

# SIFT

Scale-Invariant Feature Transform

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# SIFT

Scale-Invariant Feature Transform  
interest point detector + descriptor

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# Object Recognition from Local Scale-Invariant Features

David G. Lowe

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University of British Columbia  
Vancouver, B.C., V6T 1Z4, Canada  
[lowe@cs.ubc.ca](mailto:lowe@cs.ubc.ca)

## Abstract

*An object recognition system has been developed that uses a new class of local image features. The features are invariant to image scaling, translation, and rotation, and partially invariant to illumination changes and affine or 3D projection.*

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**“ I did submit papers on earlier versions of SIFT to both ICCV and CVPR (around 1997/98) and both were **rejected**. I then added more of a systems flavor and the paper was published at ICCV 1999, but just as a **poster**. ”**

— David Lowe

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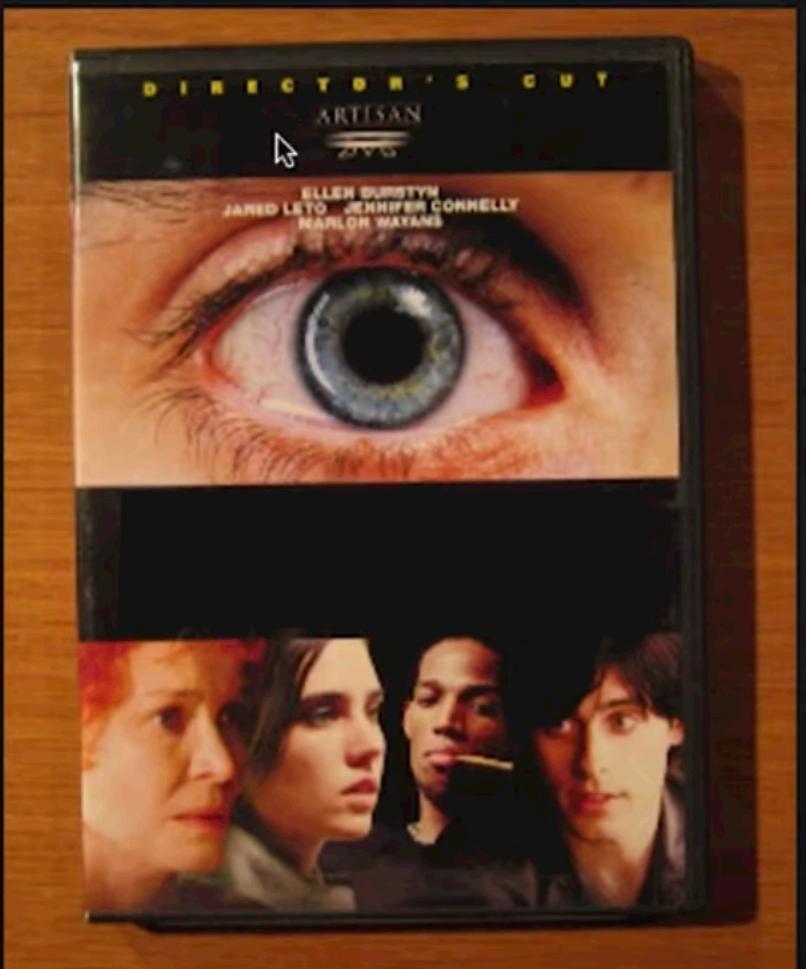
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61 + Thousand  
citations



Template



Rich 2D image

# Raw Images are Hard to Match

---



Different size, orientation, lighting, brightness, etc.

## What is an Interesting Point/Feature?

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- Has rich image content (brightness variation, color variation, etc.) within the local window
- Has well-defined representation (signature) for matching/comparing with other points
- Has a well-defined position in the image
- Should be invariant to image rotation and scaling
- Should be insensitive to lighting changes

What stuff in an image matches with stuff in another?





UNIVERSITY EDUCATION



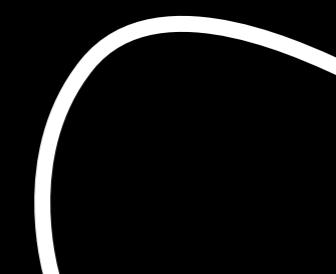


Determine corresponding regions across images



Determine corresponding regions across images  
irrespective of image translation, scale and rotation

Scale Invariant  
Detection



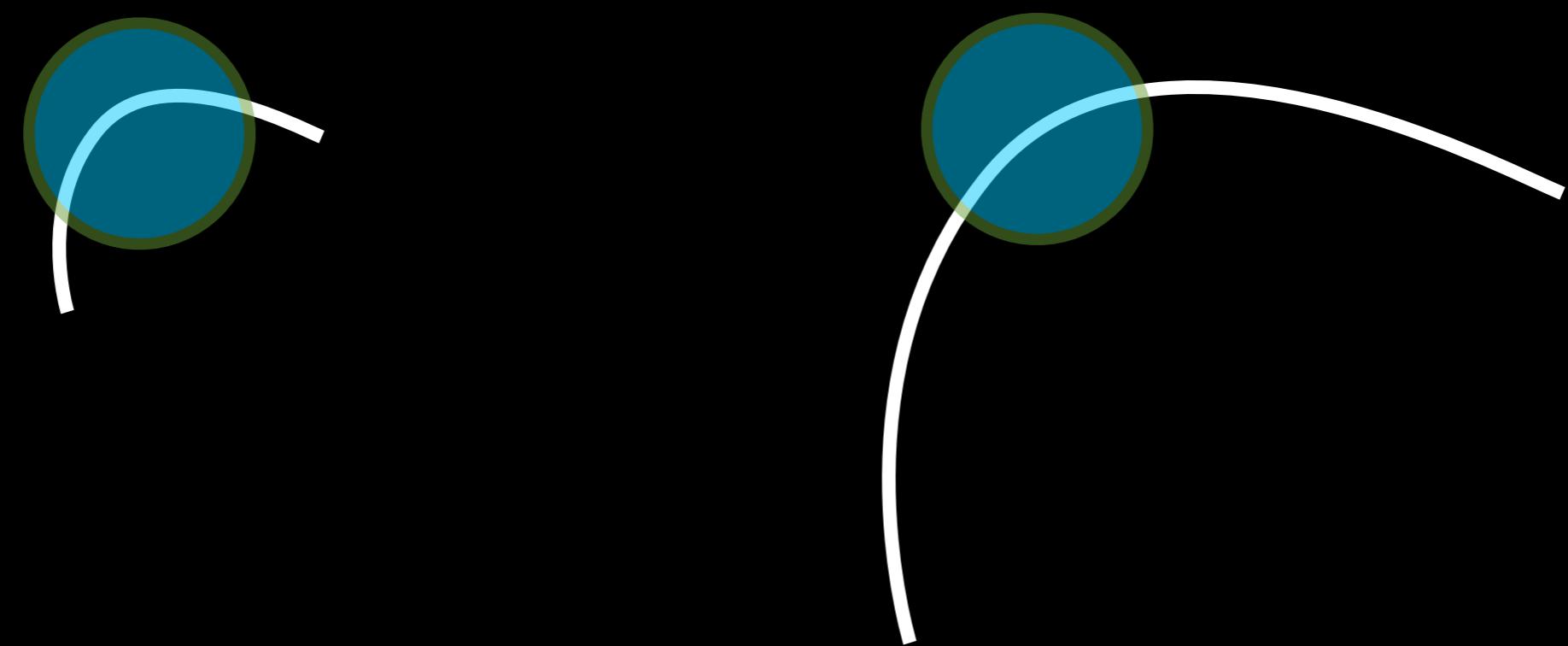
Scale Invariant  
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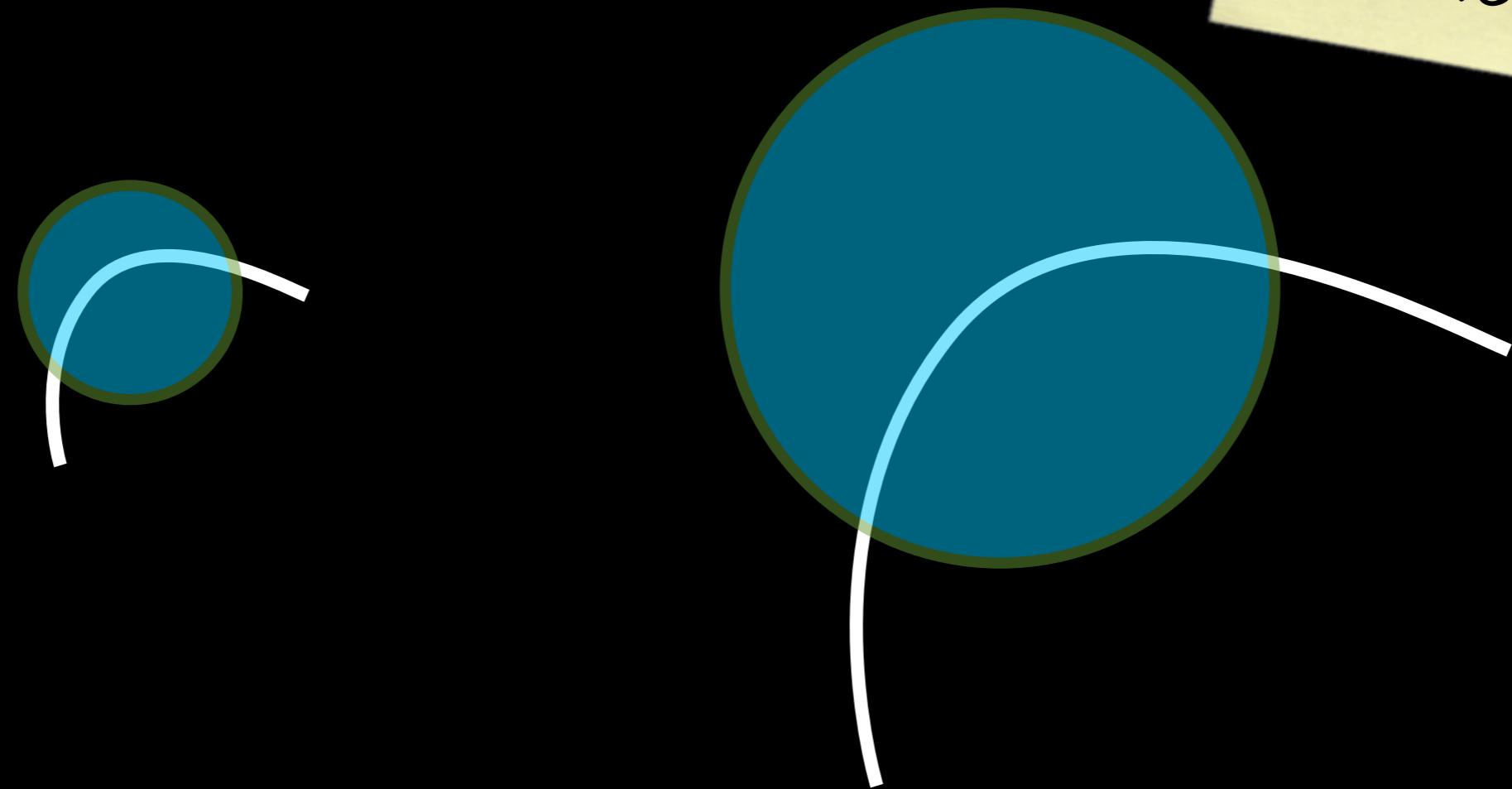
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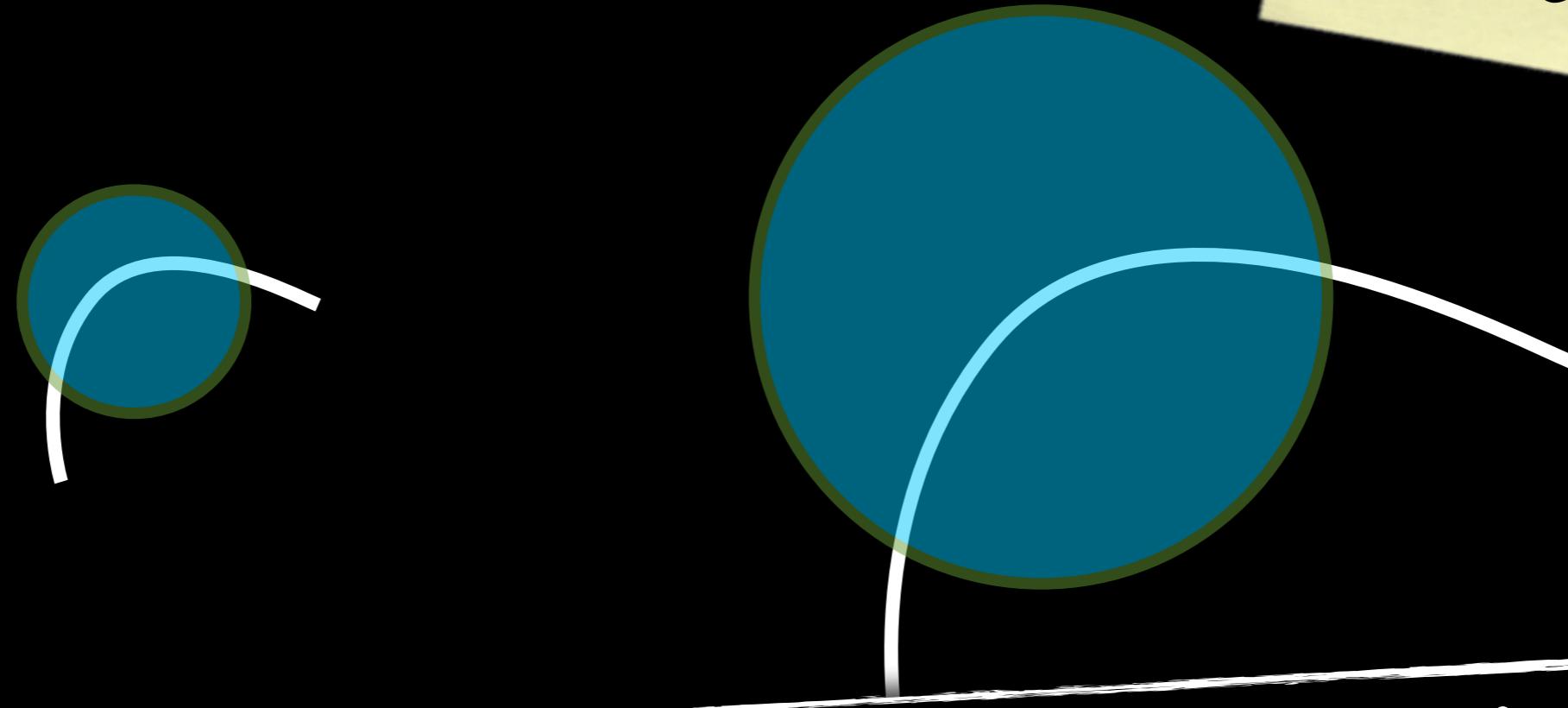
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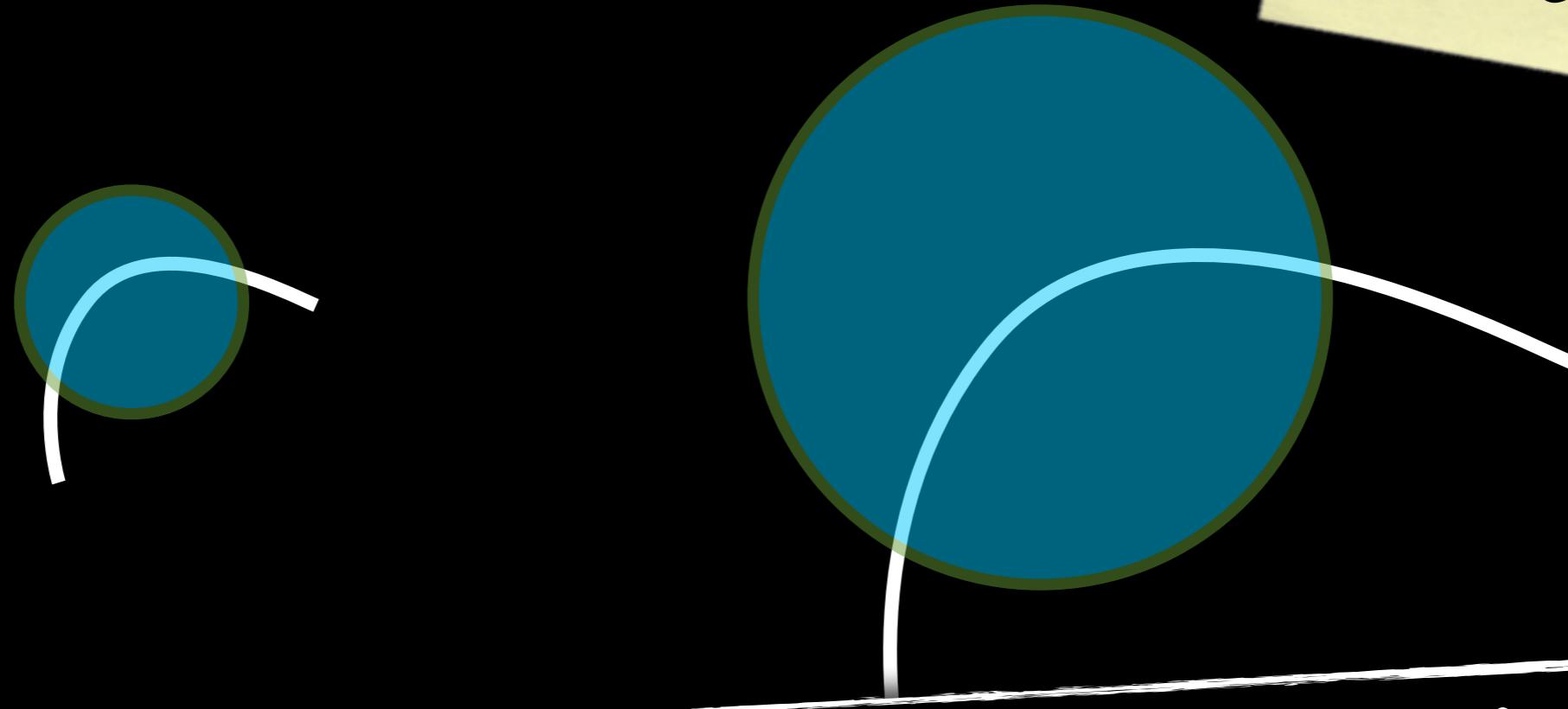


Scale Invariant  
Detection



How do we choose corresponding correct region sizes  
**independently** in each image?

## Scale Invariant Detection



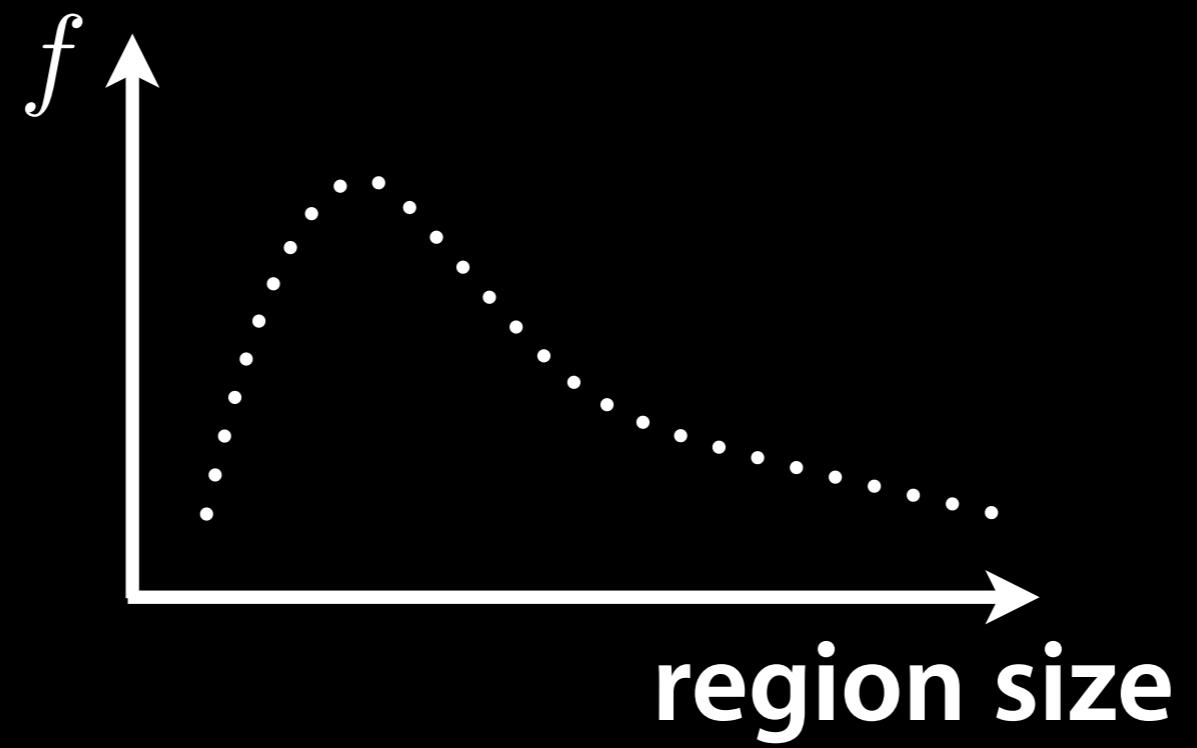
How do we choose corresponding correct region sizes  
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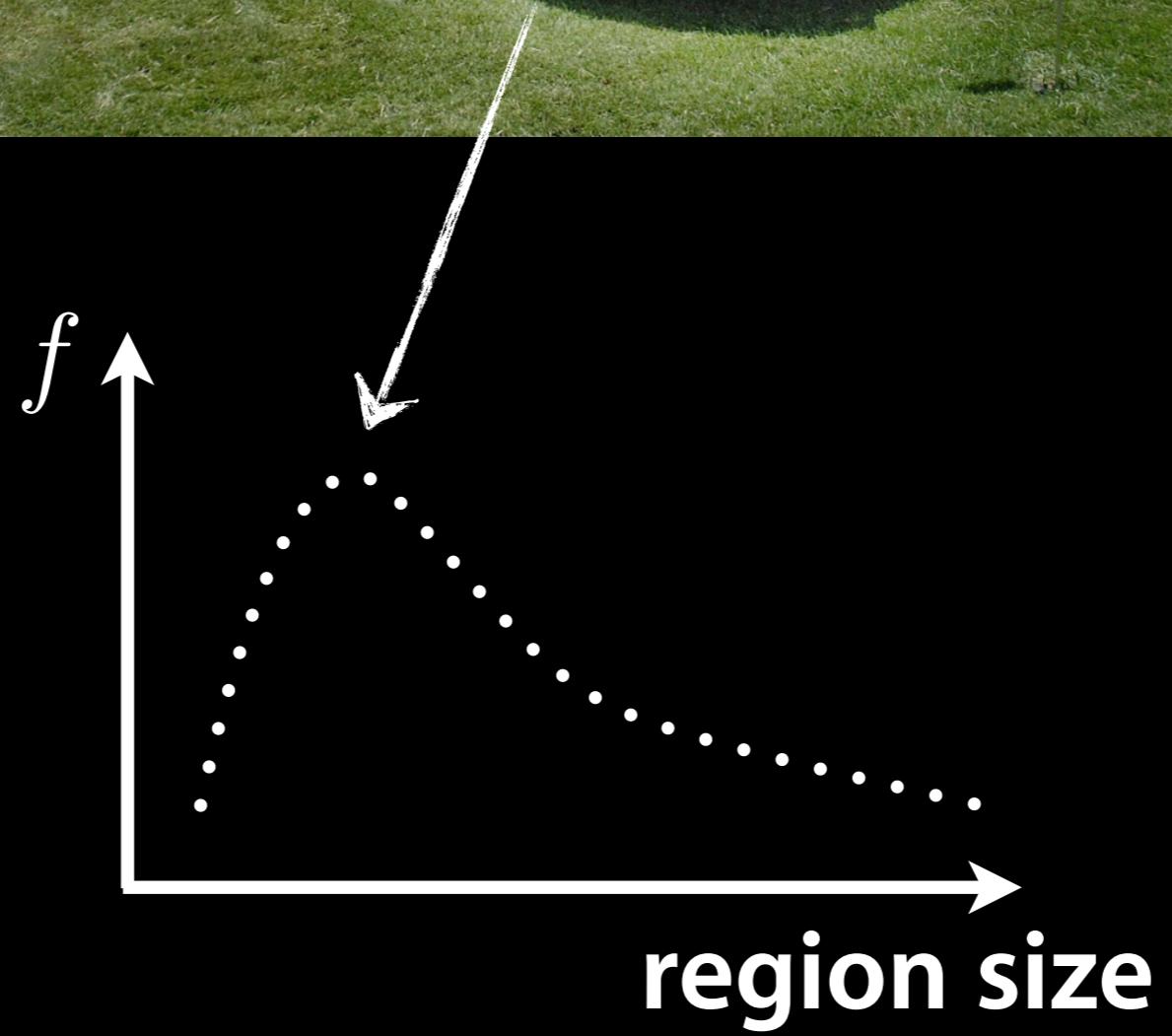
Design a **scale invariant function** on the region

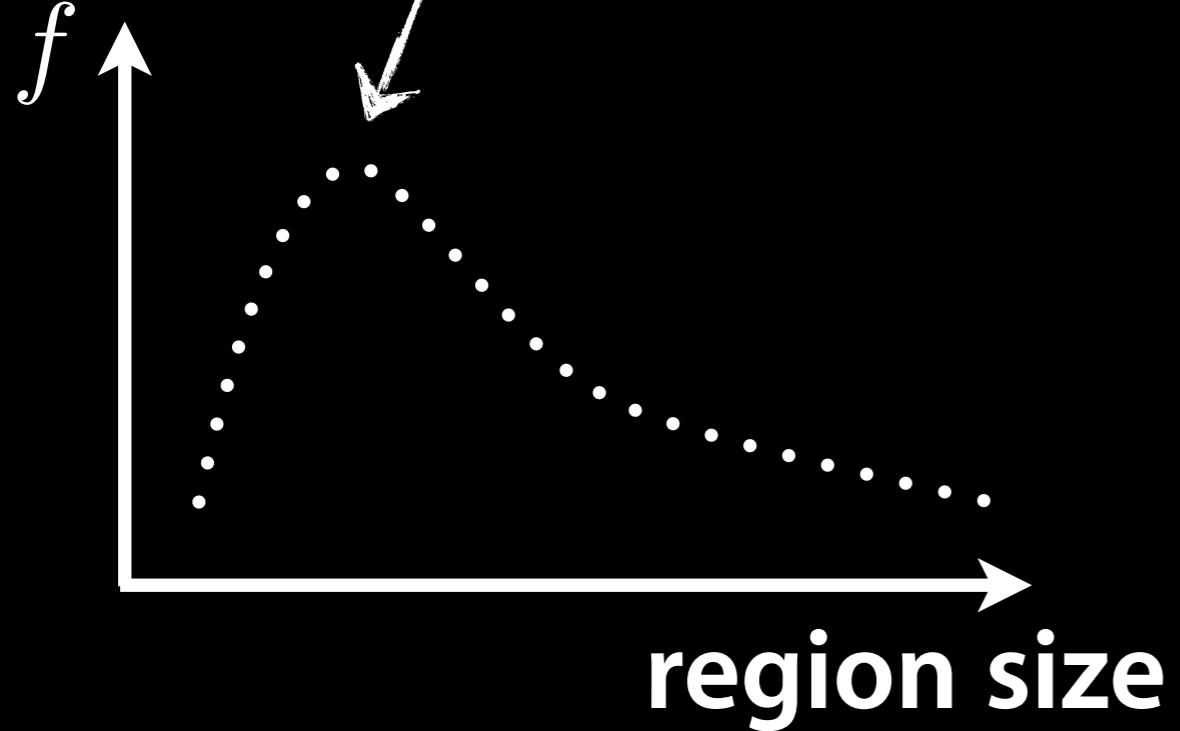


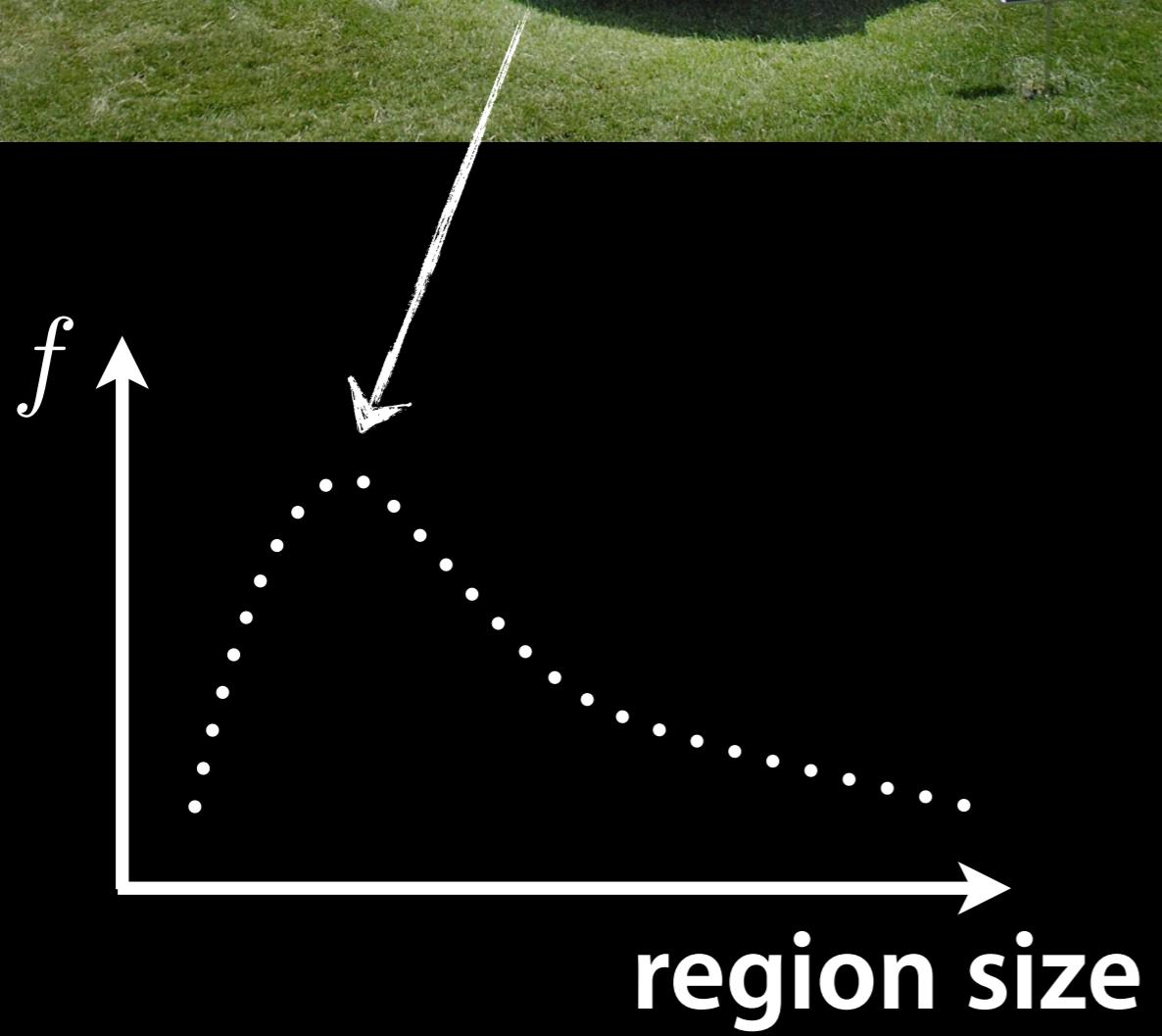


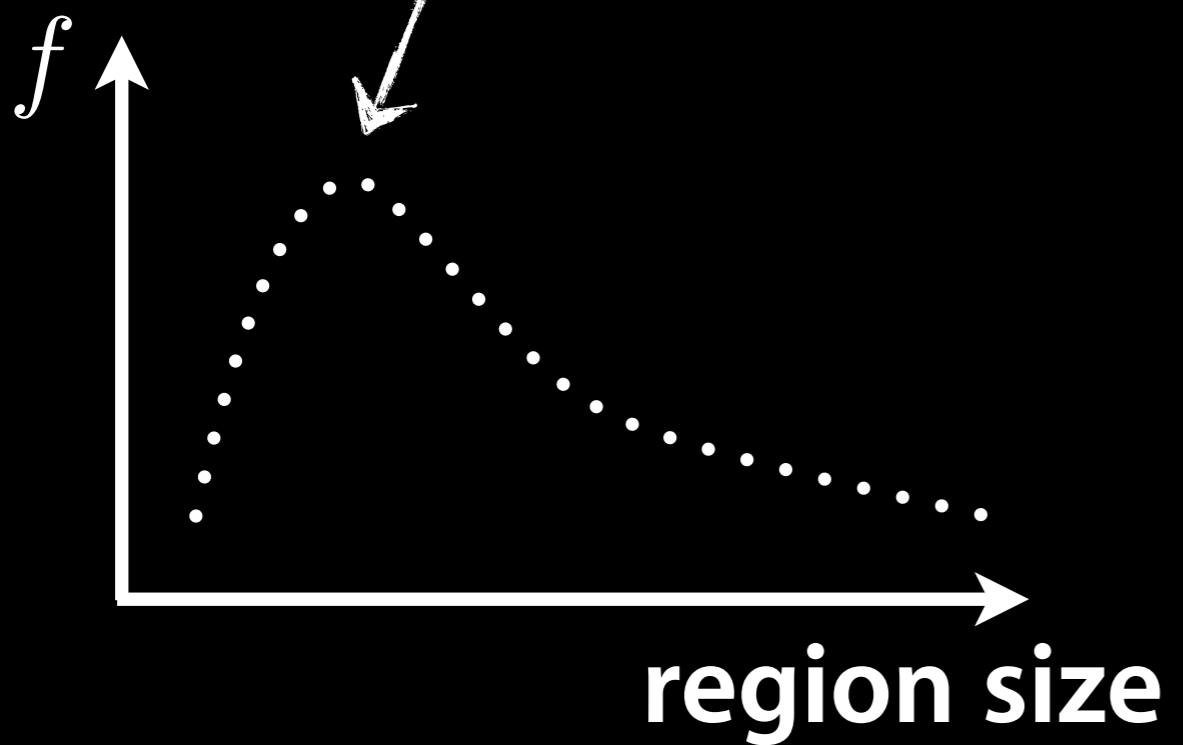


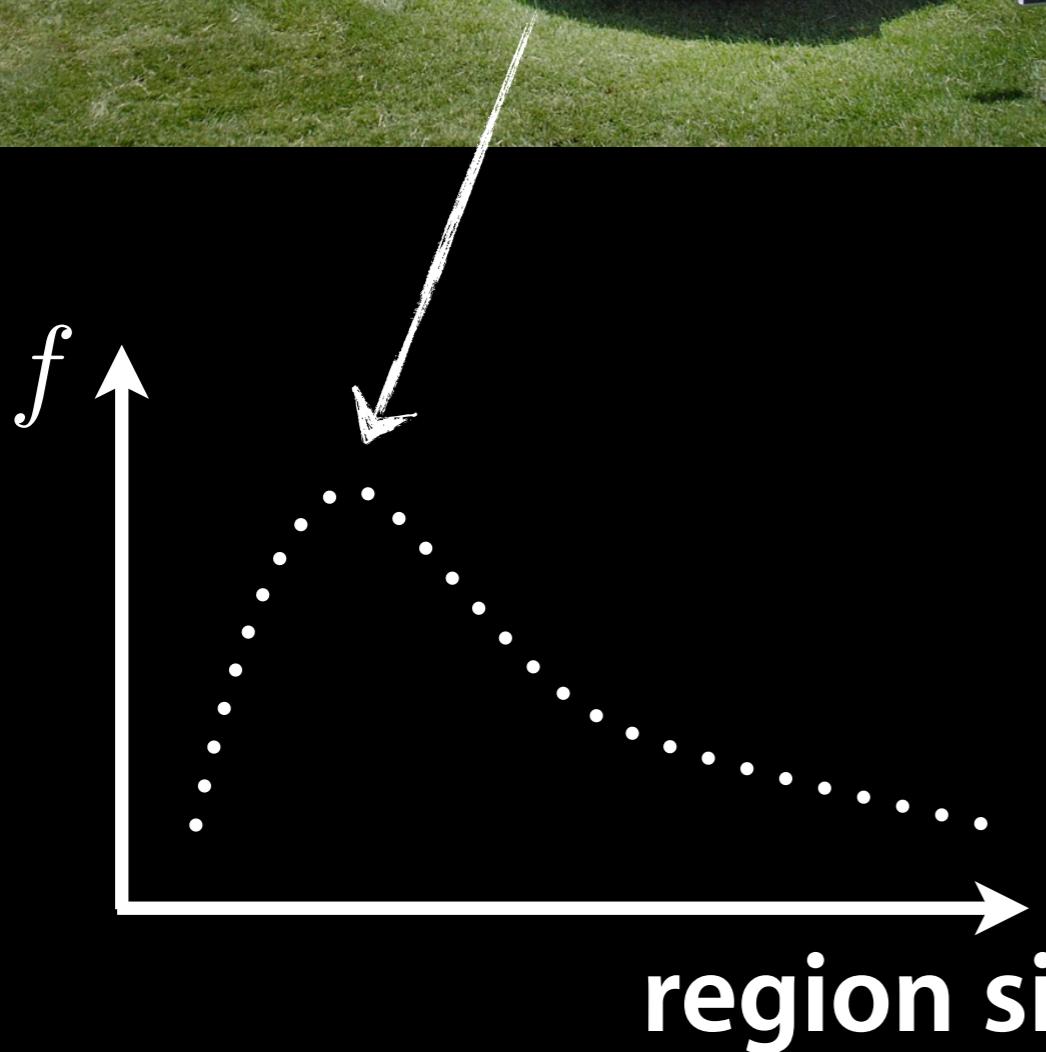


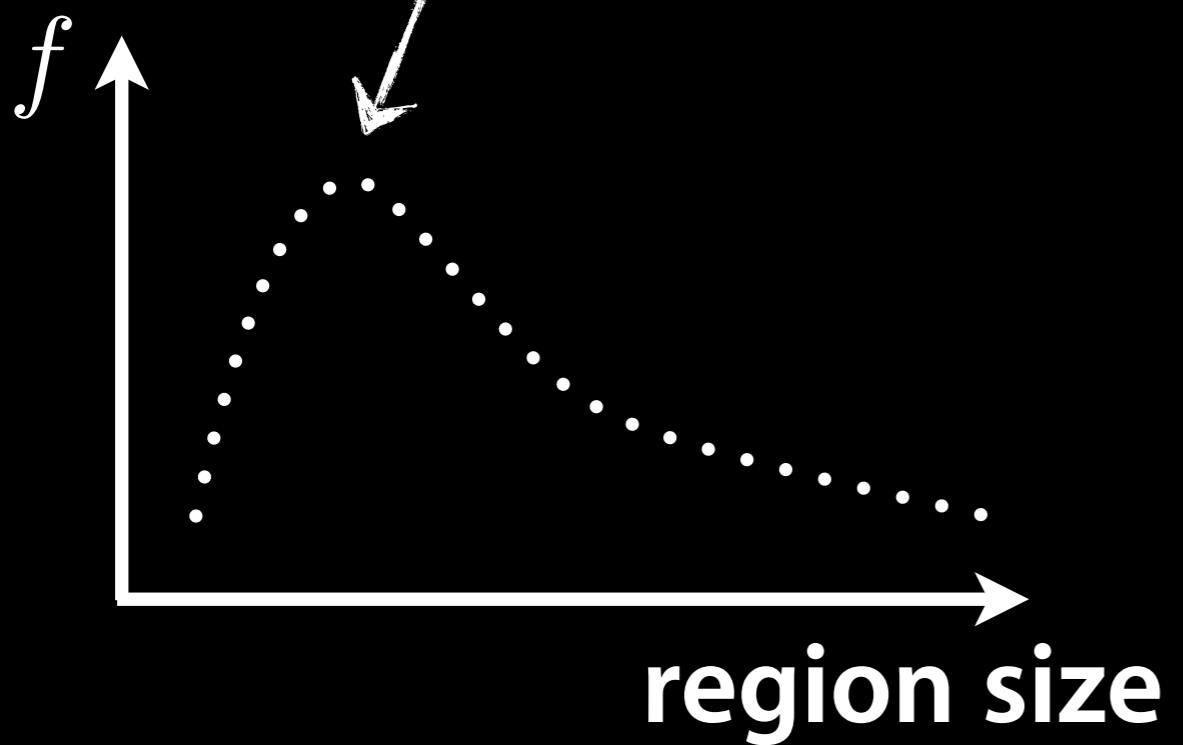


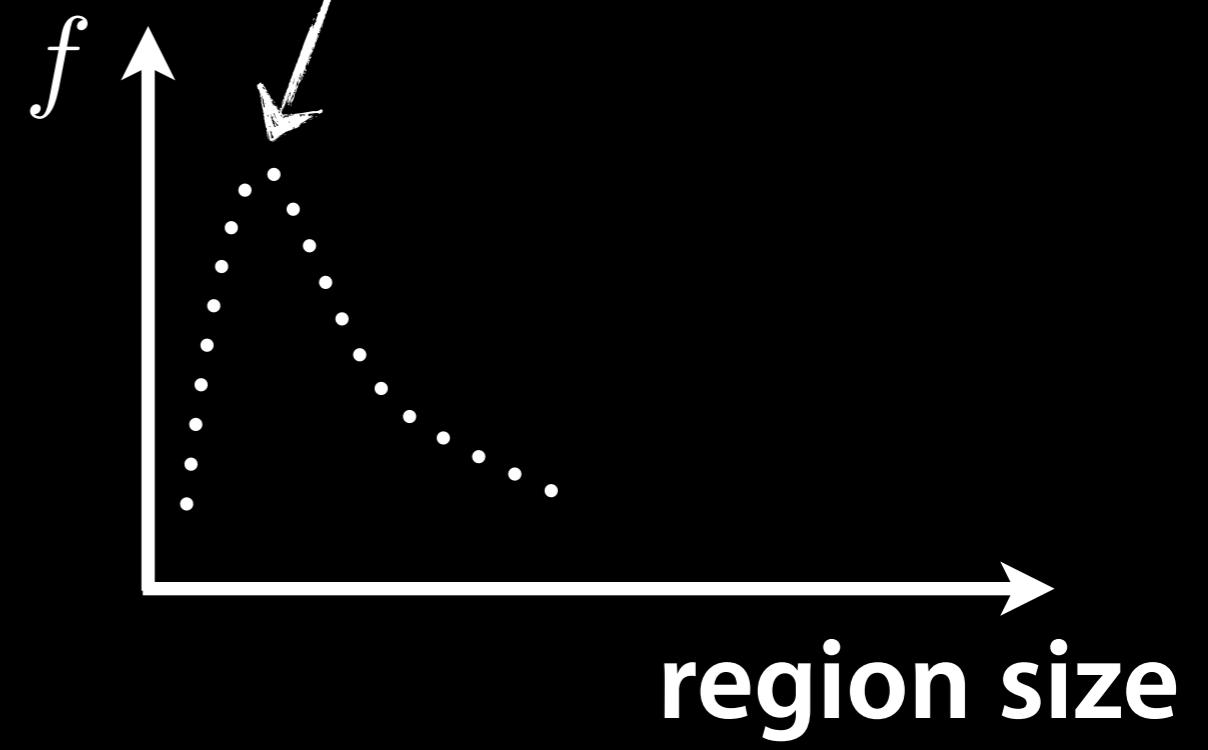
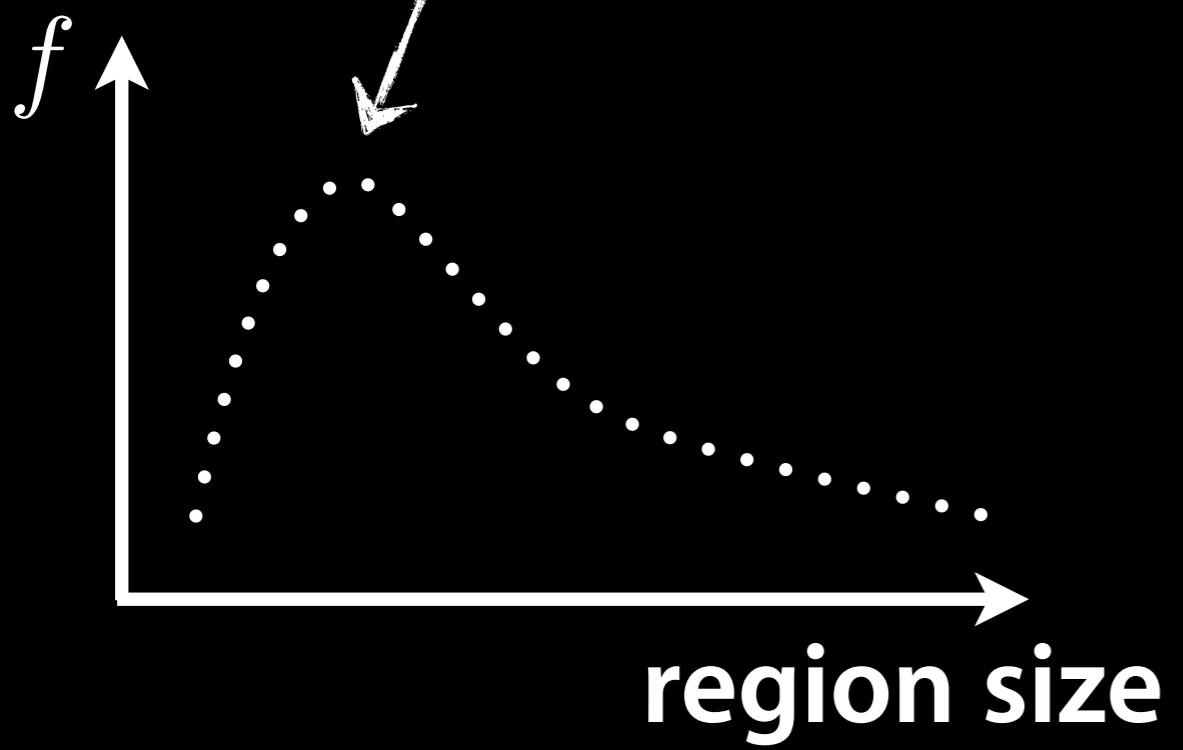












Scale Invariant  
Description



image 1



image 2

Scale Invariant  
Description



image 1



image 2

Resample image about keypoint to a canonical size

Scale Invariant  
Description



image 1



image 2

Resample image about keypoint to a canonical size

Scale Invariant  
Description



image 1



image 2

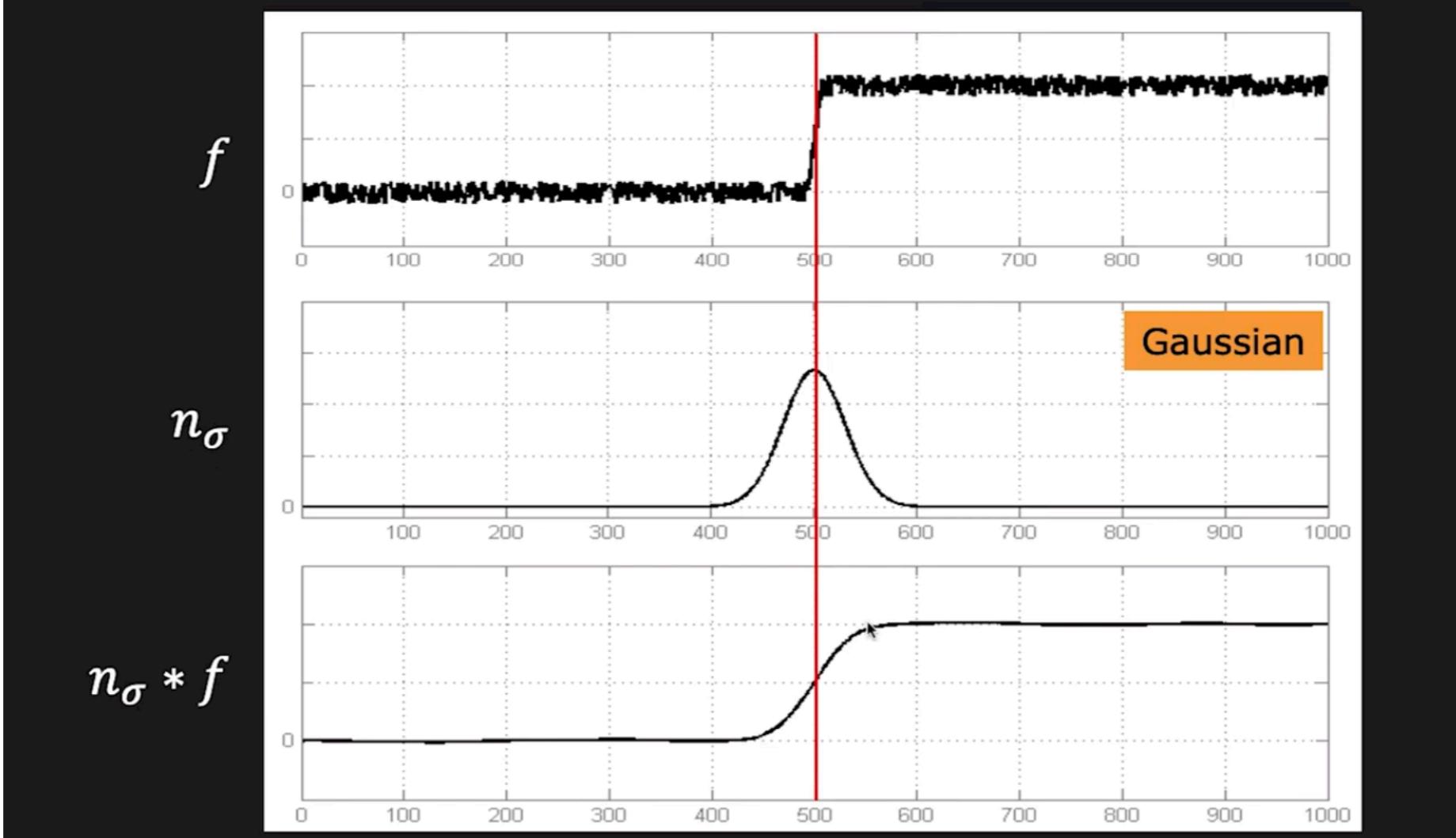
Resample image about keypoint to a canonical size

# Which feature detector?

# Which feature detector?

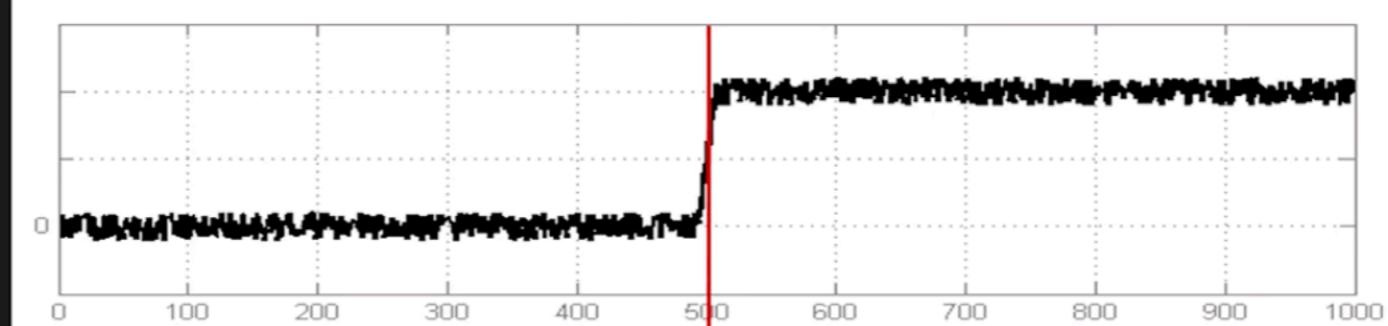
$$f = \text{Kernel} * \text{Image}$$

# Review: Gaussian Filter

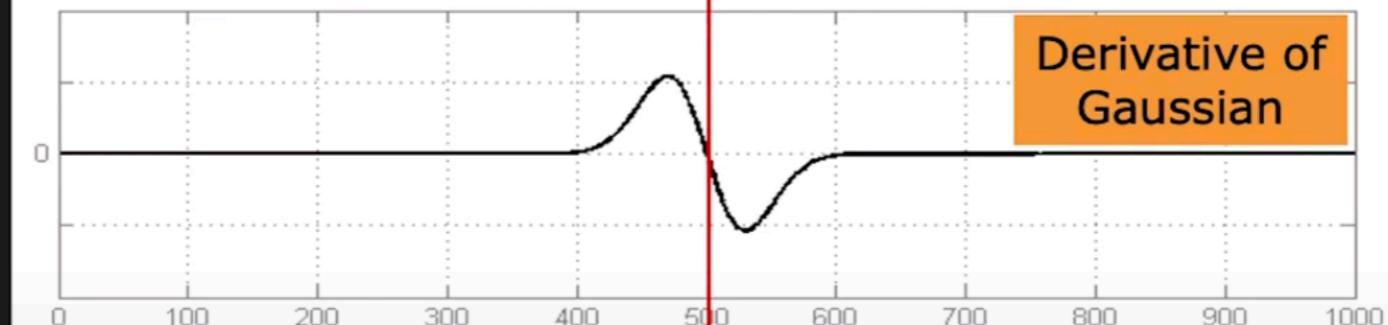


# Review: Derivative of Gaussian

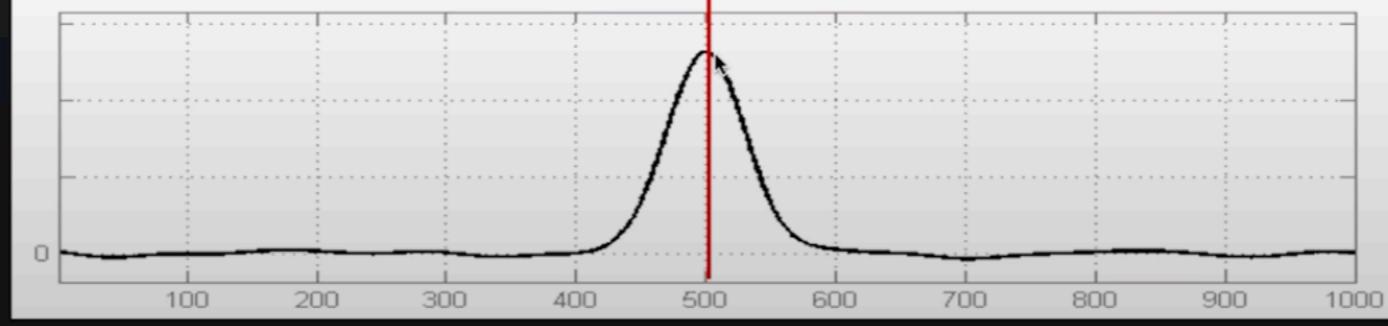
$f$



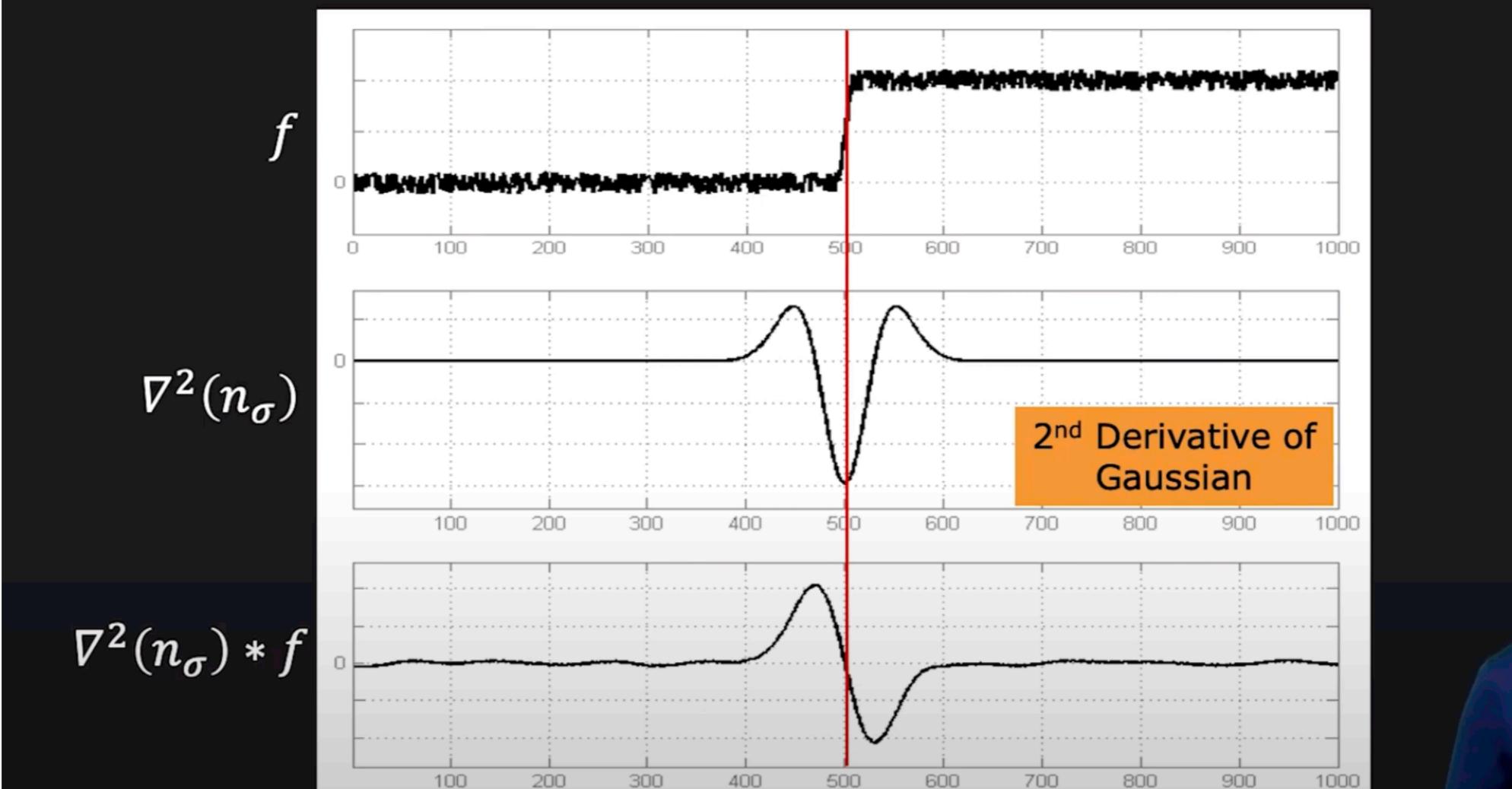
$\nabla(n_\sigma)$



$\nabla(n_\sigma) * f$

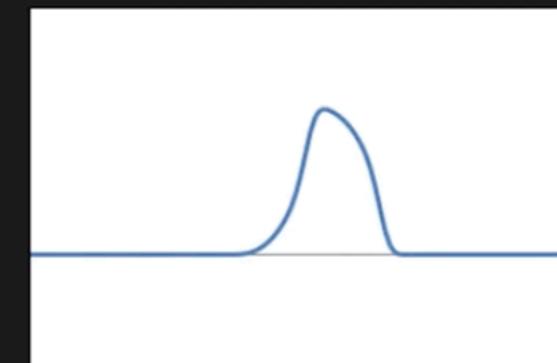
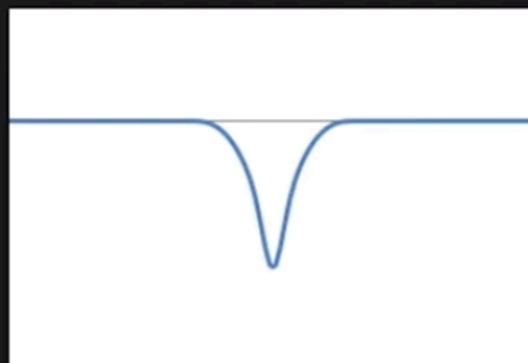
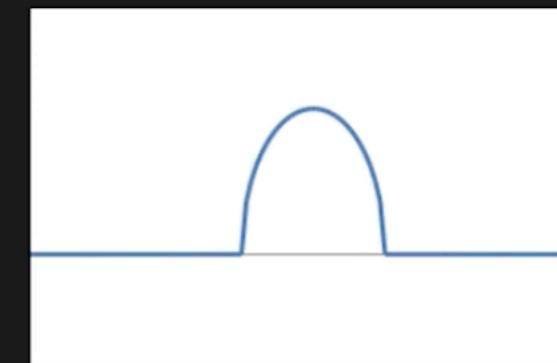
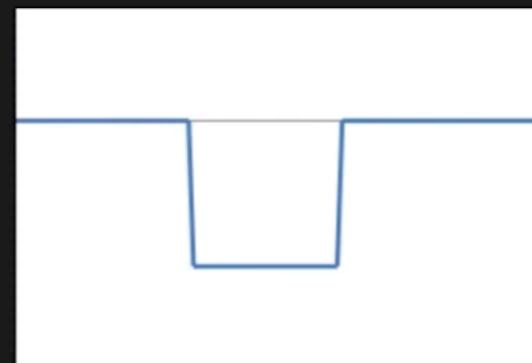


# Review: 2<sup>nd</sup> Derivative of Gaussian



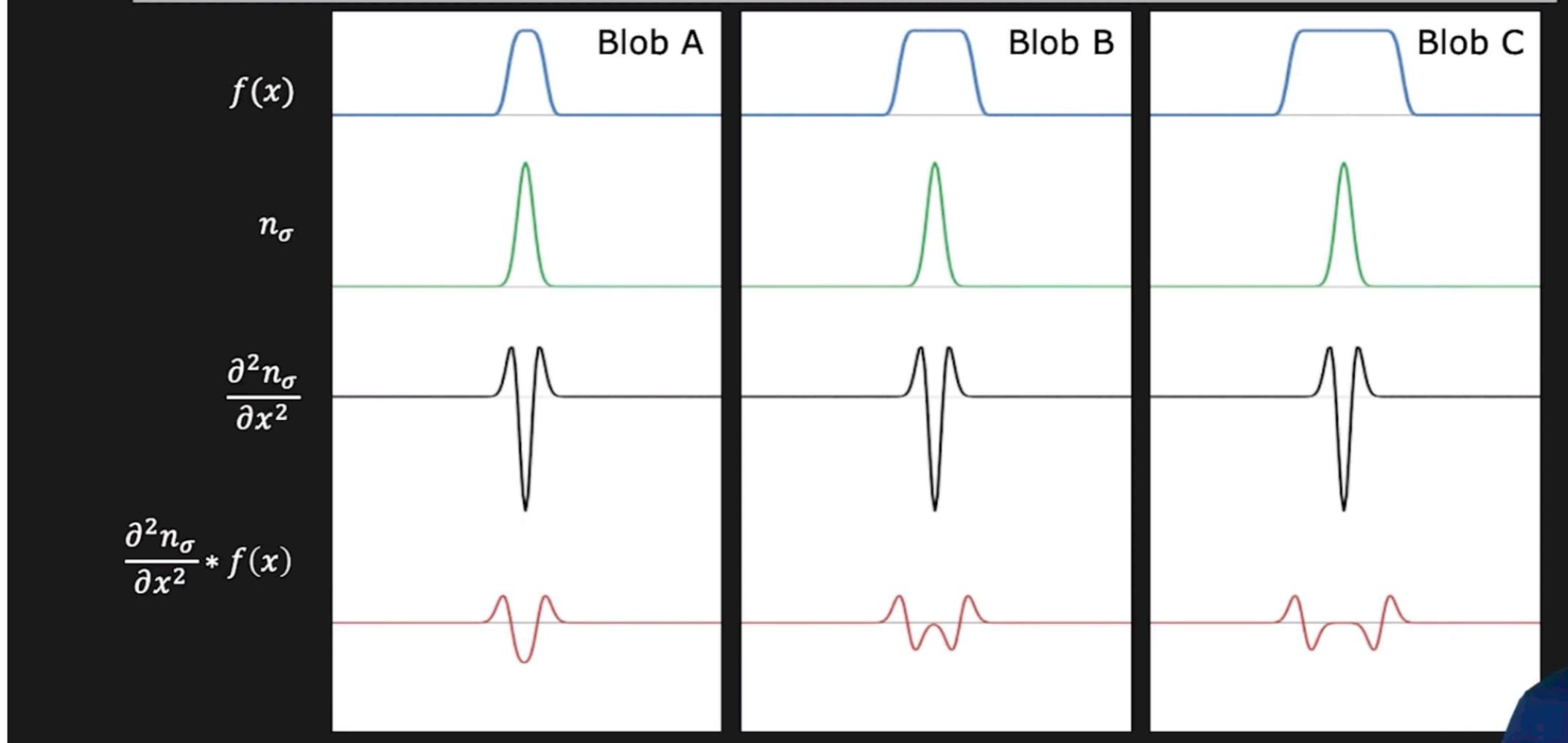
# 1D Blobs

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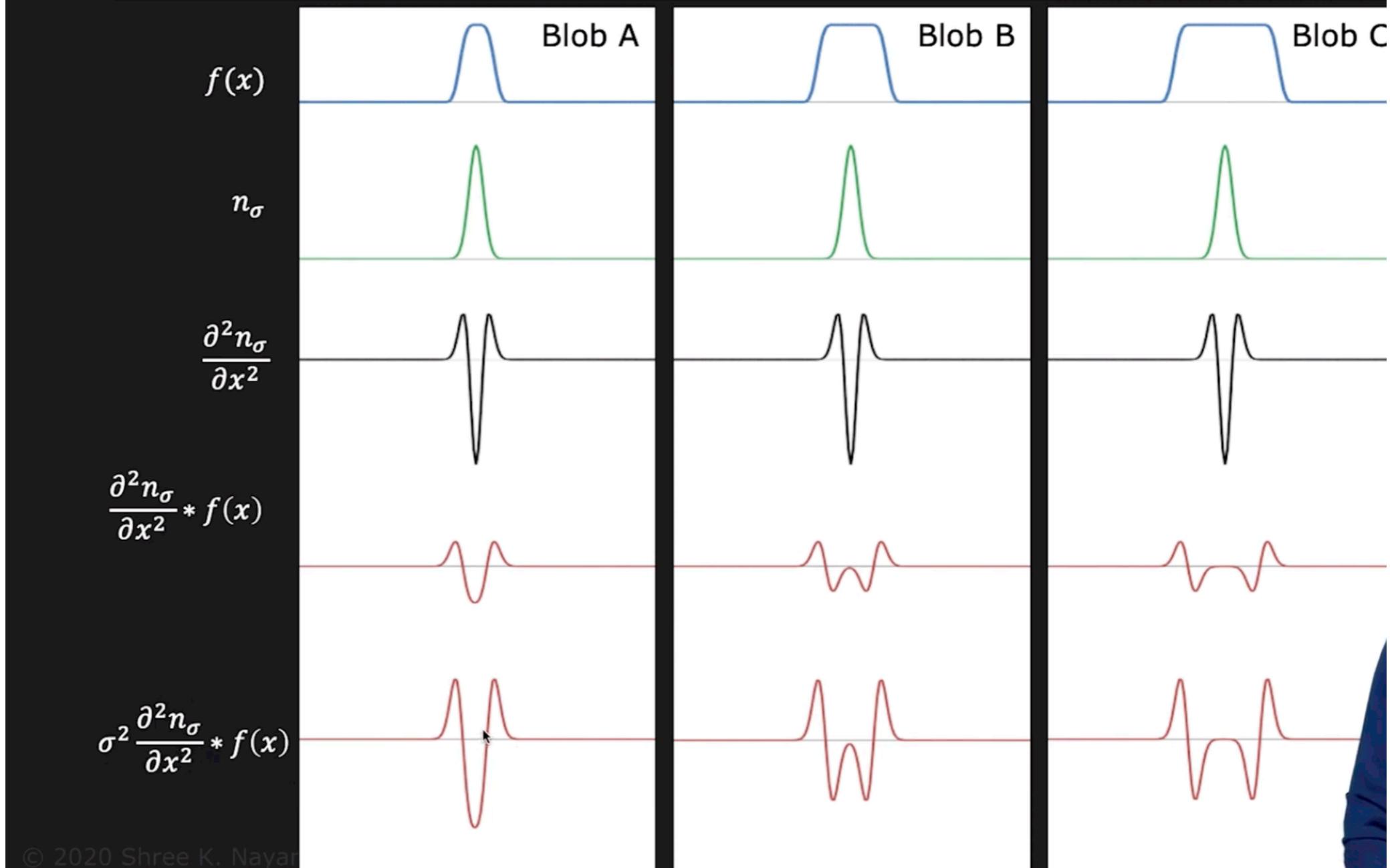


Examples of 1D Blob-like structures

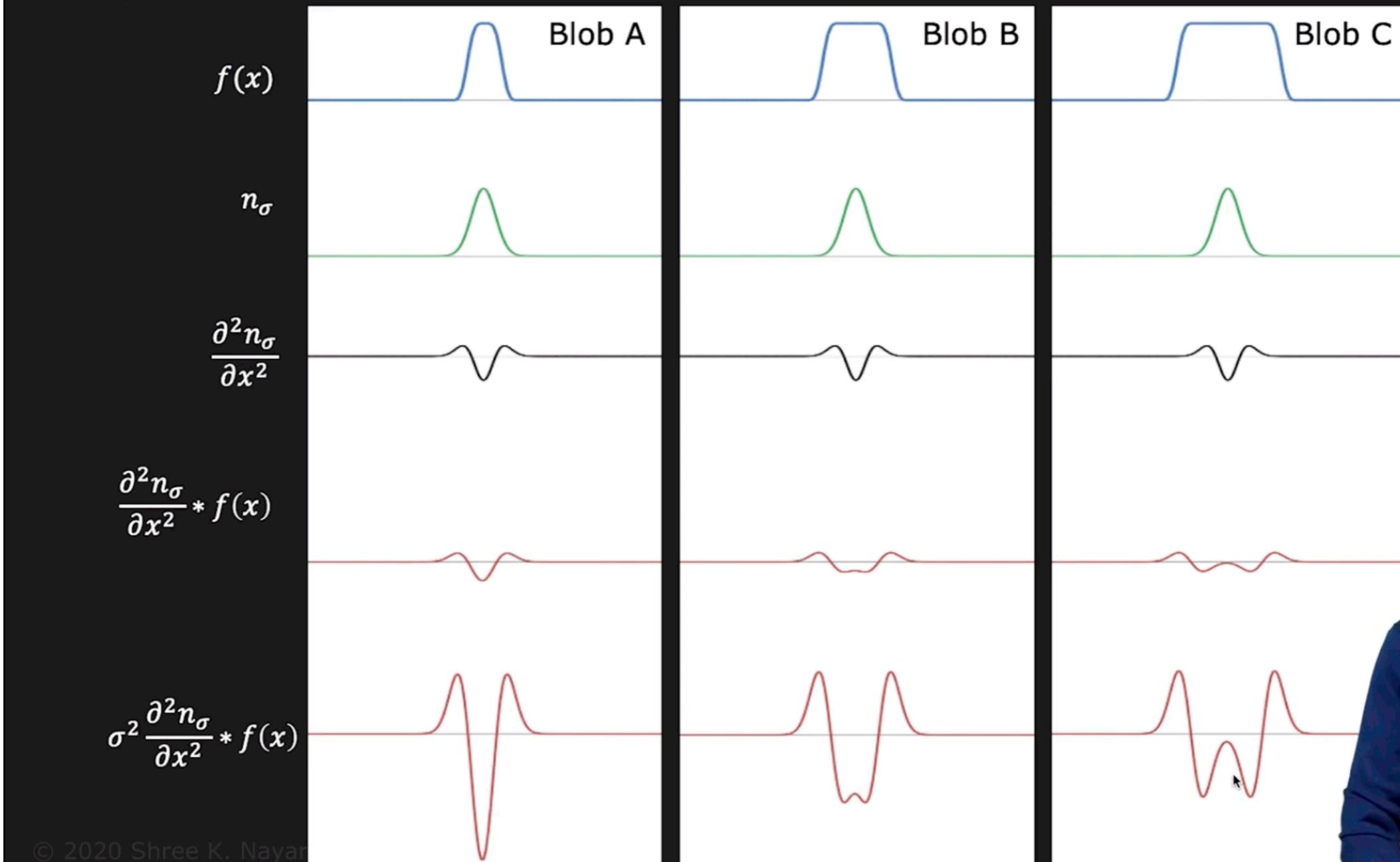
# 1D Blob and 2<sup>nd</sup> Derivative of Gaussian



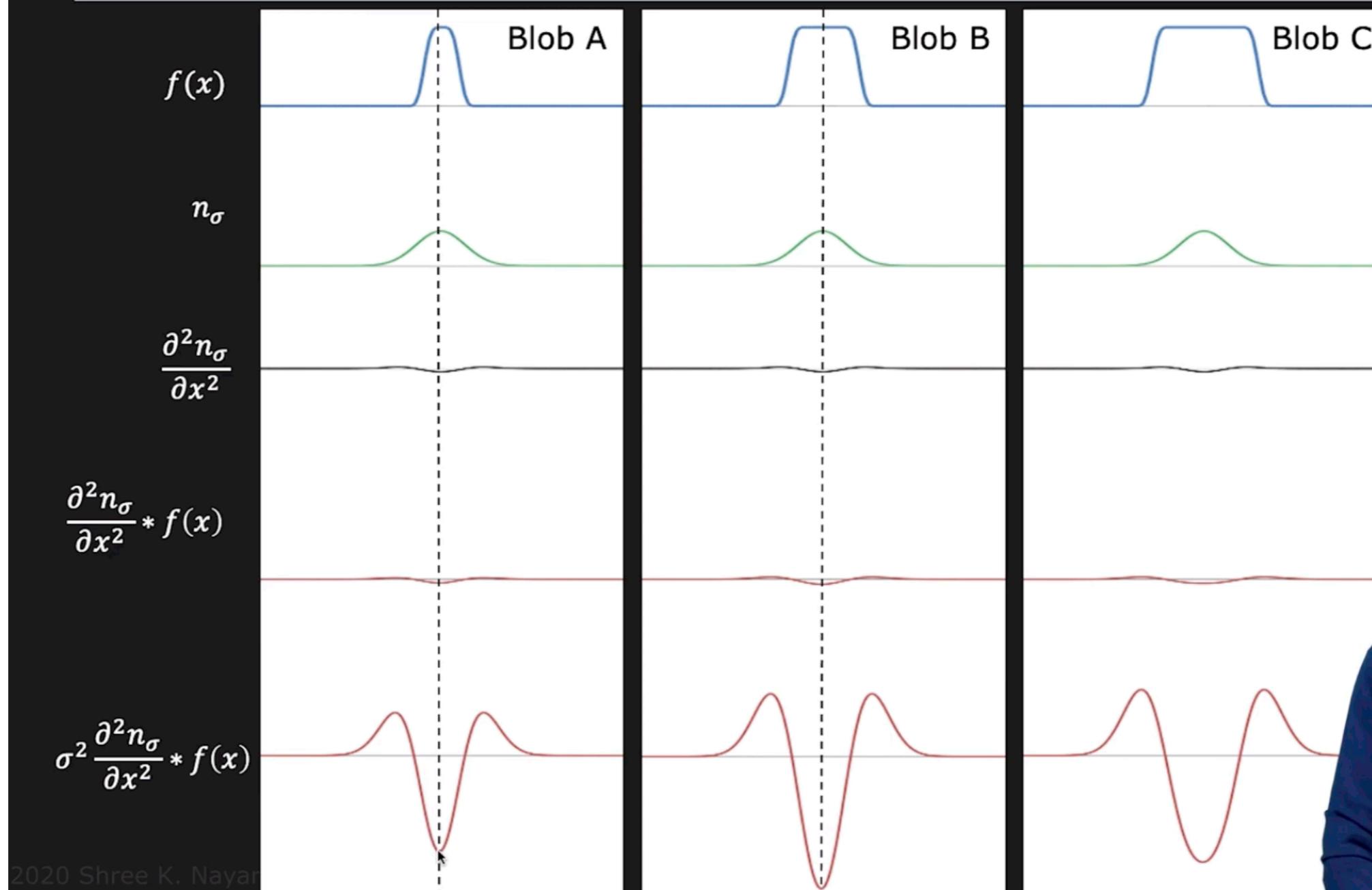
# 1D Blob and 2<sup>nd</sup> Derivative of Gaussian



# 1D Blob and 2<sup>nd</sup> Derivative of Gaussian



# 1D Blob and 2<sup>nd</sup> Derivative of Gaussian



# 1D Blob Detection Summary

Given: 1D signal  $f(x)$

Compute:  $\sigma^2 \frac{\partial^2 n_\sigma}{\partial x^2} * f(x)$  at many scales  $(\sigma_0, \sigma_1, \sigma_2, \dots, \sigma_k)$ .

Find: 
$$(x^*, \sigma^*) = \arg \max_{(x, \sigma)} \left| \sigma^2 \frac{\partial^2 n_\sigma}{\partial x^2} * f(x) \right|$$

$x^*$ : Blob Position

$\sigma^*$ : Characteristic Scale (Blob Size)

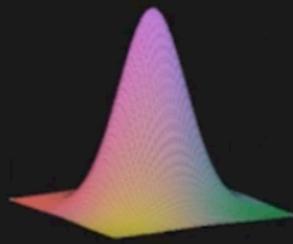
# 2D Blob Detector

Normalized Laplacian of Gaussian (NLoG) is used as the 2D equivalent for Blob Detection.

Laplacian

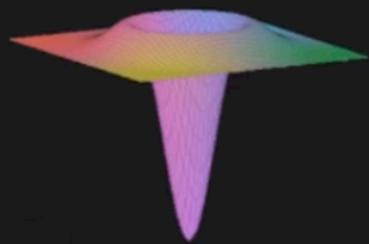
$$\nabla^2 = \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2}$$

Gaussian



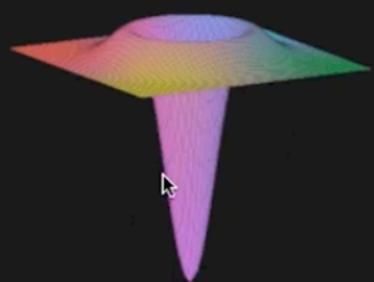
$$n_\sigma$$

LoG



$$\nabla^2 n_\sigma$$

NLoG



$$\sigma^2 \nabla^2 n_\sigma$$

Location of Blobs given by Local Extrema after applying Normalized Laplacian of Gaussian at many scales.

## 2D Blob Detection Summary

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Given an image  $I(x, y)$

Convolve the image using NLoG at many scales  $\sigma$

Find:

$$(x^*, y^*, \sigma^*) = \arg \max_{(x, y, \sigma)} |\sigma^2 \nabla^2 n_\sigma * I(x, y)|$$

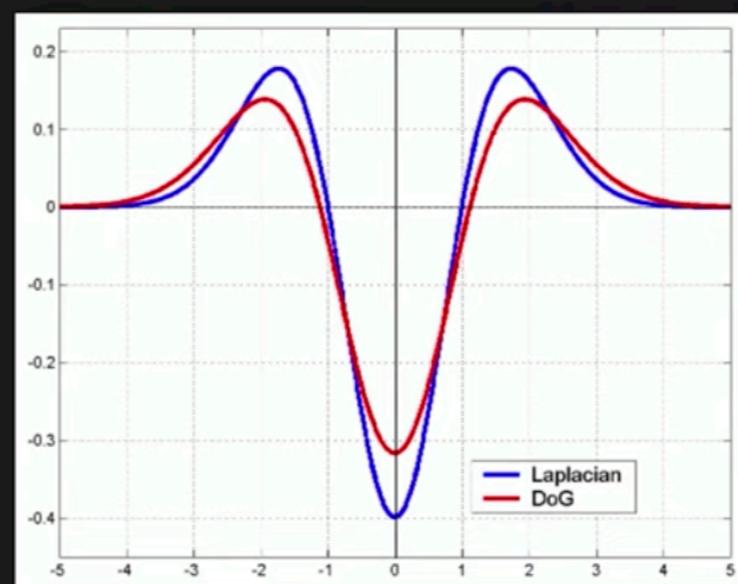
$(x^*, y^*)$ : Position of the blob

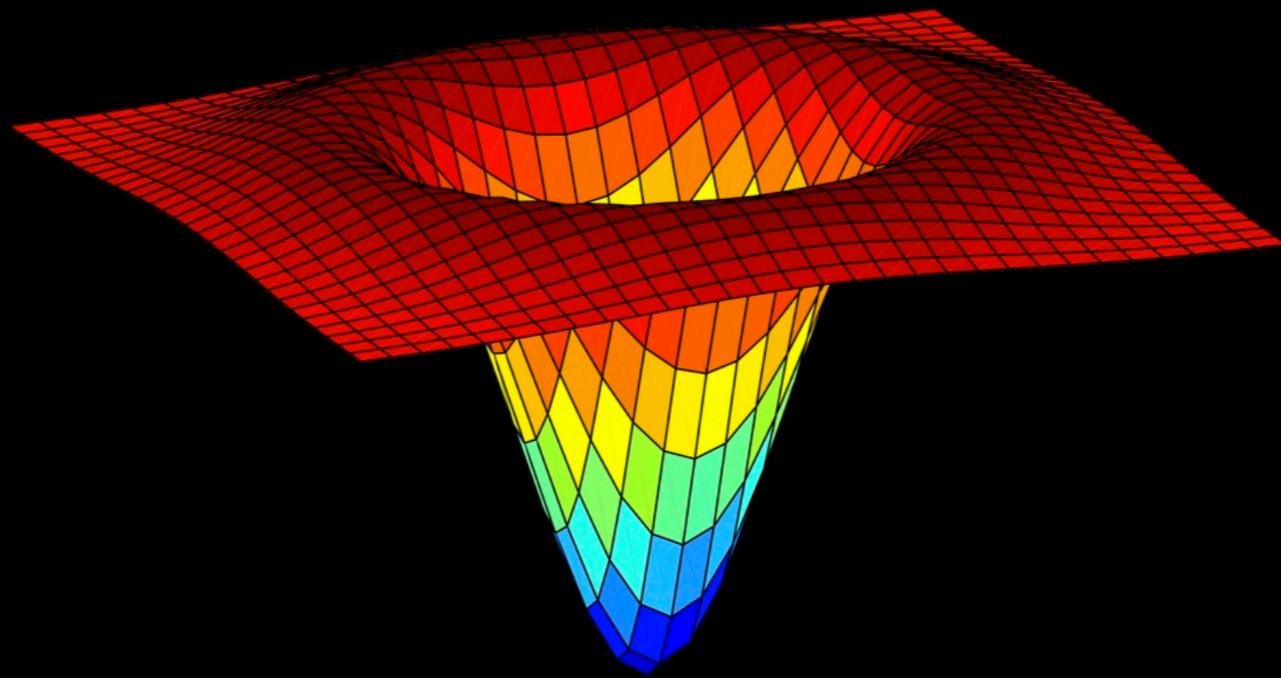
$\sigma^*$ : Size of the blob

## Fast NLoG Approximation: DoG

Difference of Gaussian (DoG) =  $(n_{s\sigma} - n_\sigma) \approx (s - 1)\sigma^2 \nabla^2 n_\sigma$

NLoG





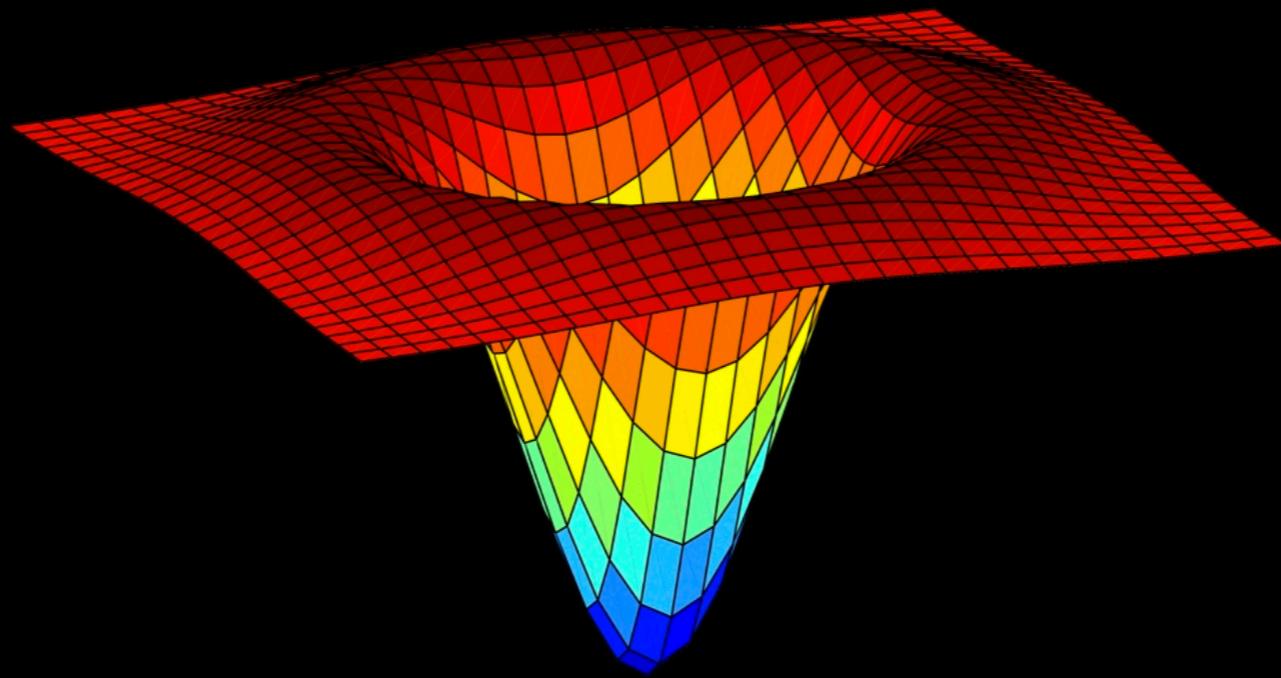
**Laplacian of Gaussian (LoG)**



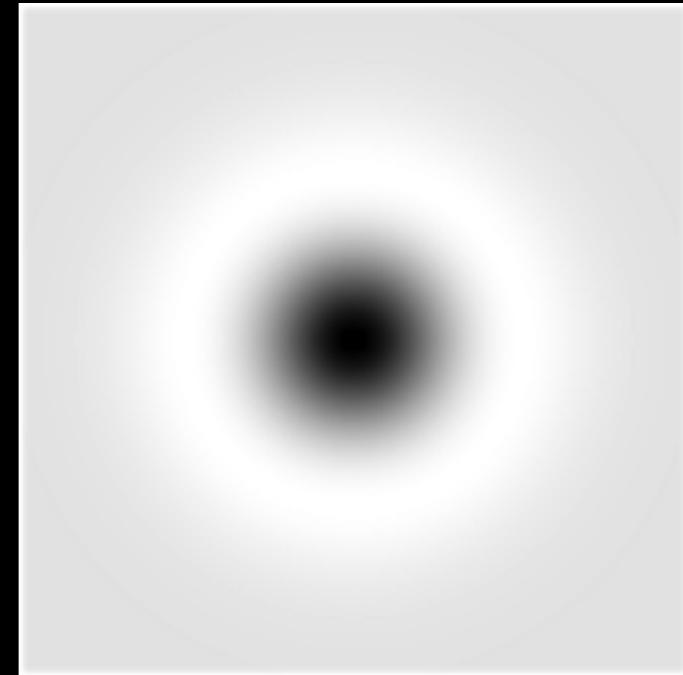
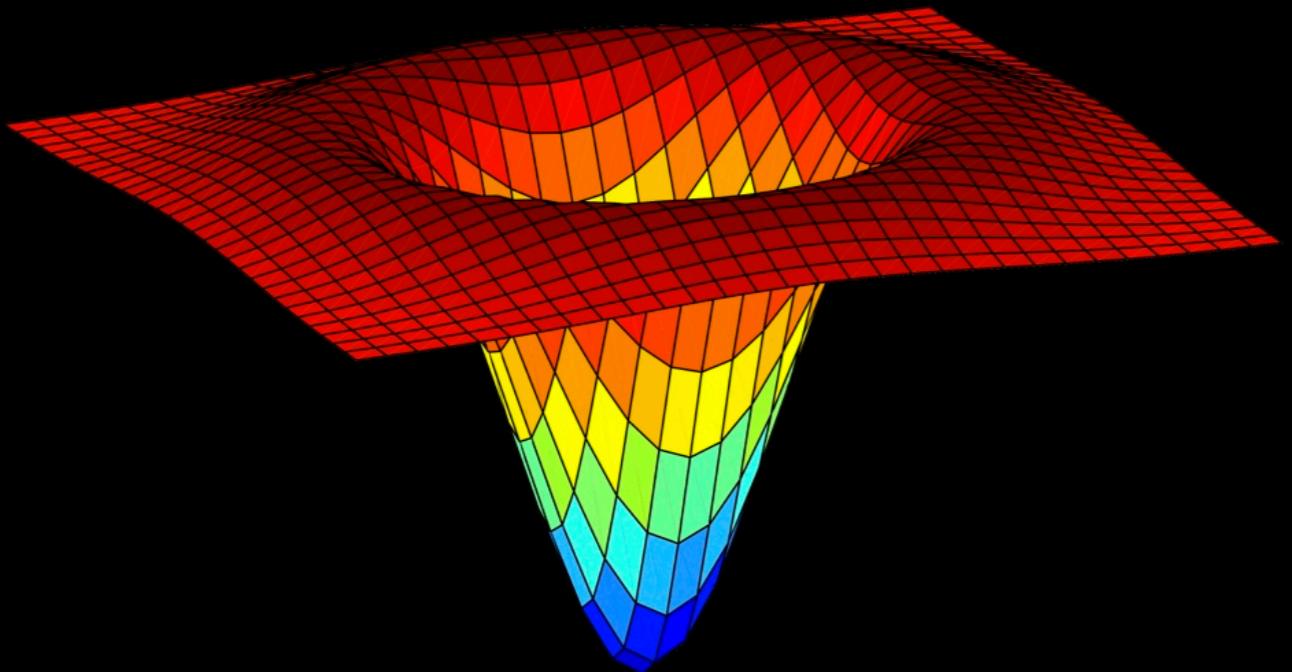
# Mexican hat operator



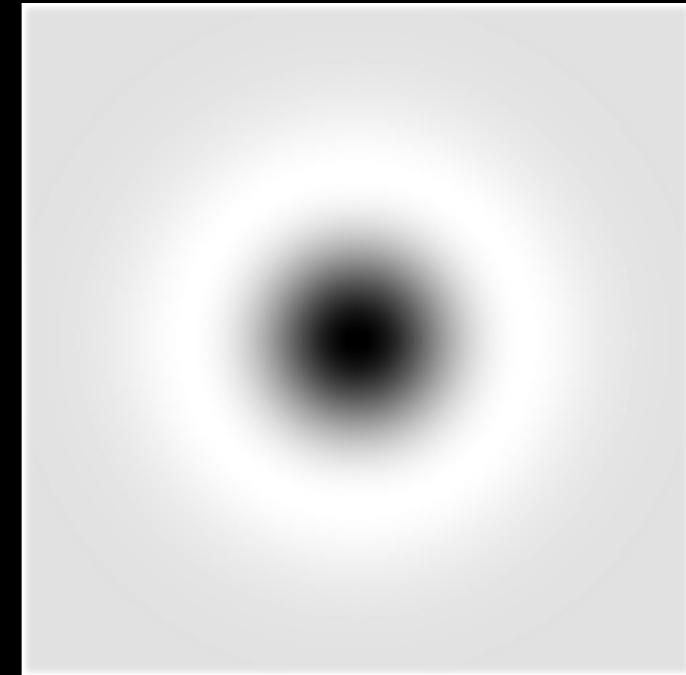
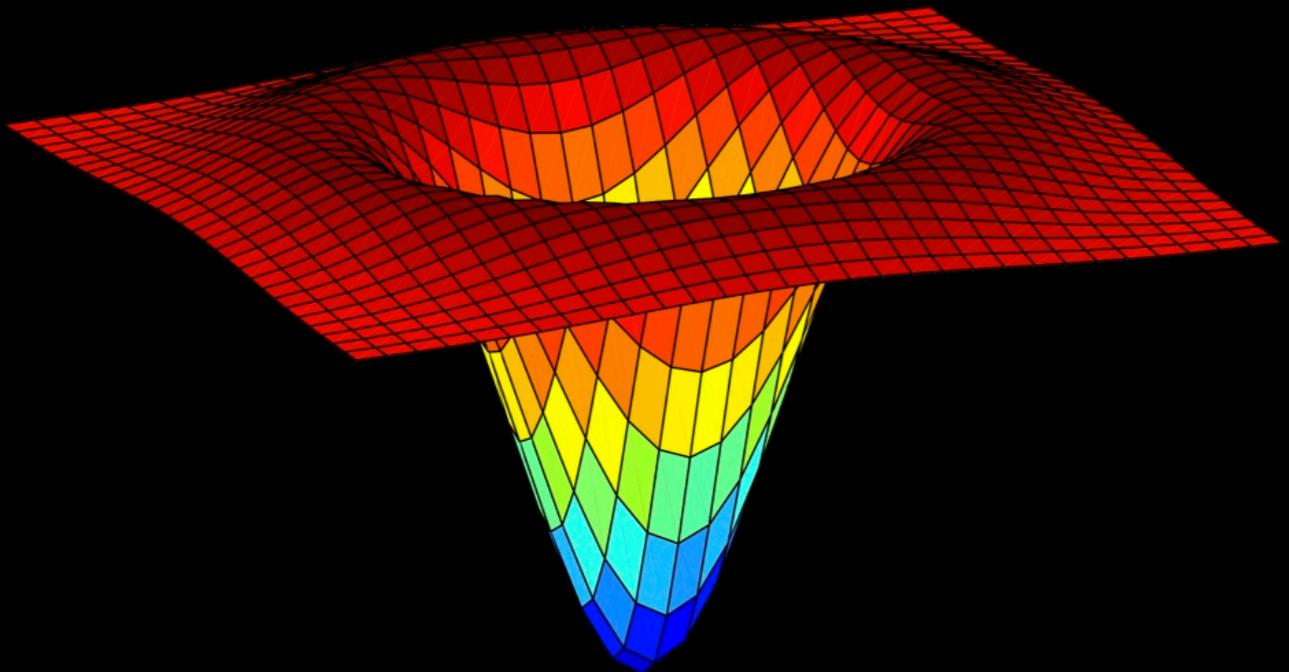
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**Laplacian of Gaussian (LoG)**

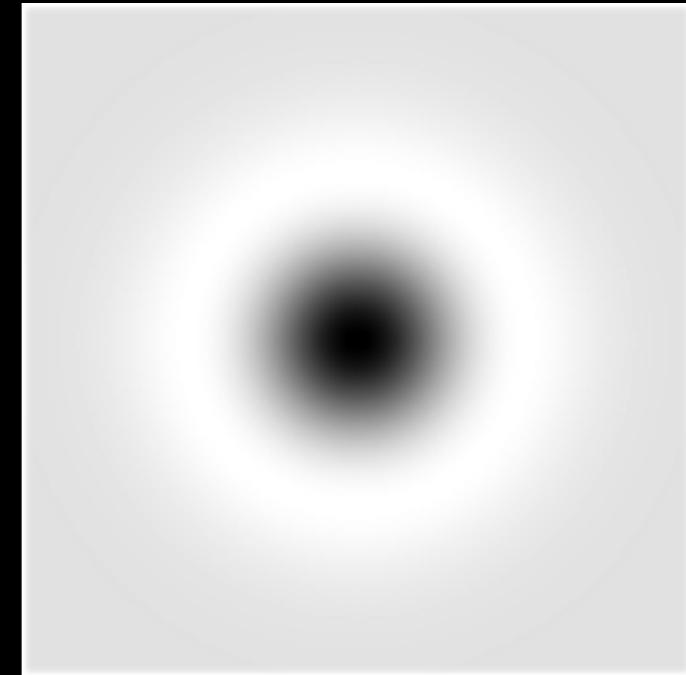
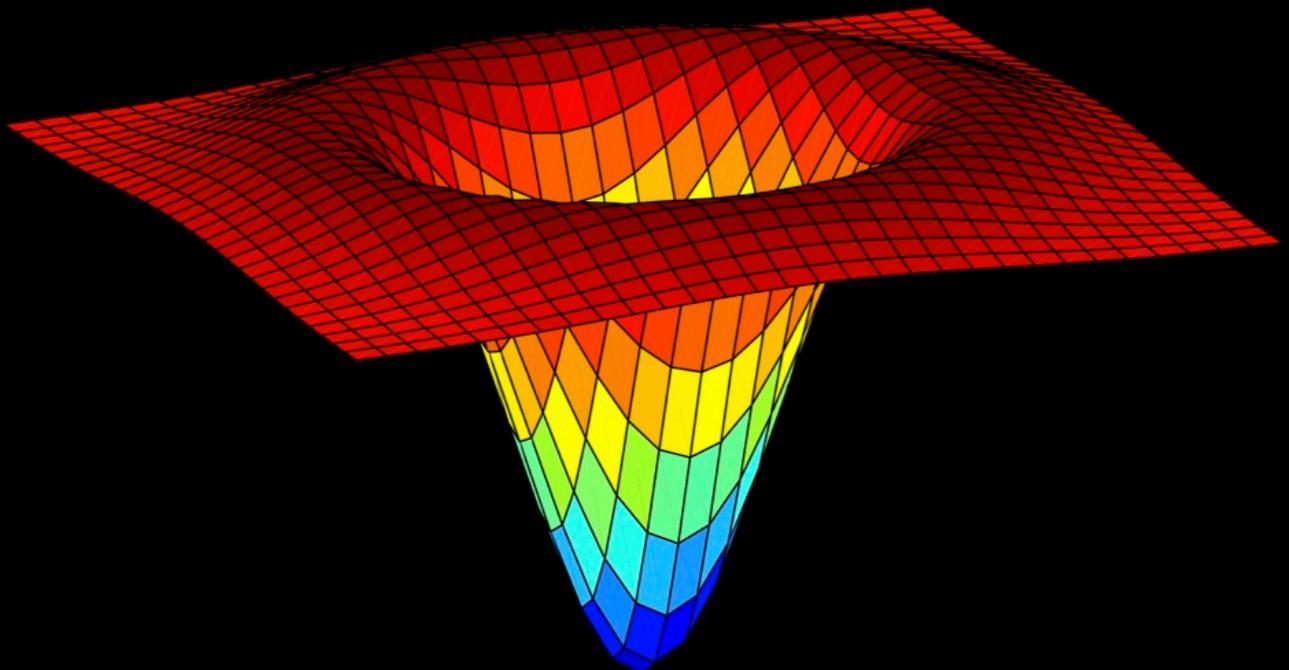


# Laplacian of Gaussian (LoG)



## Laplacian of Gaussian (LoG)

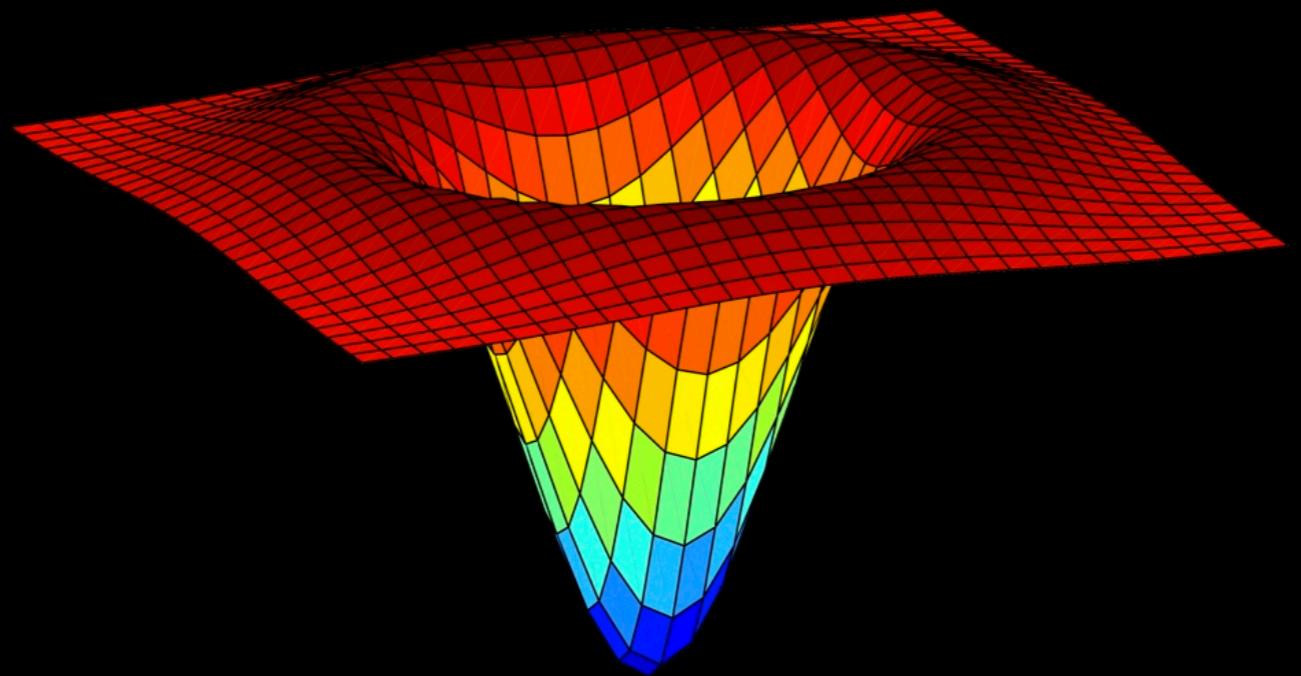
What pattern does this filter detect?



## Laplacian of Gaussian (LoG)

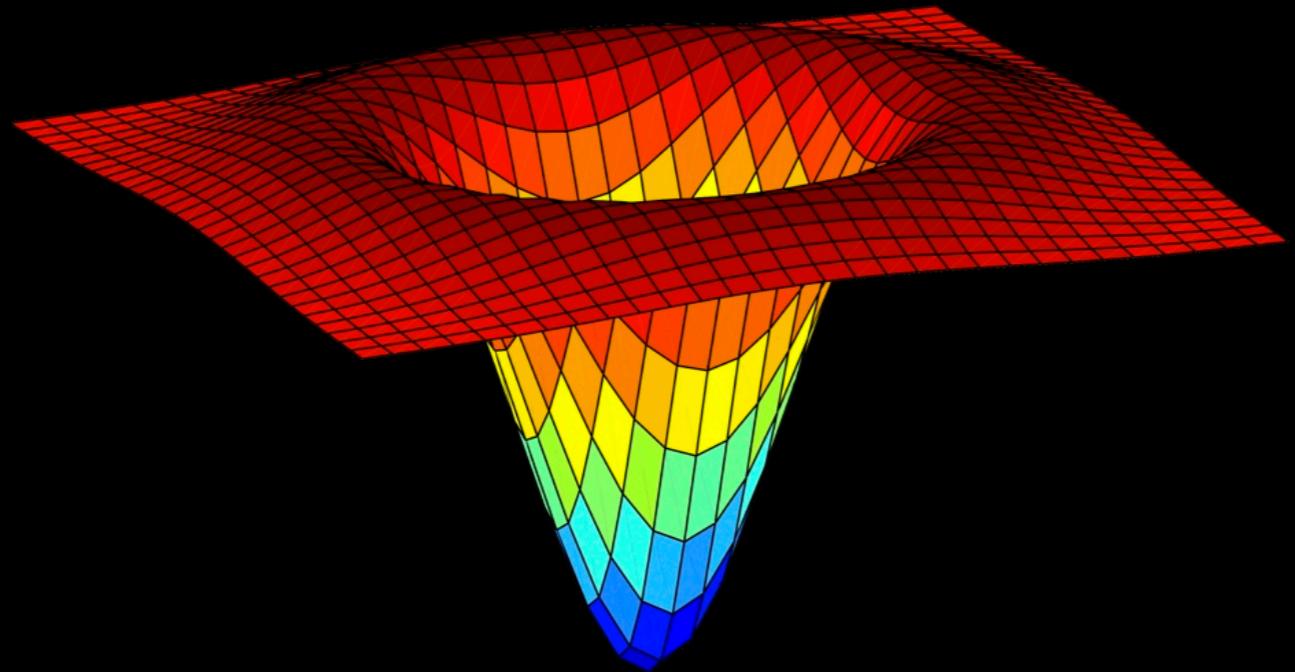
What pattern does this filter detect?

blob



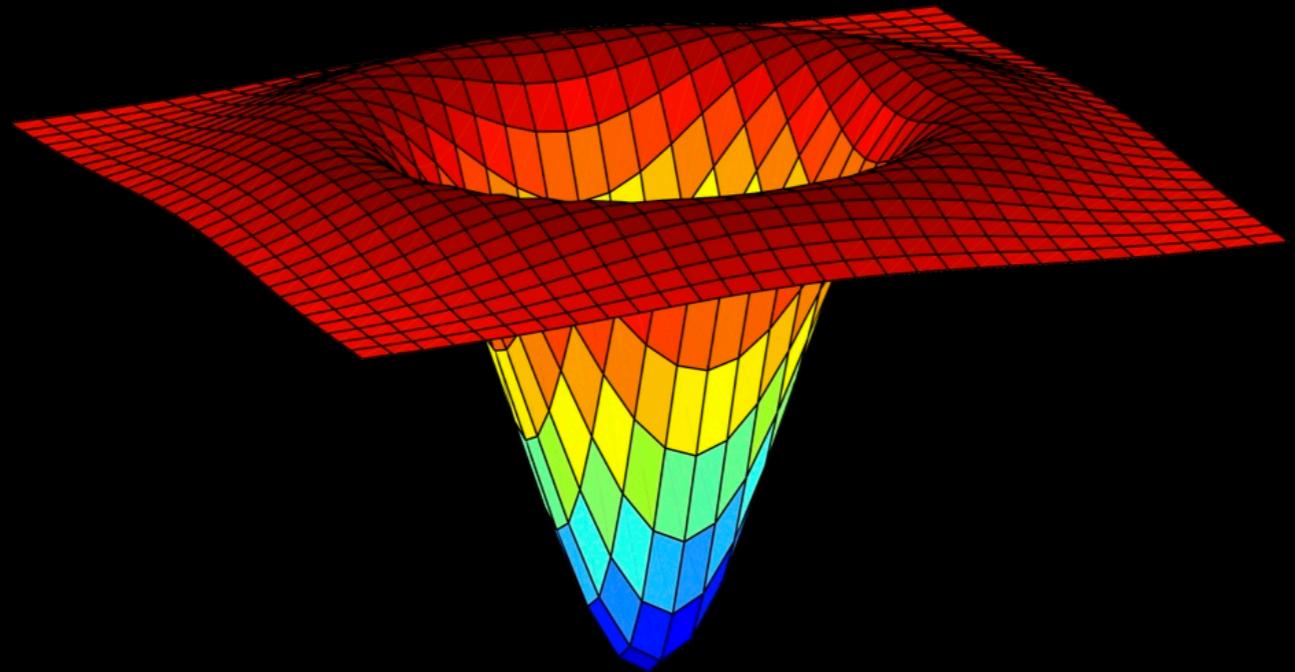
## Laplacian of Gaussian (LoG)

$$L(x, y; \sigma) = \sigma^2(G_{xx}(x, y, \sigma) + G_{yy}(x, y, \sigma))$$



## Laplacian of Gaussian (LoG)

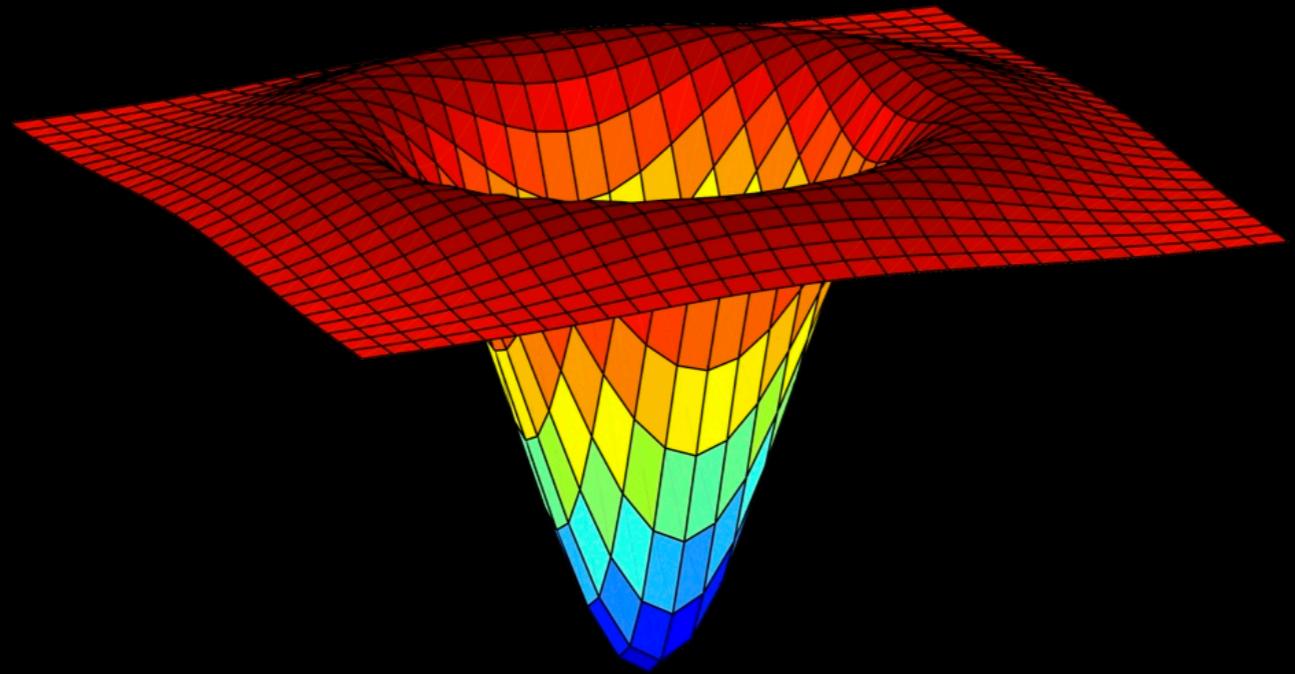
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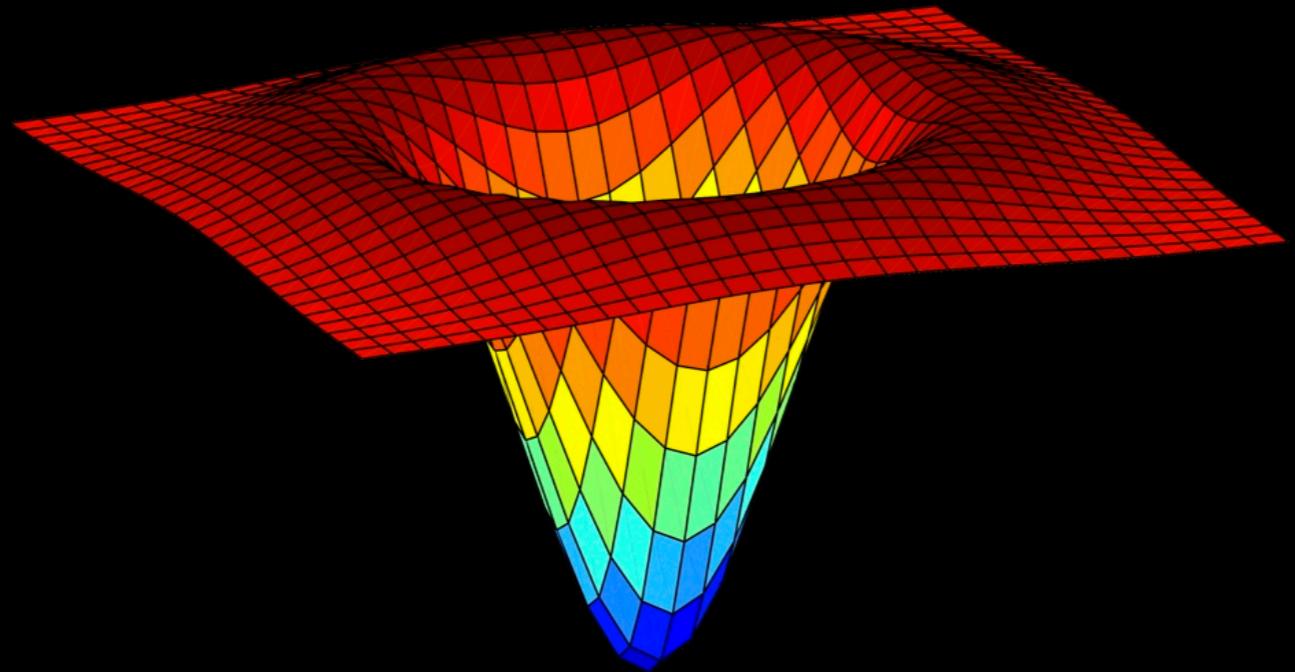
$$L(x, y; \sigma) = \sigma^2(G_{xx}(x, y, \sigma) + G_{yy}(x, y, \sigma))$$

$$f_{xx} = \frac{\partial}{\partial x}\left(\frac{\partial f}{\partial x}\right) = \frac{\partial^2 f}{\partial x^2}$$



## Laplacian of Gaussian (LoG)

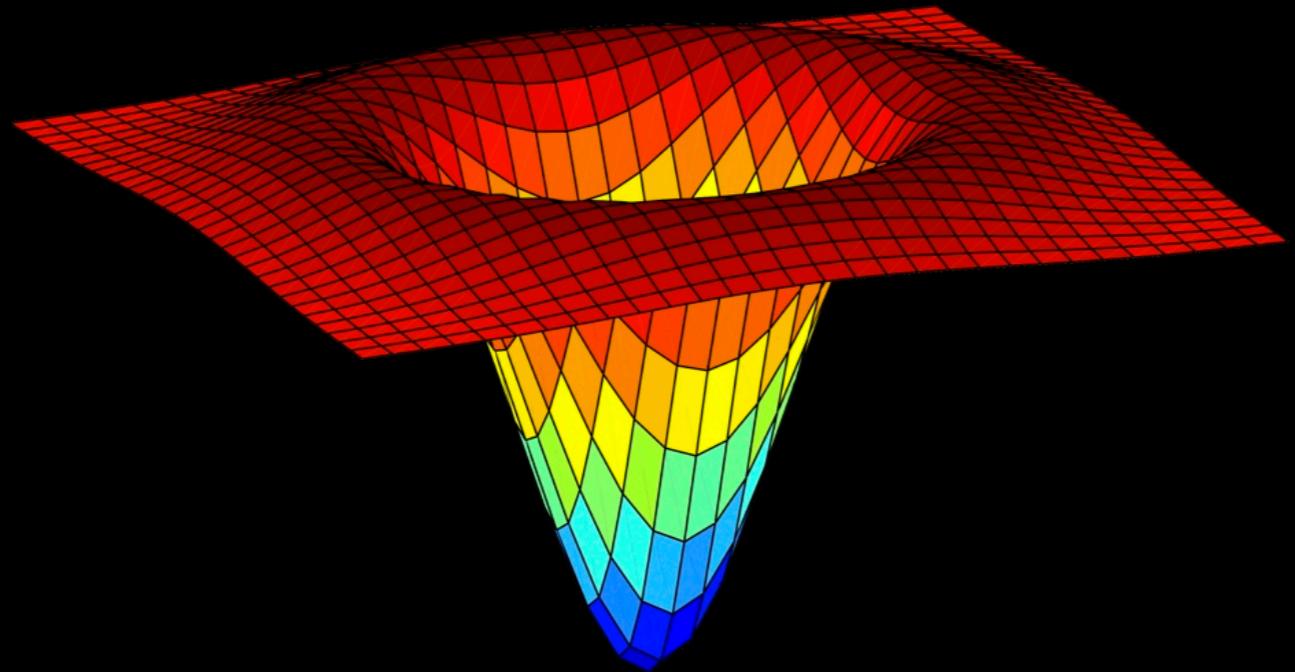
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## Laplacian of Gaussian (LoG)

$$L(x, y; \sigma) = \sigma^2(G_{xx}(x, y, \sigma) + G_{yy}(x, y, \sigma))$$

$$\approx G(x, y; k\sigma) - G(x, y; \sigma)$$

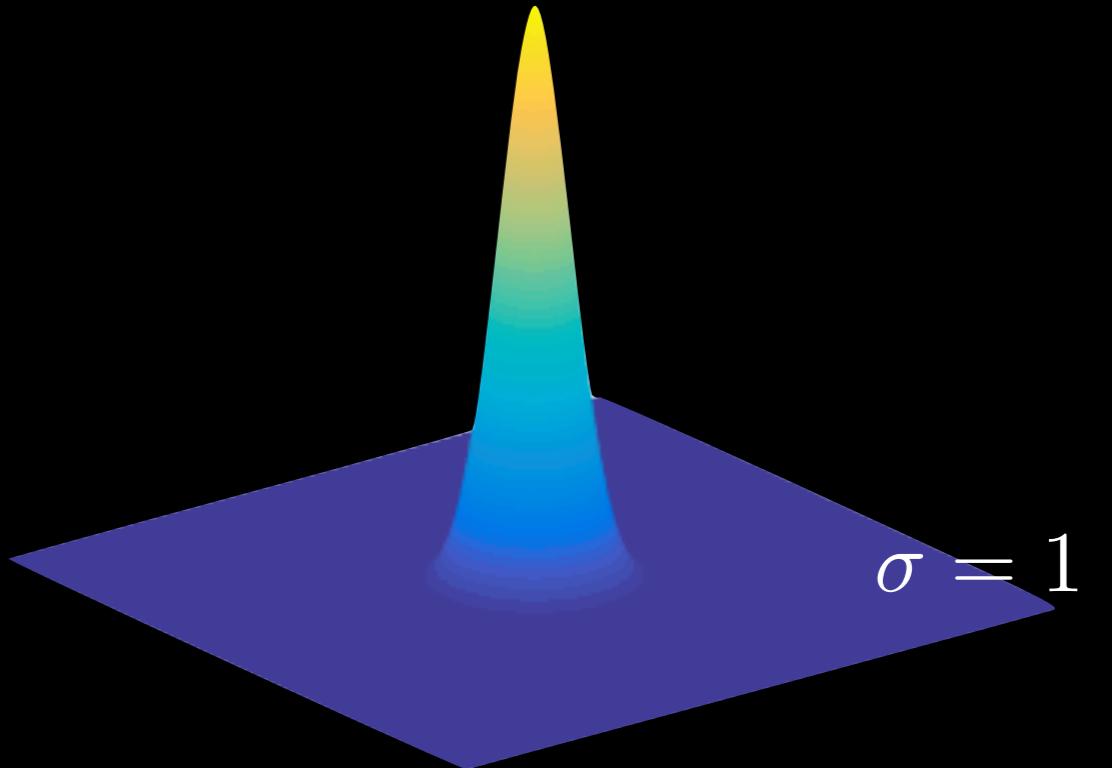
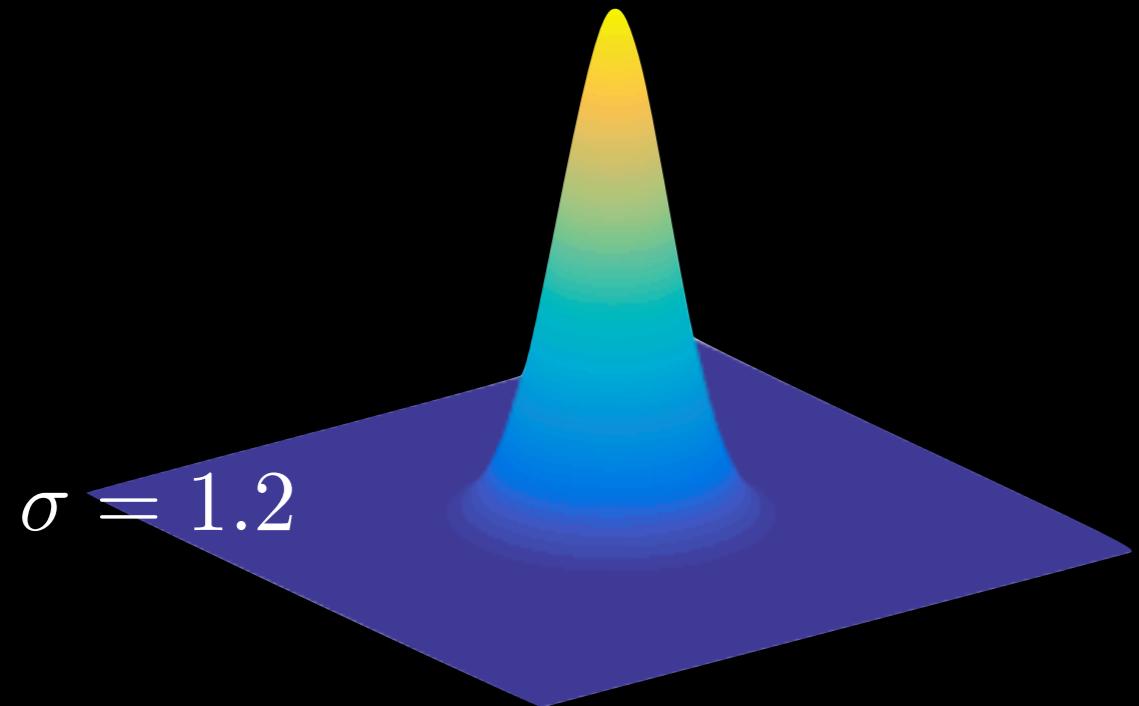


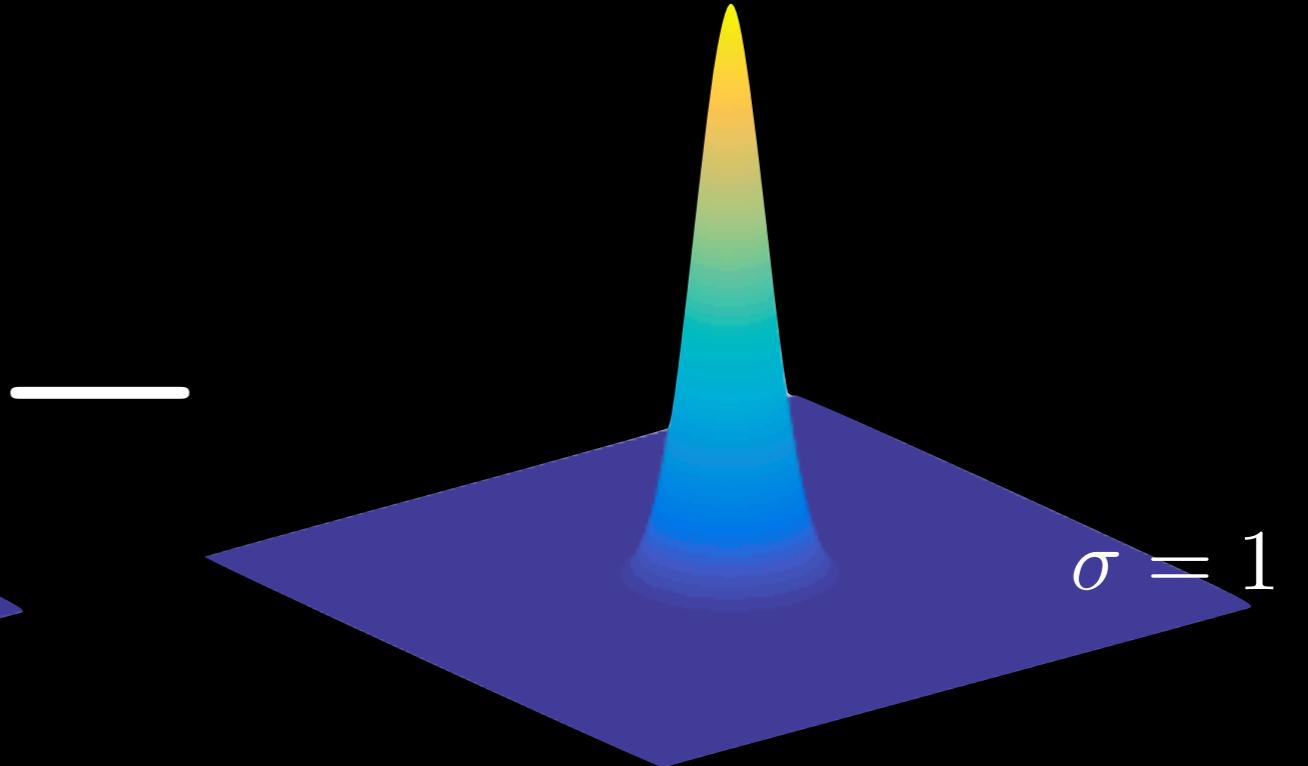
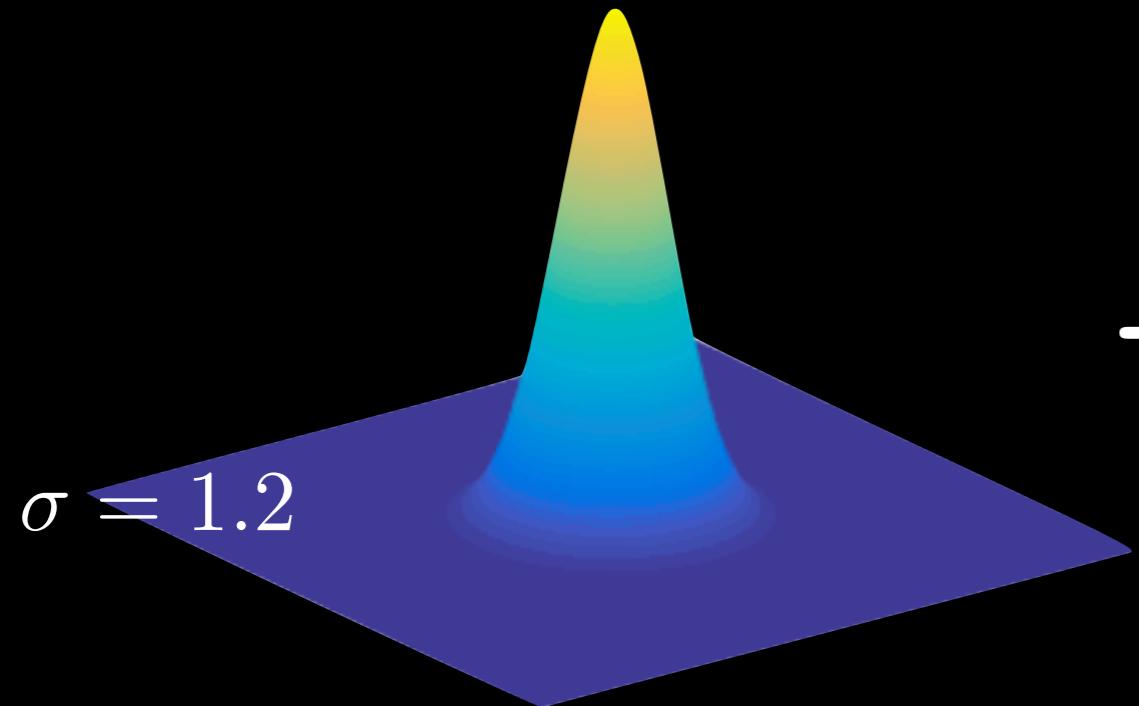
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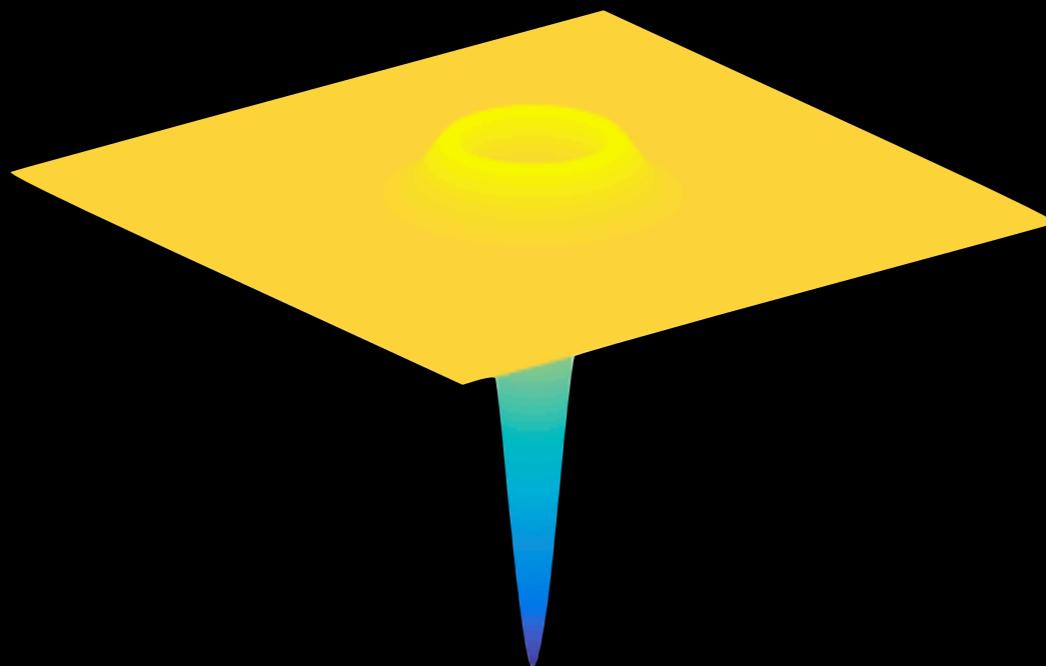
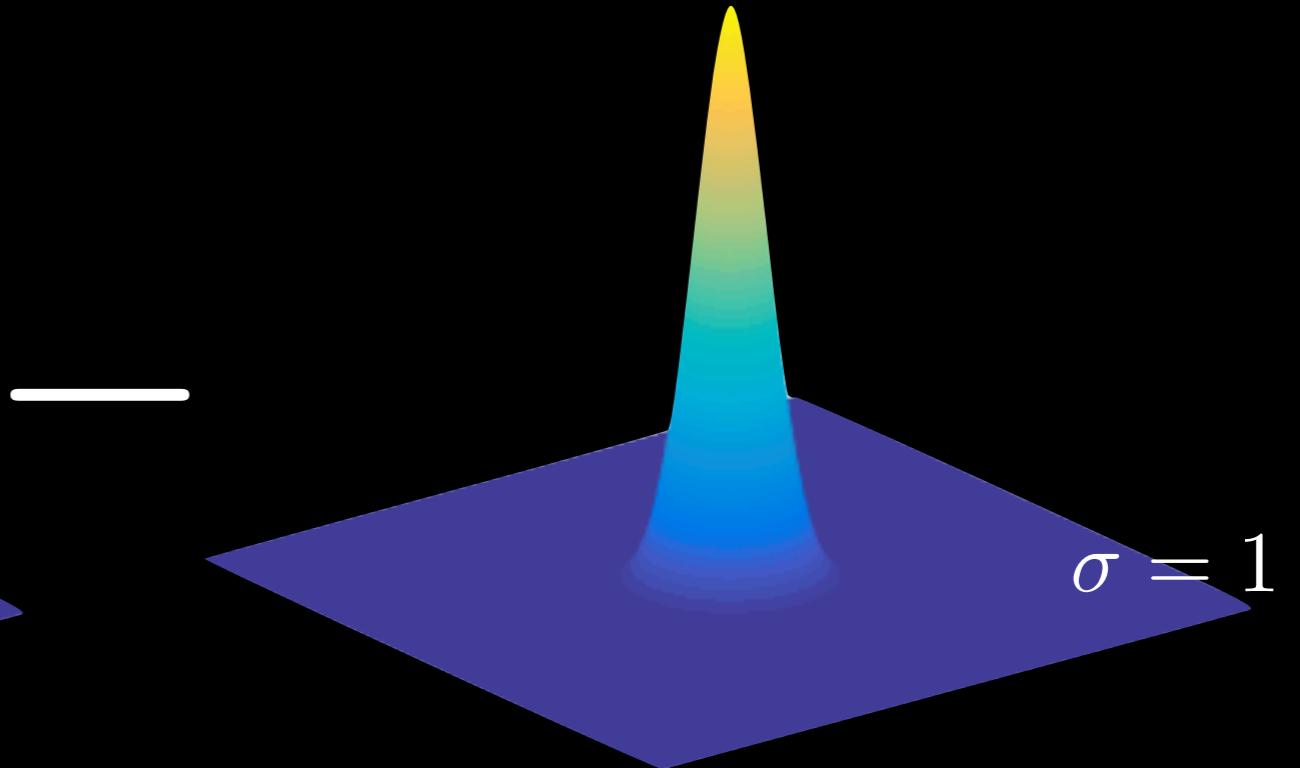
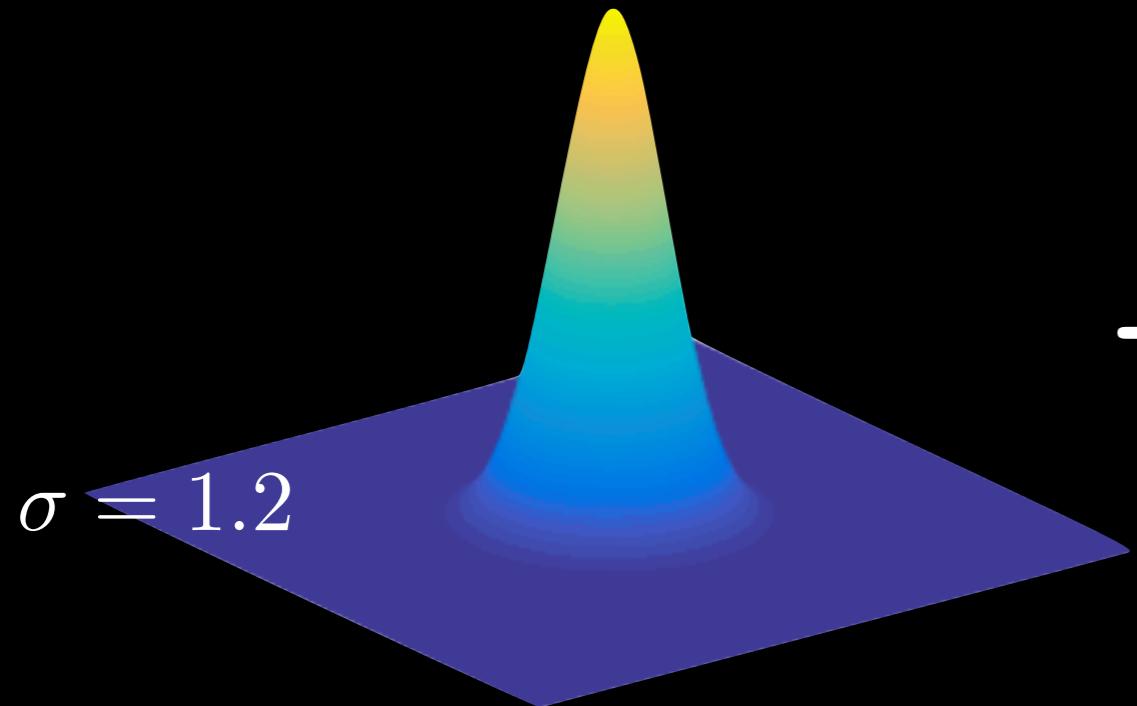
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$$\approx G(x, y; k\sigma) - G(x, y; \sigma)$$

Difference of Gaussians (DoG)

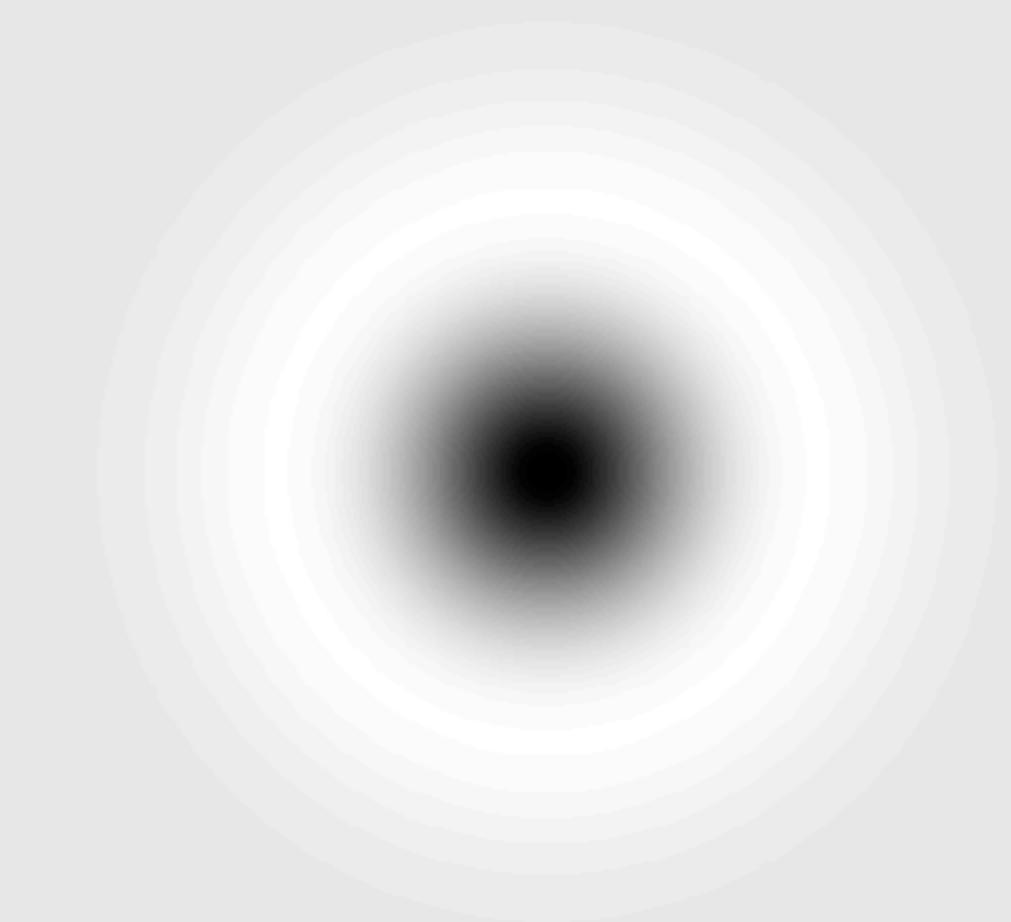






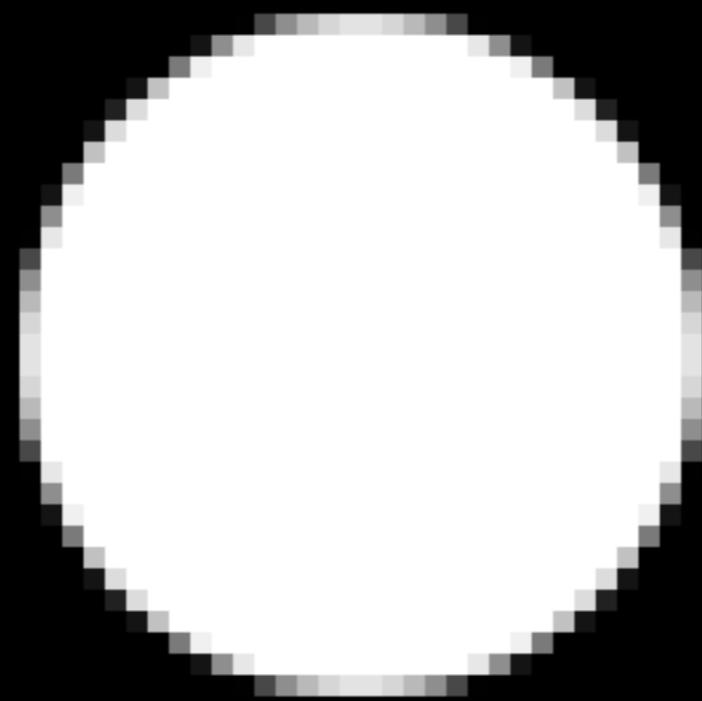


Blob  
Detection



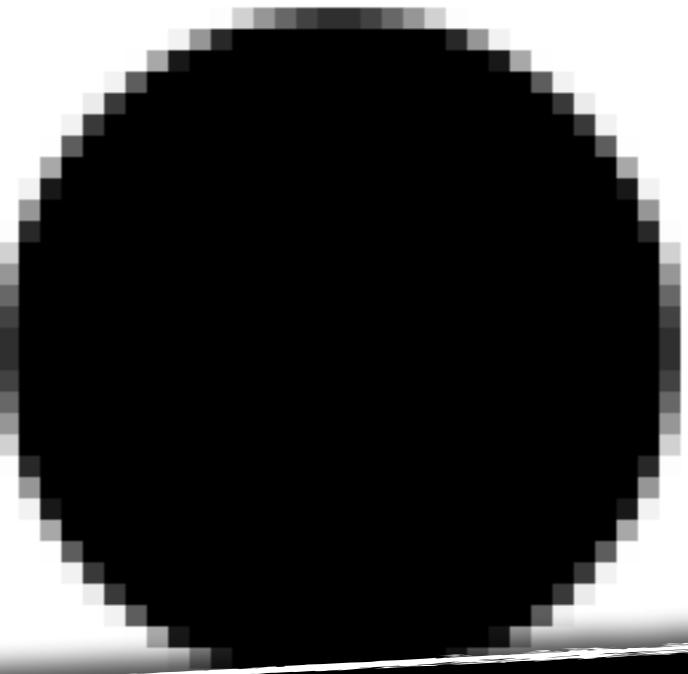
# Blob Detection

Convolve image with “blob” filter at multiple scales  
and find extrema

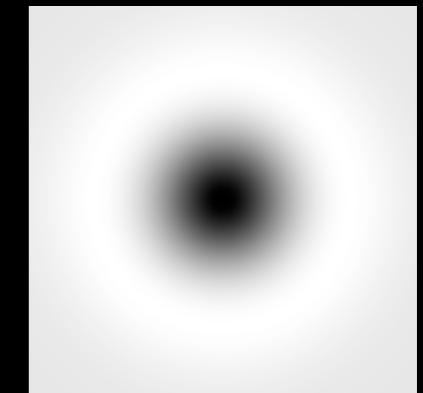
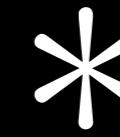




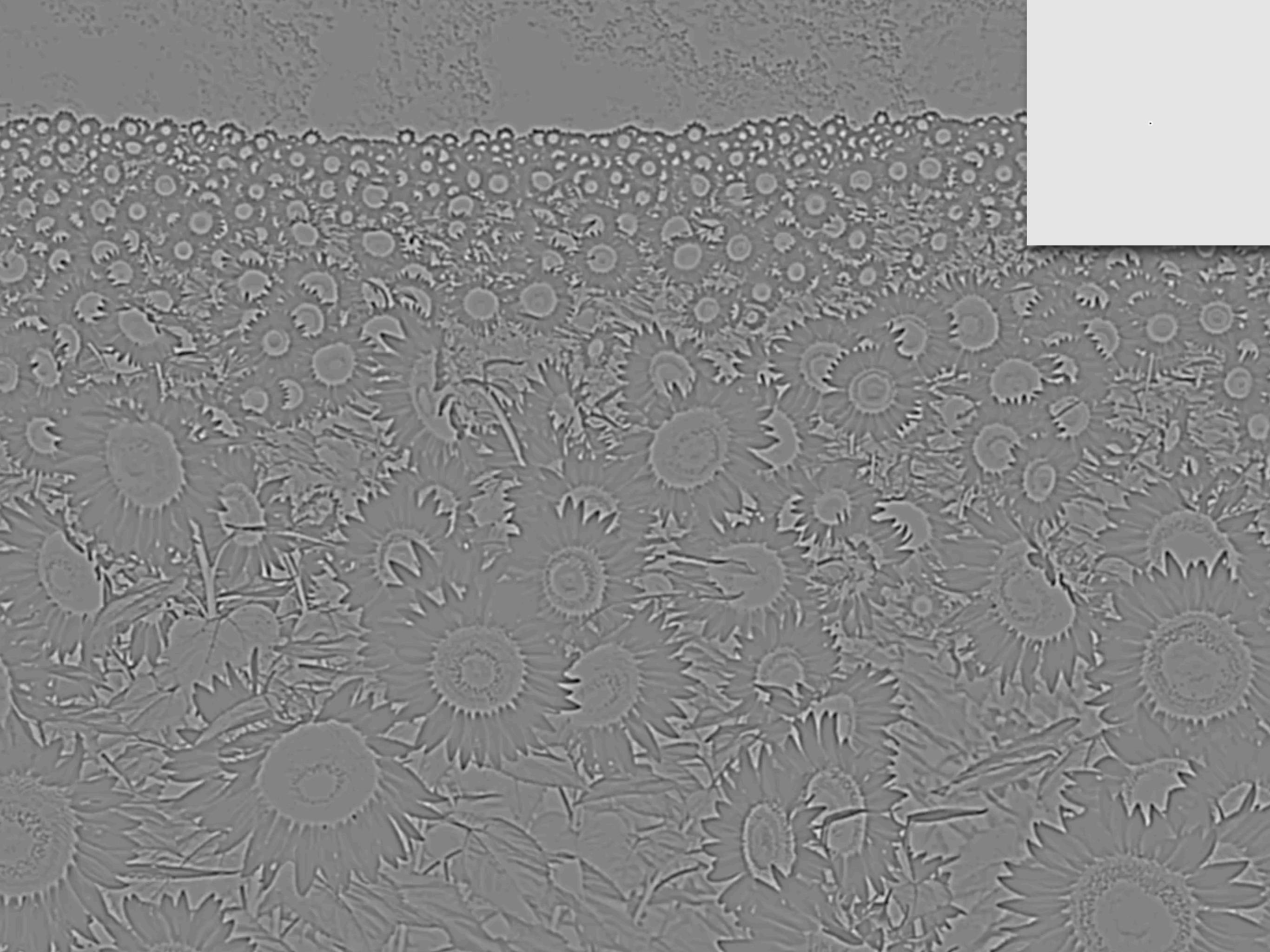
Laplacian extreme response is at  $\sigma = \text{radius}/\sqrt{2}$



Laplacian extreme response is at  $\sigma = \text{radius}/\sqrt{2}$



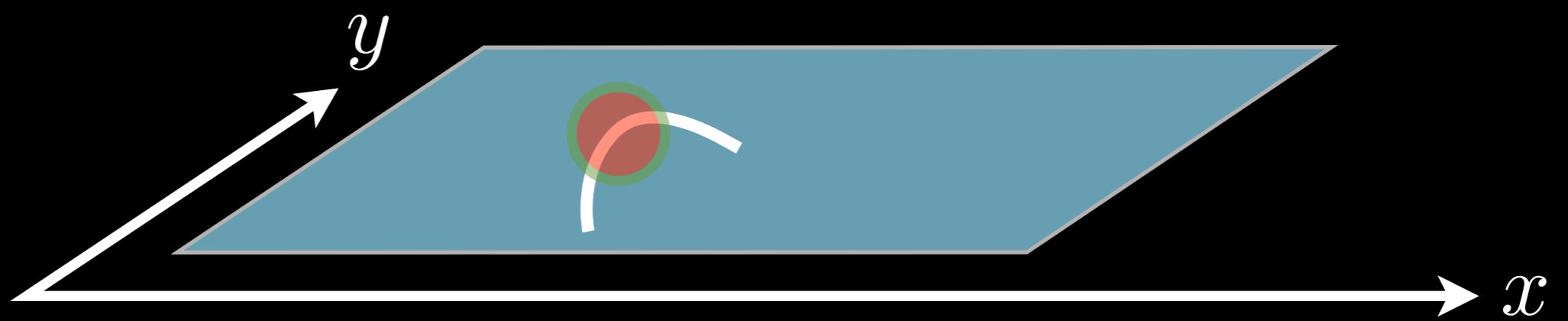






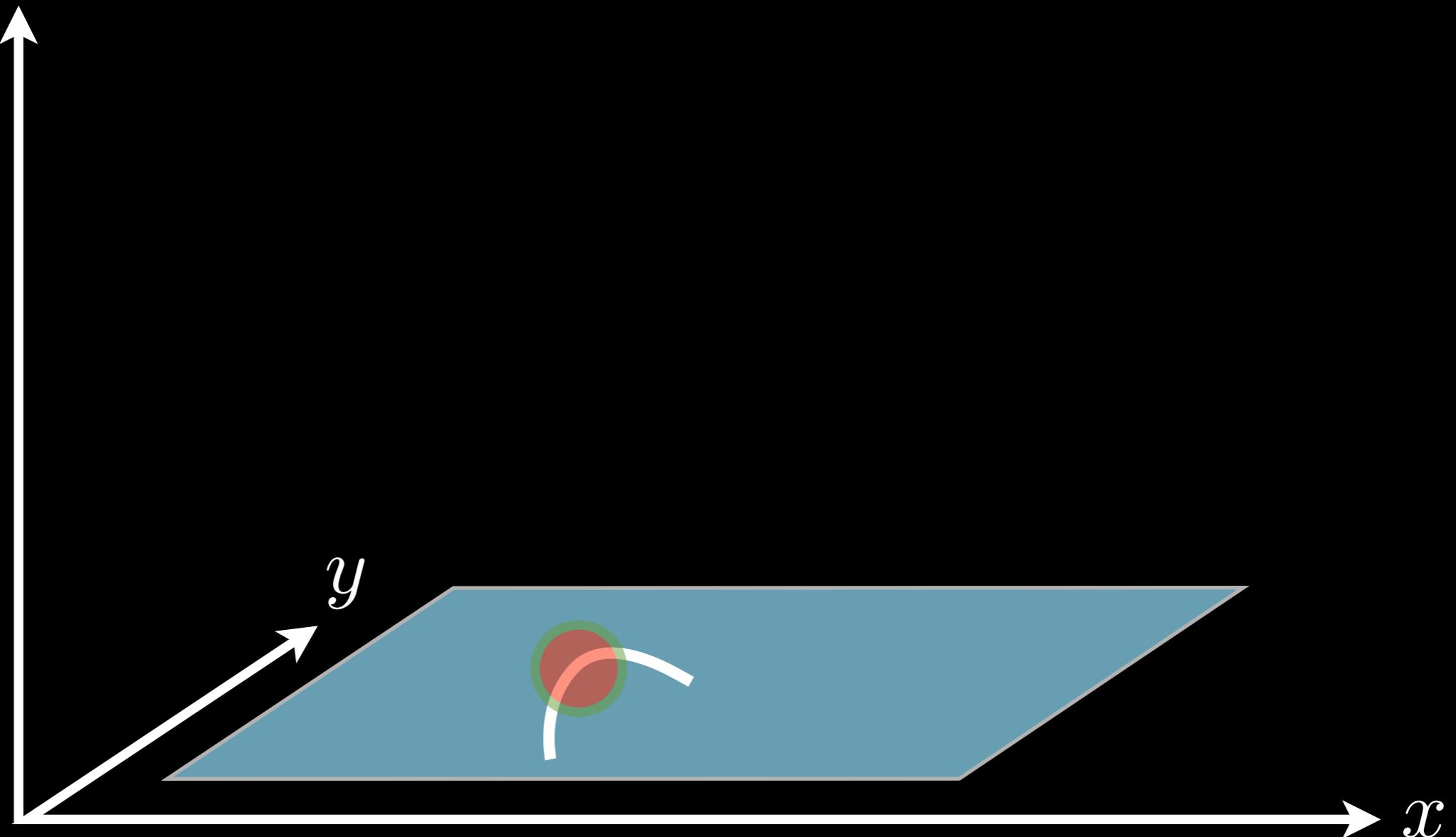


Convolve DoG across space at several scales



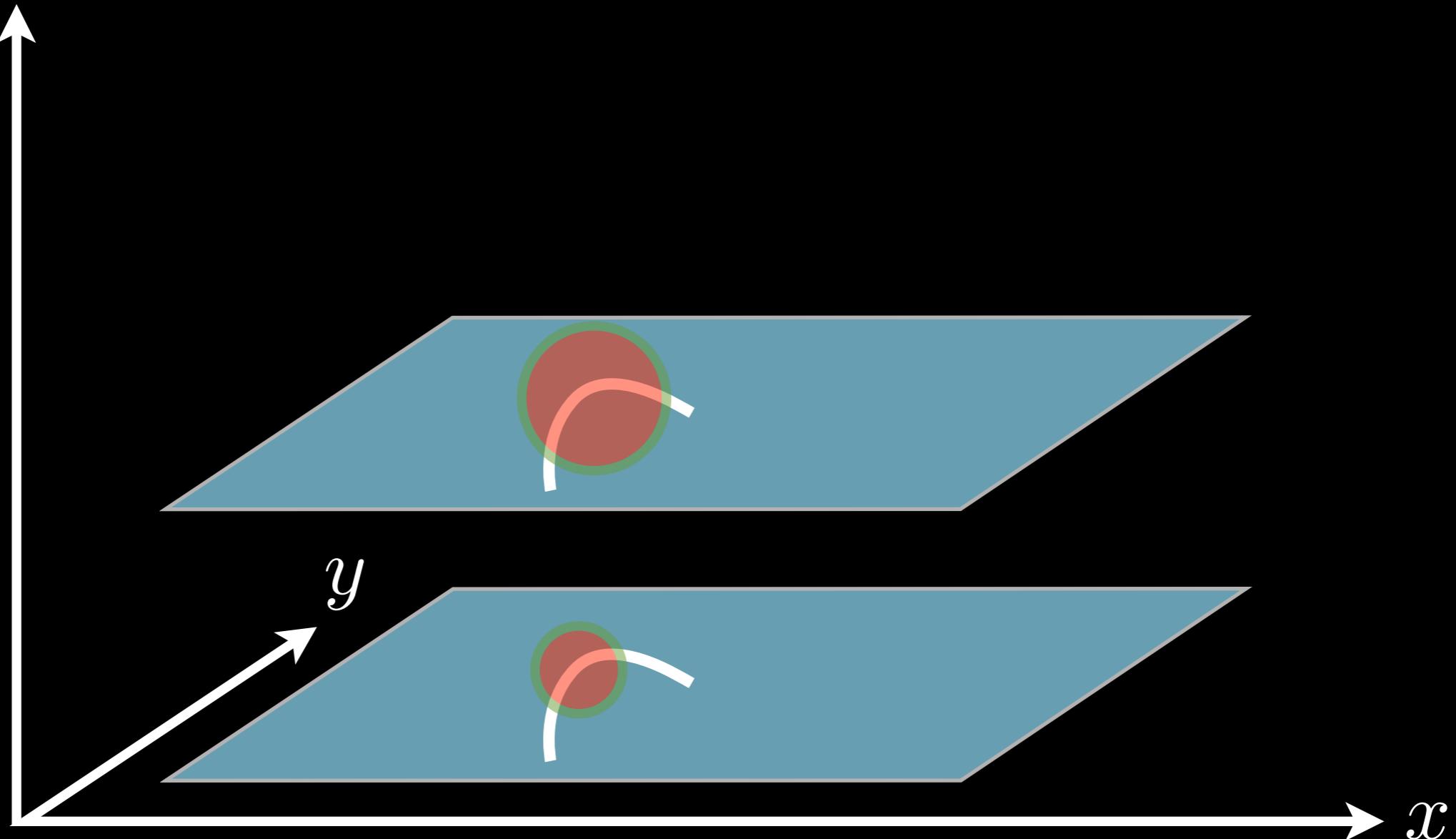
Convolve DoG across space at several scales

*scale*



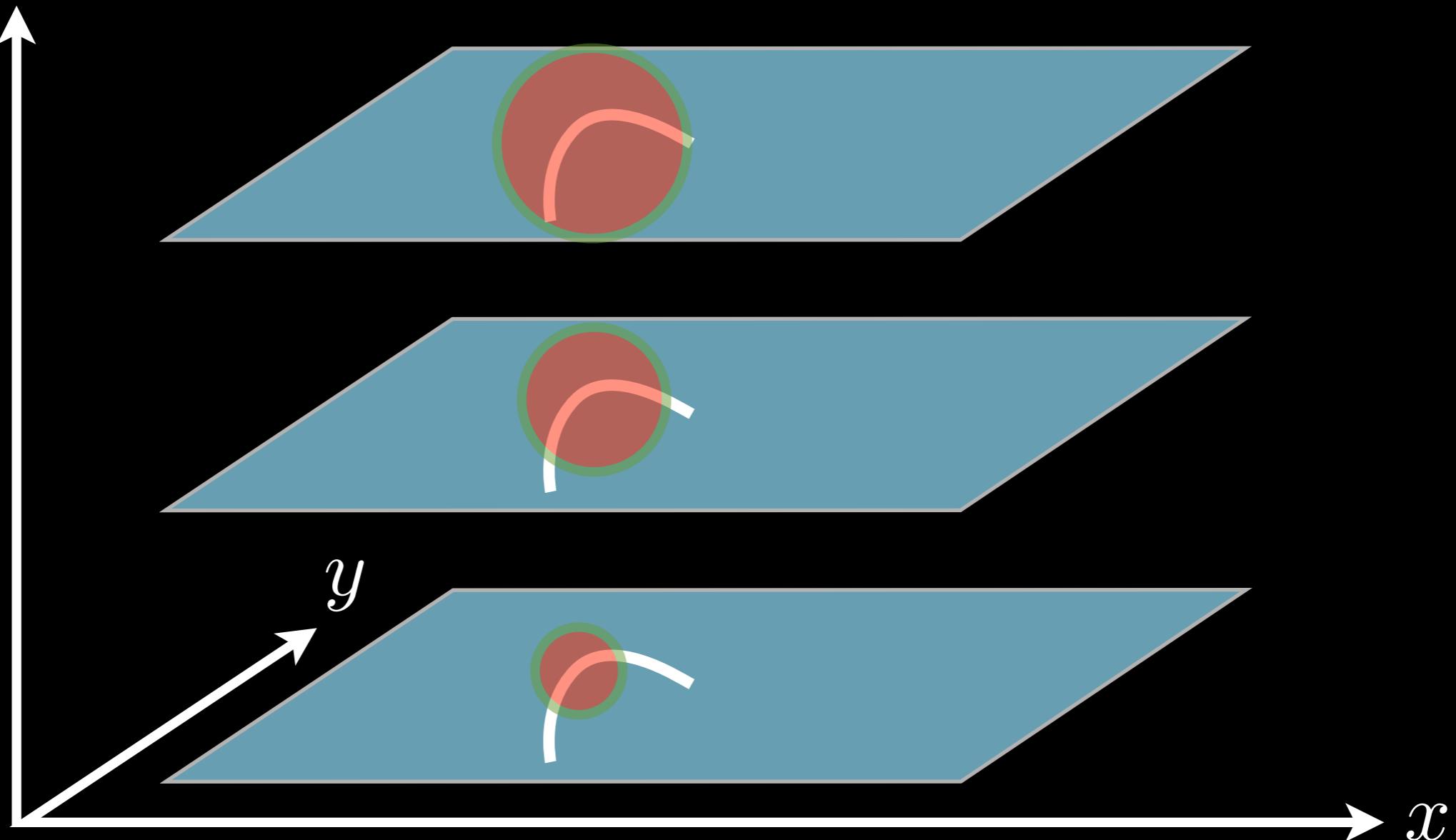
**Convolve DoG across space at several scales**

*scale*



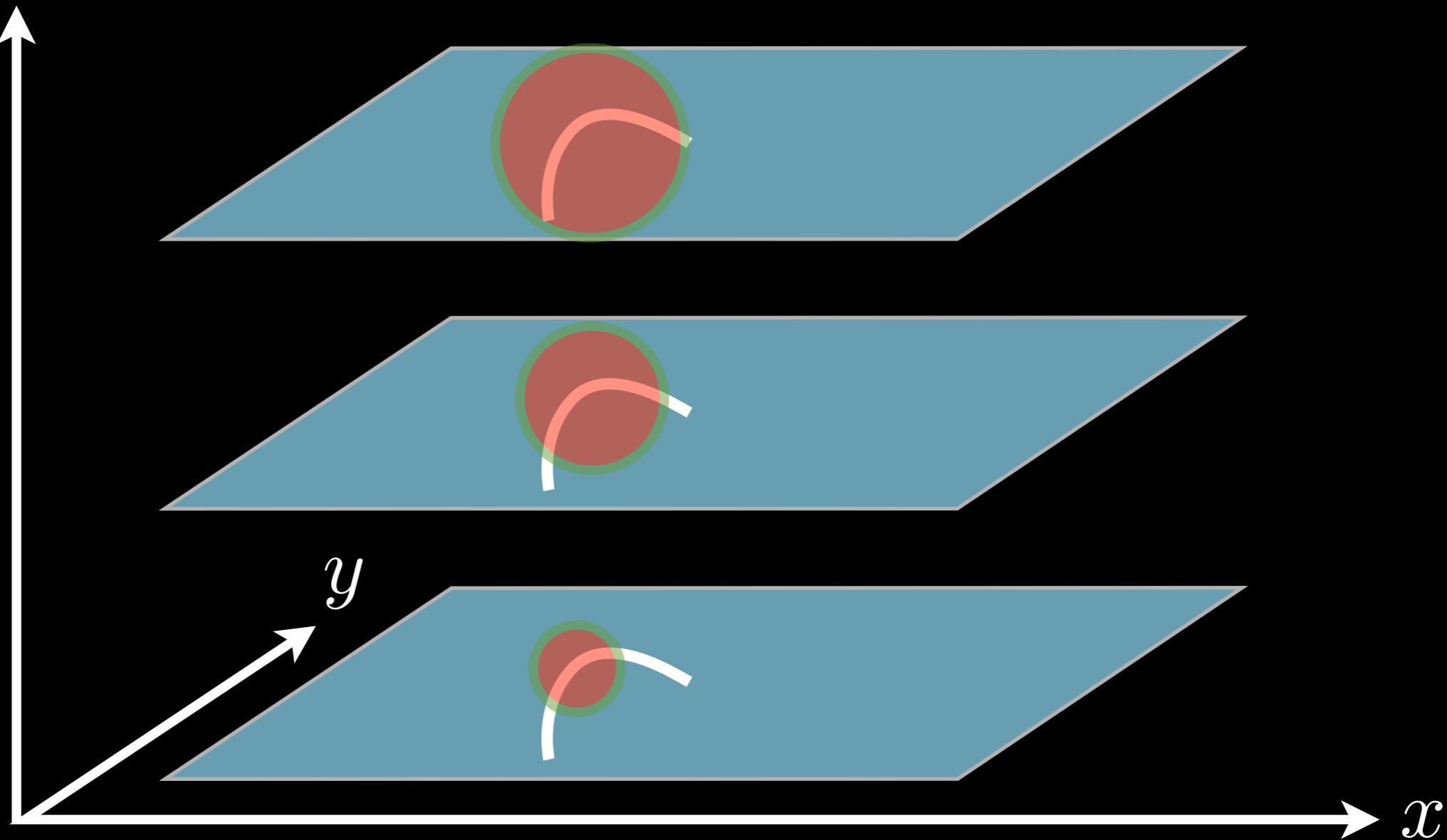
**Convolve DoG across space at several scales**

*scale*



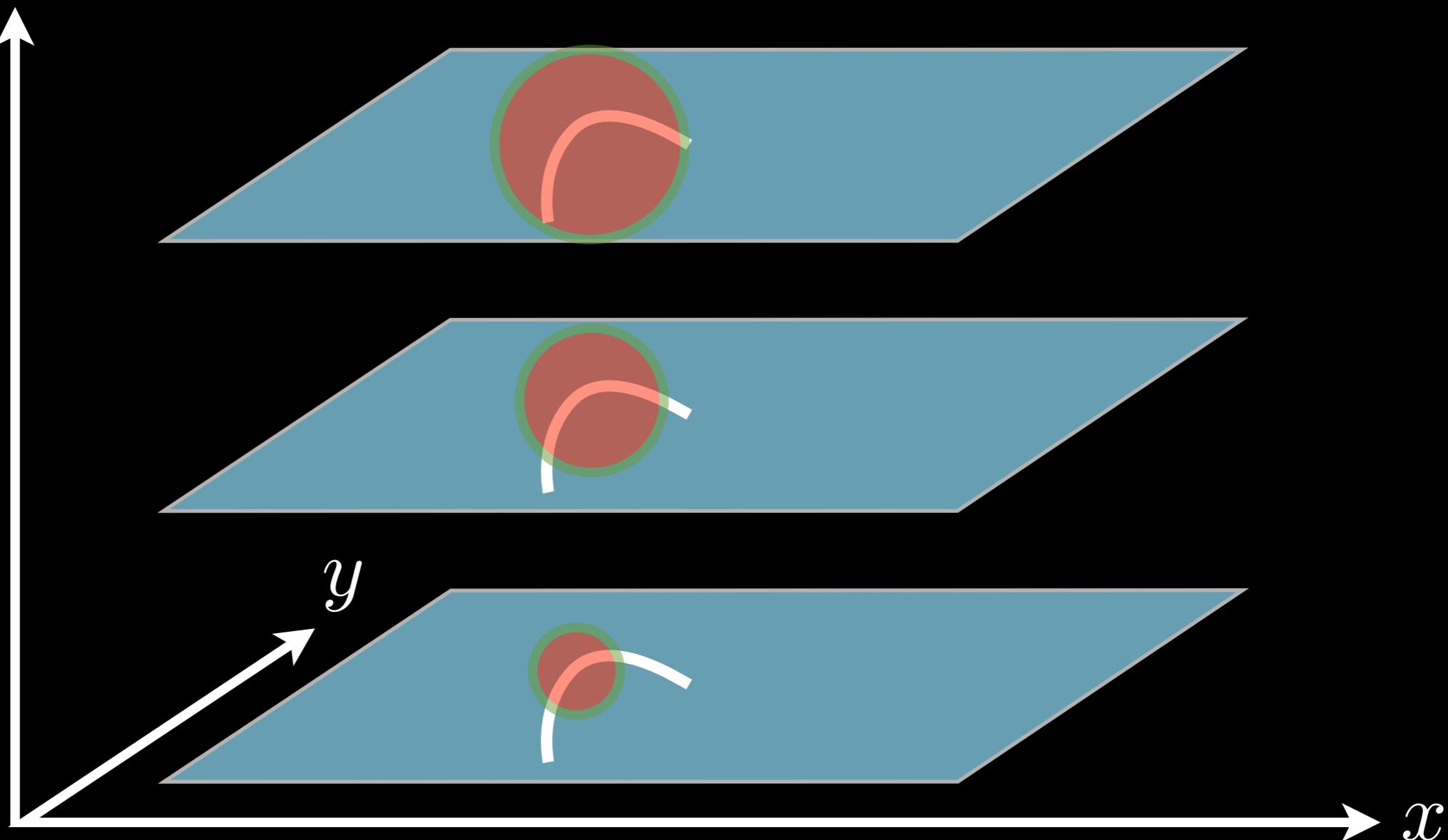
**Convolve DoG across space at several scales**

*scale*



Find local maxima of DoG in space

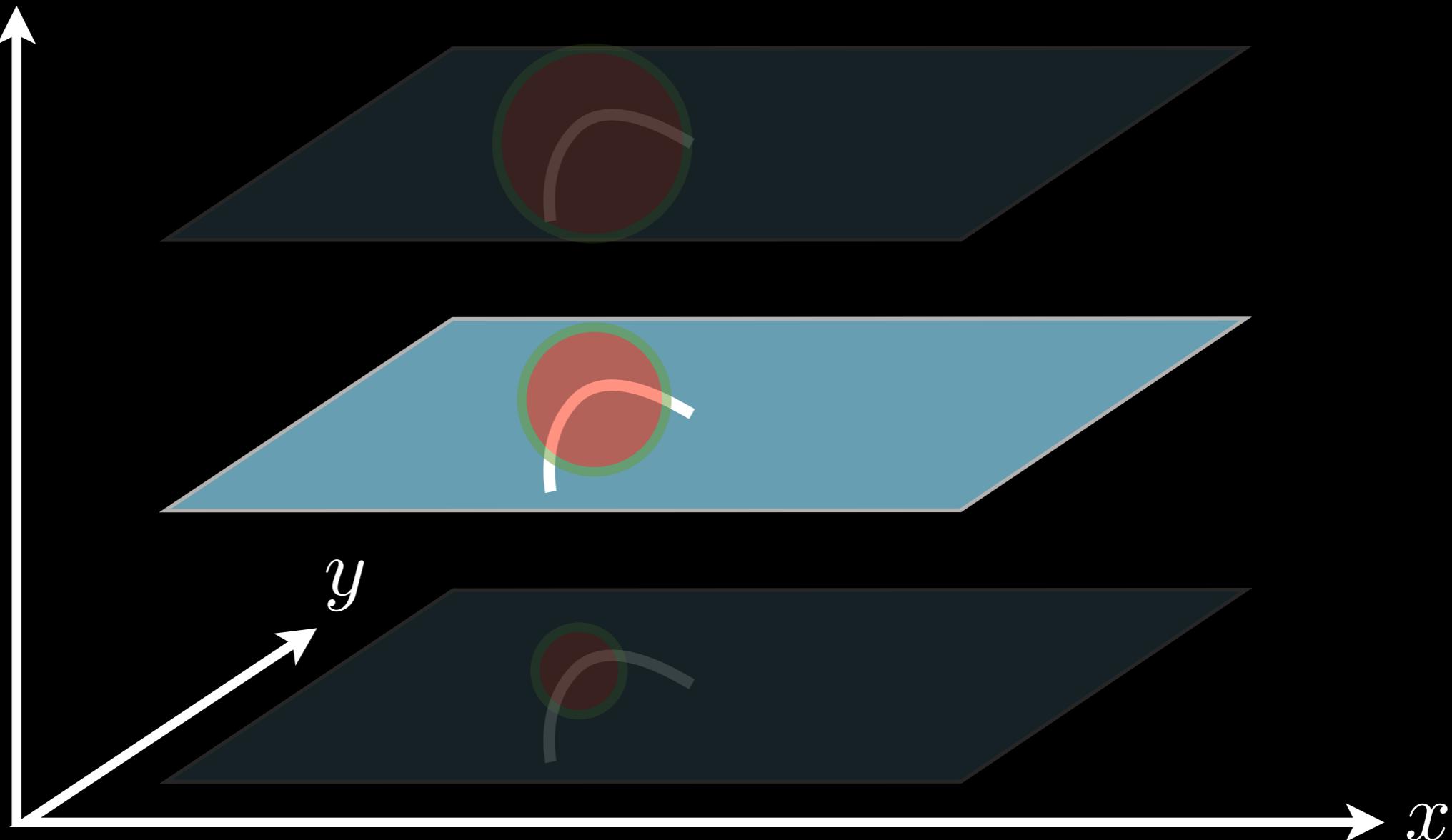
*scale*



Find local maxima of DoG in space

and scale

*scale*



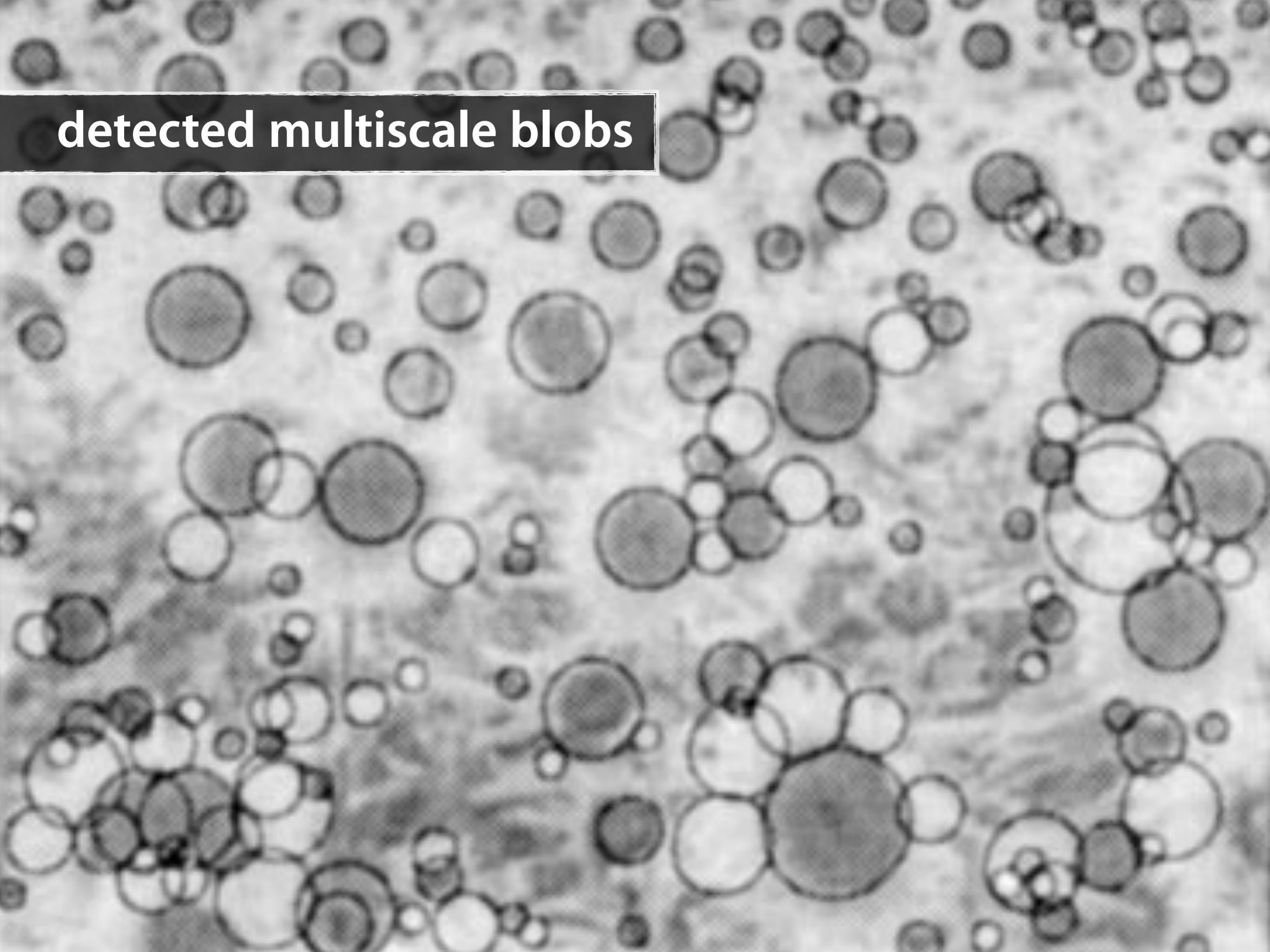
Find local maxima of DoG in space

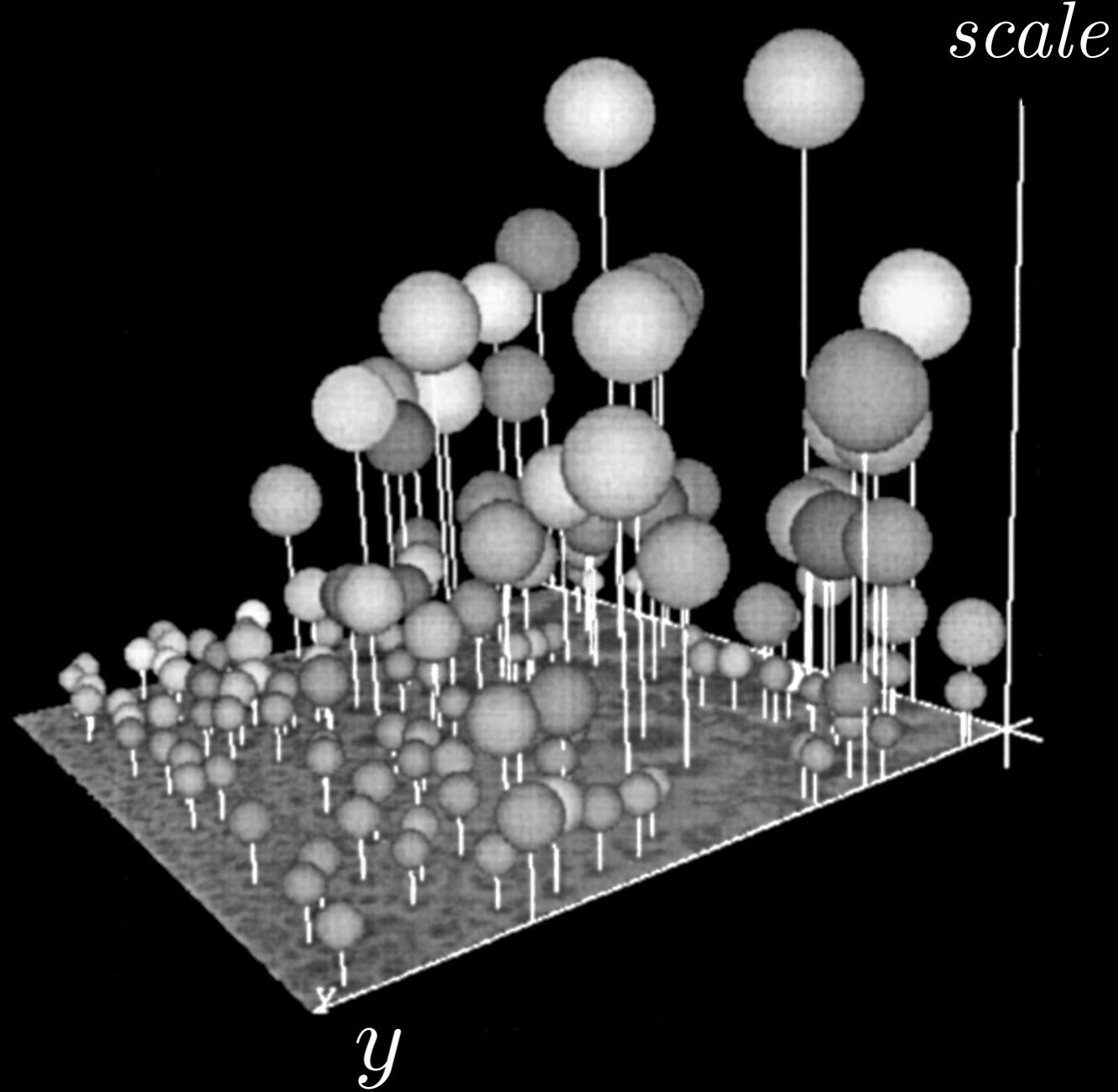
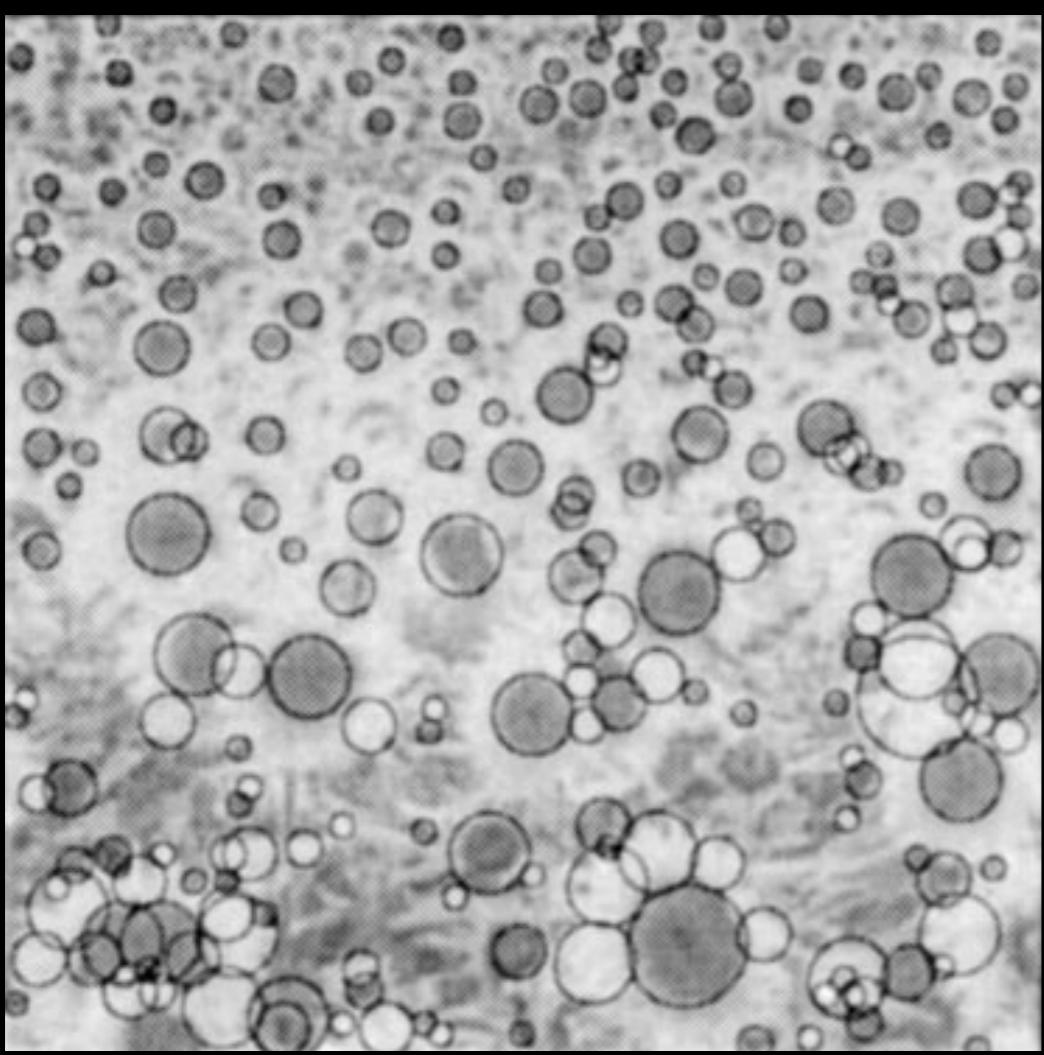
and scale

input image



detected multiscale blobs

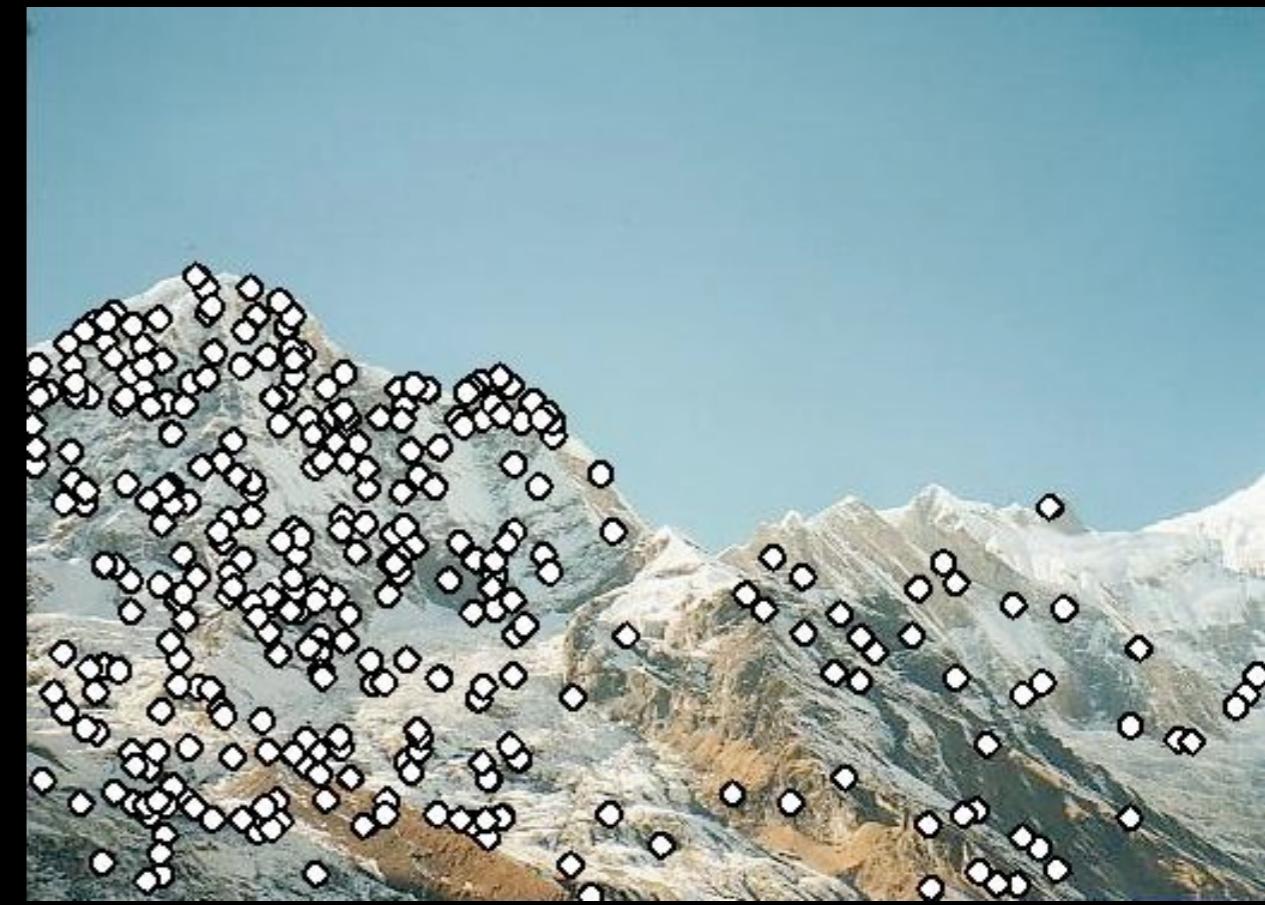


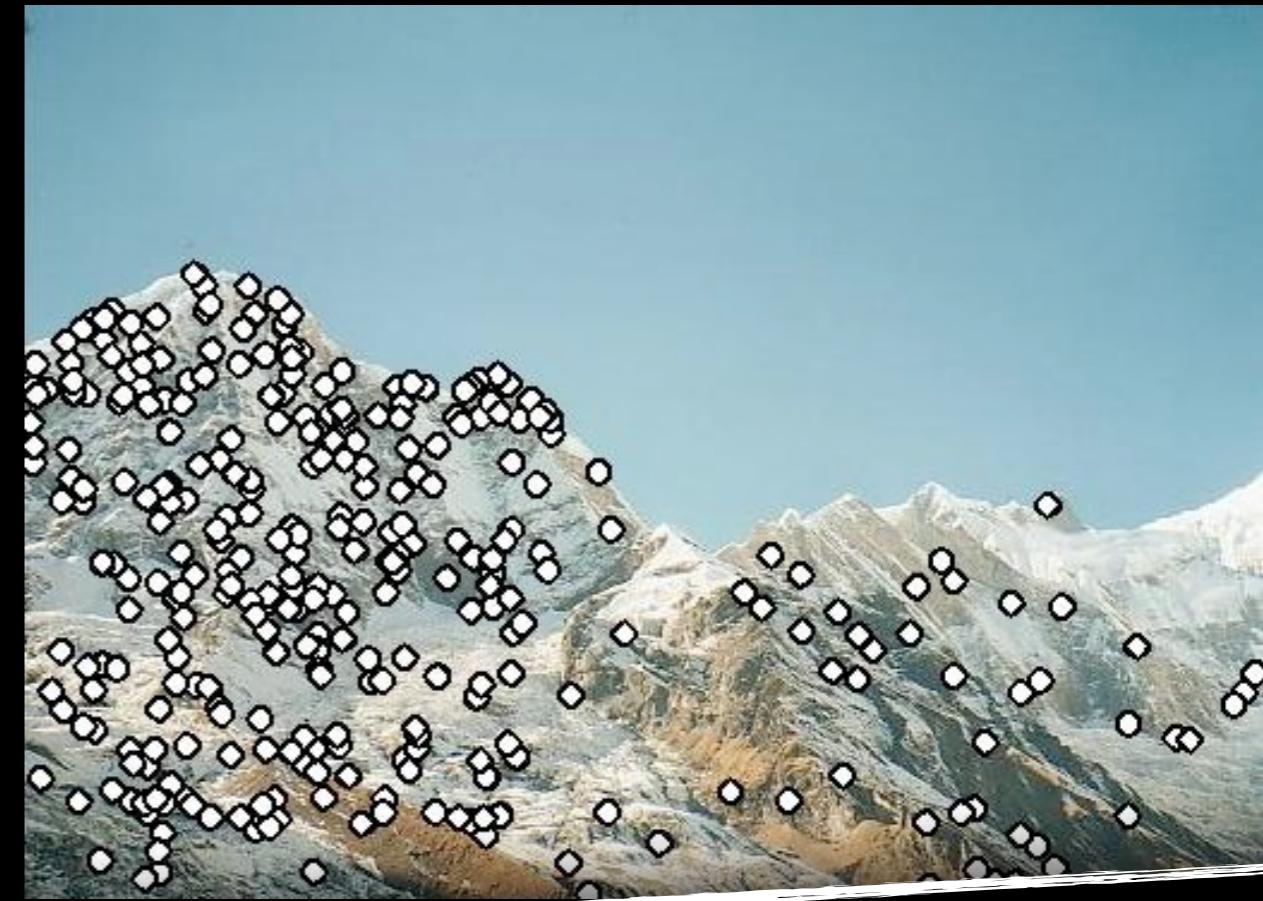


Lindeberg, Feature Detection with Automatic Scale Selection, IJCV, 1998

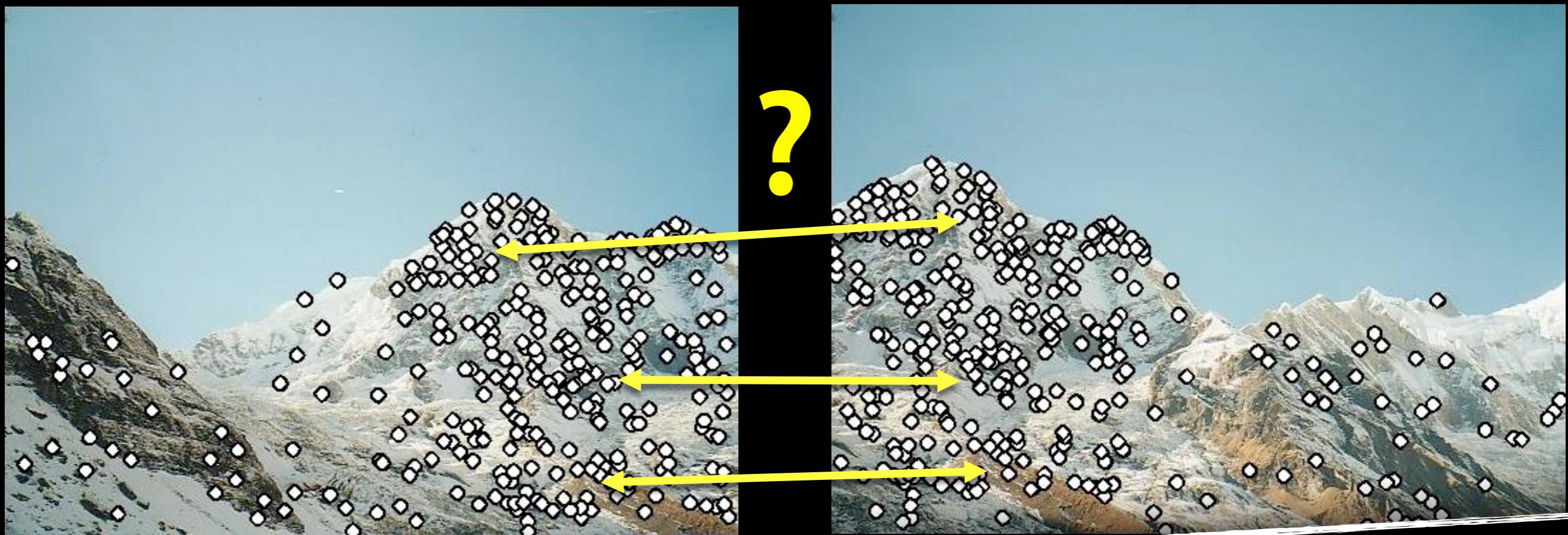
# SIFT Feature Descriptor







How do we match detected features across images?



How do we match detected features across images?

Rotation Invariant  
Description

Rotation Invariant  
Description

**Step 1: Find dominant orientation of the patch**

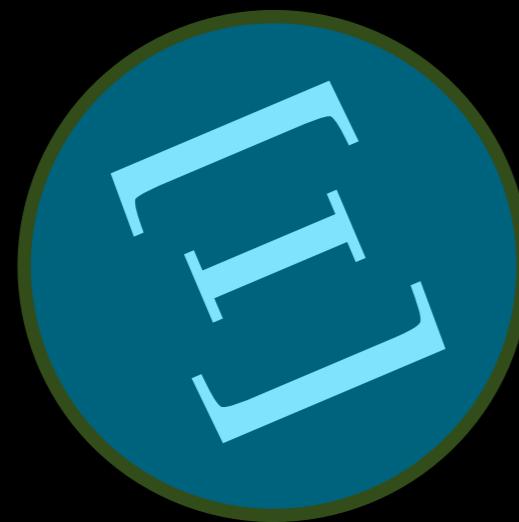
Rotation Invariant  
Description

**Step 1: Find dominant orientation of the patch**



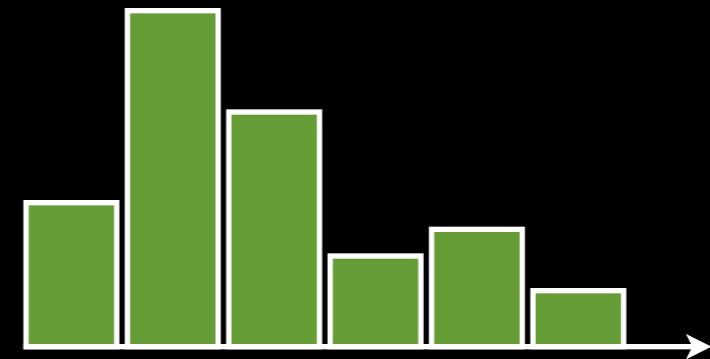
Rotation Invariant  
Description

**Step 1: Find dominant orientation of the patch**



Rotation Invariant  
Description

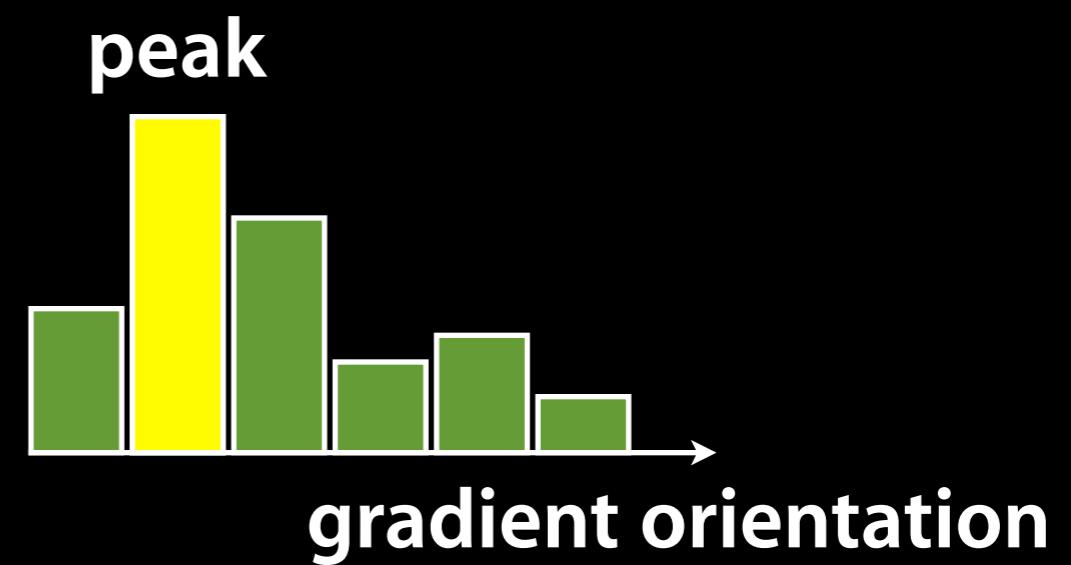
## Step 1: Find dominant orientation of the patch



gradient orientation

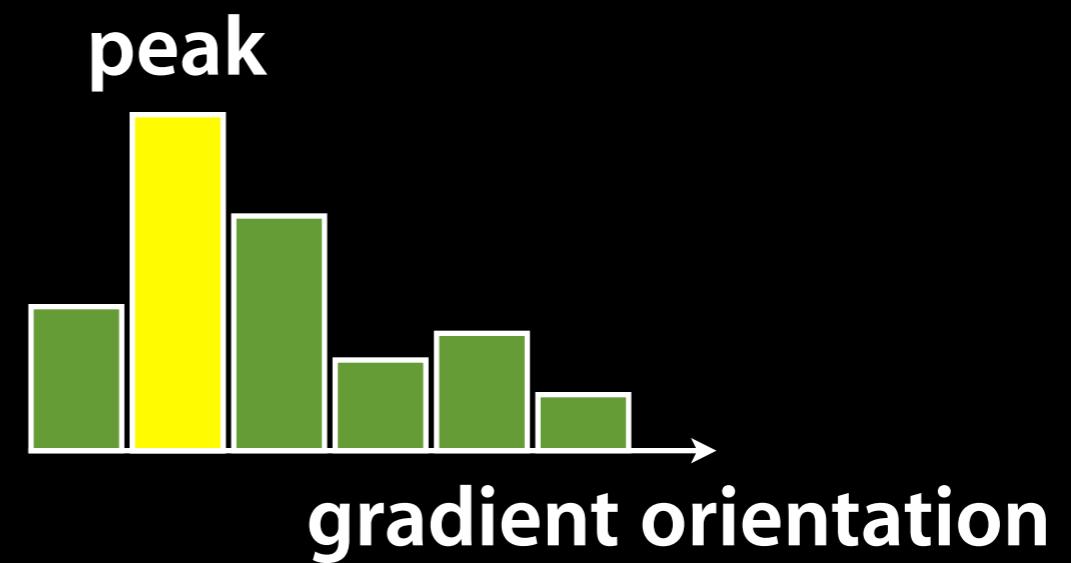
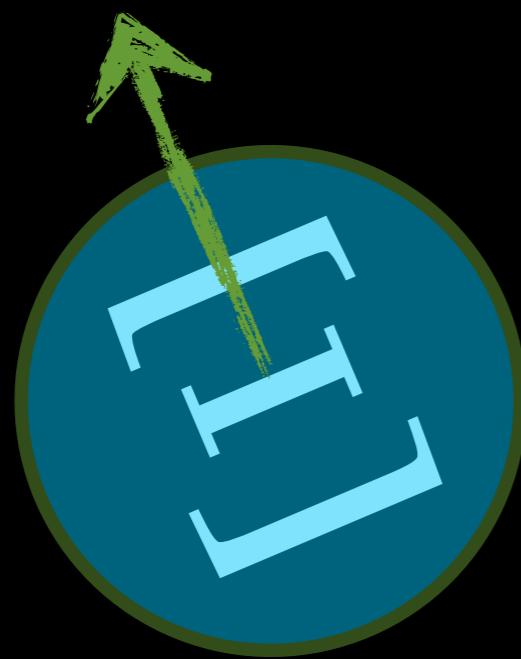
Rotation Invariant  
Description

## Step 1: Find dominant orientation of the patch



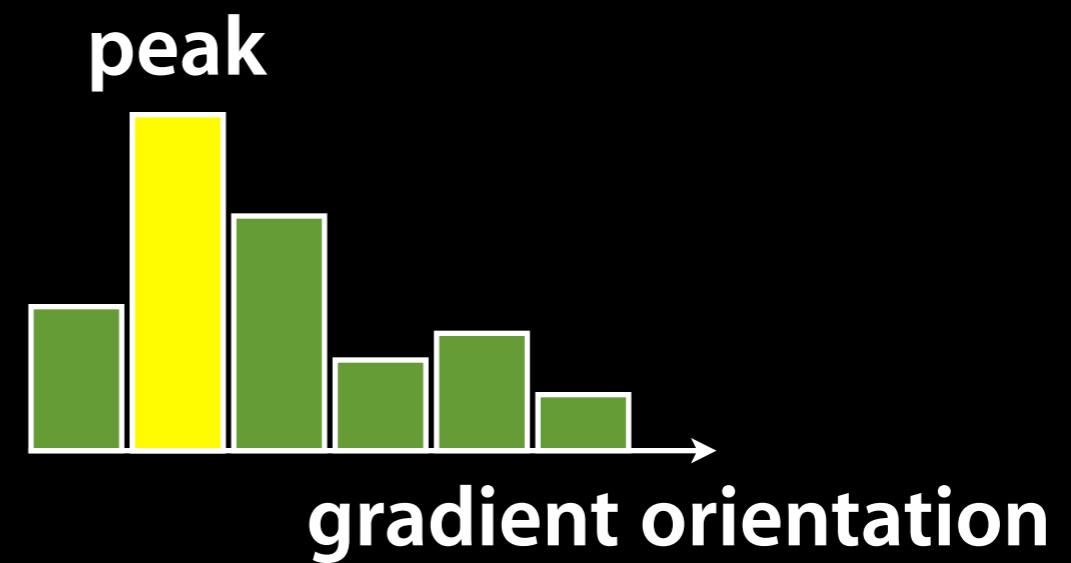
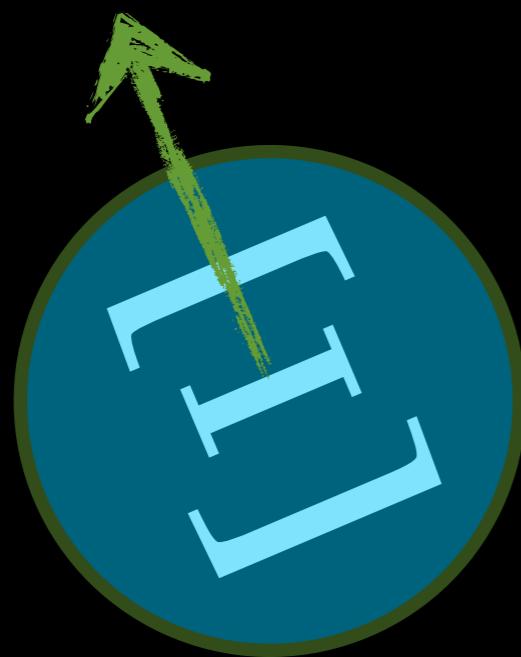
Rotation Invariant  
Description

## Step 1: Find dominant orientation of the patch



Rotation Invariant  
Description

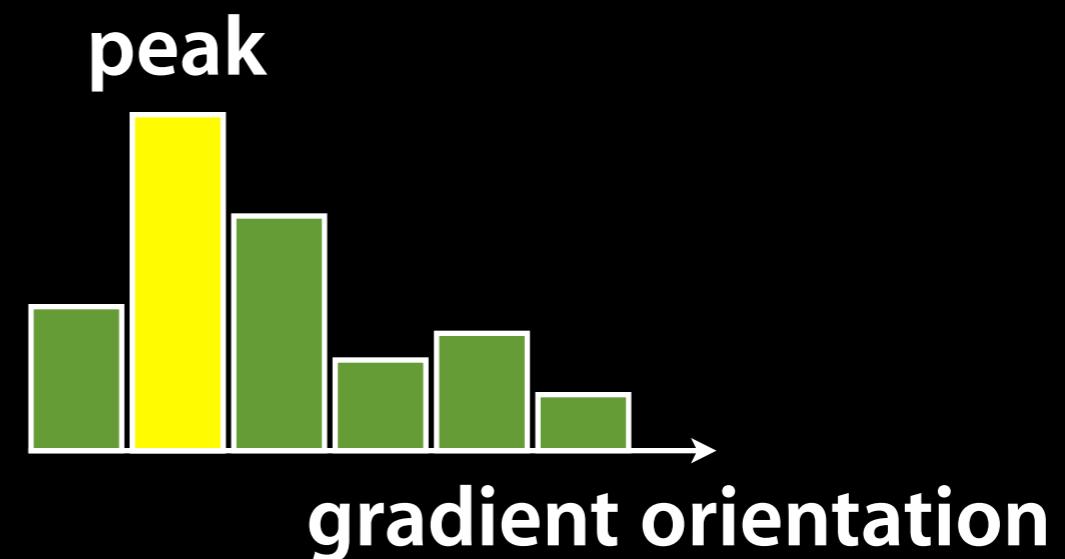
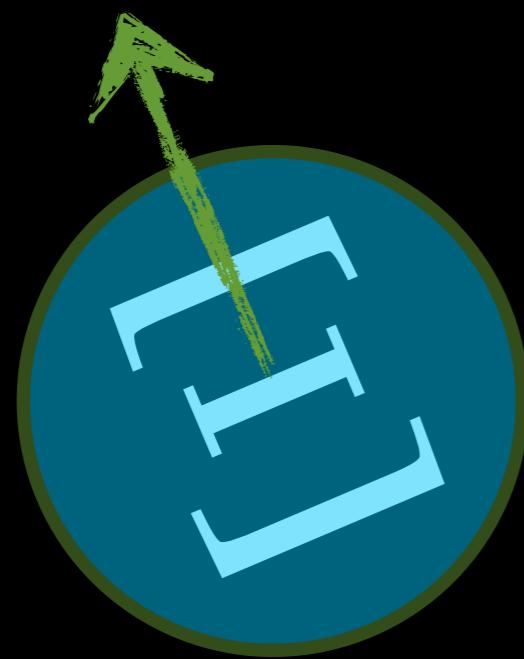
## Step 1: Find dominant orientation of the patch



Rotation Invariant  
Description

**Step 1: Find dominant orientation of the patch**

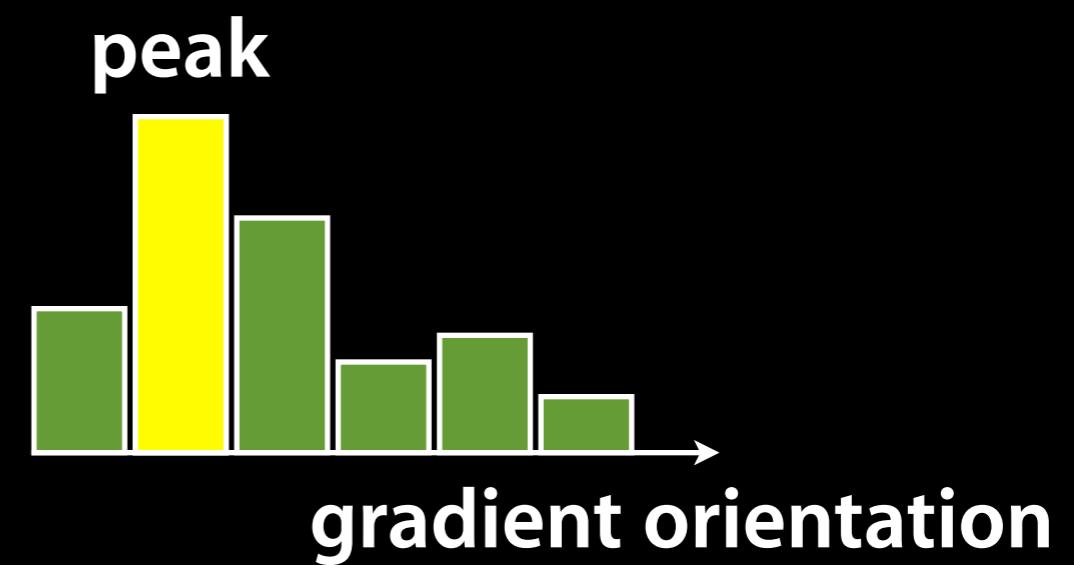
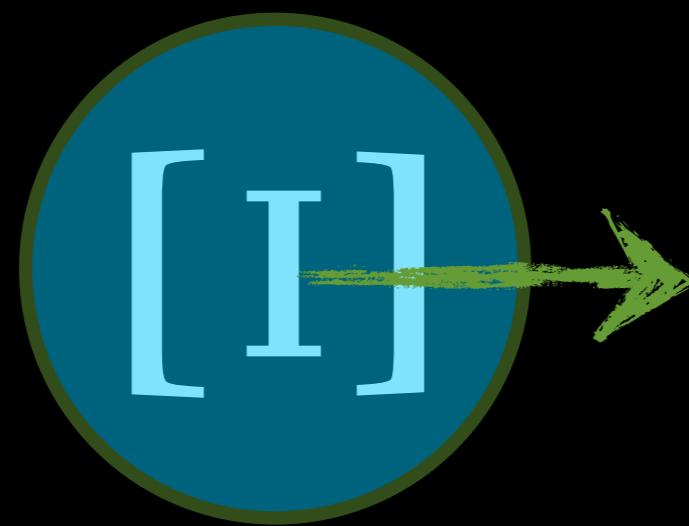
**Step 2: Rotate the patch to point along x-axis**



Rotation Invariant  
Description

Step 1: Find dominant orientation of the patch

Step 2: Rotate the patch to point along x-axis



SIFT  
Descriptor

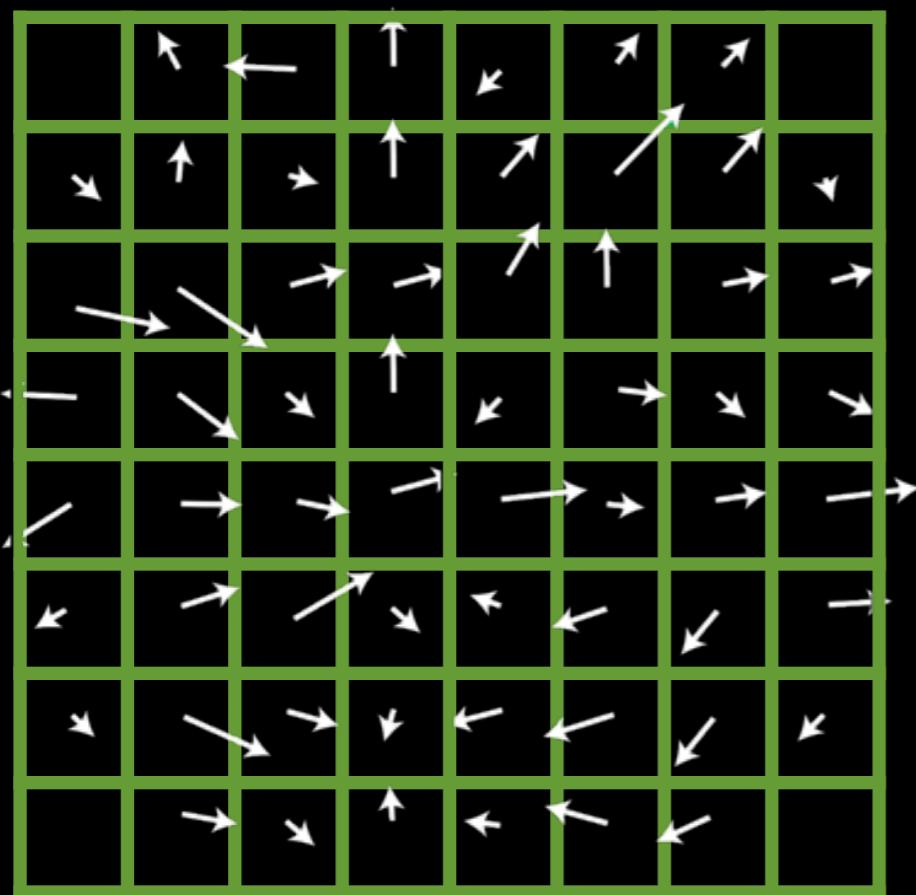


image gradients

SIFT  
Descriptor

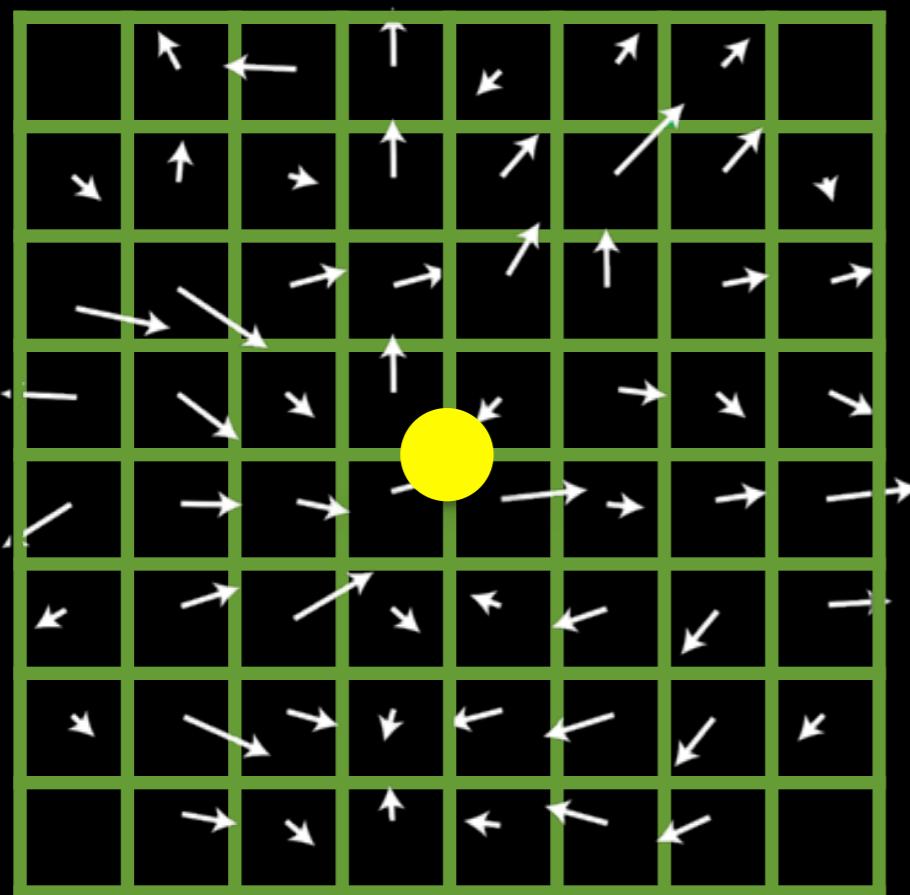


image gradients

SIFT  
Descriptor

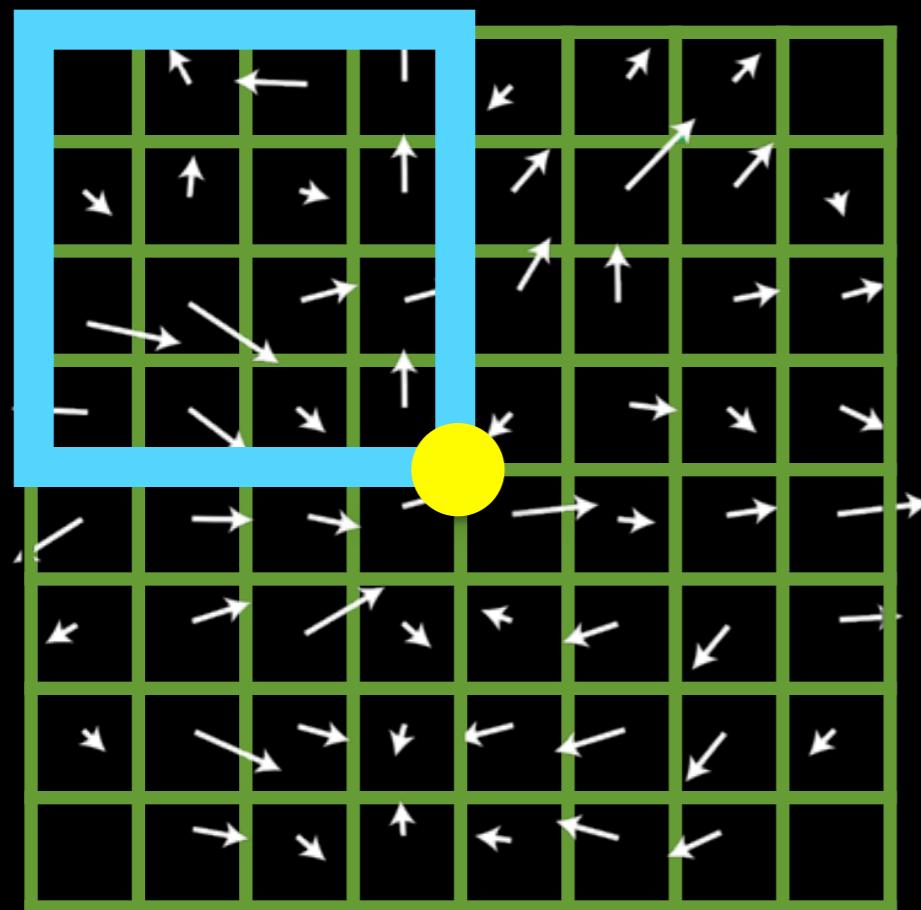


image gradients

# SIFT Descriptor

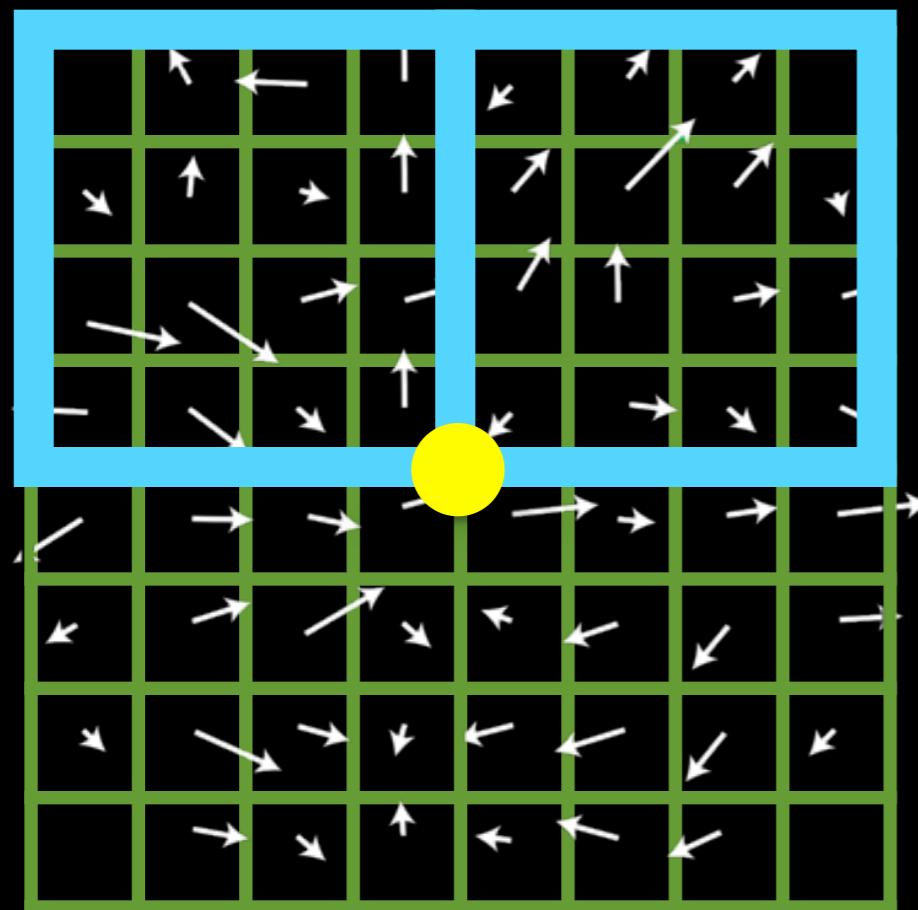


image gradients

SIFT  
Descriptor

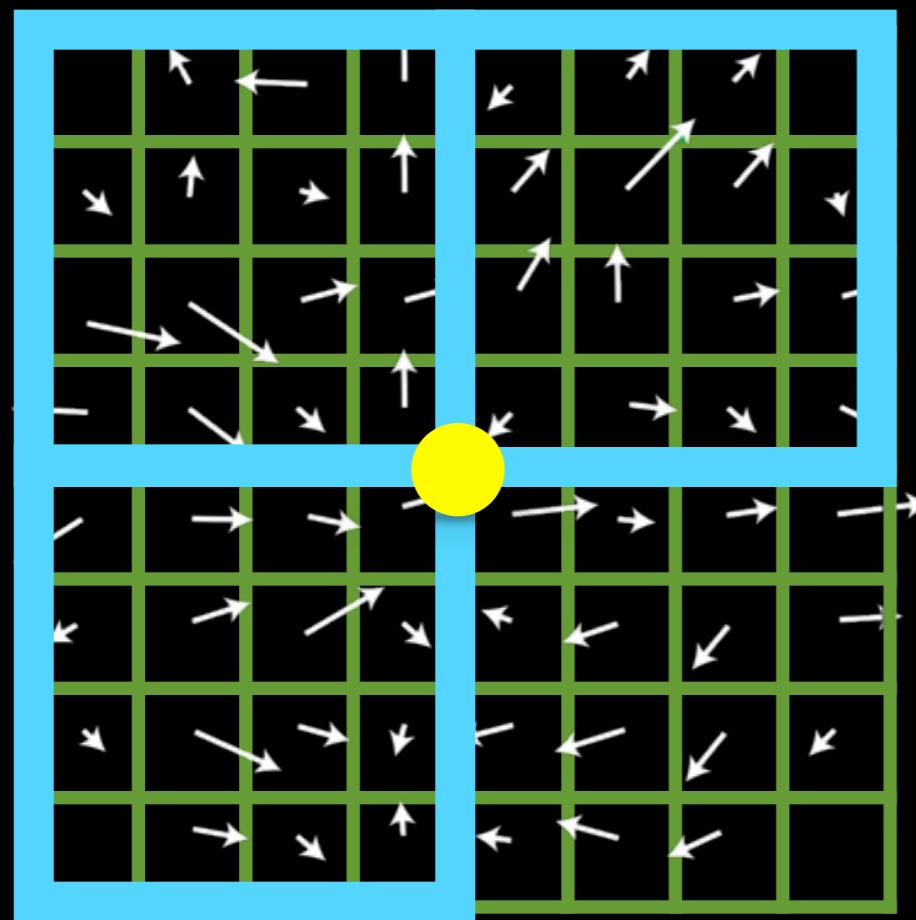


image gradients

SIFT  
Descriptor

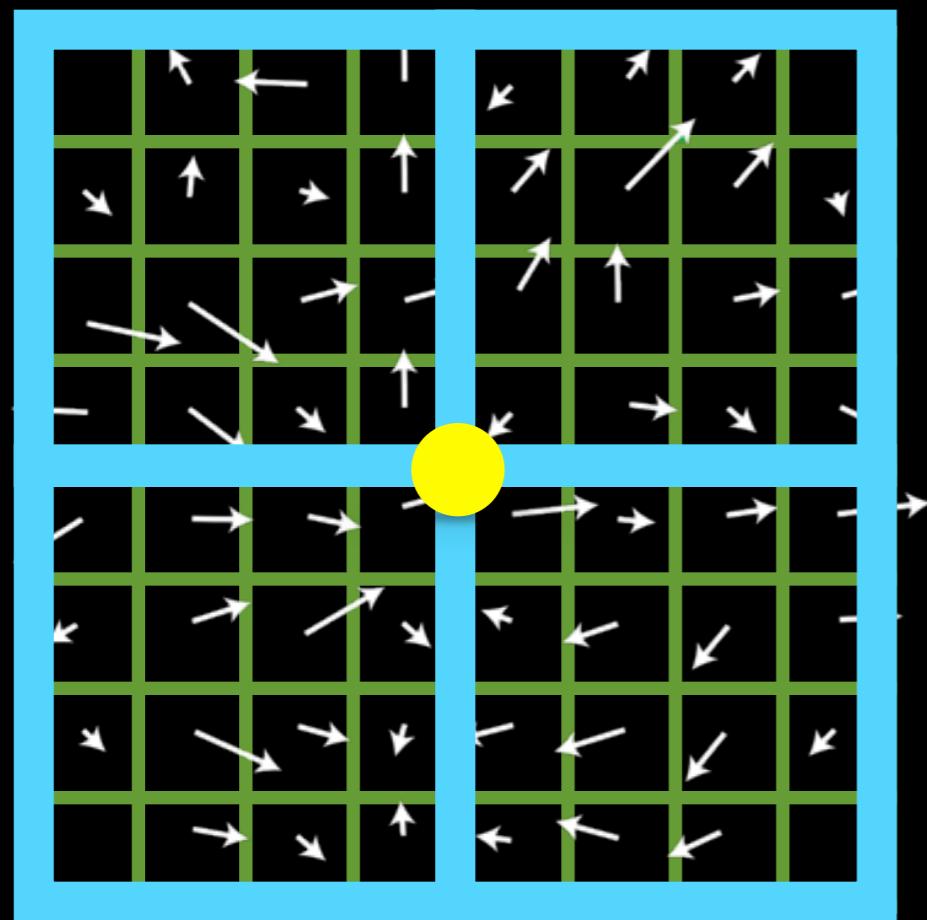


image gradients

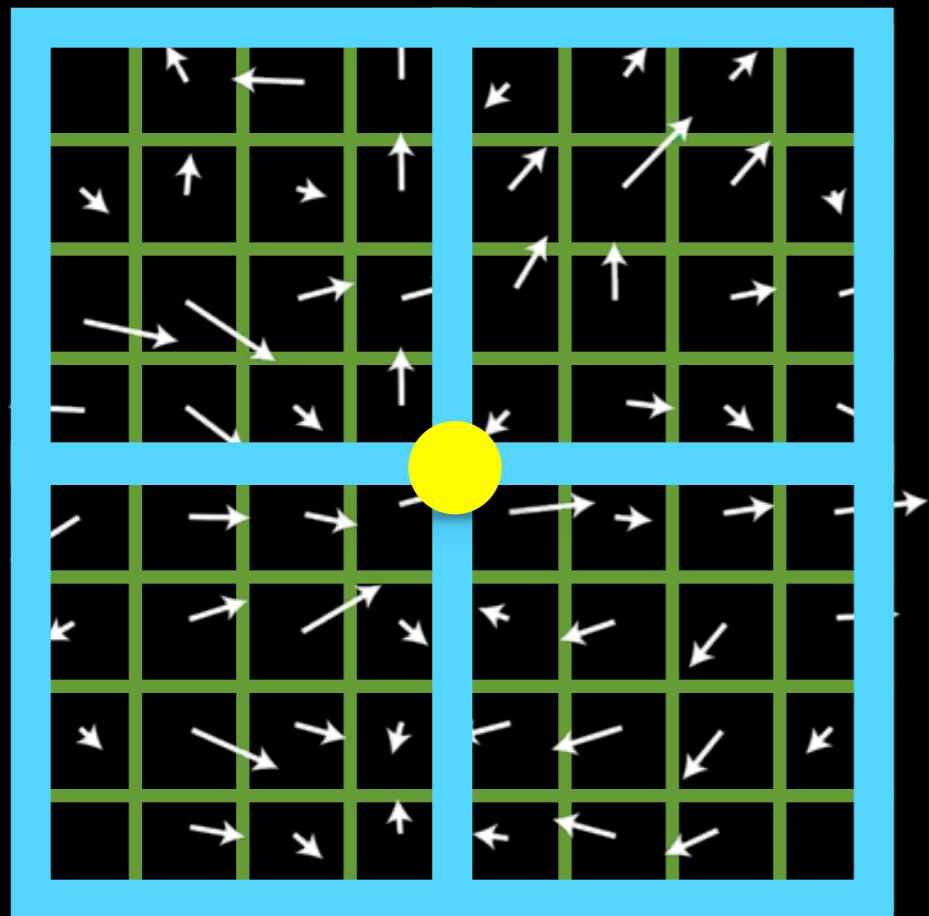
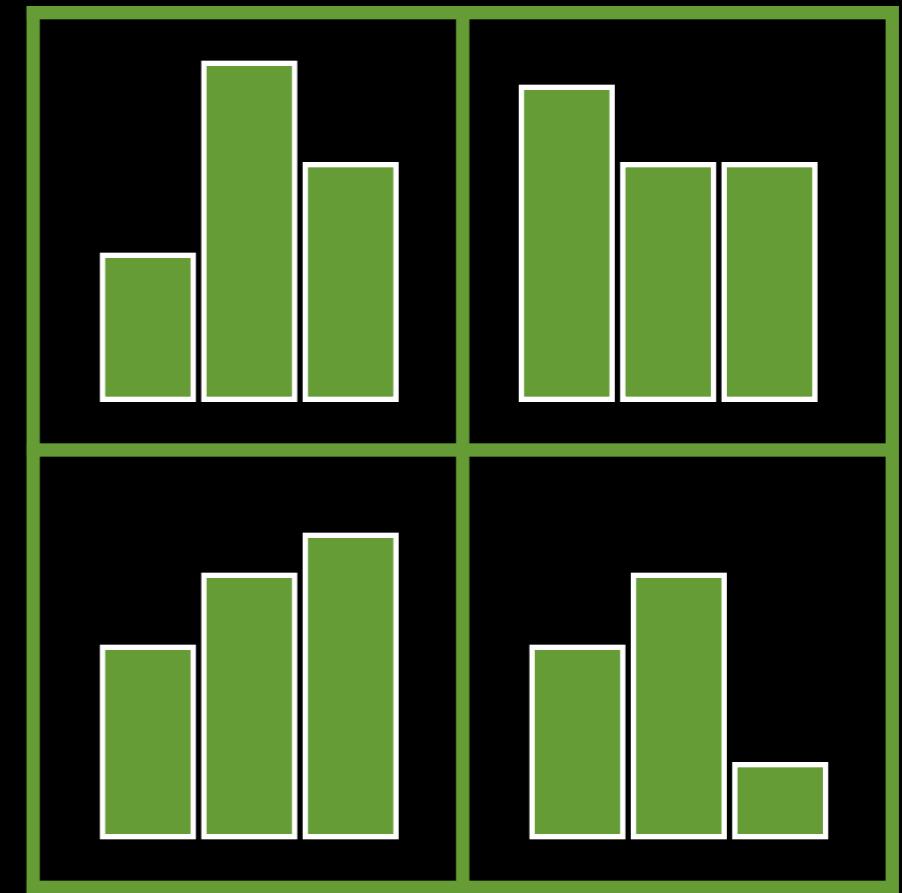


image gradients



keypoint descriptor

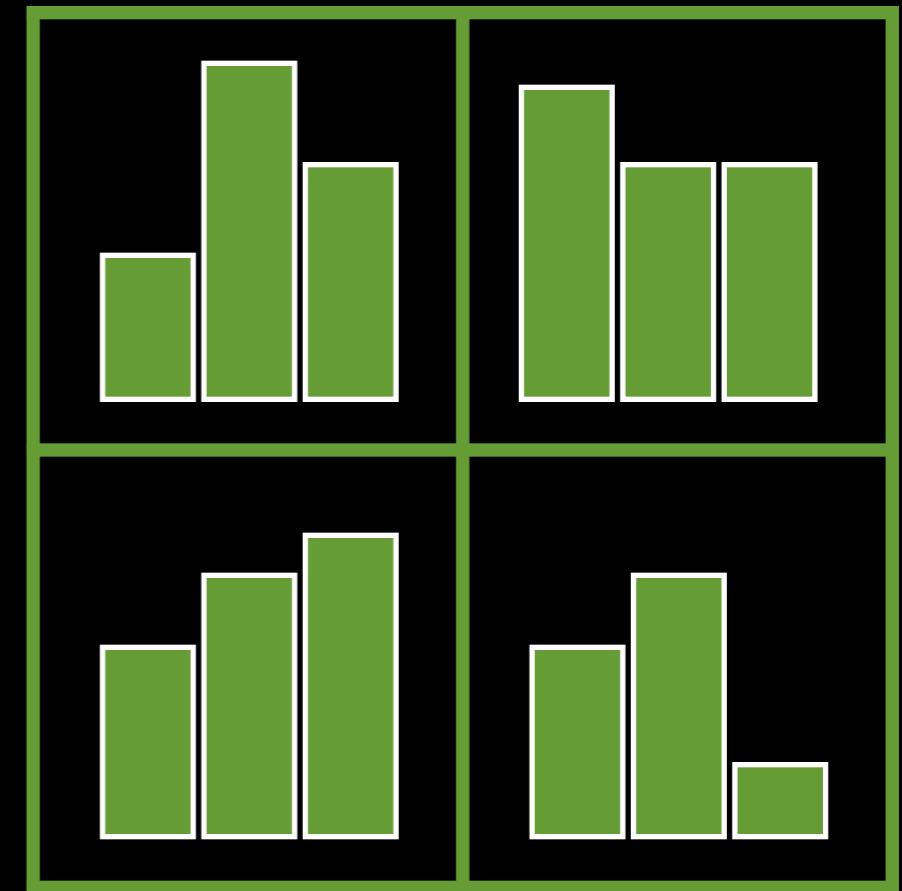
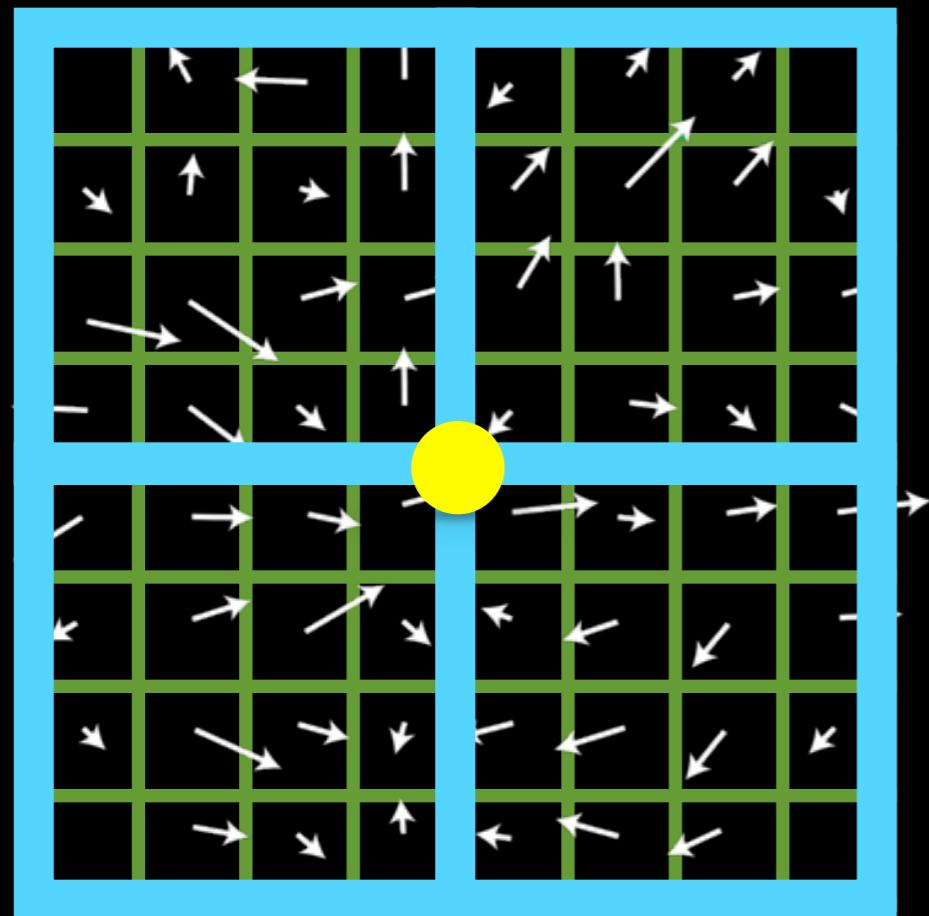


image gradients

keypoint descriptor

16 cells x 8 bins = 128 dimensional descriptor

RYERSON  
UNIVERSITY











SIFT  
Properties

# SIFT Properties

**Robust to image rotation, scale and  
intensity change**

# SIFT Properties

**Robust to image rotation, scale and intensity change**

**Robust to moderate out of plane rotation**

# SIFT Properties

**Robust to image rotation, scale and intensity change**

**Robust to moderate out of plane rotation**

**Fast and efficient**

too long; didn't listen

tidy

SIFT  
tl;dl

SIFT  
tl;dl

# 1. Keypoint detection

SIFT  
tl;dl

## 1. Keypoint detection

Search across image locations and scales for feature response extrema

SIFT  
tl;dl

## 1. Keypoint detection

Search across image locations and scales for feature response extrema

## 2. Keypoint orientation assignment

SIFT  
tl;dl

## 1. Keypoint detection

Search across image locations and scales for feature response extrema

## 2. Keypoint orientation assignment

Determine best orientation(s) for each keypoint

SIFT  
tl;dl

## 1. Keypoint detection

Search across image locations and scales for feature response extrema

## 2. Keypoint orientation assignment

Determine best orientation(s) for each keypoint

## 3. Keypoint description

SIFT  
tl;dl

## 1. Keypoint detection

Search across image locations and scales for feature response extrema

## 2. Keypoint orientation assignment

Determine best orientation(s) for each keypoint

## 3. Keypoint description

Describe keypoint region at selected scale and rotation with image gradients

SIFT  
tl;dl

## 1. Keypoint detection

Search across image locations and scales for feature response extrema

## 2. Keypoint orientation assignment

Determine best orientation(s) for each keypoint

## 3. Keypoint description

Describe keypoint region at selected scale and rotation with image gradients



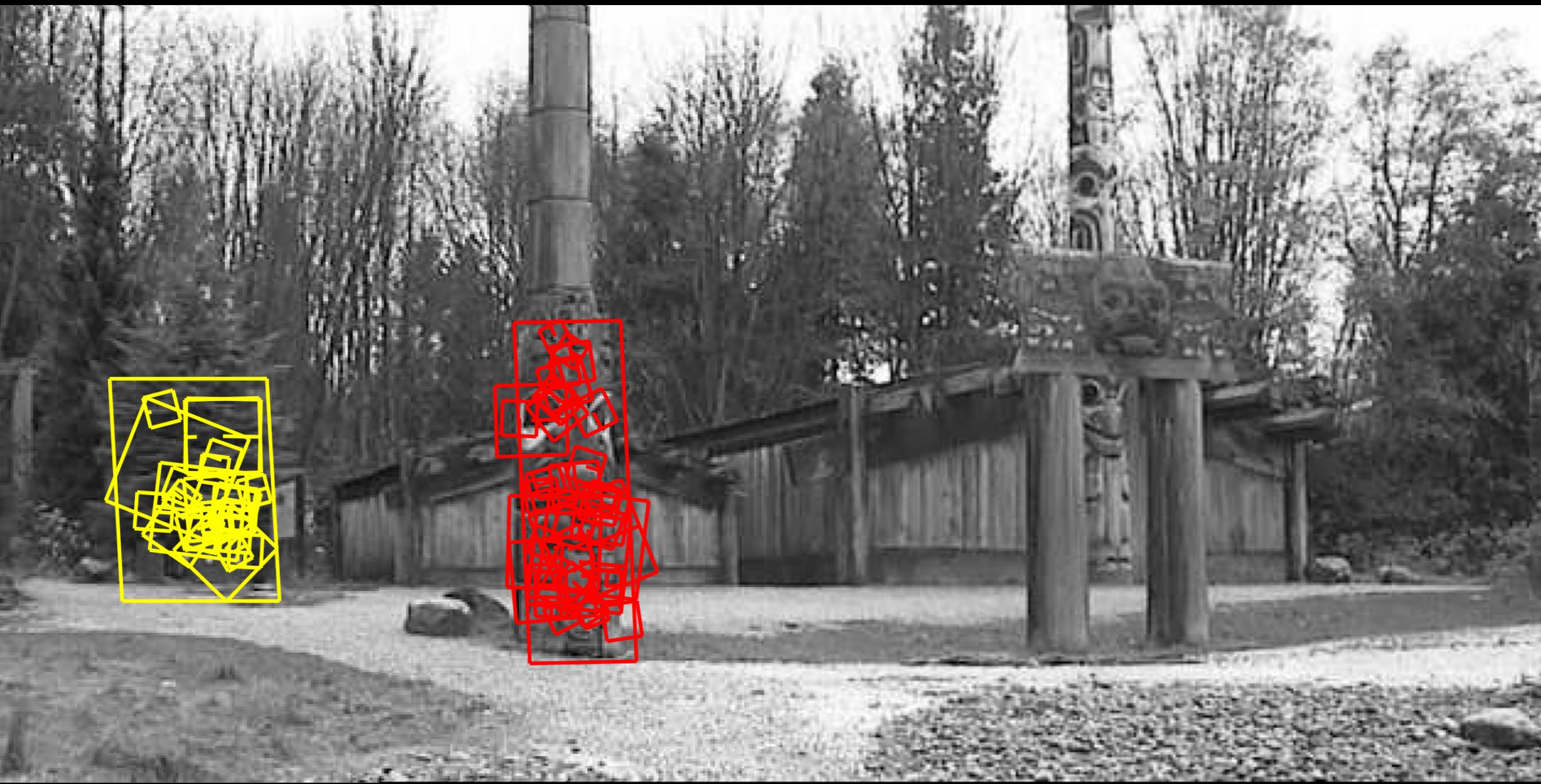


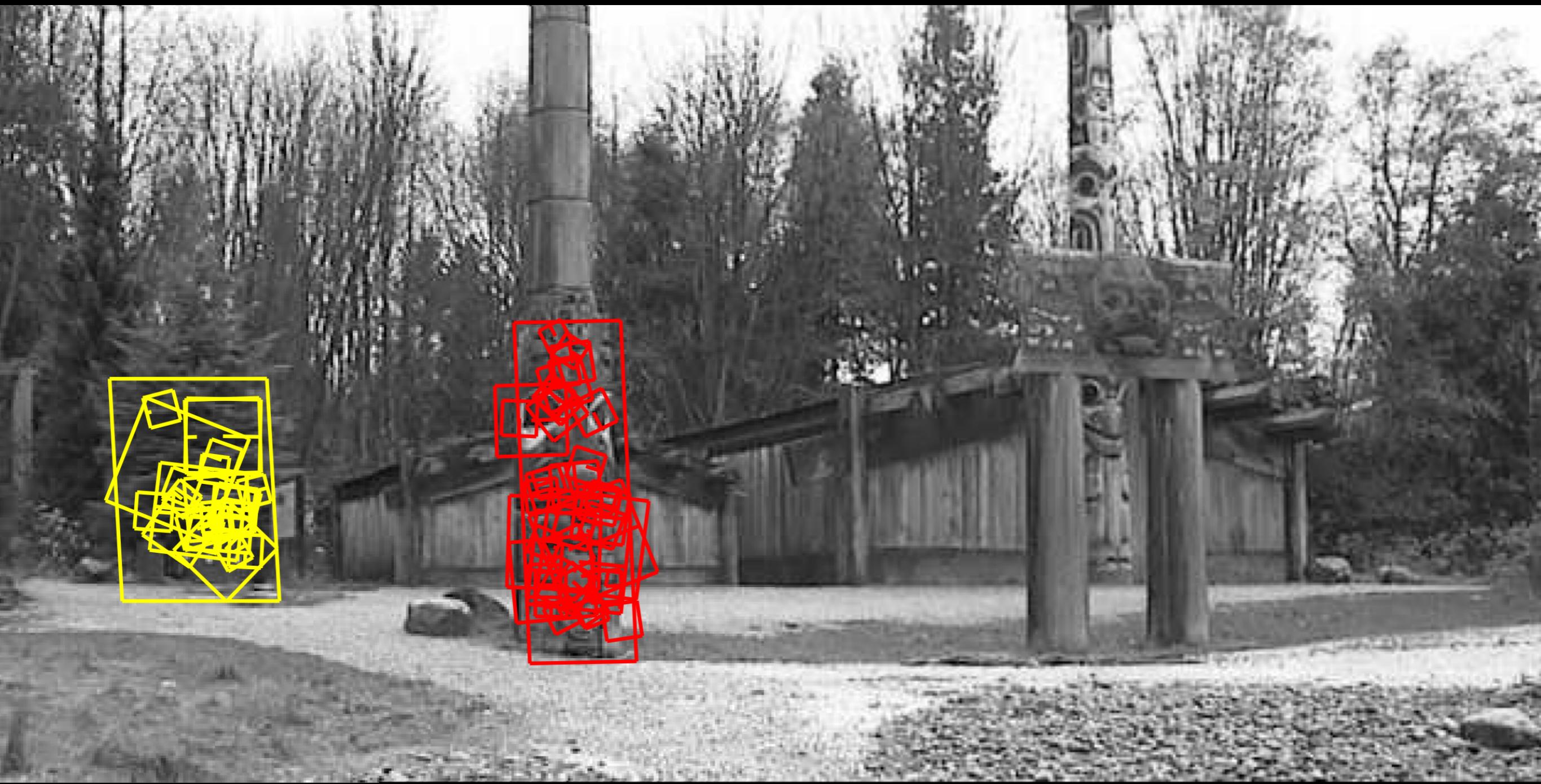
**Challenge: Find the following patches**

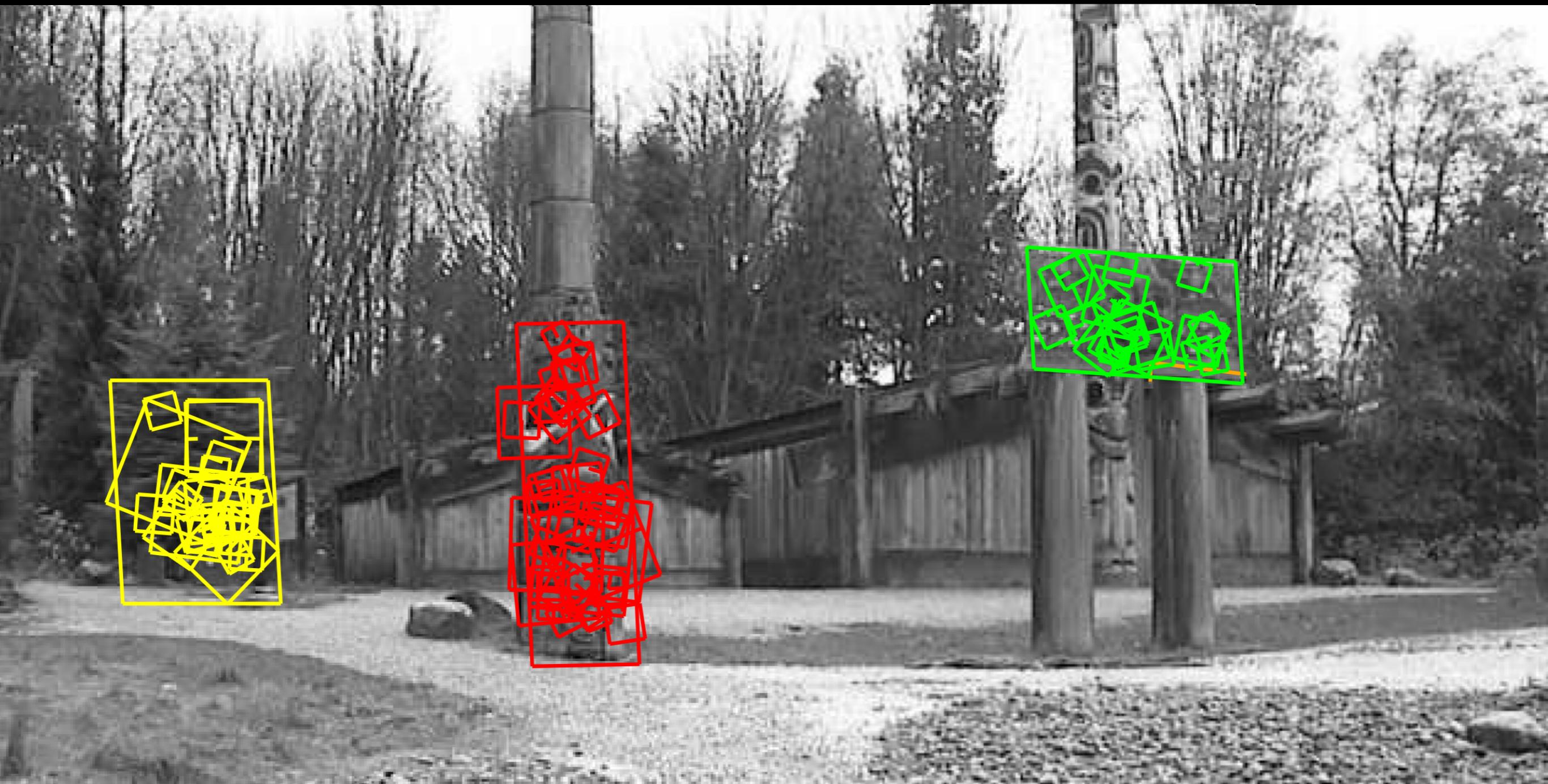


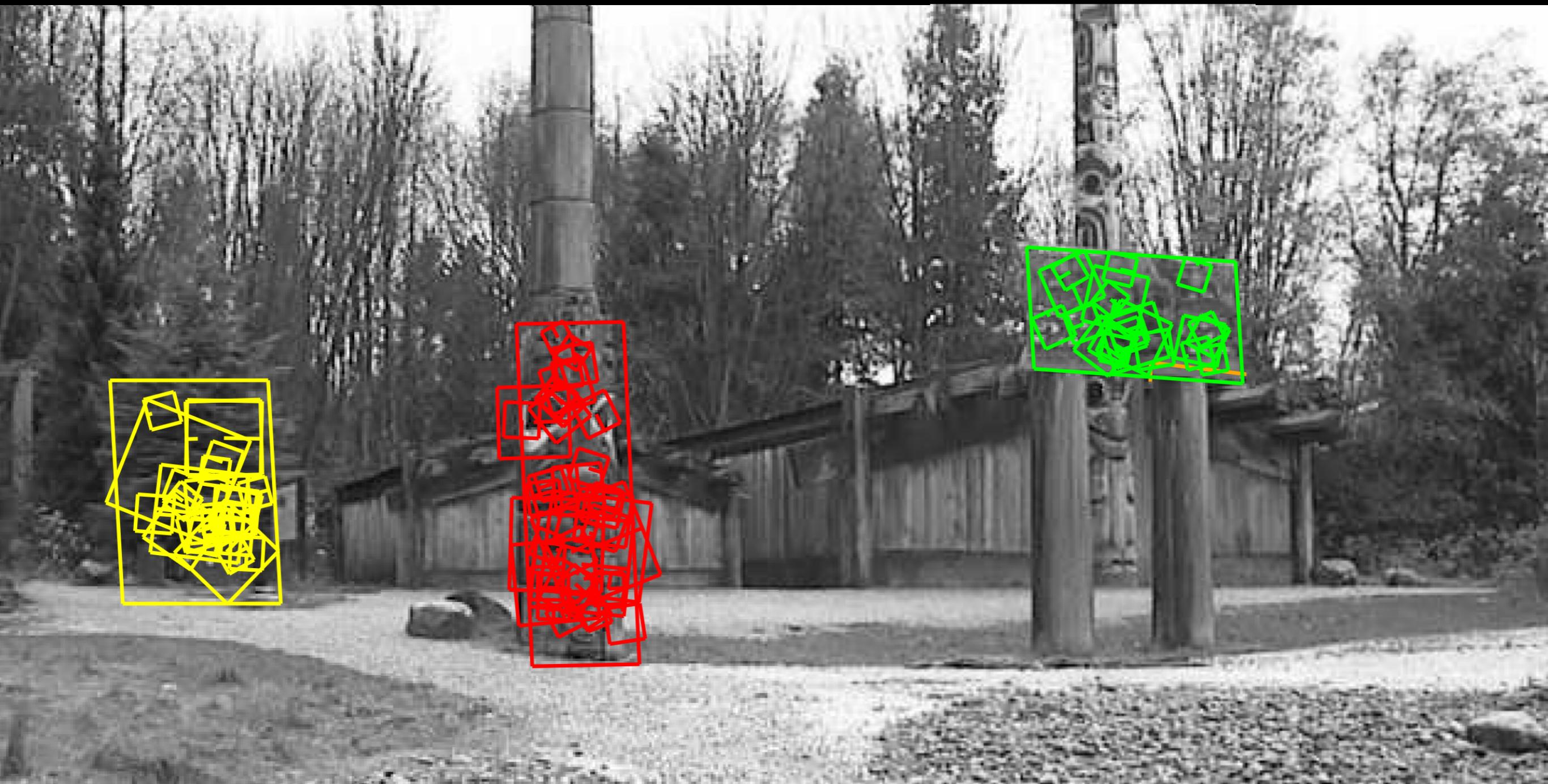


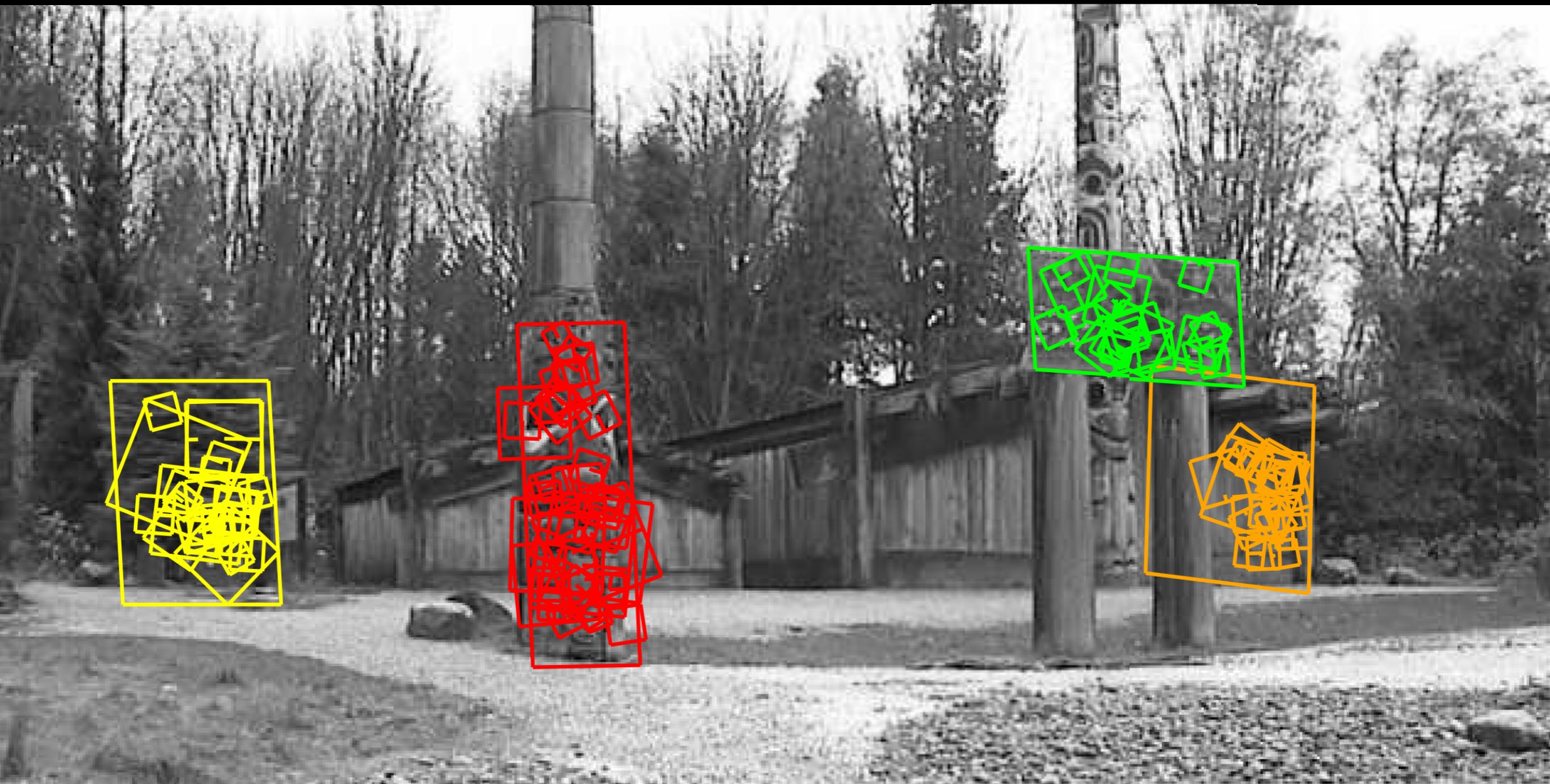














US006711293B1

(12) United States Patent  
Lowe(10) Patent No.: US 6,711,293 B1  
(45) Date of Patent: Mar. 23, 2004(54) METHOD AND APPARATUS FOR  
IDENTIFYING SCALE INVARIANT  
FEATURES IN AN IMAGE AND USE OF  
SAME FOR LOCATING AN OBJECT IN AN  
IMAGE

(75) Inventor: David G. Lowe, Vancouver (CA)

(73) Assignee: The University of British Columbia,  
Vancouver (CA)(\*) Notice: Subject to any disclaimer, the term of this  
patent is extended or adjusted under 35  
U.S.C. 154(b) by 0 days.

(21) Appl. No.: 09/519,893

(22) Filed: Mar. 6, 2000

## Related U.S. Application Data

(60) Provisional application No. 60/123,369, filed on Mar. 8,  
1999.

(51) Int. Cl. .... G06K 9/68

(52) U.S. Cl. .... 382/219, 382/220

(58) Field of Search .... 382/130, 236,  
382/219, 220

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5,617,459 A	4/1997	Makram-Ebeid et al. ....	378/62
5,666,441 A	9/1997	Rao et al. ....	382/203
5,764,802 A	* 6/1998	Simon .....	382/236

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Ballard, D.H., "Generalizing the Hough transform to detect  
arbitrary shapes", Pattern Recognition, 13, 2 (1981), pp.  
111-122.Crowley, James L., and Alice C. Parker, "A representation  
for shape based on peaks and ridges in the difference of  
low-pass transform", IEEE Trans. on Pattern Analysis and  
Machine Intelligence, 6, 2 (1984), pp. 156-170.Schmid, C., and R. Mohr, "Local grayvalue invariants for  
image retrieval", IEEE PAMI, 19, 5 (1997), pp. 530-535.

\* cited by examiner

Primary Examiner—Leo Boudreau

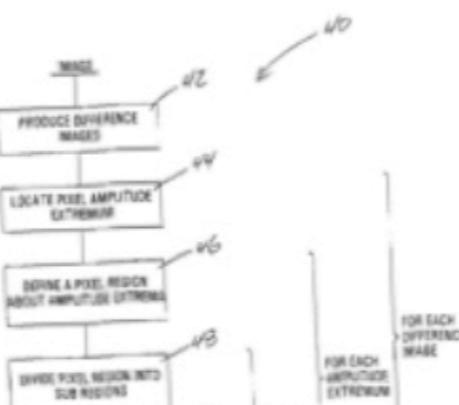
Assistant Examiner—Tom Y. Lu

(74) Attorney, Agent, or Firm—Christie, Parker & Hale,  
LLP

## (57) ABSTRACT

A method and apparatus for identifying scale invariant features in an image and a further method and apparatus for using such scale invariant features to locate an object in an image are disclosed. The method and apparatus for identifying scale invariant features may involve the use of a processor circuit for producing a plurality of component subregion descriptors for each subregion of a pixel region about pixel amplitude extrema in a plurality of difference images produced from the image. This may involve producing a plurality of difference images by blurring an initial image to produce a blurred image and by subtracting the blurred image from the initial image to produce the difference image. For each difference image, pixel amplitude extrema are located and a corresponding pixel region is defined about each pixel amplitude extremum. Each pixel region is divided into subregions and a plurality of component subregion descriptors are produced for each subregion. These component subregion descriptors are correlated with component subregion descriptors of an image under consideration and an object is indicated as being detected when a sufficient number of component subregion descriptors (scale invariant features) define an aggregate correlation exceeding a threshold correlation with component subregion descriptors (scale invariant features) associated with the object.

20 Claims, 12 Drawing Sheets





US006711293B1

(12) United States Patent  
Lowe(10) Patent No.: US 6,711,293 B1  
(45) Date of Patent: Mar. 23, 2004(54) METHOD AND APPARATUS FOR  
IDENTIFYING SCALE INVARIANT  
FEATURES IN AN IMAGE AND USE OF  
SAME FOR LOCATING AN OBJECT IN AN  
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(75) Inventor: David G. Lowe, Vancouver (CA)

(73) Assignee: The University of British Columbia,  
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(58) Field of Search .... 382/130, 236,  
382/219, 220

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5,617,459 A	4/1997	Makram-Ebeid et al. ....	378/62
5,666,441 A	9/1997	Rao et al. ....	382/203
5,764,802 A	* 6/1998	Simon .....	382/236

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Primary Examiner—Leo Boudreau

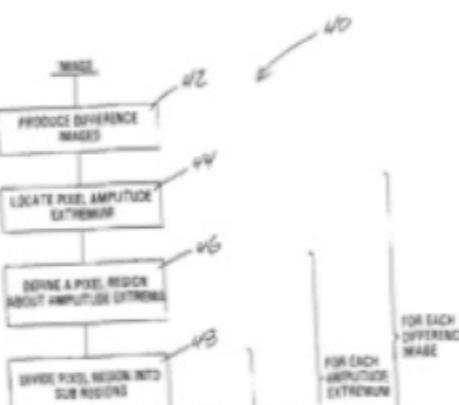
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20 Claims, 12 Drawing Sheets



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SIFT implementation

# VLFeat.org

SIFT implementation  
and much more

