

# **Modeling of dynamical systems**

# Subject guide

Last update: January 2021

### 1. General information

Name of the subject	Modeling of dynamical systems
	ivioueiiiig or dynamical systems
Code	11310040
Type of subject	Compulsory
Number of credits	3
Type of credit	2A + 1B
Weekly work hours with direct	80
teacher guidance	
Weekly Hours of independent	64
student work	
Prerequisites	Linear Algebra, Differential Equations
Corequisites	None
Schedule	
leader	Martín Andrade Restrepo
Lounge	

### 2. Lecturer and monitor information

Name of Lecturer	Martín Andrade Restrepo		
professional Profile			
Institutional email	Martin.andrade@urosario.edu.co		
Place and hours of	Edificio Cabal Of. 402		
attention	Wednesdays, Fridays 13:00 – 14:00		
Web page or other means (optional)			



Name of assistant	
professor or monitor	
Professional profile	
Institutional email	
Place and hours of attention:	
Web page, Skype or other means (optional)	

#### 3. Summary and purposes of the course

The course addresses the modeling of dynamical systems using differential and difference equations. This is extremely useful for understanding and predicting the behavior of different physical, social and computational phenomena, etc. Once the generalities of the systems of differential and difference equations have been exposed, the main analysis techniques of linear models are presented, emphasizing the representation in state space. In addition, the student is introduced to the use of specialized software to simulate the behavior of dynamical systems.

### 4. Fundamental concepts

- 1. Dynamic models in continuous time
- 2. Dynamic models in discrete time
- 3. Simulation of dynamical systems using specialized software
- 4. Representations in state space
- 5. Analysis of linear and time-invariant systems
- 6. Equilibrium points and stability
- 7. Linearization of dynamic systems

#### 5. Expected learning outcomes (RAE)

- 1. Learn typical models of systems through differential and difference equations.
- 2. Simulate the behavior of dynamical systems using specialized software.
- 3. Understand representations in state spaces of dynamical systems.
- 4. Manage different methods of analysis of linear systems.
- 5. Carry out the linearization of a system represented in state space.



## 6. Course modality

Remote mode: All students will be connected remotely from their homes or locations outside the University.

## 7. Learning strategies

- 1. Lectures where the theoretical foundations will be taught.
- 2. Tasks where students will work independently on the content seen.
- 3. Laboratories where the methods and algorithms addressed in the Lectures will be implemented.
- 4. Final project where students must apply the tools learned during the semester to solve a real problem.

#### 8. Evaluations

Topic	Activities	Percentage	Exam dates
Those corresponding to sessions 1 to 7	Individual written evaluation - First cut	20	Week 4
Those corresponding to sessions 9 to 19	Individual written evaluation - Second cut	20	Week 10
Those corresponding to sessions 21 to 29	Individual written evaluation - Third cut	20	Week 15
All sessions	Presentation and document - Final project	15	exam week



Laboratories and workshops	Individual Reports	25	Every
	and / or group Reports		week

# 9. Activity program

	Date	Topic	Description of the activity	Independent work of the student	Resources that support the activity (bibliograph y and other support resources)
done	Session 1	Presentation of the course.  Theory: Dynamic phenomena. Typical examples	Lecture, discussion, exercises.	Previously read the section (s). Complement the class by doing exercises from the section.	[Lue, 1.1- 1.4]
done	Session 2		Laboratory: intro	duction to Matlab	
done	Session 3	Theory: Difference equations. Existence and uniqueness of solutions. Examples	Lecture, discussion, exercises.	Previously read the section (s). Complement the class by doing exercises from the section.	[Lue, 2.1- 2.5]
done	Session 4	Laboratory: implementation of difference equations in Matlab			
10 de ag	Session 5	Theory: Linear difference equations. Linear equations with constant coefficients	Lecture, discussion, exercises.	Previously read the section (s). Complement the class by doing exercises from the section.	[ <b>Lue</b> , 2.6-2.7]
12 de ag	Session 6 ost	Laboratory: linear difference equations			
17 de a	Session 7	Theory: Differential equations. Existence	Lecture, discussion, exercises.	Previously read the section (s). Complement the class by doing	[ <b>Lue</b> , 2.8- 2.10]



		and uniqueness of solutions. Linear differential equations. Examples		exercises from the section.	
19 de agos	Session 8		First par	tial exam	
24 de agos	Session 9	Theory: Systems of first order equations. Representation of systems in state space. Inputs and outputs	Lecture, discussion, exercises.	Previously read the section (s). Complement the class by doing exercises from the section.	[ <b>Lue</b> , 4.1 & 4.2]
26 de ago	Session 10	Laborato	ory: solution of diff	erential equations in Matlab	
31 de agos	Session 11	Theory: Dynamic diagrams	Lecture, discussion, exercises.	Previously read the section (s). Complement the class by doing exercises from the section.	[Lue, 4.3]
2 de septiem	Session	Laboratory	y: dynamic diagram	s and introduction to Simulir	nk
7 de septie	Session 13	Theory: Homogeneous linear systems in discrete time. State transition matrix	Lecture, discussion, exercises.	Previously read the section (s). Complement the class by doing exercises from the section.	[Lue, 4.4]
9 de septi	Session 14 emb	<b>Laboratory:</b> simulation	on of linear system	s in discrete time in Matlab a	nd Simulink
14 de septie	Session 15 mb	Theory: Homogeneous linear systems in continuous time. State transition matrix	Lecture, discussion, exercises.	Previously read the section (s). Complement the class by doing exercises from the section.	[ <b>Lue</b> , 4.6]
16 de s <b>e</b>	Session 16 ptiemb	<b>Laboratory:</b> simul	•	ems in continuous time in Ma ulink	atlab and



21 de septier	Session 17 nb	Theory: Calculation of the state transition matrix for linear systems with constant coefficients using square matrix functions	Lecturer, discussion, exercises.	Previously read the section (s). Complement the class by doing exercises from the section.	[ <b>Bay</b> , 5.4]
23 de septier	Session nb <sub>8</sub>		Laboratory: squar	e matrix functions	
28 de septie	Session 19 mb	Theory: Linear systems with inputs: superposition principle	Lecture, discussion, exercises.	Previously read the section (s). Complement the class by doing exercises from the section.	[ <b>Lue</b> , 4.5 & 4.7]
30 de septiemb	Session 20		Second pa	rtial exam	
5 de octubr	Session 21	Theory: Linear systems with constant coefficients. Eigenvalues and eigenvectors of the matrix of the system	Lecture, discussion, exercises.	Previously read the section (s). Complement the class by doing exercises from the section.	[ <b>Lue</b> , 5.1 & 5.2]
7 de octubr	Session 22	Laboratory: values and eigenvectors of the system matrix			(
12 de octubr	Session 23	Theory: Change of bases and diagonalization of systems	Lecture, discussion, exercises.	Previously read the section (s). Complement the class by doing exercises from the section.	[ <b>Lue</b> , 5.3]
14 de octubr	Session 24		Laboratory: system	ms diagonalization	
19 de octubr	Session 25	Theory: Non-diagonalizable systems. Diagonalization test	Lecture, discussion, exercises.	Previously read the section (s). Complement the class by doing exercises from the section.	[Bay, 4.4]



	Session	Theory:	Lecture,	Previously read the	[Bay, 4.4]
	26	Canonical form of Jordan I:structure	discussion, exercises.	section (s). Complement the class by doing	
		Jordan i.structure	exercises.	exercises from the	
21 de	octubr			section.	
		Laborat	ory: structure of th	e canonical form of Jordan	
	Session	Theory:	Lecture,	Previously read the	[ <b>Bay</b> , 4.4]
	27	Canonical form of	discussion,	section (s). Complement	
26 de oct	ubr	Jordan II:	exercises.	the class by doing exercises from the	
		generalized eigenvectors		section.	
	Session	Theory:	Lecture,	Previously read the	[Bay, 4.4]
	28	Jordan III canonical	discussion,	section (s). Complement	
	_	form: chains of	exercises.	the class by doing	
28 de oct	ubr	generalized		exercises from the	
		eigenvectors and generalized modal		section.	
		matrix			
	<u>Se</u> ssion				
2 de novie	mbi		Laboratory: genera	alized modal matrix	
4 de novier	nβession -30	Third partial exam			
	Session	Theory:	Masterclass,	Previously read the	[ <b>Bay</b> , 4.4]
9 de noviei	<del>-31</del>	Jordan IV canonical	discussion,	section (s). Complement	
9 de noviei	ПО	form: calculation of the state transition	exercises.	the class by doing exercises from the	
		matrix		section.	
	Session	Theory:	Lecture,	Previously read the	[ <b>Lue</b> , 9.1 -
	32	Introduction to the	discussion,	section (s). Complement	9.4]
11 de nov	viemb	analysis of nonlinear	exercises.	the class by doing	
I I de IIO		systems. Balance points.linearization		exercises from the section.	
		points.inteditzation		Section.	

## 10. Success factors for this course

A series of actions are suggested below that can contribute significantly to the achievement of goals and consequently promote a successful experience in this course:

1. Plan and organize the individual work time that you will dedicate to it. to the course



- 2. Organize the study site and materials
- 3. Have a study group, seek the support of colleagues
- 4. Cultivate discipline and perseverance, work weekly, do not allow topics or work to accumulate
- 5. Constantly carry out a Self-evaluation, determine if the actions carried out are productive or if, on the contrary, strategies should be changed
- 6. Attend the teacher's consultation hours, participate in class, never be left with doubts
- 7. Use the spaces for consultation and resolution of doubts, such as Sala Gauss and Sala Knuth
- 8. Promote spaces for rest and mental hygiene, try to have good sleep habits
- 9. Have present at all times values such as honesty and sincerity, in the end it is not just about passing an exam, it is about learning and acquiring knowledge. Fraud is self-deception

#### 11. Bibliography and resources

[Lue] D. Luenberger, Introduction to Dynamic Systems: Theory, Models & Applications. Wiley & Sons. 1979

### 12. Bibliography and supplementary resources

[Bay] J. Bay, Fundamentals of linear state space systems. McGraw-Hill, 1999.

[Oga] K. Ogata, System Dynamics. Prentice-Hall. 1987.

#### 13. Agreements for the development of the course

#### **GENERAL RULES**

Lectures will be given in English. Questions and comments by students are allowed in Spanish but will be answered in English unless not understood previously. Homeworks will be solved in English and Exams will be allowed to be solved in Spanish.

There will be no approximation of grades at the end of the semester. The grades will only be



changed based on TIMELY claims within the time limits determined by the Academic Regulations. If for reasons of force majeure, the student misses a partial or quiz, he / she must follow the regular procedure determined by the Academic Regulations to present substitutes. There will be no informal agreements in this regard. No student will be exempted from any exam. The course does not have any type of Bonus. The monitoring is not regular but on demand. The monitoring schedule can be used to make up classes and / or exams.

If the student shows up 20 minutes after starting a partial or final evaluation, he / she will not be able to present it and must request a supplementary one following the institutional regulations.

#### DISCIPLINARY PROCESSES-FRAUD IN EVALUATIONS

Taking into account the training-preventive and disciplinary regulations of the Universidad del Rosario, and the certainty that fraudulent actions go against the teaching and learning processes, any corrupt act related to this subject will be notified to the corresponding academic secretariat so that the due disciplinary process begins. It is recommended that students read these regulations to know the reasons, procedures and consequences that this type of actions may cause, as well as their rights and duties associated with this type of procedure.

### 14. Respect and non-discrimination

If you have a disability, whether it is visible or not, and require some type of support to be on an equal footing with other students, please inform your teacher to that reasonable adjustments to the course can be made as soon as possible. Likewise, if you do not have the technological resources required for the development of the course, please inform the Academic Secretary of your program or the Student Office in a timely manner, so that your request can be met on time.

Remember that it is the duty of all people to respect the rights of those who are part of the Rosarista community. Any situation of harassment, sexual harassment, discrimination or bullying, whether in person or virtual, is unacceptable. Anyone who feels in any of these situations can report its occurrence by contacting the team of the Coordination of Psychology and Quality of Life of the Dean of the University Environment (Telephone or WhatsApp 322 2485756).