

## Ratios and Proportions

1) If in your class, there are 34 girls and 43 boys, then express the ratio between boys and girls ?

Solution:

Given:

Number of boys = 43

Number of girls = 34

Ratio of number of boys to girls = 43 : 34

2) What value of n will make this a proportion ,  $6 / 15 = n / 25$ ?

Given:

$$6 / 15 = n / 25$$

$$n = 25 \times 6 / 15 = 10$$

The value of n = 10 makes  $6 / 15 = n / 25$  as proportion.

3) Column A

2 inches to 4 inches

Column B

2 foot to 72 inches

Which is greater?

Solution:

$$2 \text{ inches to } 4 \text{ inches} = 2 / 4 = \frac{1}{2}$$

$$1 \text{ foot} = 12 \text{ inches}$$

$$2 \text{ foot} = 24 \text{ inches}$$

$$2 \text{ foot to } 72 \text{ inches} = 24 / 72 \\ = 1/3$$

Column A is greater than Column B.

4) A score of 72 points was shared by 3 players in a basket ball team in the proportion 2:3:4. How many more points did the highest scorer score compared to the lowest scorer?

Solution:

3 players share 72 points in the ratio 2:3:4.

That is, their points are 2k, 3k, and 4k, where k is a constant.

Total points is  $2k + 3k + 4k = 9k$ .

$$9k = 72 \implies k = 8$$

Points of the highest scorer =  $4(8) = 32$  points.

Points of the lowest scorer =  $2(8) = 16$  points.

Difference between the highest scorer and lowest scorer =  $32 - 16 = 16$  points.

5) 4 cups of tea contains milk and water in the ratio 3 : 1. How much of milk is used to prepare 4 cups of tea?

Solution:

Given:

4 cups of tea contains milk and water in the ratio 3:1.

This means that to prepare 4 cups of tea, we need 3 cups of milk and a cup of water.

So, to prepare 4 cups of tea, we need 3 cups of milk.

6) Find 3 equivalent ratios for  $1/5$  ?

Solution:

To find: 3 equivalent ratios of  $1/5$

$1/5$  can be written as  $1k/5k$ , where  $k$  is a real number not equal to 0.

For  $k = 2, 3, 4$  the three equivalent ratios of  $1/5$  is

$2/10, 3/15$ , and  $4/20$ .

7) Find whether the ratios are equal ,  $4/5 = 5/6$

Solution:

$4/5 = 5/6$  is  $4:5::5:6$

Product of the extremes =  $4 \times 6 = 24$

Product of the means =  $5 \times 5 = 25$ .

Since, they are not equal, the given ratios are not equal.

8) Angles of the triangle are in the ratio  $3:4:5$ . Find the angles?

Solution:

Given:

Angles of a triangles are in the ration  $3:4:5$ .

That is, angles are  $3k, 4k, 5k$ , where  $k$  is a non zero real number.

By the property of the triangle,  $3k + 4k + 5k = 180$  degree.

$$\implies k = 180 / 12 = 15.$$

So, the angles are  $3(15), 4(15)$ , and  $5(15)$ .

45 degrees, 60 degrees, 75 degrees.

9) Two cars consume petrol in the ratio  $4:5$ . If both the cars covers the same distance and the second car consumes 25 liters. Find how much petrol the first car uses?

Solution:

Given:

Ratio of Petrol consumption of first to second cars =  $4:5$

Car 2 consumes 25 liters of petrol.

Let car 1 consumes  $x$  liters of petrol.

It can be written in proportions as follows

$$x/25 = 4/5$$

Product of the extremes = product of the means.

$$5x = 25 \times 4$$

$$x = 20.$$

First car consumes 20 liters of petrol.

10) Column A

$$45/55$$

Column B

$$42/56$$

Which is greater?

Solution:

$$45/55 = 9/11$$

$$42/56 = 3/4$$

Let us compare  $9/11$  with  $3/4$  in order.

$$\text{Product of the extremes} = 9 \times 4 = 36$$

$$\text{Product of the means} = 3 \times 11 = 33$$

Since product 36 of the extremes  $>$  Product 33 of the means,  $9 / 11 > 3 / 4$