

Q2 prove $\text{rev-append } l1\ l2 = \text{rev-append } l1\ l2$

proof by structural induction on $l1$ (list)

Base case: $l1 = []$

$$\begin{aligned} 1. \text{rev-append } []\ l2 &\stackrel{\text{by rev-append}}{\Rightarrow} \text{append (rev } [])\ l2 \stackrel{\text{by rev}}{\Rightarrow} \text{append } []\ l2 \stackrel{\text{by append}}{\Rightarrow} l2 \\ 2. \text{rev-append } []\ l2 &\stackrel{\text{by rev-append}}{\Rightarrow} l2 \end{aligned}$$

property holds for base case $l1 = []$

Case: $l1 = h::t$

IH: $\text{rev-append } t\ l2 = \text{rev-append } t\ l2$: assumption

$$\begin{aligned} \text{rev-append } l1\ l2 &\stackrel{\text{by rev-append}}{\Rightarrow} \text{append (rev } l1)\ l2 \stackrel{\text{by rev}}{\Rightarrow} \text{append (rev } t)(\text{rev } h)\ l2 \\ &\stackrel{\text{by def of append}}{\Rightarrow} \text{append (rev } t)(\text{rev } h)\ l2 \stackrel{\text{for single element } @ \Rightarrow ::}{\Rightarrow} \text{rev } t @ (h :: l2) \stackrel{\text{by def of append}}{\Rightarrow} \text{append (rev } t)\ h :: l2 \end{aligned}$$

$$\begin{aligned} &\stackrel{\text{by def rev-append}}{\Rightarrow} \text{rev-append } t\ (h :: l2) \stackrel{\text{IH}}{\Rightarrow} \text{rev-append } t\ (h :: l2) \\ &\stackrel{\text{by def rev-append (pointback)}}{\Rightarrow} \text{rev-append } (h :: t)\ l2 \stackrel{\text{def of } l1}{\Rightarrow} \text{rev-append } l1\ l2 \quad \square \end{aligned}$$