

Model for Estimating Abundance of Parturient Females: Take 2

$$\begin{aligned}
 y_{it} &\sim \begin{cases} 0 & , z_{it} = 0 \\ \text{Bern}(p) & , z_{it} = 1 \end{cases} \\
 z_{it} &\sim \begin{cases} 0 & , r_{it} = 0 \\ \text{Bern}(\phi_{it}) & , r_{it} = 1 \end{cases} \\
 r_{it} &\sim \text{Bern}(\psi_{it}) \\
 p &\sim \text{Beta}(\alpha_p, \beta_p) \\
 \text{logit}(\phi_{it}) &= \mathbf{x}_{it}^T \boldsymbol{\beta} \\
 \text{logit}(\psi_{it}) &= \mathbf{w}_{it}^T \boldsymbol{\alpha} \\
 \boldsymbol{\beta} &\sim \text{N}(\boldsymbol{\mu}_\beta, \Sigma_\beta) \\
 \boldsymbol{\alpha} &\sim \text{N}(\boldsymbol{\mu}_\alpha, \Sigma_\alpha)
 \end{aligned}$$

Notation:

parturient: a female is parturient in a given year if she gave birth that year

parturient females in year t are individuals $i = 1, \dots, n_t, \dots, N_t, \dots, M_t$

n_t is the number of observed parturient females in year t

N_t is the total abundance of parturient females in year t

M_t is the augmented data for year t

t is years

y_{it} indicates if individual i was sighted with a pup in year t

z_{it} indicates if individual i **survived and had a pup** in year t

r_{it} indicates if individual i was recruited into the reproducing population in year t

p is probability of detecting an individual with her pup

ϕ_{it} is the probability of individual i surviving from year $t - 1$ to year t and having a pup in year t

ψ_{it} is the probability that individual i was recruited into the reproducing population in year t

Derived quantity:

$N_t = \sum_{i=1}^M z_{it}$ is the abundance of parturient females in year t

Thoughts

What are the covariates you want to include? If we only look at age and el nino then these only differ by year, not individual, and we can make p , ψ , and ϕ only differ across years.

Do we need to augment the data at all? I think I'm getting my models confused. If we are summing z_i 's I don't think we actually have to augment it at all. Right?