

1) Longest diagonal in a cube is known as Body diagonal

2) In a right cylinder Base is perpendicular to Height

3) Side of a cube is 6cm, find , (I) surface area ,(ii) volume ,(iii) face diagonal and (iv) body diagonal ?

Solution:

Given: Side of the cube = 6 cm.

$$\text{Side}^2 = 6 \times 6 = 36$$

$$\begin{aligned}\text{Surface area} &= 6 \text{ side}^2 \text{ Sqr unit.} \\ &= 6 \times 36 \\ &= 216 \text{ cm}^2\end{aligned}$$

$$\text{Volume} = \text{Side}^3 = 6 \times 6 \times 6 = 216 \text{ cm}^3$$

$$\begin{aligned}\text{Face diagonal} &= \sqrt{2} \text{ side} \\ &= 6\sqrt{2} \text{ cm}\end{aligned}$$

$$\begin{aligned}\text{Body diagonal} &= \sqrt{3} \text{ side} \\ &= 6\sqrt{3} \text{ cm}\end{aligned}$$

4) The volume of a sphere is equal to its surface area. What is its radius?

Solution:

Given: Volume of a sphere is equal to its surface area.

To find: radius of the sphere.

$$\text{Volume of the sphere} = \frac{4}{3} \pi r^3 \text{ cubic unit.}$$

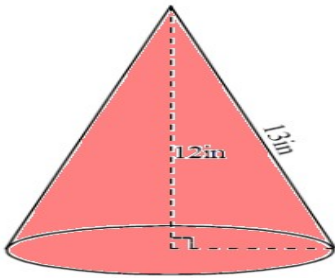
$$\text{Surface area} = 4 \pi r^2 \text{ square unit.}$$

$$\frac{4}{3} \pi r^3 = 4 \pi r^2$$

$$r = 3 \text{ units.}$$

Radius of the sphere = 3 units.

5)



Find the volume of the cone?

Solution:

Given:

Slant height of the cone $l = 13$ inches.

Height of the cone $h = 12$ inches.

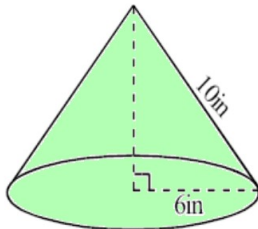
Volume of the cone $V = \frac{1}{3}\pi r^2 h \text{ inch}^2$

$$\text{radius } r = \sqrt{13^2 - 12^2} = 5 \text{ inches}$$

$$\text{Volume of the cone } V = \frac{1}{3}\pi 5^2(12) \text{ inch}^2$$

$$\text{Volume of the cone } V = 100\pi \text{ inch}^3$$

6)



Find the height of the cone ?

Solution:

This is a right circular cone.

Given:

Slant height = 10 inches.

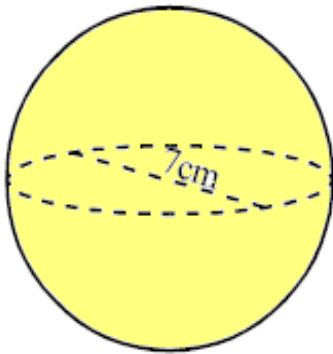
Radius = 6 inches.

$$\text{Height of the cone} = \sqrt{(\text{slant height})^2 - (\text{radius})^2}$$

$$= \sqrt{10^2 - 6^2} = 8 \text{ inches.}$$

Height of the cone = 8 inches.

7)



Find the volume of the sphere and its surface area ?

Solution:

Given:

Diameter of the sphere = 7 cm.

Radius of the sphere = $7/2$ cm.

$$\text{Volume of the sphere} = \frac{4}{3} \pi r^3 \text{ cm}^3 \text{ where, } \pi = \frac{22}{7}$$

$$= \frac{4}{3} \times \frac{22}{7} \times \left(\frac{7}{2}\right)^3 \text{ cm}^3 = \frac{539}{3}$$

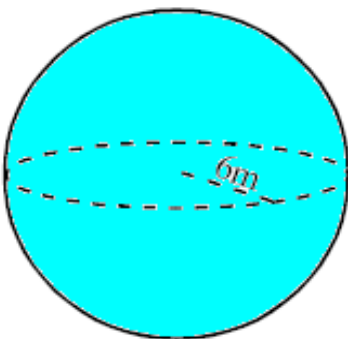
$$\text{Volume of the sphere} = \frac{539}{3} \text{ cm}^3$$

$$\text{Surface area} = 4 \pi r^2 \text{ cm}^2$$

$$= 4 \times \frac{22}{7} \times \left(\frac{7}{2}\right)^2 \text{ cm}^2 = 154 \text{ cm}^2$$

$$\text{Surface area of the sphere} = 154 \text{ cm}^2$$

8)



Find the volume of the sphere and its surface area ?

Given:

Radius of the sphere = 6 m.

$$\text{Volume of the sphere} = \frac{4}{3} \pi r^3 \text{ m}^3 \quad \text{where, } \pi = \frac{22}{7}$$

$$= \frac{4}{3} \times \pi \times 6^3 \text{ m}^3 = 288 \pi \text{ m}^3$$

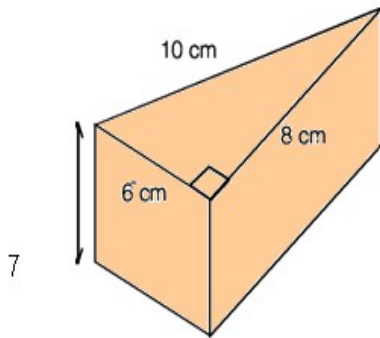
$$\text{Volume of the sphere} = 288 \pi \text{ m}^3$$

$$\text{Surface area} = 4 \pi r^2 \text{ m}^2$$

$$= 4 \times \pi \times 6^2 \text{ m}^2 = 144 \pi \text{ m}^2$$

$$\text{Surface area of the sphere} = 144 \pi \text{ m}^2$$

9)



Find the volume and surface area ?

Solution:

In the given figure, triangular prism.

Base of the triangle = 6 cm.

Height of the triangle = 8 cm.

Hypotenuse of the triangle = 10 cm.

Distance between two triangles = 7 cm

Volume of the prism = area of the triangle x distance between two triangles

$$\begin{aligned} \text{Area of the triangle} &= \text{base} \times \text{height} / 2 \\ &= 6 \times 8 / 2 = 24 \text{ cm}^2 \end{aligned}$$

$$\text{Volume of the prism} = 24 \times 7 = 168 \text{ cm}^3$$

Surface area = 2 x area of triangle + area of the base rectangle + area of side rectangles

$$\begin{aligned} &= 2 \times 24 + 7 \times 6 + 8 \times 7 + 10 \times 7 \\ &= 48 + 42 + 56 + 70 = 216 \text{ cm}^2 \end{aligned}$$

$$\text{Surface area of the given prism} = 216 \text{ cm}^2$$

10)

A sphere has a surface area of $36\pi \text{ cm}^2$. What is its volume?

Solution:

Given: Surface area of sphere = $36\pi \text{ cm}^2$
 Surface area of a sphere = $4\pi r^2 \text{ cm}^2$

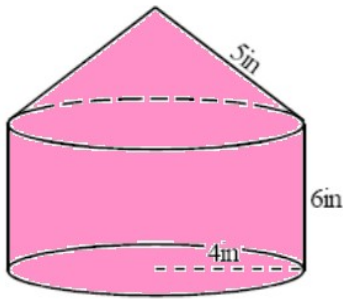
$$4\pi r^2 = 36\pi$$

$$r = 3 \text{ cm.}$$

$$\begin{aligned}\text{Volume of the sphere} &= \frac{4}{3}\pi r^3 \text{ cm}^3 \\ &= \frac{4}{3}\pi 3^3 \text{ cm}^3 = 36\pi \text{ cm}^3\end{aligned}$$

$$\text{Volume of the sphere} = 36\pi \text{ cm}^3$$

11)



Find the volume of the given figure.

Solution:

In the given figure, a cone of radius 4 in and slant height 5 has been stacked on the cylinder of height 6 inches and radius 4 inches.

To find the volume of the figure.

Volume of the figure = Volume of the cylinder + volume of the cone.

Slant height of the cone $l = 5$ inches.

Radius of the cone $r = 4$ inches.

$$\text{Volume of the cone} \quad V = \frac{1}{3}\pi r^2 h \text{ inch}^2$$

$$\text{Height } h = \sqrt{5^2 - 4^2} = 3 \text{ inches}$$

$$\text{Volume of the cone} \quad V = \frac{1}{3}\pi 4^2(3)$$

$$\text{Volume of the cone} \quad V = 16\pi \text{ inch}^3$$

$$\text{Volume of the cylinder} = \pi r^2 h \text{ inch}^3$$

Height of the cylinder $h = 6$ inches.

Radius of the cylinder $r = 4$ inches.

$$\text{Volume of the cylinder} = \pi 4^2 \times 6 = 96 \pi \text{ inch}^3$$

$$\text{Volume of the given figure} = 16 \pi + 96 \pi = 112 \pi \text{ inch}^3$$

$$\text{Volume of the given figure} = 112 \pi \text{ inch}^3$$

12)

A cone of height 24 cm and radius of base 6 cm is made up of modeling clay. A child reshapes it in the form of a sphere. Find the radius of the sphere.

Solution:

Given:

Height of the cone = 24 cm.

Radius of the cone = 6 cm.

Since no clay is left when it is reshaped, volume of the cone will be equal to the volume of the sphere.

That is,

$$\frac{1}{3} \pi r^2 h = \frac{4}{3} \pi r_1^3, \text{ where } r_1 \text{ is the radius of the sphere.}$$

$$6^2 24 = 4 r_1^3$$

$$r_1^3 = 6^3$$

$$r_1 = 6 \text{ cm.}$$

Radius of the sphere = 6 cm.