

Práctica 2

Ejercicio 1.

Cifre el mensaje "SABER Y SABERLO DEMOSTRAR ES VALER DOS VECES" mediante un criptograma de Hill trigrámico con la palabra clave "REVOLUTIO".

Multiplicamos la matriz de cifrado por cada uno de los trigramas:

$A = \{\{18, 4, 22\}, \{15, 11, 21\}, \{20, 8, 15\}\}$

$A = \{\{R, E, V\}, \{O, L, U\}, \{T, I, O\}\}$

$\text{Mod}[A \cdot \{19, 0, 1\}, 27]$

$\{13, 9, 17\}$

$\text{Mod}[A \cdot \{4, 18, 25\}, 27]$

$\{19, 0, 5\}$

$\text{Mod}[A \cdot \{19, 0, 1\}, 27]$

$\{13, 9, 17\}$

$\text{Mod}[A \cdot \{4, 18, 11\}, 27]$

$\{8, 3, 11\}$

$\text{Mod}[A \cdot \{15, 3, 4\}, 27]$

$\{19, 18, 6\}$

$\text{Mod}[A \cdot \{12, 15, 19\}, 27]$

$\{19, 15, 24\}$

$\text{Mod}[A \cdot \{20, 18, 0\}, 27]$

$\{0, 12, 4\}$

$\text{Mod}[A \cdot \{18, 4, 19\}, 27]$

$\{2, 11, 2\}$

$\text{Mod}[A \cdot \{22, 0, 11\}, 27]$

$\{17, 21, 11\}$

$\text{Mod}[A \cdot \{4, 18, 3\}, 27]$

$\{21, 24, 26\}$

$\text{Mod}[A \cdot \{15, 19, 22\}, 27]$

$\{20, 5, 26\}$

$\text{Mod}[A \cdot \{4, 2, 4\}, 27]$

$\{6, 4, 21\}$

$\text{Mod}[A \cdot \{19, 24, 24\}, 27]$

$\{21, 0, 14\}$

Y nos da el siguiente resultado:

N J Q S A F N J Q I D L S R G S O X A M E C L C Q U L U X Z T F
Z G E U U A Ñ

Descifre el mensaje "SXLEWVNKCOMX" que ha sido cifrado con un cifrado de Hill trigrámico y con palabra clave "BARCELONA".

Hacemos la inversa de la clave de cifrado para sacar la clave de descifrado y la multiplicamos por cada trigrama.

A = { {1,0,18} , {2,4,11} , {15,13,0} }
A = { {B,A,R} , {C,E,L} , {O,N,A} }

MatrixForm[B=Inverse[A,Modulus→27]]

$$\begin{pmatrix} 19 & 18 & 9 \\ 3 & 0 & 25 \\ 20 & 14 & 4 \end{pmatrix}$$

Clave descifrado = S R J D A Y T Ñ E

Mod[B. {19,24,11} ,27]
{1,8,4}
Mod[B. {4,23,22} ,27]
{13,22,4}
Mod[B. {13,10,2} ,27]
{13,8,3}
Mod[B. {15,12,24} ,27]
{15,24,24}

Y nos da el siguiente resultado:

1 8 4 13 22 4 13 8 3 15 24 24

BIEN V EN ID O X X

Ejercicio 2.

En este archivo se muestra un texto en claro y el texto cifrado correspondiente. Sabiendo que ha sido encriptado con un cifrado de Hill trigramico encuentre la clave.

Texto en claro: PIENSOLUEGOEXISTOX

Texto cifrado: UWWVZAENCSDNGMJJNY

$B = \{\{16, 8, 4, 21, 23, 23\}, \{13, 19, 15, 22, 26, 0\}, \{11, 21, 4, 4, 13, 2\}, \{6, 15, 4, 19, 3, 13\}, \{24, 8, 19, 6, 12, 9\}, \{20, 15, 24, 9, 13, 25\}\}$

PowerMod[16,-1,27]

22

Mod[22*13,27]

Mod[22*11,27]

Mod[22*6,27]

Mod[22*24,27]

Mod[22*20,27]

16

26

24

15

8

$c = \text{Mod}[\{\{16, 8, 4, 21, 23, 23\}, \{13, 19, 15, 22, 26, 0\} - 16\{16, 8, 4, 21, 23, 23\}, \{11, 21, 4, 4, 13, 2\} -$

$26\{16, 8, 4, 21, 23, 23\}, \{6, 15, 4, 19, 3, 13\} - 24\{16, 8, 4, 21, 23, 23\}, \{24, 8, 19, 6, 12, 9\} -$

$15\{16, 8, 4, 21, 23, 23\}, \{20, 15, 24, 9, 13, 25\} - 8\{16, 8, 4, 21, 23, 23\}\}, 27]$

$\{\{16, 8, 4, 21, 23, 23\}, \{0, 26, 5, 10, 9, 10\}, \{0, 2, 8, 25, 9, 25\}, \{0, 12, 16, 1, 18, 1\}, \{0, 23, 13, 15, 18, 15\},$

$\{0, 5, 19, 3, 18, 3\}\}$

PowerMod[26,-1,27]

26

Mod[26*2,27]

Mod[26*12,27]

Mod[26*23,27]

Mod[26*5,27]

25

15

4

22

$e = \text{Mod}[\{\{16, 8, 4, 21, 23, 23\}, \{0, 26, 5, 10, 9, 10\}, \{0, 2, 8, 25, 9, 25\} -$

$25\{0, 26, 5, 10, 9, 10\}, \{0, 12, 16, 1, 18, 1\} - 15\{0, 26, 5, 10, 9, 10\}, \{0, 23, 13, 15, 18, 15\} -$

$4\{0, 26, 5, 10, 9, 10\}, \{0, 5, 19, 3, 18, 3\} - 22\{0, 26, 5, 10, 9, 10\}\}, 27]$

$\{\{16, 8, 4, 21, 23, 23\}, \{0, 26, 5, 10, 9, 10\}, \{0, 0, 18, 18, 0, 18\}, \{0, 0, 22, 13, 18, 13\}, \{0, 0, 20, 2, 9, 2\}, \{0, 0, 17, 26, 9, 26\}\}$

PowerMod[18,-1,27]

PowerMod::ninv: \[NoBreak]18\[NoBreak] is not invertible modulo

\[NoBreak]27\[NoBreak]. >>

PowerMod[18,-1,27]

$f = \text{Mod}[\{\{16,8,4,21,23,23\},\{0,26,5,10,9,10\},3\{0,0,18,18,0,18\},\{0,0,22,13,18,13\},\{0,0,20,2,9,2\},\{0,0,17,26,9,26\}\},27]$
 $\{\{16,8,4,21,23,23\},\{0,26,5,10,9,10\},\{0,0,0,0,0,0\},\{0,0,22,13,18,13\},\{0,0,20,2,9,2\},\{0,0,17,26,9,26\}\}$
 Cambio 3° fila por 6°
 $\{\{16,8,4,21,23,23\},\{0,26,5,10,9,10\},\{0,0,17,26,9,26\},\{0,0,22,13,18,13\},\{0,0,20,2,9,2\},\{0,0,0,0,0,0\}\}$
 $\text{PowerMod}[17,-1,27]$
 8
 $\text{Mod}[8*22,27]$
 $\text{Mod}[8*20,27]$
 14
 25
 $f = \text{Mod}[\{\{16,8,4,21,23,23\},\{0,26,5,10,9,10\},\{0,0,17,26,9,26\},\{0,0,22,13,18,13\}-14\{0,0,17,26,9,26\},\{0,0,20,2,9,2\}-25\{0,0,17,26,9,26\},\{0,0,0,0,0,0\}\},27]$
 $\{\{16,8,4,21,23,23\},\{0,26,5,10,9,10\},\{0,0,17,26,9,26\},\{0,0,0,0,0,0\},\{0,0,0,0,0,0\},\{0,0,0,0,0,0\}\}$
 $\text{PowerMod}[26,-1,27]$
 $\text{PowerMod}[17,-1,27]$
 26
 8
 $\text{Mod}[26*8,27]$
 $\text{Mod}[8*5,27]$
 19
 13
 $\text{Mod}[\{\{16,8,4,21,23,23\}-19\{0,26,5,10,9,10\},\{0,26,5,10,9,10\}-13\{0,0,17,26,9,26\},\{0,0,17,26,9,26\},\{0,0,0,0,0,0\},\{0,0,0,0,0,0\},\{0,0,0,0,0,0\}\},27]$
 $\{\{16,0,17,20,14,22\},\{0,26,0,23,0,23\},\{0,0,17,26,9,26\},\{0,0,0,0,0,0\},\{0,0,0,0,0,0\},\{0,0,0,0,0,0\}\}$
 $\text{PowerMod}[17,-1,27]$
 8
 $\text{Mod}[8*17,27]$
 1
 $\text{Mod}[\{\{16,0,17,20,14,22\}-\{0,0,17,26,9,26\},\{0,26,0,23,0,23\},\{0,0,17,26,9,26\},\{0,0,0,0,0,0\},\{0,0,0,0,0,0\},\{0,0,0,0,0,0\}\},27]$
 $\{\{16,0,0,21,5,23\},\{0,26,0,23,0,23\},\{0,0,17,26,9,26\},\{0,0,0,0,0,0\},\{0,0,0,0,0,0\},\{0,0,0,0,0,0\}\}$
 $\text{PowerMod}[16,-1,27]$
 $\text{PowerMod}[26,-1,27]$
 $\text{PowerMod}[17,-1,27]$
 22
 26
 8
 $\text{Mod}[\{22\{16,0,0,21,5,23\},26\{0,26,0,23,0,23\},8\{0,0,17,26,9,26\},\{0,0,0,0,0,0\},\{0,0,0,0,0,0\},\{0,0,0,0,0,0\}\},27]$
 $\{\{1,0,0,3,2,20\},\{0,1,0,4,0,4\},\{0,0,1,19,18,19\},\{0,0,0,0,0,0\},\{0,0,0,0,0,0\},\{0,0,0,0,0,0\}\}$

MatrixForm[{{{1,0,0,3,2,20},{0,1,0,4,0,4},{0,0,1,19,18,19},{0,0,0,0,0,0},{0,0,0,0,0,0},{0,0,0,0,0,0}}}]

{{1, 0, 0, 3, 2, 20},
 {0, 1, 0, 4, 0, 4},
 {0, 0, 1, 19, 18, 19},
 {0, 0, 0, 0, 0, 0},
 {0, 0, 0, 0, 0, 0},
 {0, 0, 0, 0, 0, 0}}

Al final como podemos ver la clave convertida a letras sería :

D C T
 E A E
 S R S

DESCARTES

Ejercicio 2.

Descifre mediante la técnica de análisis de frecuencias (de digramas) el siguiente mensaje que ha sido cifrado por el cifrado de Playfair.

EPVRNKVFCGMFHAMTCYSGMIFCZUMUFMTSRMEUMIFUPHMGIGDNQEETGSETUZLDMSFIRPCPES
 GYSCMUUNSF CWPC LUPEDUEPQPCYBCFRGARFYKBDPETOMEESFIHDGSLUCSGSZUUPDPFUBDUF
 PCCTSGPIDTRUHASELDNTEPBMRMHCABCTSGPIEMIGPEIFIETOSFSEFIDTBMETIAMESDGV

He sacado las frecuencias de los digramas del texto

Digrama Análisis de <Sin nombre1>. Tamaño del archivo 208 bytes.
 Ordenados descendientemente por frecuencia.

Nº	Subcadena	Frecuencia (en %)	Frecuencia
1	ET	2.4155	5
2	SG	2.4155	5
3	FI	1.9324	4
4	ME	1.9324	4
5	PC	1.9324	4
6	PE	1.9324	4
7	SF	1.9324	4
8	EP	1.4493	3
9	ES	1.4493	3
10	FC	1.4493	3
11	GP	1.4493	3
12	GS	1.4493	3
13	IF	1.4493	3
14	MI	1.4493	3
15	SE	1.4493	3
16	TS	1.4493	3
17	UP	1.4493	3
18	AM	0.9662	2
19	BC	0.9662	2
20	BD	0.9662	2
21	BM	0.9662	2
22	CT	0.9662	2
23	CY	0.9662	2
24	DG	0.9662	2
25	DN	0.9662	2
26	DP	0.9662	2

Los he comparado y sustituido con los digramas mas frecuentes en español

DE
ES
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OS
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OR
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NI
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TN
TS

Pero no he conseguido sacar el texto como se puede ver en esta prueba:

ER VRNKV EL GMFHAMTCY ES NT EL ZUMUFM RA R OS UM RE AR HMGIG NI QE DE
OR DE UZLDMS EN R AD TE ES YSCMUUN IN CW AD LU TE DU ER Q AD
YBCFRGARFYKB ET DE O OS AS EN HD OR LUC ES SZUUP ET FUBDUF AD LE ES
PIDTRUHASL NI T ER BMRMHCABCTS SE IE NT G TE I EN DE O IN ST EN DTBM DE
IAM AS DGV