

# Modeling of dynamical systems

## Subject guide

Last update: January 2021

### 1. General information

|   |  |
|---|--|
| <b>Name of the subject</b>                            | Modeling of dynamical systems          |
| <b>Code</b>   | 11310040                               |
| <b>Type of subject</b>                                | Compulsory                             |
| <b>Number of credits</b>                              | 3                                      |
| <b>Type of credit</b>                                 | 2A + 1B                                |
| <b>Weekly work hours with direct teacher guidance</b> | 80                                     |
| <b>Weekly Hours of independent student work</b>       | 64                                     |
| <b>Prerequisites</b>                                  | Linear Algebra, Differential Equations |
| <b>Corequisites</b>                                   | None                                   |
| <b>Schedule</b>                                       |  |
| <b>leader</b>   | Martín Andrade Restrepo                |
| <b>Lounge</b>   |  |

### 2. Lecturer and monitor information

|   |  |
|---|--|
| <b>Name of Lecturer</b>                   | Martín Andrade Restrepo  |
| <b>professional Profile</b>               |  |
| <b>Institutional email</b>                | <a href="mailto:Martin.andrade@urosario.edu.co">Martin.andrade@urosario.edu.co</a> |
| <b>Place and hours of attention</b>       | Edificio Cabal Of. 402<br>Wednesdays, Fridays 13:00 – 14:00                        |
| <b>Web page or other means (optional)</b> |  |

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|--|--|
| <b>Name of assistant professor or monitor</b>    |  |
| <b>Professional profile</b>                      |  |
| <b>Institutional email</b>                       |  |
| <b>Place and hours of attention:</b>             |  |
| <b>Web page, Skype or other means (optional)</b> |  |

### 3. Summary and purposes of the course

The course addresses the modeling of dynamical systems using differential and difference equations. This is extremely useful for understanding and predicting the behavior of different physical, social and computational phenomena, etc. Once the generalities of the systems of differential and difference equations have been exposed, the main analysis techniques of linear models are presented, emphasizing the representation in state space. In addition, the student is introduced to the use of specialized software to simulate the behavior of dynamical systems.

### 4. Fundamental concepts

1. Dynamic models in continuous time
2. Dynamic models in discrete time
3. Simulation of dynamical systems using specialized software
4. Representations in state space
5. Analysis of linear and time-invariant systems
6. Equilibrium points and stability
7. Linearization of dynamic systems

### 5. Expected learning outcomes (RAE)

1. Learn typical models of systems through differential and difference equations.
2. Simulate the behavior of dynamical systems using specialized software.
3. Understand representations in state spaces of dynamical systems.
4. Manage different methods of analysis of linear systems.
5. Carry out the linearization of a system represented in state space.

## 6. Course modality

Remote mode: All students will be connected remotely from their homes or locations outside the University.

## 7. Learning strategies

1. Lectures where the theoretical foundations will be taught.
2. Tasks where students will work independently on the content seen.
3. Laboratories where the methods and algorithms addressed in the Lectures will be implemented.
4. Final project where students must apply the tools learned during the semester to solve a real problem.

## 8. Evaluations

| Topic                                    | Activities  | Percentage | Exam dates |
|--|---|------------|------------|
| Those corresponding to sessions 1 to 7   | Individual written evaluation<br>-<br><b>First cut</b>  | 20         | Week 4     |
| Those corresponding to sessions 9 to 19  | Individual written evaluation<br>-<br><b>Second cut</b> | 20         | Week 10    |
| Those corresponding to sessions 21 to 29 | Individual written evaluation<br>-<br><b>Third cut</b>  | 20         | Week 15    |
| All sessions                             | Presentation and document<br>-<br><b>Final project</b>  | 15         | exam week  |

|                            |  |    |               |
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| Laboratories and workshops | Individual Reports<br>and / or group Reports | 25 | Every<br>week |
|----------------------------|--|----|---------------|

## 9. Activity program

| Date      | Topic   | Description of the activity     | Independent work of the student  | Resources that support the activity (bibliography and other support resources) |
|-----------|---|---------------------------------|--|--|
| Session 1 | <b>Presentation of the course.</b><br><br><b>Theory:</b><br>Dynamic phenomena. Typical examples | Lecture, discussion, exercises. | Previously read the section (s). Complement the class by doing exercises from the section. | [Lue, 1.1-1.4]   |
| Session 2 | <b>Laboratory:</b> introduction to Matlab   |                                 |  |  |
| Session 3 | <b>Theory:</b><br>Difference equations. Existence and uniqueness of solutions. Examples         | Lecture, discussion, exercises. | Previously read the section (s). Complement the class by doing exercises from the section. | [Lue, 2.1-2.5]   |
| Session 4 | <b>Laboratory:</b> implementation of difference equations in Matlab                             |                                 |  |  |
| Session 5 | <b>Theory:</b><br>Linear difference equations. Linear equations with constant coefficients      | Lecture, discussion, exercises. | Previously read the section (s). Complement the class by doing exercises from the section. | [Lue, 2.6-2.7]   |
| Session 6 | <b>Laboratory:</b> linear difference equations  |                                 |  |  |
| Session 7 | <b>Theory:</b><br>Differential equations. Existence   | Lecture, discussion, exercises. | Previously read the section (s). Complement the class by doing                             | [Lue, 2.8-2.10]  |

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|            | and uniqueness of solutions. Linear differential equations. Examples   |                                 | exercises from the section.  |                  |
| Session 8  | <b>First partial exam</b>  |                                 |  |                  |
| Session 9  | <b>Theory:</b><br>Systems of first order equations. Representation of systems in state space. Inputs and outputs | Lecture, discussion, exercises. | Previously read the section (s). Complement the class by doing exercises from the section. | [Lue, 4.1 & 4.2] |
| Session 10 | <b>Laboratory:</b> solution of differential equations in Matlab  |                                 |  |                  |
| Session 11 | <b>Theory:</b><br>Dynamic diagrams   | Lecture, discussion, exercises. | Previously read the section (s). Complement the class by doing exercises from the section. | [Lue, 4.3]       |
| Session 12 | <b>Laboratory:</b> dynamic diagrams and introduction to Simulink   |                                 |  |                  |
| Session 13 | <b>Theory:</b><br>Homogeneous linear systems in discrete time. State transition matrix                           | Lecture, discussion, exercises. | Previously read the section (s). Complement the class by doing exercises from the section. | [Lue, 4.4]       |
| Session 14 | <b>Laboratory:</b> simulation of linear systems in discrete time in Matlab and Simulink                          |                                 |  |                  |
| Session 15 | <b>Theory:</b><br>Homogeneous linear systems in continuous time. State transition matrix                         | Lecture, discussion, exercises. | Previously read the section (s). Complement the class by doing exercises from the section. | [Lue, 4.6]       |
| Session 16 | <b>Laboratory:</b> simulation of linear systems in continuous time in Matlab and Simulink                        |                                 |  |                  |

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|            |  |                                  |  |                  |
| Session 17 | <b>Theory:</b><br>Calculation of the state transition matrix for linear systems with constant coefficients using square matrix functions | Lecturer, discussion, exercises. | Previously read the section (s). Complement the class by doing exercises from the section. | [Bay, 5.4]       |
| Session 18 | <b>Laboratory:</b> square matrix functions   |                                  |  |                  |
| Session 19 | <b>Theory:</b><br>Linear systems with inputs: superposition principle  | Lecture, discussion, exercises.  | Previously read the section (s). Complement the class by doing exercises from the section. | [Lue, 4.5 & 4.7] |
| Session 20 | <b>Second partial exam</b>   |                                  |  |                  |
| Session 21 | <b>Theory:</b><br>Linear systems with constant coefficients. Eigenvalues and eigenvectors of the matrix of the system                    | Lecture, discussion, exercises.  | Previously read the section (s). Complement the class by doing exercises from the section. | [Lue, 5.1 & 5.2] |
| Session 22 | <b>Laboratory:</b> values and eigenvectors of the system matrix  |                                  |  |                  |
| Session 23 | <b>Theory:</b><br>Change of bases and diagonalization of systems   | Lecture, discussion, exercises.  | Previously read the section (s). Complement the class by doing exercises from the section. | [Lue, 5.3]       |
| Session 24 | <b>Laboratory:</b> systems diagonalization   |                                  |  |                  |
| Session 25 | <b>Theory:</b><br>Non-diagonalizable systems. Diagonalization test   | Lecture, discussion, exercises.  | Previously read the section (s). Complement the class by doing exercises from the section. | [Bay, 4.4]       |

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| Session<br>26 | <b>Theory:</b><br>Canonical form of<br>Jordan I: structure  | Lecture,<br>discussion,<br>exercises.     | Previously read the<br>section (s). Complement<br>the class by doing<br>exercises from the<br>section. | [Bay, 4.4]          |
|               | <b>Laboratory:</b> structure of the canonical form of Jordan  |   |  |                     |
| Session<br>27 | <b>Theory:</b><br>Canonical form of<br>Jordan II:<br>generalized<br>eigenvectors  | Lecture,<br>discussion,<br>exercises.     | Previously read the<br>section (s). Complement<br>the class by doing<br>exercises from the<br>section. | [Bay, 4.4]          |
| Session<br>28 | <b>Theory:</b><br>Jordan III canonical<br>form: chains of<br>generalized<br>eigenvectors and<br>generalized modal<br>matrix | Lecture,<br>discussion,<br>exercises.     | Previously read the<br>section (s). Complement<br>the class by doing<br>exercises from the<br>section. | [Bay, 4.4]          |
| Session<br>29 | <b>Laboratory:</b> generalized modal matrix   |   |  |                     |
| Session<br>30 | <b>Third partial exam</b>   |   |  |                     |
| Session<br>31 | <b>Theory:</b><br>Jordan IV canonical<br>form: calculation of<br>the state transition<br>matrix                             | Masterclass,<br>discussion,<br>exercises. | Previously read the<br>section (s). Complement<br>the class by doing<br>exercises from the<br>section. | [Bay, 4.4]          |
| Session<br>32 | <b>Theory:</b><br>Introduction to the<br>analysis of nonlinear<br>systems. Balance<br>points. linearization                 | Lecture,<br>discussion,<br>exercises.     | Previously read the<br>section (s). Complement<br>the class by doing<br>exercises from the<br>section. | [Lue, 9.1 -<br>9.4] |

## 10. Success factors for this course

A series of actions are suggested below that can contribute significantly to the achievement of goals and consequently promote a successful experience in this course:

1. Plan and organize the individual work time that you will dedicate to it. to the course

2. Organize the study site and materials
3. Have a study group, seek the support of colleagues
4. Cultivate discipline and perseverance, work weekly, do not allow topics or work to accumulate
5. Constantly carry out a Self-evaluation, determine if the actions carried out are productive or if, on the contrary, strategies should be changed
6. Attend the teacher's consultation hours, participate in class, never be left with doubts
7. Use the spaces for consultation and resolution of doubts, such as Sala Gauss and Sala Knuth
8. Promote spaces for rest and mental hygiene, try to have good sleep habits
9. Have present at all times values such as honesty and sincerity, in the end it is not just about passing an exam, it is about learning and acquiring knowledge. Fraud is self-deception

## **11. Bibliography and resources**

[Lue] D. Luenberger, Introduction to Dynamic Systems: Theory, Models & Applications. Wiley & Sons. 1979

## **12. Bibliography and supplementary resources**

[Bay] J. Bay, Fundamentals of linear state space systems. McGraw-Hill, 1999.

[Oga] K. Ogata, System Dynamics. Prentice-Hall. 1987.

## **13. Agreements for the development of the course**

### **GENERAL RULES**

Lectures will be given in English. Questions and comments by students are allowed in Spanish but will be answered in English unless not understood previously. Homeworks will be solved in English and Exams will be allowed to be solved in Spanish.

There will be no approximation of grades at the end of the semester. The grades will only be



changed based on TIMELY claims within the time limits determined by the Academic Regulations. If for reasons of force majeure, the student misses a partial or quiz, he / she must follow the regular procedure determined by the Academic Regulations to present substitutes. There will be no informal agreements in this regard. No student will be exempted from any exam. The course does not have any type of Bonus. The monitoring is not regular but on demand. The monitoring schedule can be used to make up classes and / or exams.

If the student shows up 20 minutes after starting a partial or final evaluation, he / she will not be able to present it and must request a supplementary one following the institutional regulations.

### **DISCIPLINARY PROCESSES-FRAUD IN EVALUATIONS**

Taking into account the training-preventive and disciplinary regulations of the Universidad del Rosario, and the certainty that fraudulent actions go against the teaching and learning processes, any corrupt act related to this subject will be notified to the corresponding academic secretariat so that the due disciplinary process begins. It is recommended that students read these regulations to know the reasons, procedures and consequences that this type of actions may cause, as well as their rights and duties associated with this type of procedure.

## **14. Respect and non-discrimination**

If you have a disability, whether it is visible or not, and require some type of support to be on an equal footing with other students, please inform your teacher to that reasonable adjustments to the course can be made as soon as possible. Likewise, if you do not have the technological resources required for the development of the course, please inform the Academic Secretary of your program or the Student Office in a timely manner, so that your request can be met on time.

Remember that it is the duty of all people to respect the rights of those who are part of the Rosarista community. Any situation of harassment, sexual harassment, discrimination or bullying, whether in person or virtual, is unacceptable. Anyone who feels in any of these situations can report its occurrence by contacting the team of the Coordination of Psychology and Quality of Life of the Dean of the University Environment (Telephone or WhatsApp 322 2485756).