

# Complex Critical Systems in Event-B

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7 October 2021

- 1 Environment Modelling
- 2 Medical Devices
- 3 Formal Development
- 4 Interactive Simulation
- 5 Code Generation

# Safety-Critical System

## Definition

A **life-critical system** or **safety-critical system** is a system whose failure or malfunction may result in **serious injuries, loss of life, economical damage** and **environmental harm**.

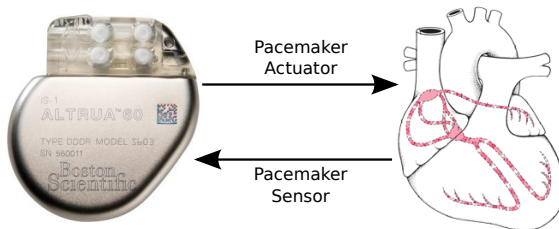


# Critical System Failure

## Systems Failure

- **Therac-25 (1985-1987):** six people overexposed through radiation.
- **Pacemaker and ICD (1990-2002):** 17,323 pacemakers and ICDs were explanted that includes 61 deaths.
- **Insulin Infusion Pump (IIP) (2010):** 5000 adverse events that includes 30 deaths.
- **Missing Malaysian Plane MH370 (8 March, 2014):** Unknown.
- **Satellite Failure:+150:** <http://www.sat-nd.com/failures/>.

# The Cardiac Pacemaker (Grand Challenge)

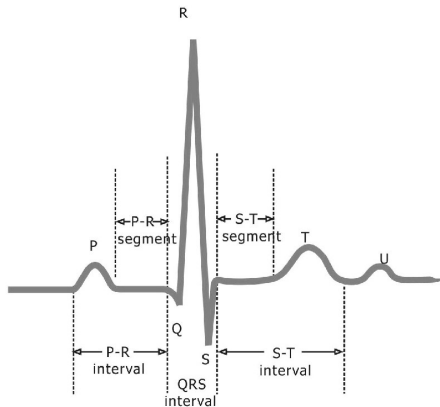


**Figure:** Closed-loop Modelling of the Heart & Cardiac Pacemaker

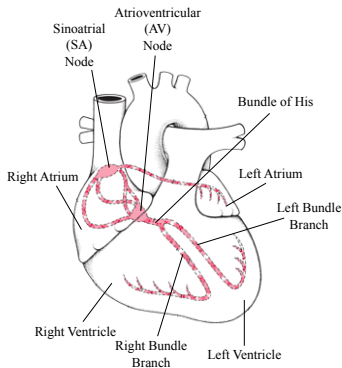
# The Human Heart

# The Heart Modeling

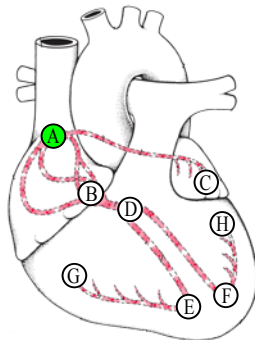
## Electrocardiogram (ECG)



## The Electrical Conduction

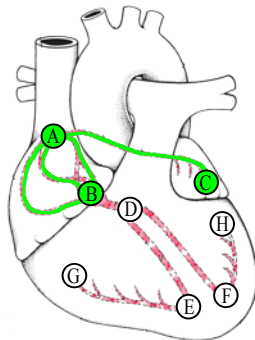


# Heart Conduction Through Landmark Nodes

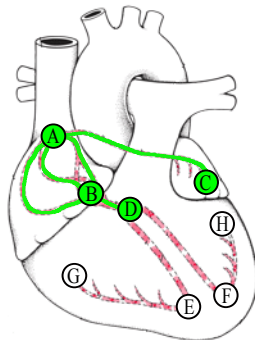




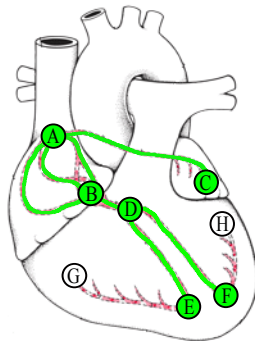
# Heart Conduction Through Landmark Nodes



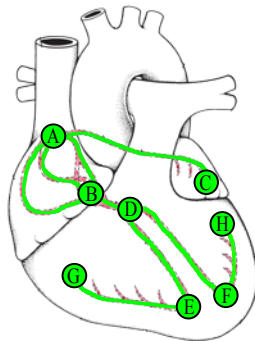
# Heart Conduction Through Landmark Nodes



# Heart Conduction Through Landmark Nodes



# Heart Conduction Through Landmark Nodes



## Definition 1 (The Heart System)

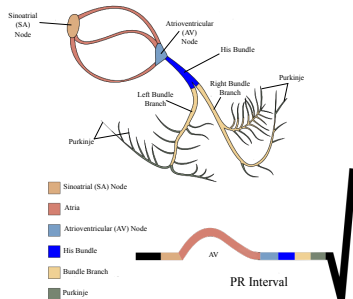
Given a set of nodes  $N$ , a transition (conduction)  $T$  is a pair  $(i, j)$ , with  $i, j \in N$ . A transition is denoted by  $i \rightsquigarrow j$ . The heart system is a tuple  $HSys = (N, T, N_0, TW_{time}, CW_{speed})$  where:

- $N = \{ A, B, C, D, E, F, G, H \}$  is a finite set of landmark nodes;
- $T \subseteq N \times N = \{ A \mapsto B, A \mapsto C, B \mapsto D, D \mapsto E, D \mapsto F, E \mapsto G, F \mapsto H \}$  is a set of transitions;
- $N_0 = A$  is the initial landmark node;
- $TW_{time} \in N \rightarrow TIME$  is a weight function as time delay;
- $CW_{speed} \in T \rightarrow SPEED$  is a weight function as impulse propagation speed.

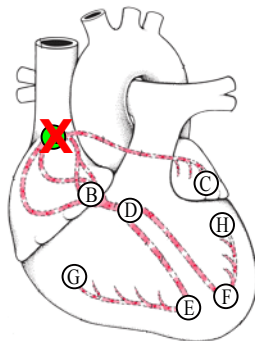
# Time Intervals and Impulse Propagation in the ECG

| Location in the heart        | Impulse Propagation Time (ms.)<br>Property 1 ( $TW_{time}$ ) | Location in the heart | Impulse Propagation Speed (cm/sec.)<br>Property 2 ( $CW_{speed}$ ) |
|------------------------------|--|-----------------------|--|
| SA Node (A)                  | 0..10  | A $\mapsto$ B         | 30..50   |
| Left atria muscle fibers (C) | 70..90   | A $\mapsto$ C         | 30..50   |
| AV Node (B)                  | 50..70   | B $\mapsto$ D         | 100..200   |
| Bundle of His (D)            | 125..160   | D $\mapsto$ E         | 100..200   |
| Right Bundle Branch (E)      | 145..180   | D $\mapsto$ F         | 100..200   |
| Left Bundle Branch (F)       | 145..180   | E $\mapsto$ G         | 300..400   |
| Right Purkinje fibers (G)    | 150..210   | F $\mapsto$ H         | 300..400   |
| Left Purkinje fibers (H)     | 150..230   |                       |  |

**Table:** Cardiac Activation Time and Cardiac Velocity

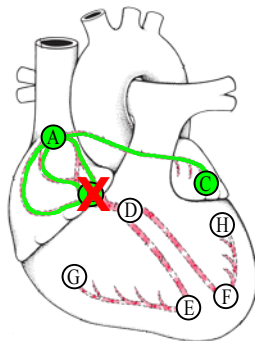


# Heart Blocks (Abnormal Heart Rhythm)



SA Block

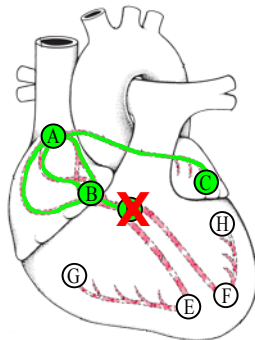
# Heart Blocks (Abnormal Heart Rhythm)



AV Block

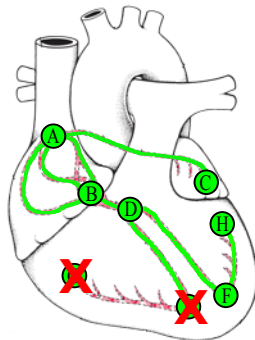


# Heart Blocks (Abnormal Heart Rhythm)



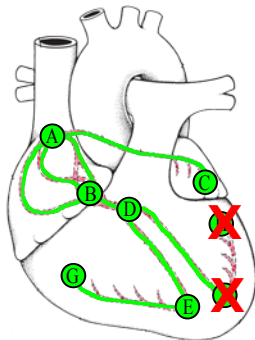
Infra-Hisian Block

# Heart Blocks (Abnormal Heart Rhythm)



Right Bundle Branch Block

# Heart Blocks (Abnormal Heart Rhythm)



Left Bundle Branch Block

# 2D Cellular Automata and State Transition Model

## Definition 3 (State Transition of a Cell)

The heart muscle system is composed of heterogeneous cells, the cellular automata model of the muscle system,  $CAM_{CA}$ , is characterized with no dependencies on the type of cells.  $CAM_{CA}$  is defined as follows:

$$CAM_{CA} = \langle S, N, T \rangle$$

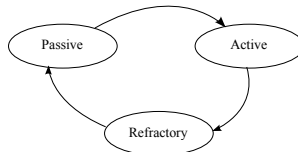
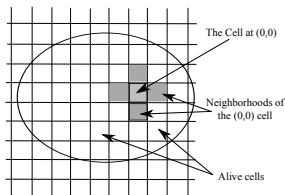
$$S = \{Active, Passive, Refractory\}$$

$$N_{m,n} = \{(m, n), (m+1, n), (m-1, n), (m, n+1), (m, n-1)\}$$

$$T : S^{|N|} \rightarrow S$$

$$s_{t+1}(m, n) = \begin{cases} \text{Refractory} & \text{if } s_t(m, n) = \text{Active} \\ \text{Passive} & \text{if } s_t(m, n) = \text{Refractory} \\ \text{Active} & \text{if } s_t(m, n) = \text{Passive} \text{ and any neighbor is in Active state} \\ \text{Passive} & \text{if } s_t(m, n) = \text{Passive} \text{ and none neighbor is in Active state} \end{cases}$$

where,  $s_t(m, n)$  denotes the state of the cell located at  $(m, n)$ .



## Abstract Model and Chain of Refinements

- Abstract Model
- Refinement 1: Introducing Steps in the Propagation
- Refinement 2: Impulse Propagation
- Refinement 3: Perturbation the Conduction
- Refinement 4: Getting a Cellular Model

## Proof Statistics

| Model             | Total number of POs | Automatic Proof | Interactive Proof |
|-------------------|---------------------|-----------------|-------------------|
| Abstract Model    | 29                  | 22(76%)         | 7(24%)            |
| First Refinement  | 9                   | 6(67%)          | 3(33%)            |
| Second Refinement | 159                 | 155(97%)        | 4(3%)             |
| Third Refinement  | 10                  | 1(10%)          | 9(90%)            |
| Fourth Refinement | 11                  | 10(91%)         | 1(9%)             |
| <b>Total</b>      | <b>218</b>          | <b>194(89%)</b> | <b>24(11%)</b>    |

# The Cardiac Pacemaker

# The Cardiac Pacemaker

## Pacemaker

A pacemaker is an electronic device implanted in a body to regulate the abnormal heart rhythm (**bradycardia**).

Type of pacemakers: 1, 2 and 3-Electrodes.

## The Cardiac Pacemaker



## Operating Modes : NASPE/BPEG Generic Code

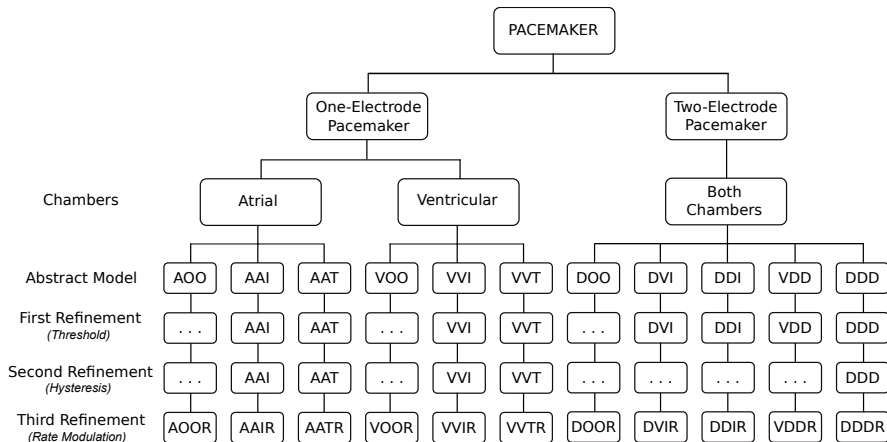
| Category | Chambers Paced   | Chambers Sensed  | Response to Sensing   | Rate Modulation           |
|----------|--|--|---|---------------------------|
| Letters  | <b>O</b> -None<br><b>A</b> -Atrium<br><b>V</b> -Ventricle<br><b>D</b> -Dual(A+V) | <b>O</b> -None<br><b>A</b> -Atrium<br><b>V</b> -Ventricle<br><b>D</b> -Dual(A+V) | <b>O</b> -None<br><b>T</b> -Triggered<br><b>I</b> -Inhibited<br><b>D</b> -Dual(T+I) | <b>R</b> -Rate Modulation |

i.e. AOO, VOO, AAI, AAT, VVI, VVT, AATR, VVTR, AOOR etc. . .

**Periodic stimuli** : (AOO, VOO and DOO)

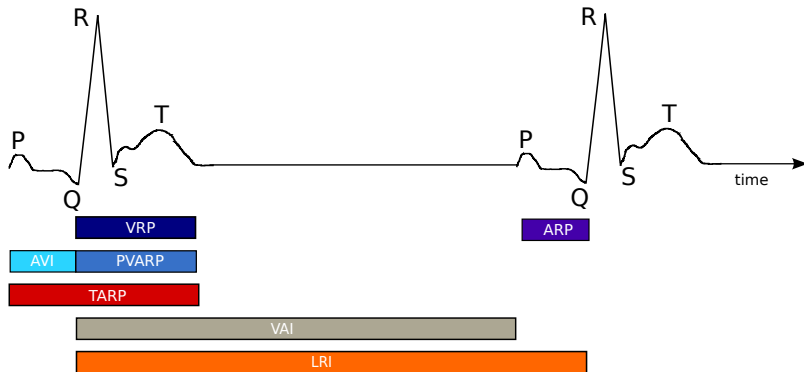
**Aperiodic stimuli** : (AAI, VVI, DDD, DDI, etc.)

# Hierarchical Development of Operating Modes





# Timing Cycles



**VRP** - Ventricular Refractory Period

**ARP** - Atrial Refractory Period

**AVI** - Atrioventricular Interval

**PVARP** - Post Ventricular Atrial Refractory Period

**TARP** - Total Atrial Refractory Period

**VAI** - Ventriculoatrial Interval

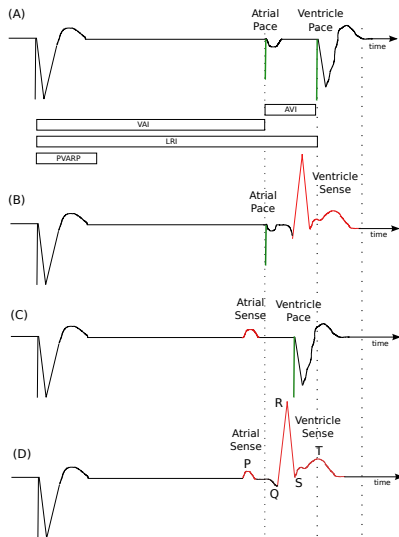
**LRI** - Lower Rate Interval

**URI** - Upper Rate Interval

# General Requirements (Boston Scientific)

- ① The bradycardia operating modes ( AOO, AAT, VVI, ... , DDDR) shall be programmable.
- ② The Pacemaker shall support single and dual chamber pacing modes.
- ③ The device shall actuate for pacing in the heart with programmable voltages and widths.
- ④ The pacing pulse amplitudes and pacing width shall be programmable for each chamber (e.g. atrial, ventricular).
- ⑤ The device shall support rate adaptive pacing in order to meet the physiological needs.

# The DDD Pacing Scenarios



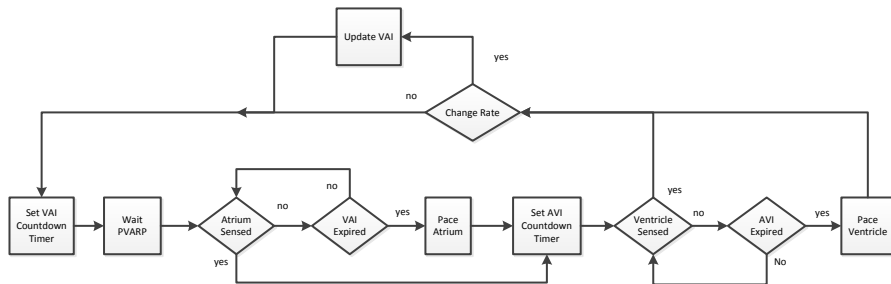
# DOO and DDD Modes Requirements

- 1 The pacemaker in **DOO** mode must pace in both atria and ventricular chambers without sensing any intrinsic activities from both chambers according to the programmable parameters.
- 2 In **DDD** mode, when the pacing system senses intrinsic activities in both chambers, the pacemaker must be triggered or inhibited to pace in both chambers according to the programmable parameters.

# Rate Adaptive Modes (AOOR, DOOR, ..., DDDR) Requirements

- 1 The pacemaker in rate adaptive mode must pace and sense in any chamber according to the selected mode by changing the rate to meet the physical needs according to the programmable parameters.

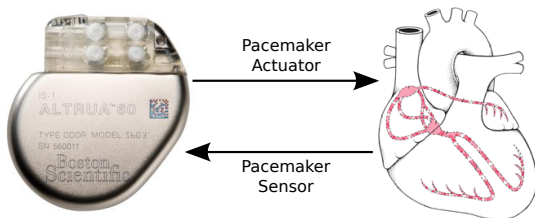
# Flowchart for DDDR Pacing Cycle



# Formal Development

# Closed-loop Model (Heart & Cardiac Pacemaker)

- Simple Pacemaker Model
- Closed-loop Model



- **Abstract Model:** Pacing and Sensing Activities + Normal and Abnormal Heart Behaviour.
- **Refinement 1:** *Threshold* + Impulse Propagation .
- **Refinement 2:** Hysteresis + Perturbation the Conduction.
- **Refinement 3:** Rate Modulation + Cellular Model.



# Formalization of the Closed-loop model: Abstract Model

*axm1* : *partition*(*ConductionNode*, {*A*}, {*B*}, {*C*}, {*D*}, {*E*}, {*F*}, {*G*}, {*H*})  
*axm2* : *ConductionTime*  $\in$  *ConductionNode*  $\rightarrow \mathbb{P}(0 \dots 230)$   
*axm3* : *ConductionPath*  $\subseteq$  *ConductionNode*  $\times$  *ConductionNode*  
*axm4* : *ConductionSpeed*  $\in$  *ConductionPath*  $\rightarrow \mathbb{P}(5 \dots 400)$   
*axm5* : *LRL*  $\in 30 \dots 175 \wedge$  *URL*  $\in 50 \dots 175 \wedge$  *PVARP*  $\in 150 \dots 500$   
*axm6* : *ARP*  $\in 150 \dots 500 \wedge$  *VRP*  $\in 150 \dots 500 \wedge$  *status* = {*ON*, *OFF*}

*inv1* : *ConductionNodeState*  $\in$  *ConductionNode*  $\rightarrow$  *BOOL*  
*inv2* : *CConductionTime*  $\in$  *ConductionNode*  $\rightarrow 0 \dots 300$   
*inv3* : *CConductionSpeed*  $\in$  *ConductionPath*  $\rightarrow 0 \dots 500$   
*inv4* : *HeartState*  $\in$  *BOOL*  
*inv5* : *PM\_Actuator\_A*  $\in$  *status*  $\wedge$  *PM\_Actuator\_V*  $\in$  *status*  
*inv6* : *PM\_Sensor\_A*  $\in$  *status*  $\wedge$  *PM\_Sensor\_V*  $\in$  *status*  
*inv7* : *Pace\_Int*  $\in$  *URI*  $\dots$  *LRI*  $\wedge$  *sp*  $\in 1 \dots$  *Pace\_Int*  
*inv8* : *sp*  $<$  *VRP*  $\wedge$  *sp*  $<$  *PVARP*

$\Rightarrow$

*PM\_Actuator\_V* = *OFF*  $\wedge$  *PM\_Sensor\_A* = *OFF*  $\wedge$   
*PM\_Sensor\_V* = *OFF*  $\wedge$  *PM\_Actuator\_A* = *OFF*

*inv9* : *PM\_Actuator\_V* = *ON*  $\Rightarrow$  *sp* = *Pace\_Int*

*inv10* : *PM\_Actuator\_A* = *ON*  $\Rightarrow$  (*sp*  $\geq$  *Pace\_Int* - *FixedAV*)

...

# DDD Pacing Modes

## EVENT Actuator\_ON\_V

### WHEN

grd1 :  $PM\_Actuator\_V = OFF$   
grd2 :  $sp = Pace\_Int$   
grd3 :  $sp \geq VRP \wedge sp \geq PVARP$

### THEN

act1 :  $PM\_Actuator\_V := ON$   
act2 :  $last\_sp := sp$

### END

## EVENT Actuator\_OFF\_V

### WHEN

grd1 :  $PM\_Actuator\_V = ON$   
grd2 :  $sp = Pace\_Int$   
grd3 :  $PM\_Actuator\_A = OFF$   
grd4 :  $PM\_Sensor\_A = OFF$

### THEN

act1 :  $PM\_Actuator\_V := OFF$   
act2 :  $AV\_Count := 0$   
act3 :  $PM\_Sensor\_V := OFF$   
act4 :  $sp := 1$

### END

## EVENT tic

### WHEN

grd1 :  $sp < Pace\_Int$

### THEN

act1 :  $sp := sp + 1$

### END

**EVENT HeartOK****WHEN**

grd1 :  $\forall i \cdot i \in \text{ConductionNode} \Rightarrow \text{ConductionNodeState}(i) = \text{TRUE}$   
grd2 :  $\forall i \cdot i \in \text{ConductionNode} \Rightarrow \text{CConductionTime}(i) \in \text{ConductionTime}(i)$   
grd3 :  $\forall i, j \cdot i \mapsto j \in \text{ConductionPath} \Rightarrow$   
 $\text{CConductionSpeed}(i \mapsto j) \in \text{ConductionSpeed}(i \mapsto j)$

**THEN**

act1 :  $\text{HeartState} := \text{TRUE}$

**END****EVENT Sensor\_ON\_V****WHEN**

grd1 :  $\text{PM\_Sensor\_V} = \text{OFF}$   
grd2 :  $(sp \geq \text{PVARP} \wedge sp > \text{VRP})$   
grd3 :  $sp > \text{Pace\_Int} - \text{FixedAV}$   
grd4 :  $\text{PM\_Actuator\_A} = \text{OFF}$

**THEN**

act1 :  $\text{PM\_Sensor\_V} := \text{ON}$

**END****EVENT Sensor\_OFF\_V****WHEN**

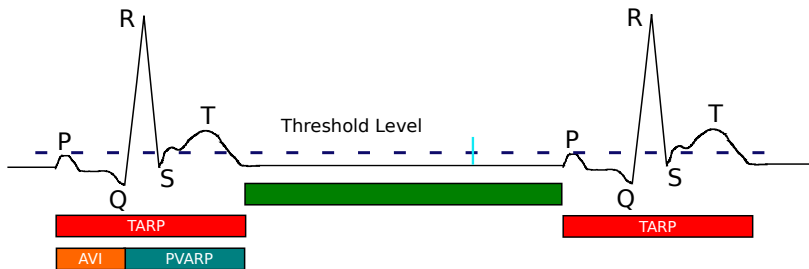
grd1 :  $\text{PM\_Sensor\_V} = \text{ON}$   
grd2 :  $sp \geq \text{VRP} \wedge sp \geq \text{PVARP}$   
grd3 :  $sp \geq \text{Pace\_Int} - \text{FixedAV}$   
grd4 :  $\text{PM\_Actuator\_V} = \text{OFF}$

**THEN**

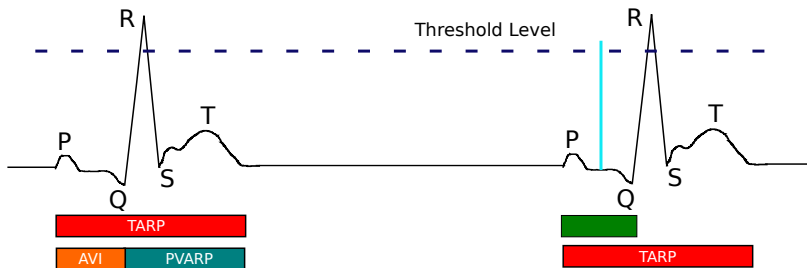
act1 :  $\text{PM\_Sensor\_V} := \text{OFF}$

**END**

# First Refinement (Threshold): Sensor Activity in DDD


$$\begin{aligned} \text{inv1} : & sp > PVARP \wedge sp < Pace\_Int - FixedAV \\ \Rightarrow & \\ & PM\_Sensor\_A = \text{ON} \wedge \\ & PM\_Sensor\_V = \text{OFF} \wedge \\ & PM\_Actuator\_A = \text{OFF} \wedge \\ & PM\_Actuator\_V = \text{OFF} \end{aligned}$$

# First Refinement (Threshold): Sensor Activity in DDD


$$\begin{aligned} \text{inv1 : } & sp > \text{Pace\_Int} - \text{FixedAV} \wedge sp < \text{Pace\_Int} \\ \Rightarrow & \\ & PM\_Sensor\_V = \text{ON} \wedge \\ & PM\_Sensor\_A = \text{OFF} \wedge \\ & PM\_Actuator\_A = \text{OFF} \wedge \\ & PM\_Actuator\_V = \text{OFF} \end{aligned}$$

# Second Refinement: Hysteresis

## What is Hysteresis?

Hysteresis is a programmed feature whereby the pacemaker paces at a faster rate than the sensing rate and it provides consistent pacing to the atrial or ventricle, or prevents the constant pacing of the atrial or ventricle. The main purpose of hysteresis is to allow the patient to have his or her own underlying rhythm as much as possible.

```
EVENT Hyt_Pace_Updating Refines Change_Pace_Int
ANY
  Hyt_Pace_Int
WHERE
  grd1 : Pace_Int_flag = TRUE
  grd2 : Hyt_Pace_Int_flag = TRUE
  grd3 : Hyt_Pace_Int  $\in$  Pace_Int .. LRI
THEN
  act1 : Pace_Int := Hyt_Pace_Int
  act2 : Hyt_Pace_Int_flag := FALSE
  act3 : HYT_State := TRUE
END
```

# Third Refinement: Rate Modulation

## What is Rate Modulation?

**Increase.Interval Refines Change.Pace.Int**

**WHEN**

*grd1 : grd1 : Pace\_Int\_flag = TRUE*

*grd1 : acler\_sensed  $\geq$  threshold*

*grd1 : HYT\_State = FALSE*

**THEN**

*act1 : Pace\_Int := 60000/MSR*

*act1 : acler\_sensed\_flag := TRUE*

**END**

*inv3 : acler\_sensed < acc\_thr  $\wedge$  acler\_sensed\_flag = TRUE  $\Rightarrow$  Pace\_Int = 60000/LRL*

*inv4 : acler\_sensed  $\geq$  acc\_thr  $\wedge$  acler\_sensed\_flag = TRUE  $\Rightarrow$  Pace\_Int = 60000/MSR*

## ProB Model Checker

The ProB model checker is used for,

- to **verify** the developed system requirements;
- to check the **required behaviour** of the pacemaker for each operating mode;
- **deadlock checking**;
- to discover the **counter examples**;



# Simple Model Vs. Closed-loop Model

| Model                          | Total number of POs | Automatic Proof | Interactive Proof |
|--------------------------------|---------------------|-----------------|-------------------|
| Simple One-electrode pacemaker |                     |                 |                   |
| Abstract Model                 | 203                 | 199(98%)        | 4(2%)             |
| First Refinement               | 48                  | 44(91%)         | 4(9%)             |
| Second Refinement              | 12                  | 8(66%)          | 4(34%)            |
| Third Refinement               | 105                 | 99(94%)         | 6(6%)             |
| Simple Two-electrode pacemaker |                     |                 |                   |
| Abstract Model                 | 204                 | 195(95%)        | 9(5%)             |
| First Refinement               | 234                 | 223(95%)        | 11(5%)            |
| Second Refinement              | 3                   | 3(100%)         | 0(0%)             |
| Third Refinement               | 83                  | 74(89%)         | 9(11%)            |
| <b>Total</b>                   | <b>892</b>          | <b>845(94%)</b> | <b>47(6%)</b>     |

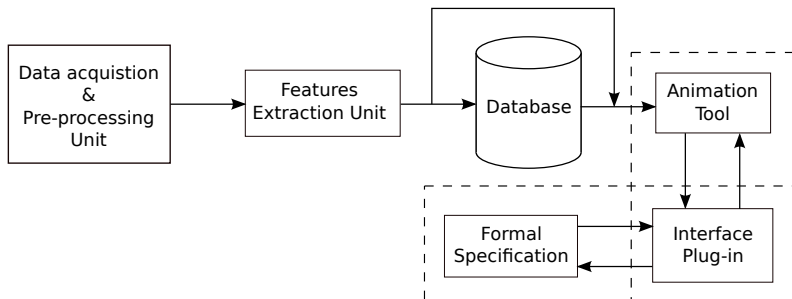
| Model  | Total number of POs | Automatic Proof  | Interactive Proof |
|--|---------------------|------------------|-------------------|
| Closed-loop model of One-electrode pacemaker |                     |                  |                   |
| Abstract Model                               | 304                 | 258(85%)         | 46(15%)           |
| First Refinement                             | 1015                | 730(72%)         | 285(28%)          |
| Second Refinement                            | 72                  | 8(11%)           | 64(89%)           |
| Third Refinement                             | 153                 | 79(52%)          | 74(48%)           |
| Closed-loop model of Two-electrode pacemaker |                     |                  |                   |
| Abstract Model                               | 291                 | 244(84%)         | 47(16%)           |
| First Refinement                             | 1039                | 766(74%)         | 273(26%)          |
| Second Refinement                            | 53                  | 2(4%)            | 51(96%)           |
| Third Refinement                             | 122                 | 60(49%)          | 62(51%)           |
| <b>Total</b>                                 | <b>3049</b>         | <b>2147(70%)</b> | <b>902(30%)</b>   |

# Interactive Simulation

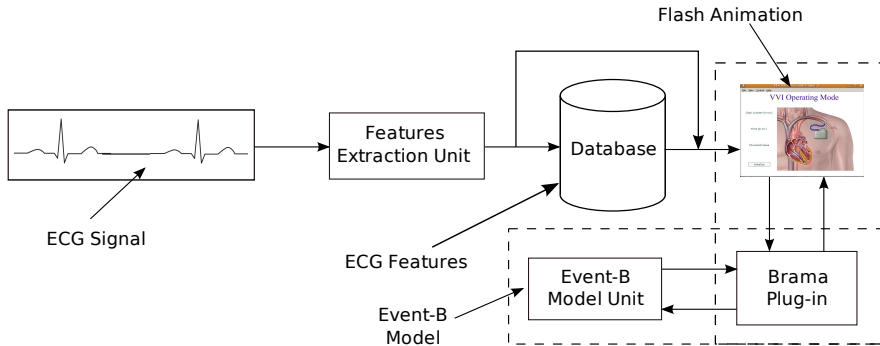
# An Architecture of Real-time Animator

## Real-Time Animator

Visual representation of a proved formal model using **real-time data set** to show the system behaviour to **domain experts**.



# Real-time Animation : Pacemaker



- MIT-BIH Database Distribution
- Algorithms to calculate ECG Features  
(<http://ecg.mit.edu/index.html>)

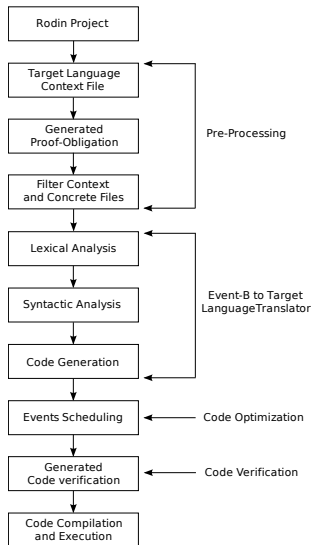
# Demo

# EB2ALL: Automatic Code Generation from Event-B Models

# EB2ALL Code Generation tool

## EB2ALL (Event-B to All)

- EB2C
- EB2C++
- EB2J
- EB2C#



## EB2ALL Tool Architecture



# Pre-Processing

- Objective : Make a system deterministic
- Clean termination approach
- Introduction of new Context Files

| Event-B type     | Formal Range          | C & C++ type      | Java type | C# type |
|------------------|-----------------------|-------------------|-----------|---------|
| <i>tl_int16</i>  | $-2^{15}..2^{15} - 1$ | int               | short     | short   |
| <i>tl_uint16</i> | $0..2^{16} - 1$       | unsigned int      | -         | ushort  |
| <i>tl_int32</i>  | $-2^{31}..2^{31} - 1$ | long int          | int       | int     |
| <i>tl_uint32</i> | $0..2^{32} - 1$       | unsigned long int | -         | uint    |
| <i>tl_int64</i>  | $-2^{63}..2^{63} - 1$ | -                 | long      | long    |
| <i>tl_uint64</i> | $0..2^{64} - 1$       | -                 | -         | ulong   |

**Table:** Integer bounded data type declaration in different context files

Example :

$Id \in \mathbb{N}_1$

$Id \in tl\_uint16$

# Basic Principles of Code Generation

| Event-B  | 'C' & 'C++' Language        | Comment               |
|--|-----------------------------|-----------------------|
| $n..m$   | int                         | Integer type          |
| $x \in Y$  | $Y \ x;$                    | Scalar declaration    |
| $x \in \text{tl\_int16}$                                       | int x;                      | 'C' & 'C++' Contexts  |
| $x \in n..m \rightarrow Y$                                     | $Y \ x \ [m+1];$            | Array declaration     |
| $x : \in Y$  | $/* \text{ No Action } */$  | Indeterminate Init.   |
| $x :   Y$  | $/* \text{ No Action } */$  | Indeterminate Init.   |
| $x = y$  | if(x==y) {                  | Conditional           |
| $x \neq y$   | if(x!=y) {                  | Conditional           |
| $x < y$  | if(x<y) {                   | Conditional           |
| $x \leq y$   | if(x<=y) {                  | Conditional           |
| $x > y$  | if(x>y) {                   | Conditional           |
| $x \geq y$   | if(x>=y) {                  | Conditional           |
| $(x>y) \wedge (x \geq z)$                                      | if ((x>y) && (x>=z) {       | Conditional           |
| $(x>y) \vee (x \geq z)$  | if ((x>y)    (x>=z) {       | Conditional           |
| $x := y + z$   | $x = y + z;$                | Arithmetic assignment |
| $x := y - z$   | $x = y - z;$                | Arithmetic assignment |
| $x := y * z$   | $x = y * z;$                | Arithmetic assignment |
| $x := y \div z$  | $x = y / z;$                | Arithmetic assignment |
| $x := F(y)$  | $x = F(y);$                 | Function assignment   |
| $a := F(x \mapsto y)$  | $a = F(x, y);$              | Function assignment   |
| $x := a(y)$  | $x = a[y];$                 | Array assignment      |
| $x := y$   | $x = y;$                    | Scalar action         |
| $a := a \Leftarrow \{x \mapsto y\}$                            | $a[x] = y;$                 | Array action          |
| $a := a \Leftarrow \{x \mapsto y\} \Leftarrow \{i \mapsto j\}$ | $a[x]=y; a[i]=j;$           | Array action          |
| $X \Rightarrow Y$  | if(!X    Y){                | Logical Implication   |
| $X \Leftrightarrow Y$  | if((!X    Y) && (!Y    X)){ | Logical Equivalence   |
| $\neg x < y$   | if(!(x<y)){                 | Logical not           |
| $x \in \mathbb{N}$   | unsigned long int x         | Natural numbers       |
| $x \in \mathbb{Z}$   | signed long int x           | Integer numbers       |
| $\forall$  | $/* \text{ No Action } */$  | Quantifier            |
| $\exists$  | $/* \text{ No Action } */$  | Quantifier            |

# Tool Installation

Web: <http://eb2all.loria.fr/> (Until Rodin 2.8)

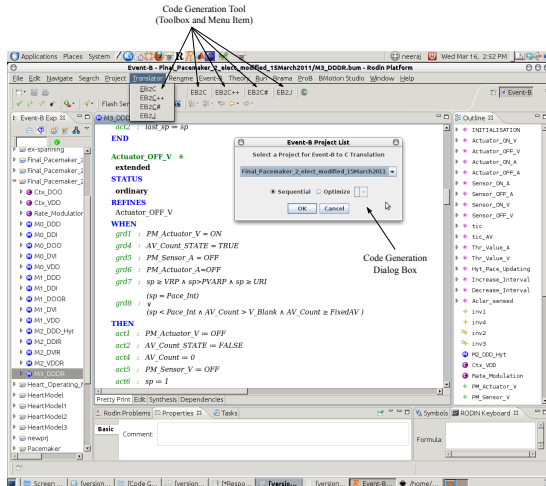


Figure: Screen shots of the Code Generation Tool: EB2ALL

# An Example - Code Generation

```
EVENT Actuator_ON.V
WHEN
  Actuator_ON.V.Guard1 : PM_Actuator_V = OFF
  Actuator_ON.V.Guard2 : (sp = Pace.Int)
    ∨
    (sp < Pace.Int ∧
     AV_Count > V_Blank ∧
     AV_Count ≥ FixedAV)
  Actuator_ON.V.Guard3 : sp ≥ VRP ∧ sp ≥ PVARP
THEN
  Actuator_ON.V.Action1 : PM_Actuator_V := ON
  Actuator_ON.V.Action2 : last_sp := sp
END
```

```
...
BOOL Actuator\_ON\_V(void)
{
  /* Guards No. 1*/
  if(PM_Actuator_V == OFF){
    /* Guards No. 2*/
    if((sp == Pace_Int) || ((sp < Pace_Int) &&
    (AV_Count > V_Blank) && (AV_Count >= FixedAV))){
      /* Guards No. 3*/
      if((sp >= VRP) && (sp >= PVARP) && (sp >= URI)){
        /* Actions */
        PM_Actuator_V = ON;
        last_sp = sp;
        return TRUE;
      }}
    return FALSE;
  }
  ...
}
```

# Demo

Neeraj Kumar Singh

# Using Event-B for Critical Device Software Systems

 Springer

