Describing Variation & Patterns of Diversity

BIOL 1435

January 31, 2023

Icebreaker

Name, Year, Major, and what was the last song you listened to today?

Overview

1. ATGC's of life & encoding DNA

2. Measures of sequence diversity

3. In class coding exercise

Overview

1. ATGC's of life & encoding DNA

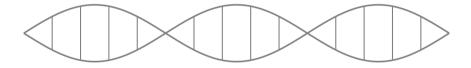
2. Measures of sequence diversity

3. In class coding exercise

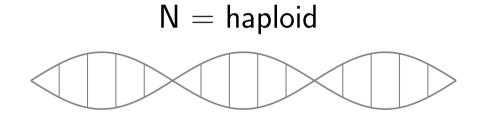
DNA consists of four nucleotides

ATGC

DNA is organized onto chromosomes

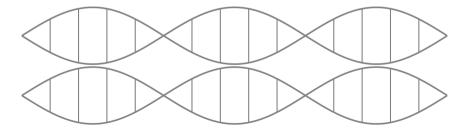


Ploidy (#N): number of sets of chromosomes



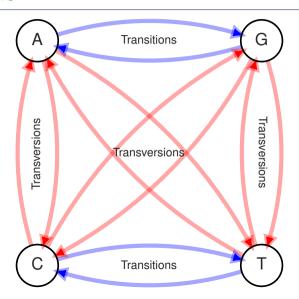
Ploidy (#N): number of sets of chromosomes

2N = diploid



Q: How does genetic variation arise?

A: Mutations



How do we encode DNA?

$$m$$
 (sites) $\times n$ (chromosomes)

How do we encode DNA?

Genotype matrices

0 = reference or ancestral allele

1 =alternative or derived allele

Genotype matrices

```
\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix}
```

Genotype matrices

$$egin{bmatrix} egin{bmatrix} 0 & 0 & 0 & 0 & 0 \ 0 & 1 & 1 & 0 & 1 \ 0 & 1 & 0 & 1 & 1 \ 0 & 0 & 0 & 0 & 1 \ 1 & 0 & 0 & 0 & 0 \end{bmatrix} = egin{bmatrix} 0 & 1 & 1 & 0 & 1 \ 0 & 1 & 0 & 1 & 1 \ 0 & 0 & 0 & 0 & 1 \ 1 & 0 & 0 & 0 & 0 \end{bmatrix}$$

Some terminology...

- Single nucleotide polymorphism (SNP)
- Single nucleotide variant (SNV)
- Variant site
- Segregating site

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How would you summarize this genotype matrix?

```
\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix}
```

Measurements of genetic variation

- Segregating sites (S)
- Site frequency spectrum (SFS)
- Gene diversity (h & H)
 - Also referred to as expected heterozygosity
- Nucleotide diversity ($\Pi \& \pi$)

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Definition

A segregating site is a site that is polymorphic in the data—i.e., there are multiple alleles observed.

```
\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix}
```

$$\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix} \rightarrow \begin{bmatrix} 0 \\ 1 \\ 1 \\ 1 \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix} \rightarrow \begin{bmatrix} 0 \\ 1 \\ 1 \\ 1 \\ 1 \end{bmatrix} \rightarrow S = 4$$

Measurements of genetic variation

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Definition

Minor allele frequency spectrum: Histogram of the frequency of the less common allele which range from 1/n to 0.5 where n is the total number of chromosomes.

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Derived allele frequency spectrum: Histogram of the frequency of the derived allele—normally determined by the use of an outgroup—which range from 1/n to (n-1)/n.

Definition

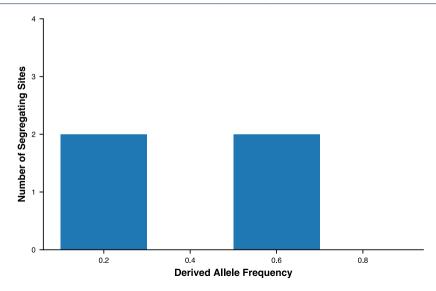
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Note

 $\label{eq:minor_spectrum} \mbox{Minor allele frequency spectrum} = \mbox{Folded SFS}$

Derived allele frequency spectrum = Unfolded SFS



Measurements of genetic variation

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Definition

Gene diversity is the probability that two random DNA sequences are different.

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Equation

$$h = 1 - \sum_{i=1}^{m} p_i^2 \tag{1}$$

Where p_i is the frequency of the i^{th} allele out of m observed alleles.

$$H = \frac{1}{L} \sum_{i=1}^{L} h_j \tag{2}$$

Where h_i is the gene diversity for site j and L is to the total number of sites.

Dave's tips and tricks

Note

$$h = 1 - (p^2 + q^2)$$

Where p is the frequency of the derived/alternate allele and q = (1 - p)

```
\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix}
```

$$\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix} \rightarrow \begin{bmatrix} 1 - (1^2 + 0^2) \\ 1 - (2^2/5^2 + 3^2/5^2) \\ 1 - (2^2/5^2 + 3^2/5^2) \\ 1 - (1^2/5^2 + 4^2/5^2) \\ 1 - (1^2/5^2 + 4^2/5^2) \end{bmatrix}$$

$$egin{bmatrix} 0 & 0 & 0 & 0 & 0 \ 0 & 1 & 1 & 0 & 1 \ 0 & 1 & 0 & 1 & 1 \ 0 & 0 & 0 & 0 & 1 \ 1 & 0 & 0 & 0 & 0 \end{bmatrix}
ightarrow egin{bmatrix} 1 - (1^2 + 0^2) \ 1 - (2^2/5^2 + 3^2/5^2) \ 1 - (2^2/5^2 + 3^2/5^2) \ 1 - (1^2/5^2 + 4^2/5^2) \ 1 - (1^2/5^2 + 4^2/5^2) \end{bmatrix}
ightarrow h_j = egin{bmatrix} 0 \ 12/25 \ 12/25 \ 8/25 \ 8/25 \ 8/25 \ \end{bmatrix}$$

$$\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix} \rightarrow \begin{bmatrix} 1 - (1^2 + 0^2) \\ 1 - (2^2/5^2 + 3^2/5^2) \\ 1 - (2^2/5^2 + 3^2/5^2) \\ 1 - (1^2/5^2 + 4^2/5^2) \end{bmatrix} \rightarrow h_j = \begin{bmatrix} 0 \\ 12/25 \\ 12/25 \\ 8/25 \\ 8/25 \end{bmatrix}$$

 $H = 40/25 \times 1/5 = 8/25$

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Equation

$$\Pi = \frac{\sum_{i < j} k_{ij}}{\binom{n}{2}} \tag{3}$$

Where k_{ij} is the number of nucleotide differences between the i^{th} and j^{th} sequence in the sample and the denominator represents the number of unique comparisons being made between n sequences.

$$\pi = \frac{\Pi}{I} \tag{4}$$

Where L is to the total number of sites.

Dave's tips and tricks

Note

$$\binom{n}{2} = \frac{n(n-1)}{2}$$

```
\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix}
```

```
\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix} \quad \begin{matrix} (0+0+0+0) = 0 \\ (3+1+1+1) = 6 \\ \rightarrow (3+1+2+0) = 6 \\ (1+1+1+1) = 4 \\ (4+0+0+0) = 4 \end{matrix}
```

$$\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix} \quad \begin{matrix} (0+0+0+0) = 0 \\ (3+1+1+1) = 6 \\ \rightarrow (3+1+2+0) = 6 \rightarrow \Pi = 20 \div \frac{5(5-1)}{2} = 2 \\ (1+1+1+1) = 4 \\ (4+0+0+0) = 4 \end{matrix}$$

$$\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix} \xrightarrow{ \begin{pmatrix} (0+0+0+0) = 0 \\ (3+1+1+1) = 6 \\ \to (3+1+2+0) = 6 \to \Pi = 20 \div \frac{5(5-1)}{2} = 2 \\ (1+1+1+1) = 4 \\ (4+0+0+0) = 4 \end{bmatrix} = 2$$

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