

PIXY: Unbiased estimation of nucleotide diversity and divergence in the presence of missing data

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Abstract

Population genetic analyses often use summary statistics to describe patterns of genetic variation and provide insight into evolutionary processes. Among the most fundamental of these summary statistics are π and d_{XY} , which are used to describe genetic diversity within and between populations, respectively. Here, we address a widespread issue in π and d_{XY} calculation: systematic bias generated by missing data of various types. Many popular methods for calculating π and d_{XY} operate on data encoded in the variant call format (VCF), which condenses genetic data by omitting invariant sites. When calculating π and d_{XY} using a VCF, it is often implicitly assumed that missing genotypes (including those at sites not represented in the VCF) are homozygous for the reference allele. Here, we show how this assumption can result in substantial downward bias in estimates of π and d_{XY} that is directly proportional to the amount of missing data. We discuss the pervasive nature and importance of this problem in population genetics, and introduce a user-friendly UNIX command line utility, *pixy*, that solves this problem via an algorithm that generates unbiased estimates of π and d_{XY} in the face of missing data. We compare *pixy* to existing methods using both simulated and empirical data, and show that *pixy* alone produces unbiased estimates of π and d_{XY} regardless of the form or amount of missing data. In summary, our software solves a long-standing problem in applied population genetics and highlights the importance of properly accounting for missing data in population genetic analyses.

KEYWORDS

bioinformatics/phyloinformatics, genomics/proteomics, molecular evolution, population genetics – empirical, software

1 | INTRODUCTION

Population geneticists often use summary statistics to describe patterns of genetic variation and to estimate population genetic parameters such as effective population size or mutation rate (Gillespie, 2004; Hartl et al., 1997). The calculation of summary statistics is thus often the first step in a population genetic analysis, be it an exploratory study, a test of an evolutionary hypothesis, or the training

of a machine-learning model (Flagel et al., 2019; Hahn, 2019; Hartl et al., 1997). As such, accurate and unbiased algorithms for computing summary statistics are critical to the practice of population genetics.

Many summary statistics are based on the comparison of DNA sequences. Two important summary statistics in this class are π , the average number of nucleotide differences between genotypes drawn from the same population (Nei & Li, 1979); and d_{XY} , the average number of

nucleotide differences between genotypes drawn from two different populations (Nei & Li, 1979). These two summary statistics underlie a large variety of descriptive and inferential procedures in population genetics. For example, π is often used as an estimator of the central population genetic parameter θ (and is thus sometimes styled as θ_π). Similarly, d_{XY} is a key statistic for exploring patterns of divergence between populations, particularly in the context of divergence with gene flow (Burri, 2017; Cruickshank & Hahn, 2014; Noor & Bennett, 2009).

1.1 | Calculation of π and d_{XY}

For a single biallelic locus, π is usually calculated using one of three expressions shown in Equation (1), all of which are exactly equivalent (Gillespie, 2004; Hahn, 2019; Nei & Li, 1979):

where k_{ij} corresponds to the count of allelic differences between

$$\pi = \frac{\sum_{i < j} k_{ij}}{\binom{n}{2}} = \frac{c_0 c_1}{\frac{n(n-1)}{2}} = \left(\frac{n}{n-1}\right) 2 \left(\frac{c_0}{n}\right) \left(\frac{c_1}{n}\right) \quad (1)$$

the i th and j th haploid genotypes, n is the number of samples, and c_0 and c_1 are the respective counts of the two alleles at the locus. Note that the last expression is simply the sample-size corrected expected heterozygosity (i.e., the “2pq” term in the Hardy-Weinberg equation).

d_{XY} is usually calculated using an all pairwise comparisons method (similar to the first expression in Equation 1), with the only difference being that comparisons are only made between genotypes from different populations (Wakeley, 2016).

$$d_{XY} = \frac{1}{n_X n_Y} \sum_{i=1}^{n_X} \sum_{j=1}^{n_Y} k_{ij} \quad (2)$$

where n_X and n_Y correspond to the number of individuals in populations X and Y , and k_{ij} corresponds to the count of allelic differences between the i th (from population X) and j th (from population Y) haploid genotypes. There are also methods that use allele frequencies to approximate the result of Equation (2) (e.g., Smith & Kronforst, 2013), but note that these ignore differences in sample size among sites.

Often, π and d_{XY} are computed for multilocus genomic regions or in sliding windows. In order to standardize these statistics between sequences of different lengths, it is common to convert them to per-site estimates by dividing their raw value (computed for the whole sequence) by the total number of base pairs in the window (Hahn, 2019; Hartl et al., 1997). However, two types of missing data can complicate this procedure (Figure 1). First, when genotype information at a site is missing in all samples, the sequence length must be adjusted accordingly downward. Second, when genotype information at a site is missing in some samples, the denominator of the raw value of π and d_{XY} (n in Equations 1 and 2) is variable across sites—a fact which must be accounted for in order to avoid the introduction of statistical bias in the final per site estimates (Nei & Roychoudhury, 1974).

Many population genetics texts introduce the calculation of π and d_{XY} using full sequence data (as seen in Figure 1a). When DNA data are represented in this way, the distinction between missing, variant (polymorphic), and invariant (monomorphic) sites is obvious and straightforward. However, modern population genomic data is rarely encoded in this way. In fact, one of the most common formats for encoding genomic data, the variant call format (VCF), typically includes only sites that are genotyped as variant and does not usually explicitly distinguish invariant (but genotyped in the samples) sites from sites that are truly missing (Danecek et al., 2011). The data summarized by VCFs can include both categories of missing data described above: sites that are entirely missing and genotypes that are missing within a site. The strategy of only reporting variant sites means that genotypes missing within a variant site are indicated, but sites that are entirely missing are omitted from the VCF and are thus indistinguishable from sites that were genotyped as invariant. This feature is usually intentional, as including information on millions of invariant sites massively increases file size and is superfluous for many analyses.

Unfortunately, information on both invariant and missing data is not superfluous for the calculation of π and d_{XY} , and the absence of this information precludes the unbiased calculation of both statistics (Figure 1). This fact may be surprising to the reader, as many population genetics software tools provide methods of calculating π (and more rarely d_{XY}) from variants-only VCFs. How then, do these tools distinguish missing from invariant sites, as is necessary for the unbiased calculation of per-site π and d_{XY} ? The answer to this question, as will be explored in depth here, is that the vast majority of existing tools make the simplifying assumption that missing sites are present but invariant (Case 1 in Figure 1). This assumption leads to downwardly biased estimates of π and d_{XY} in the presence of missing data. This approach is problematic for a variety of reasons: along with the general underestimation of π and d_{XY} it also creates a correlation between π/d_{XY} and “missingness”, which can itself covary with various features of the genome, e.g., TEs or structural variants (Carmena & González, 1995; Kent et al., 2017).

The problematic nature of calculating π and d_{XY} in the presence of missing data is well known to practitioners of population genetics and is often overcome using a variety of ad hoc methods. One common approach involves the creation of a VCF containing both invariant and variant sites (sometimes called an “all sites” or “invariant sites” VCF), from which information on truly missing sites can then be inferred (Burri, 2017; Irwin et al., 2018; Korunes et al., 2019; Samuk et al., 2017). However, this approach has not been formalized as a general-purpose tool.

Here, we introduce *pixy*, a user-friendly command line utility for calculating π and d_{XY} from VCFs with invariant sites that correctly accounts for missing data. We compare the accuracy of *pixy*'s estimates of π and d_{XY} to those of existing methods using both simulated and empirical data. We show that *pixy* alone produces unbiased estimates of both statistics under a wide range of missing data conditions. More generally, we discuss the pervasive nature of missing data in population genetics, and use *pixy* to demonstrate the importance of accounting for it in the context of the calculation of π and d_{XY} .

2 | NEW APPROACHES

Pixy is a command-line tool, written in PYTHON 3 and available on GITHUB and via conda-forge for installation under Linux/OSX systems. The user supplies an “all sites” VCF and a populations file listing the population(s) of interest and the associated sample names as listed

in the VCF genotype columns. Pixy's documentation (<https://pixy.readthedocs.io/>) provides guidance on VCF generation and filtering. Pixy makes use of data structures provided by the Python module scikit-allel to efficiently handle invariant sites VCFs (Miles et al., 2019). The user can quickly compute π and d_{XY} over genomic windows of arbitrary size.

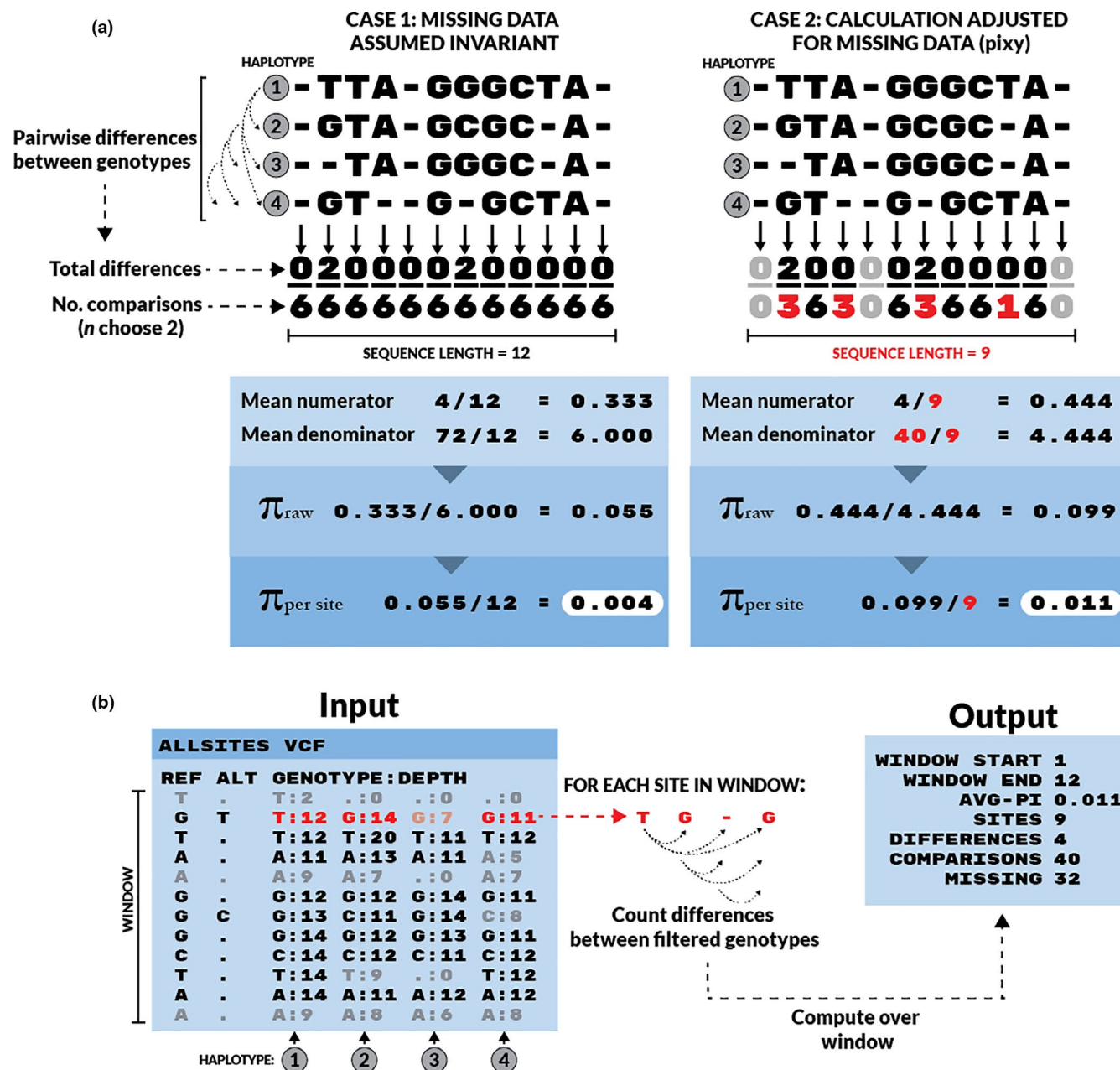


FIGURE 1 The logic and input/output of pixy demonstrated with a simple haploid example. (a) Comparison of two methods for computing π (or d_{XY}) in the face of missing data. These methods follow the first expression of Equation 1 but differ in how they calculate the numerator and denominator. In Case 1, all missing data is assumed to be present but invariant. This results in a deflated estimate of π . In Case 2, missing data are simply omitted from the calculation, both in terms of the number of sites (the final denominator) and the component denominators for each site (the n choose 2 terms). This results in an unbiased estimate of π . (b) The adjusted π method (Case 2) as implemented for VCFs in pixy. The example VCF (input) contains the same four haplotypes as (a). Invariant sites are represented as sites with no ALT allele, and greyed-out sites are those that failed to pass a genotype filter requiring a minimum number of reads covering the genotype (Depth ≥ 10 in this case) [Colour figure can be viewed at [wileyonlinelibrary.com](https://onlinelibrary.wiley.com/doi/10.1111/1755-0998.13326)]

The key difference between pixy and existing methods is the handling of missing data via dynamic adjusting of site-level denominators (which are propagated properly during windowed operations) and the adjustment of effective sequence length (Figure 1a). Case 1 in Figure 1a shows the calculation of π across four sequences under the simplifying assumption that missing sites are present but invariant; i.e., if a genotype is missing in a pairwise comparison, that genotype is assumed to be the reference allele. In contrast, the strategy implemented in pixy (Case 2 in Figure 1a) excludes missing sites from both the numerator and the denominator of π or d_{XY} . To illustrate how this strategy applies to a VCF, Figure 1b shows a simplified example of an “all sites” VCF file, where each genotype is accompanied by details about the data at that genotype (in this example, read depth). If a genotype is missing or filtered out, it does not contribute to either the numerator or the denominator in pixy’s calculations. Because π and d_{XY} utilize all pairwise comparisons between genotypes at each site, this process does not depend on phasing, and the comparisons are the same regardless of ploidy. To illustrate how this logic transfers to a diploid example, Figure S1 shows the same sequences as Figure 1, but depicts them as four haplotypes from two diploid individuals, rather than four haploid individuals. In the diploid example, genotypes from the same individual are paired in the VCF. This pairing changes only the formatting of the input, not the pairwise comparisons between genotypes or subsequent calculation of π or d_{XY} .

Note that pixy, like most methods, estimates π and d_{XY} using discrete genotype calls of biallelic SNPs. As such, in order to minimize error from low-depth genotype calls, we recommend that the input VCF be filtered at the site level (e.g., using GATK best practices-style hard filters) prior to input. In addition, pixy can apply user-specified individual genotype level filters prior to the calculation of summary statistics. At minimum, we recommend that users apply a cutoff of DP >10 and GQ >30 for individual genotypes, and/or an average site-level depth >10 and quality >30 (INFO-DP and QUAL / total # individuals). More stringent filters will result in lower variance in π and d_{XY} estimates due to exclusion of genotyping errors, but for most studies, and given the number of sites in a typical windowed calculation of π and d_{XY} (e.g., 10 kilobases) a cutoff of 10×/Q30 provides a good trade-off between retaining sites and filtration of errors (see Fumagalli, 2013). We outline the general workflow for filtering a VCF in the documentation (<https://pixy.readthedocs.io/>).

The output of pixy also includes all the raw information for all π and d_{XY} estimates (i.e., the component numerators and denominators for all computations). The name pixy is a play on the original parameter name π_{XY} , which was used by (Nei & Li, 1979) in place of d_{XY} . All code is freely available on Github <https://github.com/ksamuk/pixy>, and detailed documentation is provided via readthedocs <https://pixy.readthedocs.io/>. The software is also available for installation via Anaconda on the conda-forge channel <https://anaconda.org/conda-forge/pixy>. The a static version of the version of pixy used in this manuscript is archived at <http://doi.org/10.5281/zenodo.4432294> (Korunes & Samuk, 2021).

3 | MATERIALS AND METHODS

3.1 | Simulated data: Coalescent simulations via msprime

To provide ground-truthed data sets for evaluating the performance of pixy, we simulated sequence data using the coalescent simulator msprime (Kelleher et al., 2016). We created 10,000 simulated data sets, each with the following parameters: Effective population size = 1×10^6 , mutation rate = 1×10^{-8} , sample size = 100, number of sites = 10,000. We converted these to VCFs with invariant sites using a custom script (see code supplement). These data sets represent the case of “no missing data”. To explore the effects of different types of missing data, we randomly selected 100 of these original data sets as “parent” VCFs and then used these to simulate variable proportions of missing data (ranging from 0.0 to 0.99, in steps of 0.01). To simulate missing sites, we randomly dropped rows from each parent VCF. To simulate missing genotypes, we randomly converted a fixed proportion of genotypes in each parent VCF at every site to “.” (missing). This resulted in a total of 30,000 VCFs of simulated data (10,000 original VCFs, and 10,000 “missing sites” VCFs and 10,000 “missing genotypes” VCFs).

3.2 | Empirical data: *Anopheles gambiae* whole genome data

To evaluate the performance of pixy in a realistic use case, we obtained short-read whole-genome sequencing data from two populations of *Anopheles gambiae* sequenced by the Ag1000G (*Anopheles gambiae* 1000 Genomes) Consortium (MalariaGEN, 2016). We selected 18 individuals each from two populations: BFS (Burkina Faso) and KES (Kenya). Sample accessions and sequencing details are provided in Table S2. All sequences were aligned to the *Anopheles gambiae* Agamp4.12 reference genome (Giraldo-Calderón et al., 2015) using BWA-0.7.5a (Li & Durbin, 2009), after using Picard to mark adapters and duplicates (Broad Institute, 2019). Variants were called using GATK version 4.1.1.0, using the “-all-sites” flag of GenotypeGVCFs to generate “all sites” VCFs for input into pixy (McKenna et al., 2010; Van der Auwera et al., 2013).

3.3 | Comparison to existing methods using both simulated and empirical data

We compared the accuracy of pixy’s estimates of π and d_{XY} with several popular existing tools: VCFtools, ANGSD, POPGENOME, and SCIKIT-ALLEL (Danecek et al., 2011; Korneliussen et al., 2014; Miles et al., 2019; Pfeifer et al., 2014). We computed π using PIXY, VCFtools, POPGENOME, SCIKIT-ALLEL, and ANGSD. Note that ANGSD was only applied to the empirical data, since its diversity functions are not designed to work with VCFs. We computed d_{XY} using PIXY, POPGENOME, SCIKIT-ALLEL, and the ANGSD companion script “calcDxy” (<https://github.com/mfuma>).

galli/ngsPopGen/blob/master/scripts/calcDxy.R). For VCFtools, we used the “--window-pi” method to estimate windowed π . For scikit-allel, we used the `allel.sequence_diversity` and `allel.sequence_divergence` functions to estimate windowed π and d_{XY} , respectively. For PopGenome, we used the `nuc.diversity.within` and `nuc.diversity.between` functions, following the recommendations in the manual. We stress that the PopGenome manual explicitly warns that computing π and d_{XY} in the presence of missing data will result in biased estimates (Pfeifer et al., 2014). We have chosen to include it here because PopGenome is commonly used to estimate π and d_{XY} in spite of this warning.

We first used our simulated data sets to examine pixy's accuracy in comparison to these existing methods. To obtain two simulated populations for evaluating d_{XY} , we split the 100 simulated samples into two random groups. To standardize sample sizes between π and d_{XY} estimates, we computed π using the first half of the simulated individuals ($n = 50$), and d_{XY} by designating the first half of the individuals as drawn from “Population 1” and the second half as drawn from “Population 2” (each with $n = 50$ individuals). We computed π and d_{XY} in 10 kb windows in each of the VCFs with variable missing data. pixy was run using default settings, and each pre-existing method was applied using the functions described above (see code supplement).

We then compared the accuracy of each method using the empirical *Anopheles gambiae* data. To do this, we first applied a basic genotype-level hard filter ($DP \geq 10$, $GQ \geq 40$, $RGQ \geq 40$) to the invariant sites VCF produced by GATK. We also removed all variants apart from biallelic SNPs – like other existing methods, pixy does not support the calculation of summary statistics for INDELs or other structural variants. The filtered VCF was used as the input file for all methods apart from ANGSD (see below). We then computed π (PIXY, VCFTOOLS, ANGSD, POPGENOME, SCIKIT-ALLEL) and d_{XY} (PIXY, POPGENOME, SCIKIT-ALLEL, ANGSD) in 10 kb windows. We computed π separately for the BFS and KES populations. For ANGSD, the BAM files generated from the *Anopheles* BFS and KES populations were used as input, resulting in estimates of both π (ANGSD's “pairwise theta”) and d_{XY} (obtained via a companion script: `calcDxy` – by Joshua Penalba, <https://github.com/mfumagalli/ngsPopGen/blob/master/scripts/calcDxy.R>). In the case of π , we explicitly divided the raw estimates of pairwise theta by the number of sites (`nSites`) provided by ANGSD, and not the window size (10,000).

Full details and scripts for all of the above procedures are available at https://github.com/ksamuk/pixy_analysis.

4 | RESULTS

4.1 | Validation of pixy results

We examined pixy's accuracy as an estimator of π and d_{XY} by comparing pixy's results to pre-existing methods and theoretical expectations. We conducted 10,000 simulations to generate data sets in which all samples have observed genotypes at all sites (i.e., no

missing data). Neutral simulations with a known effective population size and mutation rate allow us to compare pixy's output to the simple theoretical expectation of $E(\pi) = 4N_e\mu$ (Hartl et al., 1997; Wakeley, 2016). To evaluate d_{XY} , we split the simulated population into two random groups. In this case, $4N_e\mu$ is also the expected value of d_{XY} (this can be conceptualized as computing d_{XY} between two populations with a divergence time of zero: Hahn, 2019).

Using these simulated data, we compared the accuracy of pixy's estimates of π and d_{XY} with several popular existing tools: VCFtools, PopGenome, and scikit-allel (Danecek et al., 2011; Korneliusson et al., 2014; Miles et al., 2019; Pfeifer et al., 2014). These tools represent some of the most cited software packages for calculating π and d_{XY} . Notably, the PopGenome manual acknowledges that π and d_{XY} estimates will be biased by missing data and includes a warning about computing estimates in the presence of missing data (Pfeifer et al., 2014). Nonetheless, users can and do use PopGenome to estimate π and d_{XY} in the presence of missing data, so we chose to include it here. Using each of these software packages, we computed π (and d_{XY} where available) for each of the simulated data sets. Using the resulting sampling distribution of π and d_{XY} from each estimation method, we compared the mean to the expected value of $4N_e\mu = 0.04$ ($N_e = 1 \times 10^6$, $\mu = 1 \times 10^{-8}$). In the absence of missing data, all examined methods provide estimates of π and d_{XY} that closely match theoretical expectations (Figure 2a,b; mean = 0.0398, standard error = 0.000189 for all sampling distributions). Estimates of π generated by pixy are identical to those of all other methods ($R^2 = 1.000$, $F = 1.47 \times 10^6$, $df = 19,998$, $p < 2.2 \times 10^{-16}$) and estimates of d_{XY} are nearly identical ($R^2 = 0.987$, $F = 1.47 \times 10^6$, $df = 19,998$, $p < 2.2 \times 10^{-16}$) (Figure 2c,d). Overall, all compared methods have high accuracy and provide nearly identical estimates when data are complete.

4.2 | Pixy is unbiased in the presence of missing data

We next examined pixy's accuracy in the presence of missing data. For a random set of 100 of the previously simulated data sets, we created subsets with varying quantities of missing data. This means that for each data set with missing data, we had a corresponding “parent” data set with complete data. Again, we computed π and d_{XY} for each data set with the popular existing programs VCFtools, PopGenome, and scikit-allel.

In order to better visualize the effects of missing data, we scaled estimates of π and d_{XY} for each data set with missing data by dividing by the estimate obtained from the parent data set with no missing data. This normalizes any initial differences in π among data sets due to sampling variance. After this normalization, we observed that pixy's π and d_{XY} estimates remain unbiased in the face of missing data (Figure 3, left column). As the proportion of missing data increases, the variance in estimates of π and d_{XY} increases. This spread in estimates across both sides of the $y = 1$ line in Figure 3 increases as a function of missing data. Note, however,

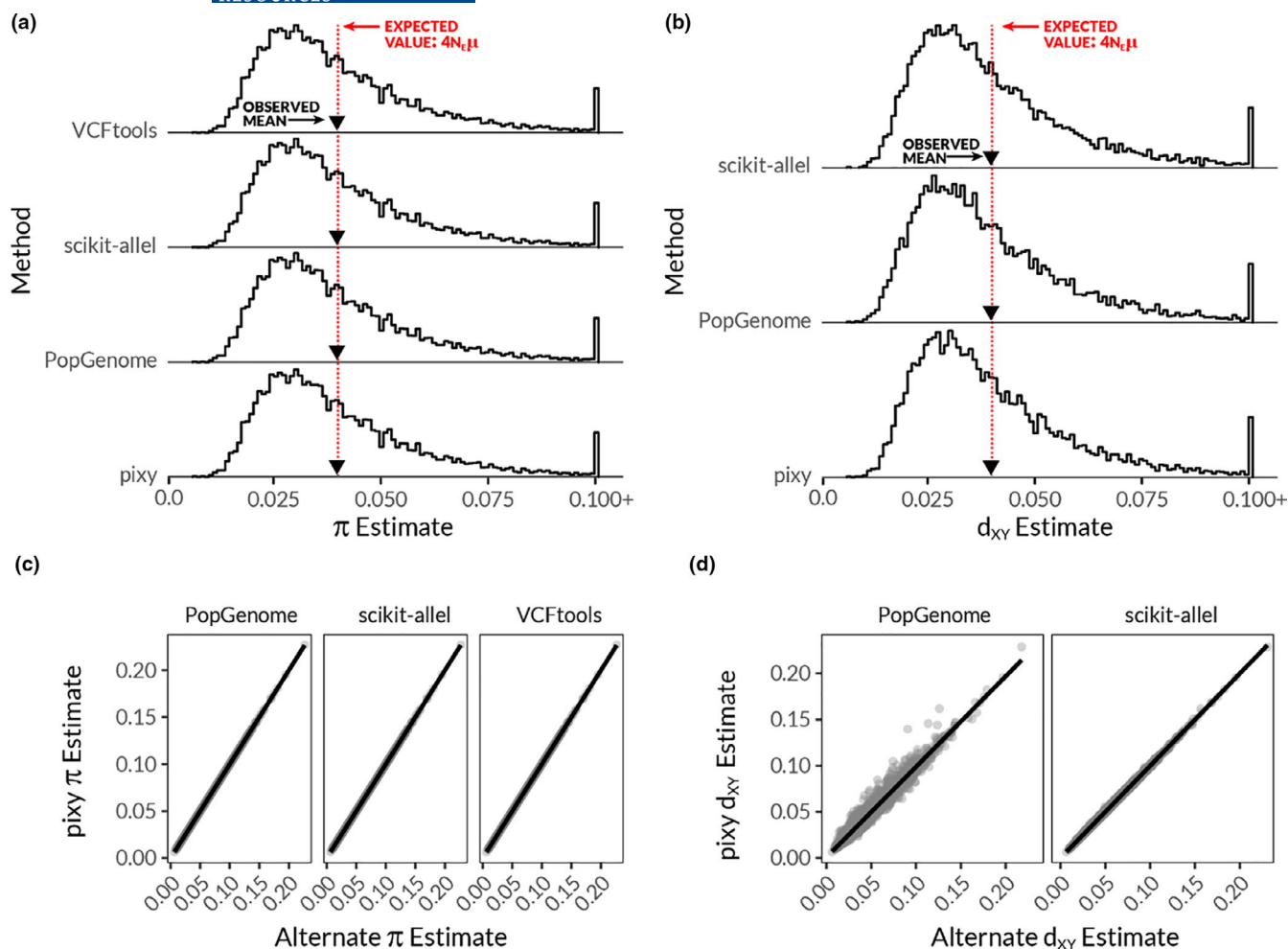


FIGURE 2 Comparison between pixy and existing methods in complete data sets. (a, b) The sampling distribution of π (a) and d_{xy} (b), as estimated from 10,000 simulated data sets using pixy and a variety of existing methods (see text for details). The red dotted line denotes the theoretical expectation for the mean of the sampling distribution, $4N_e\mu = 0.04$ (which is the same for π and d_{xy} in this particular case). The observed means of the sampling distributions are marked with inverted triangles. For clarity, estimates of π and d_{xy} above 0.100 are aggregated in the last bin ("0.100+"). (c, d) direct comparisons between pixy's estimates of π (c) and d_{xy} (d) and those from existing methods [Colour figure can be viewed at [wileyonlinelibrary.com](https://onlinelibrary.wiley.com/doi/10.1111/1755-0998.13326)]

that the mean (expected) values of π and d_{xy} for pixy do not exhibit any significant trend (flat red lines, pixy panels, Figure 3, linear model slope does not differ significantly from 0 for sites or for genotypes, $p > 0.2$, Table S1). This is the expected behavior of an unbiased summary statistic in the face of missing data. In contrast, the three other methods all display a downward bias in their estimates of π and d_{xy} that increases as a function of the proportion of missing sites or genotypes (nonpixy panels, Figure 3; all slopes significantly negative for missing sites and genotypes, all $p < 2.2 \times 10^{-16}$, Table S1). The effect of this bias was strongest for the case of completely missing sites, whereas missing genotypes (sites with missing genotypes for some samples) only begin to display strong bias around 80% missing data for most methods (Figure 3). The notable exception to this was VCFtools which displayed a sharper increase in bias for "missing genotypes" than "missing sites" (Figure 3).

4.3 | Analysis of empirical data: *Anopheles gambiae*

Finally, we applied pixy to an empirical data set: deep sequencing of *Anopheles gambiae* provided by the Ag1000 Genomes Consortium. We used pixy to generate windowed estimates of π on the X chromosome for a sample ($n = 18$) of the *A. gambiae* Burkina Faso (BFS) population, and we compared these estimates to those generated by popular pre-existing methods. We also examined d_{xy} between the 18 BFS samples and 18 additional samples from the KES (Kenya) population (Table S2). In addition to the three previously explored programs (VCFtools, PopGenome, and scikit-allele), we included estimates of π and d_{xy} from the software ANGSD (Korneliussen et al., 2014). ANGSD relies on genotype likelihoods calculated using the reads covering a position, making it incompatible with our simulated data but equipped to handle empirical sequencing data.

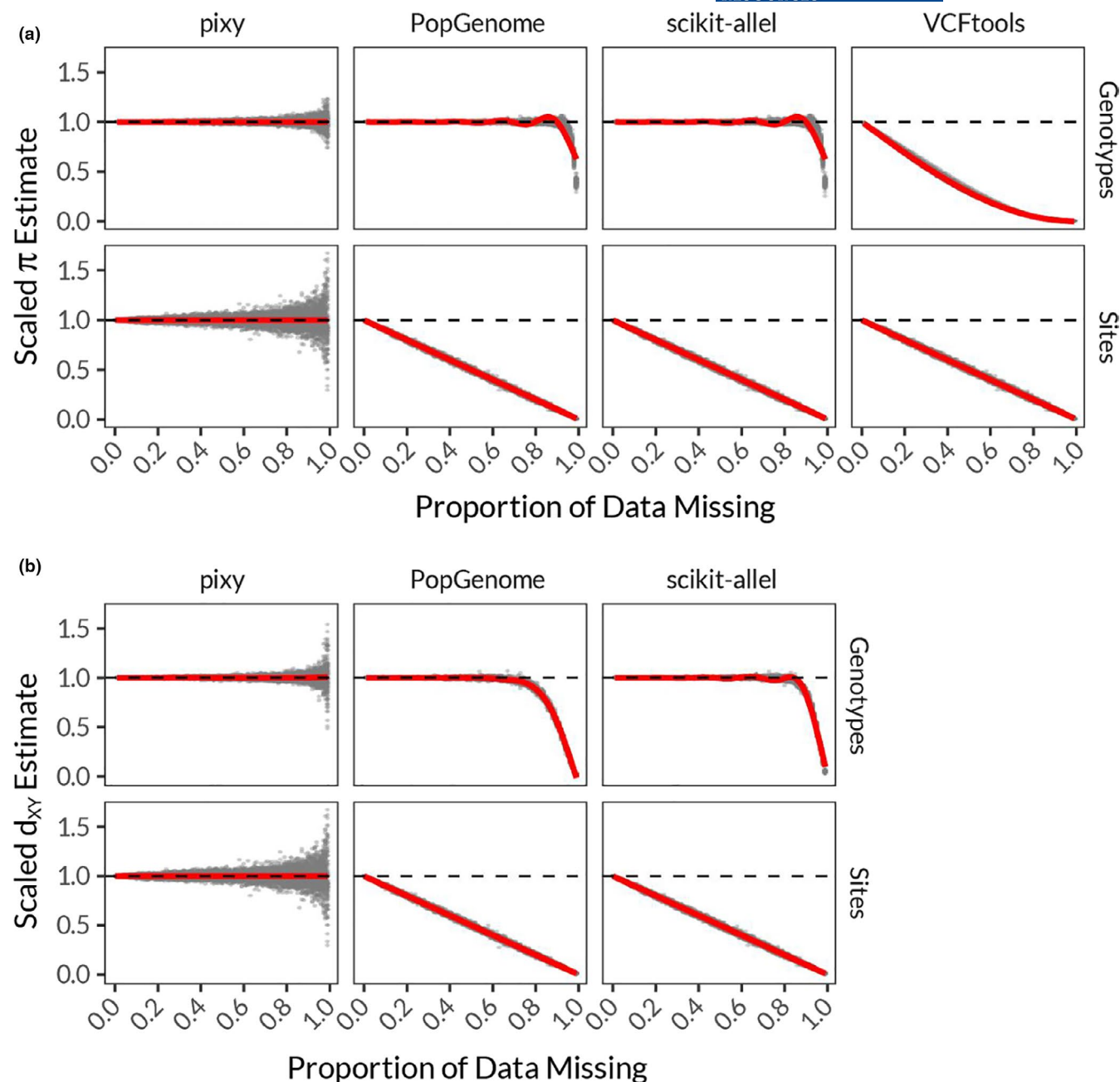


FIGURE 3 Comparison between pixy and existing methods in the presence of missing data. (a) π and (b) d_{xy} are shown as scaled estimates (each estimate is scaled by dividing by the estimate obtained from the parent data set with no missing data). Perfect congruence between estimates in the presence and absence of missing data is shown with the dotted line at $y = 1$. Estimates were obtained from data sets with varying proportions of missing genotypes (top row, a and b) and sites (bottom row, a and b) [Colour figure can be viewed at wileyonlinelibrary.com]

All four methods yielded estimates of π that were correlated with pixy's estimates (Figure 4, $R^2 = 0.68$ for VCFtools, 0.82 for ANGSD, and 0.79 for both PopGenome and scikit-allele). However, the previously identified biases caused by missing data appeared to result in substantial differences in estimates of π in many cases (Figure 4). In general, the compared methods tend to underestimate π , with the exception being ANGSD. This downward bias is seen as the grouping of estimates above the $y = x$ line in Figure 4a,c,d.

As expected, the magnitude of this bias was closely correlated with the proportion of missing data (Figure 4, Figure S2). For the relatively complete regions of our subset of the Ag1000g data set, the apparent underestimation of π was low (around -5%), but rapidly increased in cases of even moderate missingness (e.g., as much as -95% in cases of just 25% missing data, Figure S2). As expected, the same pattern of bias was also apparent for estimates of d_{xy} (Figures S3 and S4).

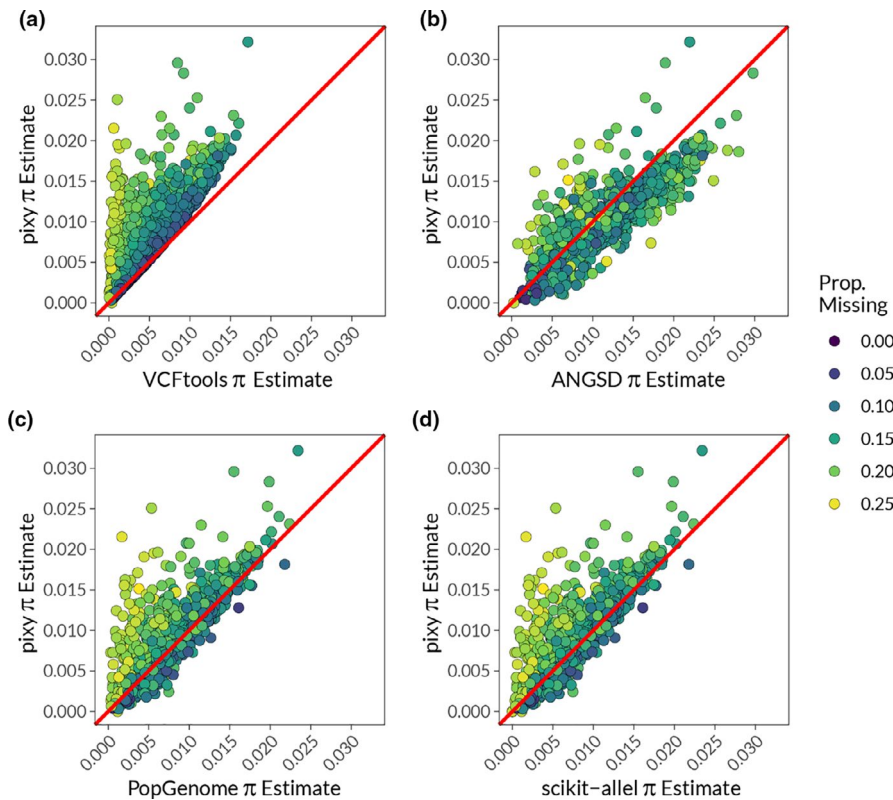


FIGURE 4 Comparisons of estimates of π from whole genome data derived from 18 *Anopheles gambiae* individuals from the Ag1000G Burkina Faso (BFS) population. Each panel (a–d) depicts the estimates of π for the X chromosome performed using pixy (y-axis) and four other methods (x-axis, a–d). Points are coloured according to the proportion of missing data (of any type) calculated by pixy. The 1:1 line is shown in red [Colour figure can be viewed at [wileyonlinelibrary.com](https://onlinelibrary.wiley.com/doi/10.1111/1755-0998.13326)]

5 | DISCUSSION

Modern population genomic analyses frequently rely on π and d_{XY} as measures of diversity and divergence, but these summary statistics are deceptively difficult to accurately calculate (Gillespie, 2004; Hartl et al., 1997). Specifically, the correct handling of missing and invariant sites presents a common pitfall in the calculation of π and d_{XY} . This challenge stems in part from the way genetic variation data is commonly encoded. The widely used Variant Call Format typically condenses data down to only variant sites and does not maintain information about which sites had insufficient data for genotyping and which sites were genotyped as invariant (Danecek et al., 2011). If π and d_{XY} are calculated under the assumption that missing data are invariant, then the resulting estimates of π and d_{XY} are likely to be downwardly biased in many cases.

We observe this downward bias in our application of several popular tools using both simulated and empirical data sets. While many population geneticists recognize that such tools must be applied with caution, the lack of formalized best practices and available software for calculating π and d_{XY} in the presence of missing data leads to inconsistent approaches across studies. It also places the onus on the user to devise ad hoc methods to handle missing data when using common software. Pixy provides a user-friendly command line utility for estimating π and d_{XY} in a manner unbiased by the presence of missing data. We leverage a common strategy for distinguishing missing and invariant sites by (i) making use of VCFs including invariant sites, and (ii) employing algorithms that explicitly account for missing data. More generally, our comparison of pixy to existing tools demonstrates the consequences of failing to handle

missing data properly and underscores the potential pervasiveness of this problem in population genetics.

In addition to generally underestimating π and d_{XY} failing to properly handle missing data can also create a correlation between π/d_{XY} and “missingness”, or the proportion of missing genotypes. This relationship is noteworthy since missingness is often tied to various features of the genome or of the data itself. For example, genomic features such as transposable elements or structural variation can cause variable assembly and mapping quality (O’Leary et al., 2018). Relatedly, individuals within a sample often have variable missingness (e.g., due to sample quality variation), which can generate false differences in π and d_{XY} if these vary systematically among biological units (e.g., between populations). Differences in genomic library preparation technique can also affect missingness, for example genome complexity reduction techniques (e.g., RAD-Seq or GBS) may present particularly variable and high levels of missingness relative to high-coverage whole-genome sequencing (Elshire et al., 2011; Lowry, 2017). However, as seen with our case study of *Anopheles gambiae* data, even $\sim 30\times$ coverage whole-genome sequencing can exhibit significant downward bias in π estimation when missing data is not taken into account (e.g., Figure S2). This is concerning, as this relatively high-quality, well-curated data set is probably close to a “best case” scenario for missingness, and most data sets will probably fare much worse. Given these considerations, we argue that best practices for calculating π and d_{XY} should always explicitly account for missing data.

One notable exception to the patterns we identified here was the likelihood-based method ANGSD (Korneliussen et al., 2014). ANGSD did not appear to display a systematic underestimation of π

or d_{XY} in the face of missing data. However, the estimates produced by ANGSD are not fully congruent with pixy, and ANGSD appears to generate systematically higher estimates of π or d_{XY} in some scenarios (Figure S2). While it is outside the scope of our current effort to systematically explore how ANGSD reacts to missing data, we note that it employs a rather different approach to analysis by working with allele frequencies derived from genotype likelihoods rather than directly counting called genotypes. This approach does have the advantage of potentially reducing biases due to low sequencing coverage and/or reference bias (although these biases could be mitigated by more stringent depth filters). It is also important to note that the calculation of d_{XY} using ANGSD required post-processing using a third party script, as well as further processing using a custom script (written by the authors of this paper) to average over windows (see code supplement). As such, readers are cautioned that (i) ANGSD itself does not actually provide estimates of d_{XY} , and (ii) the ad hoc method that many users cite has not to our knowledge been formally validated. The lack of a single validated protocol for calculating d_{XY} (or even π) using ANGSD suggests there may be a great deal of interstudy variation in estimates produced with ANGSD. It also differs from the other software used here in that ANGSD was not designed to analyse VCFs (though recent versions do input and output VCFs with some limitations), and thus may be more difficult to apply to many data sets.

While pixy was designed to provide a user-friendly end-to-end solution for the unbiased calculation of π and d_{XY} , it may be possible for more advanced users to achieve similar results with existing tools. For example, with the inclusion of a user-created “accessibility mask”, it should be possible to avoid the “missing sites” effect seen in Figure 3a. Further, in response to the preprint of this manuscript, scikit-allel provided options to address the “missing genotypes” effect. As such, scikit-allel is a good option for Python-literate advanced users who are aware of the potential pitfalls of calculating population genetic statistics like π and d_{XY} . Pixy is naturally less flexible, but guides users more explicitly to confront and avoid common pitfalls.

While the unbiased methods provided by pixy are an important resource for facilitating π and d_{XY} calculation, much work remains to correct systemic issues in estimating diversity and divergence. Future studies are needed to address how missing data may affect the wide variety of other population summary statistics and tests (e.g., Wong et al., 2019). Another important area of future work is the development of file formats that efficiently store genetic data while maintaining the ability to distinguish well-supported invariant sites from sites which have insufficient information to determine whether they are truly invariant. As the field of population genetics advances, we hope that articulating this issue will provide groundwork for handling missing data as new file formats arise and new tools are developed.

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DATA AVAILABILITY STATEMENT

All code used to generate and analyse data, is available on the Github repository https://github.com/ksamuk/pixy_analysis. The development code for the pixy software itself is available at <https://github.com/ksamuk/pixy>. The Ag1000G genomic data used for testing is available at <https://www.malariagen.net/projects/ag1000g>.

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SUPPORTING INFORMATION

Additional supporting information may be found online in the Supporting Information section.

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