

All PDA's are defined as the 6-tuple:  $(Q, \Sigma, \Gamma, \delta, q_0, F)$ , where:

$Q$ : State Set

$\Sigma$ : Automaton Alphabet

$\Gamma$ : Stack Alphabet

$\delta: Q \times \Sigma_\epsilon \times \Gamma_\epsilon \rightarrow P(Q \times \Gamma_\epsilon)$ : Transition Function

$q_0$ : Starting State

$F$ : Accepting State Set

### Exercise 1:

Draw the PDA for the language:

$$L_1 = \{a^i b^j c^k \mid i = j \vee j = k, \forall i, j, k \geq 0\}$$

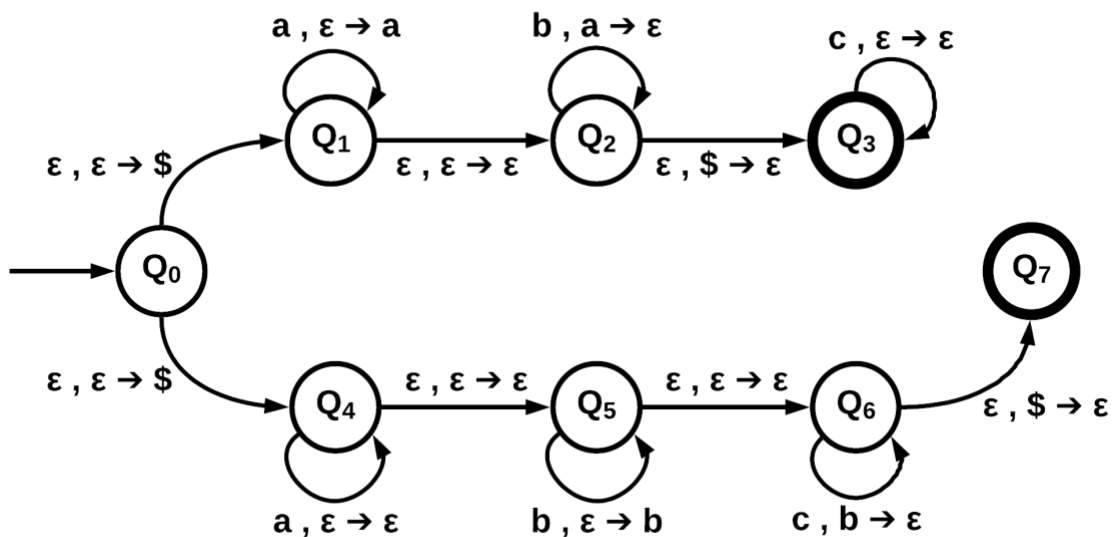
$$Q = \{Q_0, \dots, Q_7\}$$

$$\Sigma = \{a, b, c\}$$

$$\Gamma = \{a, b\}$$

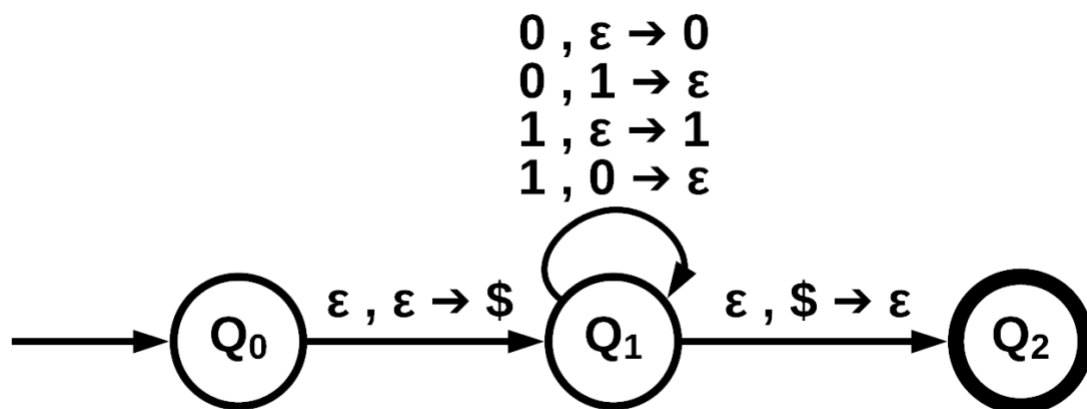
$Q_0$  is the starting state

$$F = \{Q_3, Q_7\}$$



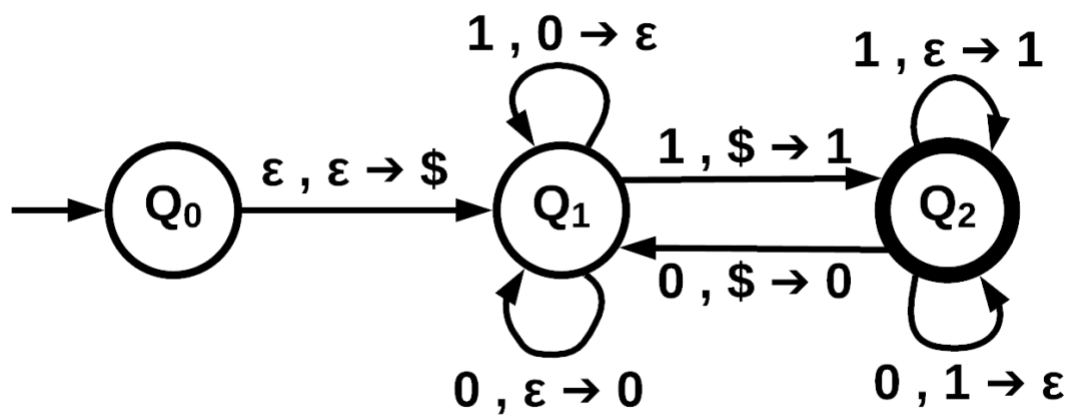
## Exercise 2:

Draw the PDA for the language:

 $L_2 = \{w \mid w \text{ has as many 1s as 0s}\}$  $Q = \{Q_0, Q_1, Q_2\}$  $\Sigma = \Gamma = \{0, 1\}$  $Q_0$  is the starting state $F = \{Q_2\}$ 

## Exercise 3:

Draw the PDA for the language:

 $L_3 = \{w \mid w \text{ has more 1s than 0s}\}$  $Q = \{Q_0, Q_1, Q_2\}$  $\Sigma = \Gamma = \{0, 1\}$  $Q_0$  is the starting state $F = \{Q_2\}$ 

## Exercise 4:

Draw the PDA for the language:

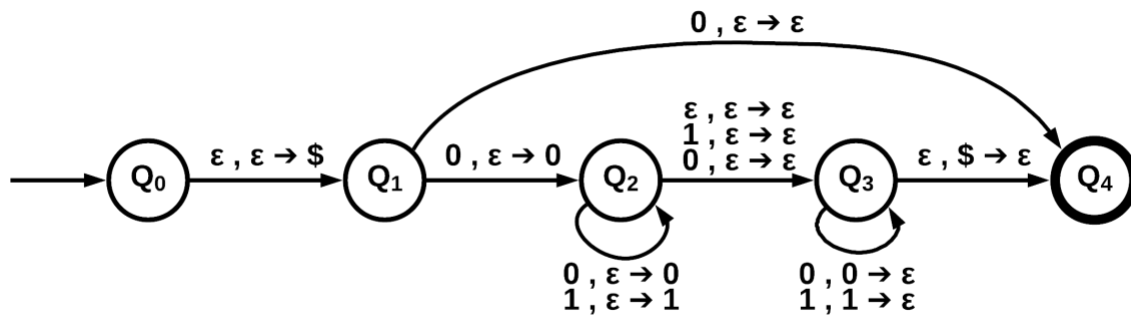
$L_4 = \{w \mid w \text{ is a palindrome and starts with } 0\}$

$Q = \{Q_0, Q_1, Q_2, Q_3, Q_4\}$

$\Sigma = \Gamma = \{0, 1\}$

$Q_0$  is the starting state

$F = \{Q_4\}$



## Exercise 5:

Draw the PDA for the language:

$L_5 = \{w \mid w \text{ has odd length and the middle symbol is a } 0\}$

$Q = \{Q_0, Q_1, Q_2, Q_3\}$

$\Sigma = \{0, 1\}$

$\Gamma = \{1\}$

$Q_0$  is the starting state

$F = \{Q_3\}$

