

Lecture 18:-

Regular language.

→ Regex.

Properties:-

→ Closure.

→ Complement.

→ Intersection.

How to Compute Intersection.

L_1 & L_2 be two languages.

$$L_1 \cap L_2 = (L_1' \cup L_2')'$$

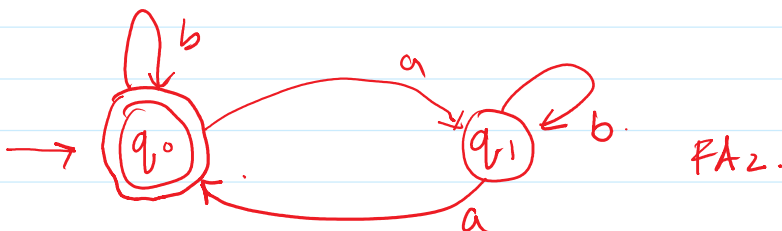
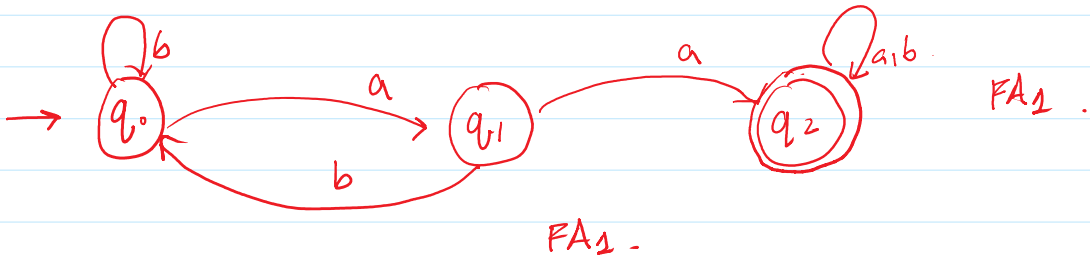
$$= (L_1' + L_2')'$$

$$(A \cap B)' = A' \cup B'$$

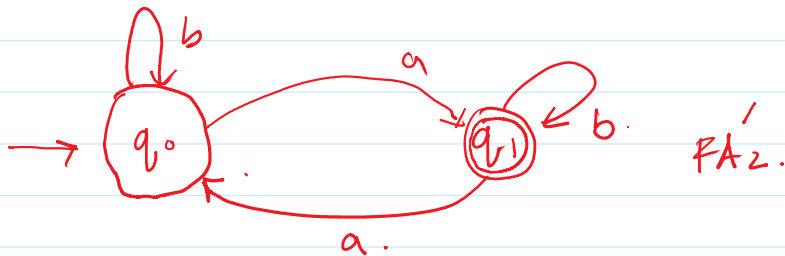
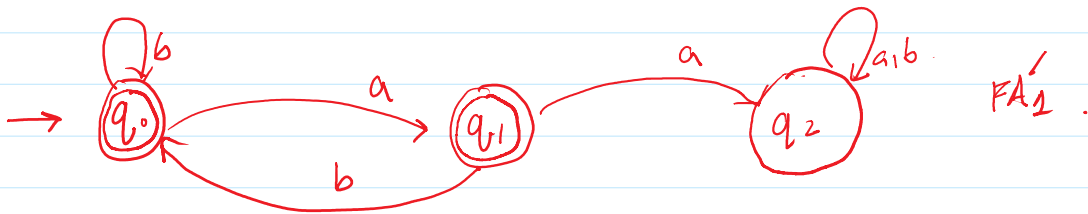
$$((A \cap B)')' = (A' \cup B')'$$

$$\underline{A \cap B} = \underline{(A' \cup B')}'$$

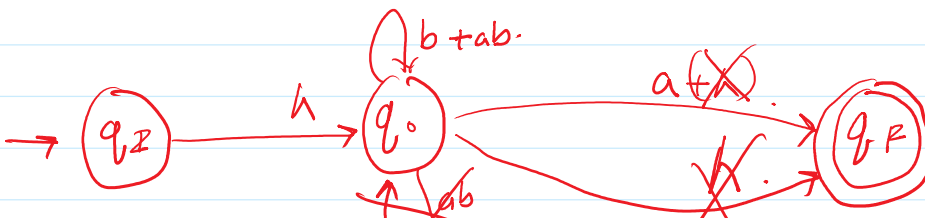
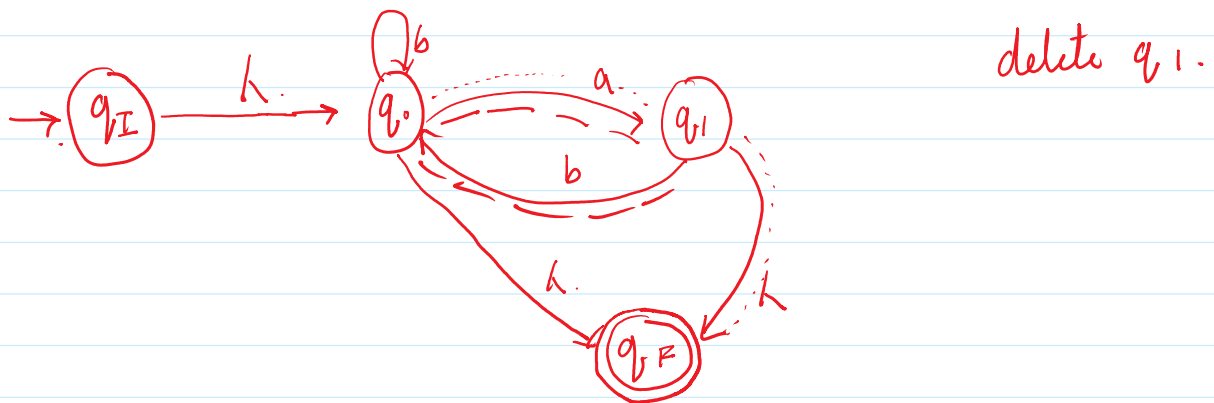
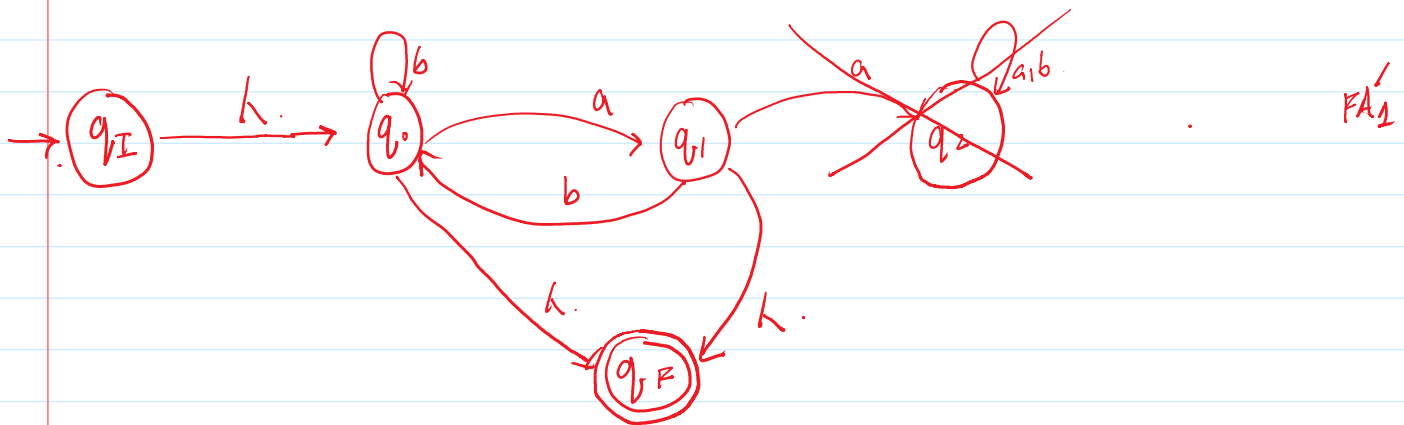
Ex:- $L_1 \rightarrow \gamma_1 = (a+tb)^* aa (a+tb)^*$
 $L_2 \rightarrow \gamma_2 = b^+ (ab^+ab^+)^*$

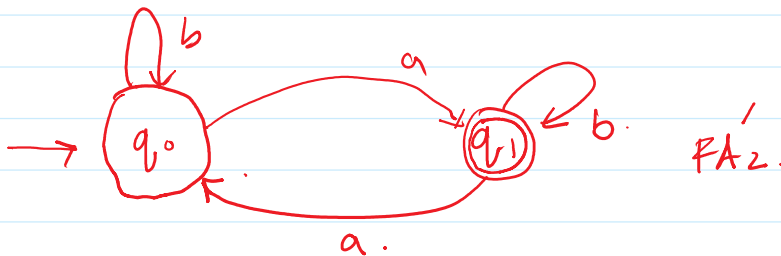
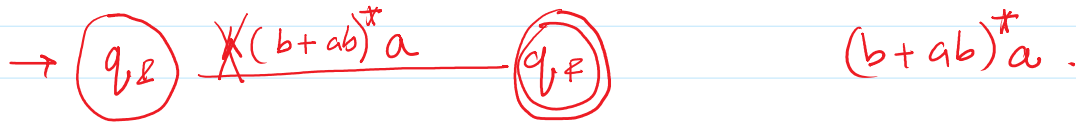
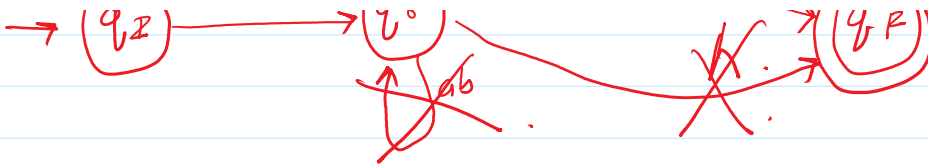


Complement Computation.



Computing Regexes of the Complemented Automata's.





FA2.

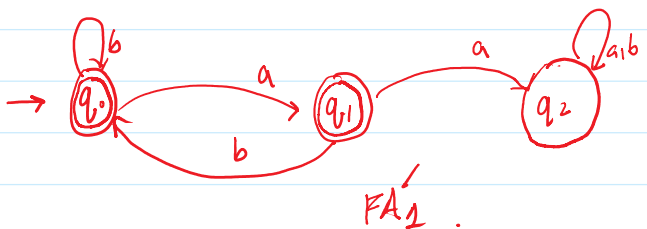
Activity -
Regex = $(b+ab^*a)^*ab^*$

Confirm this HW.

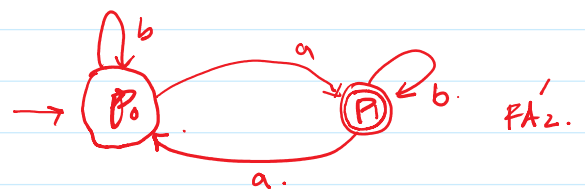
$$L_1' + L_2'$$

$$= (b+ab)^*a + (b+ab^*a)^*ab^*$$

How to Complement this.



FA1.



FA2.

old state

$$z_1^+ \equiv (q_0, p_0)$$

$$z_2^+ \equiv (q_1, p_1)$$

$$z_3^+ \equiv (q_2, p_0)$$

$$z_4^+ \equiv (q_0, p_1)$$

$$z_5^+ \equiv (q_2, p_1)$$

$$z_6^+ \equiv (q_1, p_0)$$

Transition at "a"

$$z_2^+ \equiv (q_1, p_1)$$

$$z_3^+ \equiv (q_2, p_0)$$

$$z_5^+ \equiv (q_2, p_1)$$

$$z_6^+ \equiv (q_1, p_0)$$

$$z_3^+ \equiv (q_2, p_0)$$

$$z_5^+ \equiv (q_2, p_1)$$

Transition at "b"

$$z_1^+ \equiv (q_0, p_0)$$

$$z_4^+ \equiv (q_0, p_1)$$

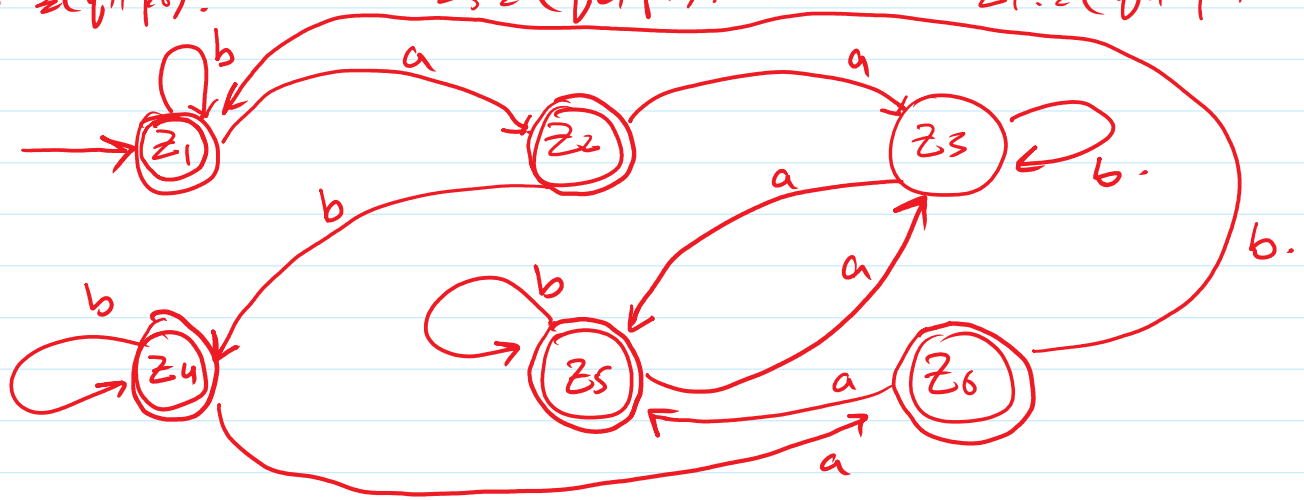
$$z_3^+ \equiv (q_2, p_0)$$

$$z_4^+ \equiv (q_0, p_1)$$

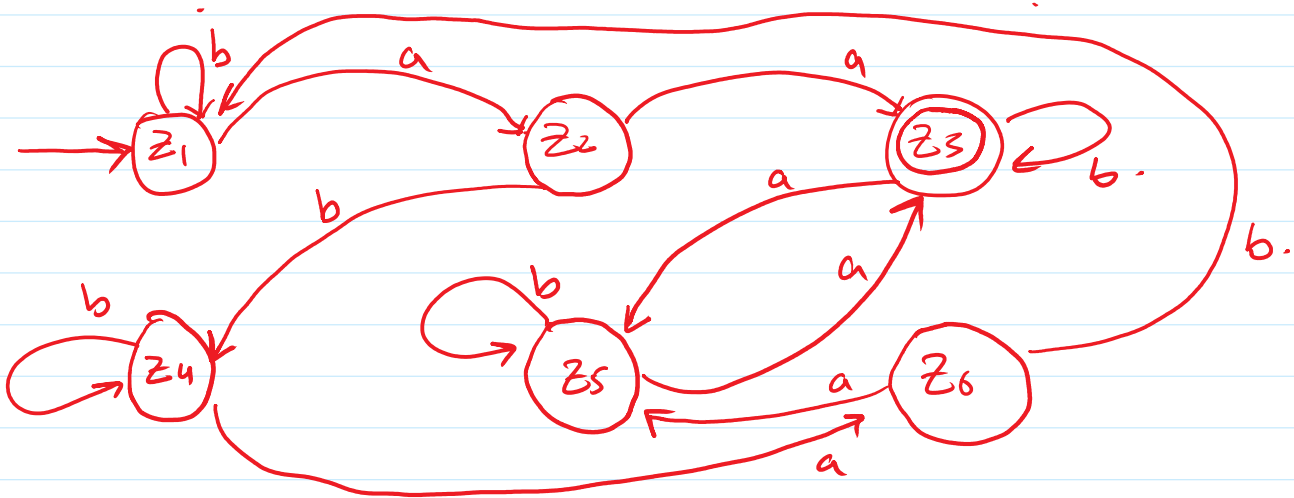
$$z_5^+ \equiv (q_2, p_1)$$

$$z_1^+ \equiv (q_0, p_0)$$





Taking Complement Again.



Compute Regx Again.

- Step 1 :- Make PA_1' & PA_2' .
- Step 2 :- $PA_1' + PA_2'$ Using Transition Tables.
- Step 3 :- Make $(PA_1' + PA_2') \equiv PA_3'$ Construct Using TT .
- Step 4 :- Find PA_3' .
- Step 5 :- Find Regx Against PA_3' .

Non-REGULAR:-

- No Regex.

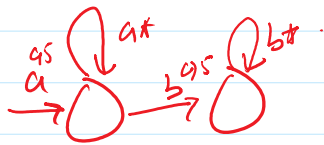
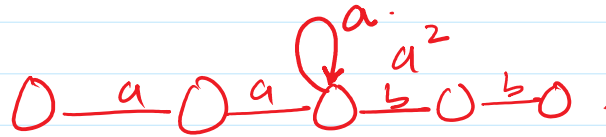
Ex:- $L = \{a^n b^n, n = 0, 1, \dots\}$.

$a^* b^*$. X .

a^{22} .

$a^{100} b^{200}$.

FA:-



$a^{95} a^{(m)} b^{95}$

7 .

$a \geq 95$.

$a^{95+7+7+7+7+7+7} b^{95}$.

$* =$

$a^n b^n$.

$a^{95} (a^7)^m b^{95} (b^7)^m$

$m = 0, 1, \dots$

$a^* b^*$:

