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1 (* Interfaces d'iterateurs / de flux *)
2 module type SimpleIter =
3 sig
4   type 'a t
5   val vide : 'a t
6   val cons : 'a -> 'a t -> 'a t
7   val unfold : ('s -> ('a * 's) option) -> 's -> 'a t
8   val filter : ('a -> bool) -> 'a t -> 'a t
9   val append : 'a t -> 'a t -> 'a t
10  val constant : 'a -> 'a t
11  val map : ('a -> 'b) -> 'a t -> 'b t
12 end
13
14 module type Iter =
15 sig
16   include SimpleIter
17   val uncons : 'a t -> ('a * 'a t) option
18   val apply : ('a -> 'b) t -> 'a t -> 'b t
19   val map2 : ('a -> 'b -> 'c) -> 'a t -> 'b t -> 'c t
20 end
21
22 (* Le module Flux implantant l'interface de flux Iter *)
23 type 'a flux = Tick of ('a * 'a flux) option Lazy.t;;
24 module Flux : Iter with type 'a t = 'a flux =
25 struct
26   type 'a t = 'a flux = Tick of ('a * 'a t) option Lazy.t;;
27
28   let vide = Tick (lazy None);;
29
30   let cons t q = Tick (lazy (Some (t, q)));;
31
32   let uncons (Tick flux) = Lazy.force flux;;
33
34   let rec apply f x =
35     Tick (lazy (
36       match uncons f, uncons x with
37       | None, _ -> None
38       | _, None -> None
39       | Some (tf, qf), Some (tx, qx) -> Some (tf tx, apply qf qx)));;
40
41   let rec unfold f e =
42     Tick (lazy (
43       match f e with
44       | None -> None
45       | Some (t, e') -> Some (t, unfold f e')));;
46
47   let rec filter p flux =
48     Tick (lazy (
49       match uncons flux with
50       | None -> None
51       | Some (t, q) -> if p t then Some (t, filter p q)
52                          else uncons (filter p q)));;
53
54   let rec append flux1 flux2 =
55     Tick (lazy (
56       match uncons flux1 with
57       | None -> uncons flux2
58       | Some (t1, q1) -> Some (t1, append q1 flux2)));;
59

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60   let constant c = unfold (fun () -> Some (c, ())) ();;
61   (* implantation rapide mais inefficace de map *)
62   let map f i = apply (constant f) i;;
63
64   let map2 f i1 i2 = apply (apply (constant f) i1) i2;;
65 end
66
67 (* Parametres globaux de la simulation *)
68 (* dt : pas de temps *)
69 (* box_x : paire d'abscisses (xmin, xmax) *)
70 (* box_y : paire d'ordonnees (ymin, ymax) *)
71 module type Frame =
72 sig
73   val dt : float
74   val box_x : float * float
75   val box_y : float * float
76 end
77
78 module Drawing (F : Frame) =
79 struct
80   let draw r =
81     let ref_r = ref r in
82     let ref_handler_alarm = ref Sys.(Signal_handle (fun _ -> ())) in
83     let ref_handler_int = ref Sys.(Signal_handle (fun _ -> ())) in
84     let handler_alarm i =
85       begin
86         match Flux.uncons !ref_r with
87         | None ->
88           begin
89             Sys.(set_signal sigalarm !ref_handler_alarm);
90             Sys.(set_signal sigint !ref_handler_int)
91           end
92         | Some ((x, y), (dx, dy)), r' ->
93           begin
94             (*Format.printf "r=(%f, %f); dr = (%f, %f)@." x y dx dy;*)
95             Graphics.clear_graph ();
96             Graphics.draw_circle (int_of_float x) (int_of_float y) 5;
97             Graphics.synchronize ();
98             (*ignore (read_line ());*)
99             ref_r := r'
100           end
101         end in
102     let handler_int i =
103       begin
104         ref_r := Flux.vide
105       end in
106     begin
107       let (inf_x, sup_x) = F.box_x in
108       let (inf_y, sup_y) = F.box_y in
109       let size_x = int_of_float (sup_x -. inf_x) in
110       let size_y = int_of_float (sup_y -. inf_y) in
111       Graphics.open_graph (Format.sprintf " %dx%d" size_x size_y);
112       Graphics.auto_synchronize false;
113       Sys.(ref_handler_alarm := signal sigalarm (Signal_handle
114         handler_alarm));
115       Sys.(ref_handler_int := signal sigint (Signal_handle handler_int));
116       Unix.(setitimer ITIMER_REAL { it_interval = F.dt; it_value = F.dt })
117     end
118   end
119 end

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119 (* Caracteristiques du système: *)
120 (* pas de temps + etat du mobile *)
121 module type Params =
122   sig
123     val dt : float
124     val masse0 : float
125     val position0 : float * float
126     val vitesse0 : float * float
127   end
128
129 module FreeFall (F : Frame) =
130   struct
131     let (|+|) (x1, y1) (x2, y2) = (x1 +. x2, y1 +. y2)
132     let (|*|) k (x, y) = (k *. x, k *. y)
133
134     let integre dt flux =
135       let init = (0., 0.) in
136       let rec acc =
137         Tick (lazy (Some (init, Flux.map2 (fun a f -> a |+| (dt |*| f)) acc
138 flux)))
139       in acc
140
141     let g = 9.81;;
142     (* r = r0 + Integ dr
143      dr = dr0 + Integ ddr
144      ddr = 0, -g
145      *)
146     let run (position0, vitesse0) =
147       let acceleration = Flux.constant (0., -. g) in
148       let vitesse = Flux.(map2 ( |+| ) (constant vitesse0) (integre F.dt
149 acceleration)) in
150       let position = Flux.(map2 ( |+| ) (constant position0) (integre
151 F.dt vitesse)) in
152       Flux.map2 (fun a b -> (a, b)) position vitesse
153     end
154
155 module Bouncing (F : Frame) =
156   struct
157     (* version avec unfold sans récursivité directe *)
158     let unless flux cond f_cond =
159       Flux.unfold (fun (init, f) ->
160         match Flux.uncons f with
161         | None -> None
162         | Some (v, f') -> if not (init && cond v)
163           then Some (v, (init, f'))
164           else match Flux.uncons (f_cond v) with
165             | None -> None
166             | Some (v, f') -> Some (v, (false, f'))
167       ) (true, flux)
168
169     (* version avec récursivité, donc paresse explicite *)
170     let rec unless flux cond f_cond =
171       Tick (lazy (
172         match Flux.uncons flux with
173         | None -> None
174         | Some (t, q) -> if cond t then Flux.uncons (f_cond t) else
175         Some (t, unless q cond f_cond)
176       ))
177   end

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175   let contact_1d (infx, supx) x dx = (x <= infx && dx < 0.) || (x >= supx
176   && dx > 0.)
177
178   let rebond ((x, y), (dx, dy)) =
179     (x, y),
180     ((if contact_1d F.box_x x dx then -. dx else dx),
181      (if contact_1d F.box_y y dy then -. dy else dy))
182
183   let contact ((x, y), (dx, dy)) = contact_1d F.box_x x dx || contact_1d
184   F.box_y y dy
185
186   module FF = FreeFall (F)
187
188   let rec run etat0 =
189     unless (FF.run etat0) contact (fun etat -> run (rebond etat))
190   end
191
192   module Init =
193     struct
194       let dt = 0.01
195       let box_x = (0., 800.)
196       let box_y = (0., 600.)
197     end
198
199   module Draw = Drawing (Init)
200   module Bounce = Bouncing (Init)
201
202   let _ =
203     let position0 = (300., 400.) in
204     let vitesse0 = (25., 15.) in
205     Draw.draw (Bounce.run (position0, vitesse0));;
206
207
208

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