## Describing Variation & Patterns of Diversity

**BIOL 1435** 

January 31, 2023

## **Icebreaker**

Name, Year, Major, and what was the last song you listened to today?

## **Overview**

1. ATGC's of life & encoding DNA

2. Measures of sequence diversity

3. In class coding exercise

## **Overview**

## 1. ATGC's of life & encoding DNA

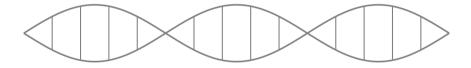
2. Measures of sequence diversity

3. In class coding exercise

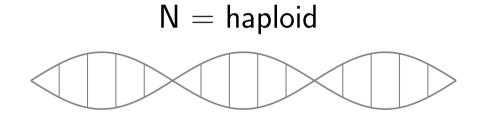
## **DNA** consists of four nucleotides

## **ATGC**

## **DNA** is organized onto chromosomes

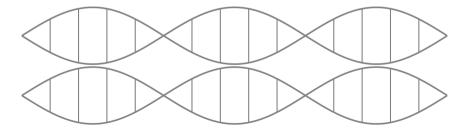


## Ploidy (#N): number of sets of chromosomes



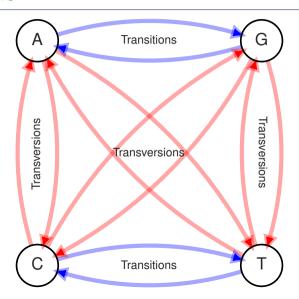
## Ploidy (#N): number of sets of chromosomes

## 2N = diploid



# Q: How does genetic variation arise?

## **A:** Mutations



## How do we encode DNA?

$$m$$
 (sites)  $\times n$  (chromosomes)

### How do we encode DNA?

## **Genotype matrices**

0 = reference or ancestral allele

1 =alternative or derived allele

## **Genotype matrices**

```
\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix}
```

## **Genotype matrices**

$$egin{bmatrix} egin{bmatrix} 0 & 0 & 0 & 0 & 0 \ 0 & 1 & 1 & 0 & 1 \ 0 & 1 & 0 & 1 & 1 \ 0 & 0 & 0 & 0 & 1 \ 1 & 0 & 0 & 0 & 0 \end{bmatrix} = egin{bmatrix} 0 & 1 & 1 & 0 & 1 \ 0 & 1 & 0 & 1 & 1 \ 0 & 0 & 0 & 0 & 1 \ 1 & 0 & 0 & 0 & 0 \end{bmatrix}$$

## Some terminology...

- Single nucleotide polymorphism (SNP)
- Single nucleotide variant (SNV)
- Variant site
- Segregating site

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## How would you summarize this genotype matrix?

```
\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix}
```

## Measurements of genetic variation

- Segregating sites (S)
- Site frequency spectrum (SFS)
- Gene diversity (h & H)
  - Also referred to as expected heterozygosity
- Nucleotide diversity ( $\Pi \& \pi$ )

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#### Definition

A segregating site is a site that is polymorphic in the data—i.e., there are multiple alleles observed.

```
\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix}
```

$$\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix} \rightarrow \begin{bmatrix} 0 \\ 1 \\ 1 \\ 1 \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix} \rightarrow \begin{bmatrix} 0 \\ 1 \\ 1 \\ 1 \\ 1 \end{bmatrix} \rightarrow S = 4$$

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#### **Definition**

Minor allele frequency spectrum: Histogram of the frequency of the less common allele which range from 1/n to 0.5 where n is the total number of chromosomes.

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Derived allele frequency spectrum: Histogram of the frequency of the derived allele—normally determined by the use of an outgroup—which range from 1/n to (n-1)/n.

#### Definition

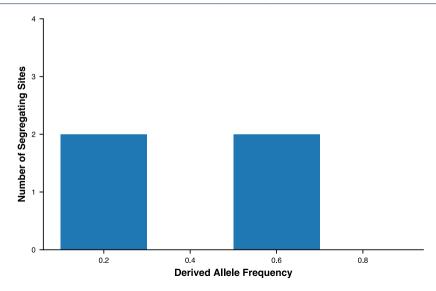
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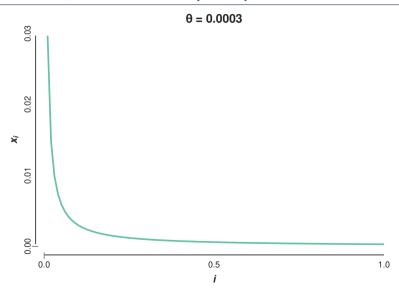
Derived allele frequency spectrum: Histogram of the frequency of the derived allele—normally determined by the use of an outgroup—which range from 1/n to (n-1)/n.

#### Note

 $\label{eq:minor_spectrum} \mbox{Minor allele frequency spectrum} = \mbox{Folded SFS}$ 

Derived allele frequency spectrum = Unfolded SFS





## Measurements of genetic variation

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#### Definition

Gene diversity is the probability that two random DNA sequences are different.

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#### Equation

$$h = 1 - \sum_{i=1}^{m} p_i^2 \tag{1}$$

Where  $p_i$  is the frequency of the  $i^{th}$  allele out of m observed alleles.

$$H = \frac{1}{L} \sum_{i=1}^{L} h_j \tag{2}$$

Where  $h_i$  is the gene diversity for site j and L is to the total number of sites.

## Dave's tips and tricks

#### Note

$$h = 1 - (p^2 + q^2)$$

Where p is the frequency of the derived/alternate allele and q = (1 - p)

```
\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix}
```

$$\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix} \rightarrow \begin{bmatrix} 1 - (1^2 + 0^2) \\ 1 - (2^2/5^2 + 3^2/5^2) \\ 1 - (2^2/5^2 + 3^2/5^2) \\ 1 - (1^2/5^2 + 4^2/5^2) \\ 1 - (1^2/5^2 + 4^2/5^2) \end{bmatrix}$$

$$egin{bmatrix} 0 & 0 & 0 & 0 & 0 \ 0 & 1 & 1 & 0 & 1 \ 0 & 1 & 0 & 1 & 1 \ 0 & 0 & 0 & 0 & 1 \ 1 & 0 & 0 & 0 & 0 \end{bmatrix} 
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$$\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix} \rightarrow \begin{bmatrix} 1 - (1^2 + 0^2) \\ 1 - (2^2/5^2 + 3^2/5^2) \\ 1 - (2^2/5^2 + 3^2/5^2) \\ 1 - (1^2/5^2 + 4^2/5^2) \end{bmatrix} \rightarrow h_j = \begin{bmatrix} 0 \\ 12/25 \\ 12/25 \\ 8/25 \\ 8/25 \end{bmatrix}$$

 $H = 40/25 \times 1/5 = 8/25$ 

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#### Definition

Nucleotide diversity is the average number of pairwise differences between genotypes drawn from the same population.

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#### Equation

$$\Pi = \frac{\sum_{i < j} k_{ij}}{\binom{n}{2}} \tag{3}$$

Where  $k_{ij}$  is the number of nucleotide differences between the  $i^{th}$  and  $j^{th}$  sequence in the sample and the denominator represents the number of unique comparisons being made between n sequences.

$$\pi = \frac{\Pi}{I} \tag{4}$$

Where L is to the total number of sites.

## Dave's tips and tricks

#### Note

$$\binom{n}{2} = \frac{n(n-1)}{2}$$

```
\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix}
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```

$$\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix} \quad \begin{matrix} (0+0+0+0) = 0 \\ (3+1+1+1) = 6 \\ \rightarrow (3+1+2+0) = 6 \rightarrow \Pi = 20 \div \frac{5(5-1)}{2} = 2 \\ (1+1+1+1) = 4 \\ (4+0+0+0) = 4 \end{matrix}$$

$$\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix} \xrightarrow{ \begin{pmatrix} (0+0+0+0) = 0 \\ (3+1+1+1) = 6 \\ \to (3+1+2+0) = 6 \to \Pi = 20 \div \frac{5(5-1)}{2} = 2 \\ (1+1+1+1) = 4 \\ (4+0+0+0) = 4 \end{bmatrix} = 2$$

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