Cut Sets

A set of edges whose removal results in a disconnected graph, provided that no sub-set of the set also results in a disconnected graph.

A cut set reduces the rank of a graph by one.

Rank R = N - k

Nullity $\mu = E - N + k$

Application: Finding weak spots in communication networks & strengthening roads and communication networks

<u>Theorem:</u> Every cut-set in a connected graph G must contain at least 1 branch of every spanning tree of G

<u>Theorem:</u> Every circuit has an even number of edges common with any cut-set.

Fundamental Cut Set

A cut set that contains one and only one branch of a spanning tree of graph G.

<u>Theorem:</u> A chord that creates a fundamental circuit α occurs in every fundamental cut set associated with the branches of α .

Edge Connectivity: The number of edges in smallest cut-set

Vertex Connectivity: Minimum number of vertices whose removal disconnects a graph

<u>Cut Vertex</u>: The vertex whose removal results in a disconnected graph

<u>Theorem:</u> A vertex v3 is a cut vertex if and only if there exists two vertices v1 and v2 such that every path between v1 and v2 passes through v3.

<u>Theorem:</u> Edge connectivity of a graph G cannot be more than a vertex in G having minimum degree.

Theorem: Vertex connectivity of a graph G cannot be more than the edge connectivity.

Theorem: Maximum vertex connectivity in a graph G is the integer part of relation 2e/n

Vertex connectivity <= Edge connectivity <= 2e/n

K-Isomorphism --- Related Examples