selection • EN

Multiselect (selection)

William has recently been working on select algorithms! In case you're not already familiar with them, these algorithms receive an array of length M and an index $K \leq M-1$ in input. Then, through M steps they rearrange the array contents, so that the K-th element is in position K of the array, with all smaller elements sitting on its left side, and all larger elements on its right side. No relative order, however, can be assumed between elements within a same side.

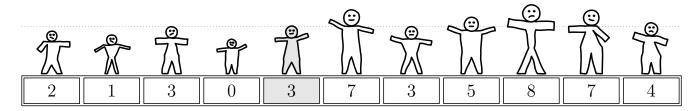


Figure 1: A possible result of a select routine with K=4.

The select algorithm is ready, however, the problem William has to tackle requires a bit more work. He needs to process a very large array of length M, so that at the end N given different indexes $K_0, \ldots K_{N-1}$ are all partitioning the array.

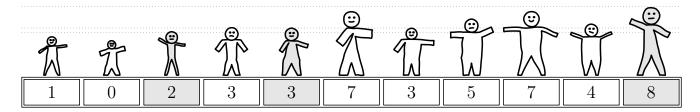


Figure 2: A possible result of a multi-select routine with N=3 and indexes 2, 4 and 10.

Since William is lazy, he doesn't want to write a new algorithm from scratch! Instead, he plans to re-use the *select* algorithm multiple times to achieve the desired effect. For example, assume that M=11, N=3 and the indexes K_i are 2, 4, 10, as in Figure 2. One possible way to achieve the effect could be:

- first, run select on the whole vector with K=4 (as in Figure 1), spending 11 algorithm steps;
- then, run select on the sub-vector [0...3] with K=2, which requires 4 algorithm steps;
- finally, run select on the sub-vector [5...10] with K=10, which requires 6 algorithm steps.

Overall, the procedure will require 11 + 4 + 6 = 21 algorithm steps. Notice that this is not the only possible way to obtain the result! Another could be:

- run select on the whole vector with K = 10, spending 11 steps;
- run select on the sub-vector [0...9] with K=2, spending 10 steps;
- run select on the sub-vector [2...9] with K=4, spending 8 steps.

With this other strategy, the procedure will require 11 + 10 + 8 = 29 steps...not so good! Help William perform his task, minimising the number of algorithm steps required.

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Among the attachments of this task you may find a template file **selection**.* with a sample incomplete implementation.

Input

The first line contains the two integers N and M. The second line contains N integers K_i .

Output

You need to write a single line with an integer: the minimum total number of algorithm steps required to multi-select the given indexes from an array of length M.

Constraints

- $1 \le N \le 1000$.
- $1 \le M \le 10^8$.
- $0 \le K_0 < K_1 < \ldots < K_{N-1} < M$.

Scoring

Your program will be tested against several test cases grouped in subtasks. In order to obtain the score of a subtask, your program needs to correctly solve all of its test cases.

- Subtask 1 (0 points)	Examples.
- Subtask 2 (19 points)	N = M.
- Subtask 3 (25 points)	$N \leq 5$.
- Subtask 4 (40 points)	$N \le 100.$
- Subtask 5 (16 points)	No additional limitations.

Examples

input	output
3 11 2 4 10	21
3 101 49 50 51	152

Explanation

The **first sample case** is the one described in the problem statement.

In the **second sample case**, one way of achieving the lowest amount of steps is to first select $K_0 = 49$ in 101 steps, then $K_2 = 51$ in further 51 steps, getting $K_1 = 50$ in place for free.

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