$ represents the magnitude of spatial gradient for local illumination change

Rigid motion in image plane

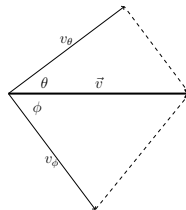
Constant velocity assumption (translation only)



- The overall 2D motion of a rigid object can be estimated from the perceived motion at various points on the contour.

- Need minimum two points ($\theta \neq \phi$)

- ▶ Let $\vec{V} = (v_x, v_y)$
- ▶ $v_\theta = v_x \cdot \cos\theta + v_y \cdot \sin\theta$
- ▶ $v_\phi = v_x \cdot \cos\phi + v_y \cdot \sin\phi$
- ▶ Solve for v_x, v_y



Error resilience

Why we should observe at many points

- Minimize RMS error in

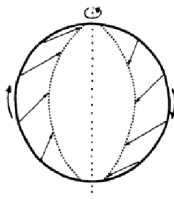
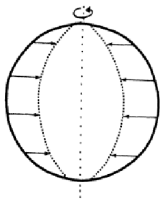
$$\begin{bmatrix} \alpha_1 & \beta_1 & -v_1 \\ \alpha_2 & \beta_2 & -v_2 \\ \dots & \dots & \dots \\ \alpha_n & \beta_n & -v_n \end{bmatrix} \begin{bmatrix} v_x \\ v_y \\ 1 \end{bmatrix} = 0$$

- where $\alpha_1 = \cos\theta$, $\beta_1 = \sin\theta$, $v_1 = v_\theta$ etc.
- Use Singular Value Decomposition (SVD)

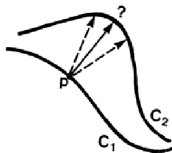
SVD through example

Ambiguity in motion estimation

More general cases



Motion in 3D

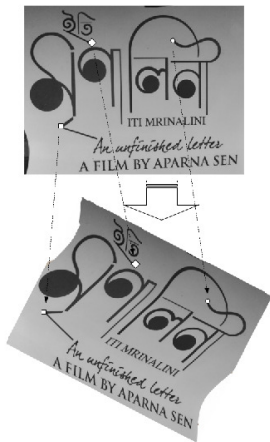


Elastic motion

- Sources of information loss
 - ▶ Projection of 3D object to 2D image
 - ▶ Projection of movement to intensity variation
- $\vec{V} = v_{\perp} \cdot \vec{u}_{\perp} + v_{\top} \cdot \vec{u}_{\top}$
 - ▶ v_{\top} cannot be estimated
- Assumption on additional constraints are needed to estimate v_{\top}

Token based method

Motivated by higher level perception (token recognition)



- Tokens (distinctive points) are identified in the scene
 - ▶ Feature points (SIFT, SURF, etc.) can be used
- Tokens are tracked over time
 - ▶ Motion at tokens are estimated
 - ▶ Motion at other points interpolated

Token based method

(Continued)

- Depends of successful tracking of tokens
- Not an easy problem
 - ▶ Appearance of tokens may change
 - ▶ Two tokens are similar
- Tokens may be confused with each other during motion
- Additional domain-specific constraints need to be imposed
 - ▶ Relative geometry of tokens are maintained
 - ▶ Tokens have moved minimum distance
- Sometimes leads to illusion
 - ▶ A fan or a bicycle wheel appears to rotate in the opposite direction

Quiz 02-05

End of Module 02-05