

Permutations Rule :

$$P_r^n = \frac{n!}{(n-r)!}$$

Combinations Rule :

$$C_r^n = \frac{n!}{r!(n-r)!}$$

Union : $A \cup B$

Intersection : $A \cap B$

Mutually Exclusive :

$$P(A \cup B) = P(A) + P(B)$$

Complement :

$$P(A) = 1 - P(\bar{A})$$

Joint Probability :

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

Conditional Probability :

$$P(A|B) = \frac{P(A \cap B)}{P(B)} \text{ and } P(B|A) = \frac{P(A \cap B)}{P(A)}$$

$$P(A \cap B) = P(A) * P(B|A) = P(B) * P(A|B)$$

For Independent :

$$P(A|B) = P(A) \text{ and } P(B|A) = P(B)$$

$$P(A \cap B) = P(A) * P(B)$$

$$\text{Law of Total Probability : } P(A) = P(B_1 \cap A) + P(B_2 \cap A) + P(B_3 \cap A) = P(B_1)P(A|B_1) + P(B_2)P(A|B_2) + \dots + P(B_n)P(A|B_n)$$

Prior Probability

Posterior Probability

$$\text{Bayes' Theorem : } P(B_k|A) = \frac{P(B_k \cap A)}{P(A)} = \frac{P(B \cap A)}{P(B \cap A) + P(\bar{B} \cap A)}$$

$$\text{Circle : } (n-1)!$$

Expected Value :

$$\mu = E(X) = \sum x * P(x)$$

The Variance of X is :

$$\sigma^2 = Var(X) = \sum (x - \mu)^2 * P(x)$$

Binomial Formula :

$$P(x) = P(X = x) = \binom{n}{x} p^x (1 - p)^{n-x}$$

Under this case : (X Bin(n, p))

$$\mu = E(X) = np$$

$$\sigma^2 = Var(X) = np(1 - p)$$

Poisson Probability Distribution Formula :

$$P(x) = P(X = x) = \frac{\lambda^x e^{-\lambda}}{x!}$$

Under this Case :

$$\mu = E(X) = \lambda$$

$$\sigma^2 = Var(X) = \lambda$$

Hypergeometric Probability Distribution Formula :

$$P(x) = P(X = x) = \frac{\binom{r}{x} \binom{N-r}{n-x}}{\binom{N}{n}}$$

Under this Case :

$$\mu = E(X) = \frac{nr}{N}$$

$$\sigma^2 = Var(X) = n \left(\frac{r}{N} \right) \left(\frac{N-r}{N} \right) \left(\frac{N-n}{N-1} \right)$$

Negative Binomial Distribution :

$$P(X = k) = \binom{k-1}{r-1} p^r (1-p)^{k-r}$$

Under this case : (X NegBin(r, p))

$$\mu = E(X) = \frac{r}{p}$$

$$\sigma^2 = Var(X) = \frac{r(1-p)}{p^2}$$

Geometric Distribution : $N \sim Geo(x)$

$$P(N = x) = p(1-p)^{x-1}$$

Sampling Distribution(\bar{x})

$$\bar{x} \sim N\left(\mu, \left(\frac{\sigma}{\sqrt{n}}\right)^2\right)$$

$$(if \frac{n}{N} > 0.05) \sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}} \times \sqrt{\frac{N-n}{N-1}}$$

Normal Distribution ==> Binomial Distribution

(if $np > 5$ & $n(1-p) > 5$)

$$\mu = np\sigma = \sqrt{np(1-p)}$$

1. $\bar{x} \pm z_{\frac{\alpha}{2}} \times \frac{\sigma}{\sqrt{n}}$
2. $v = n - 1$
3. (*Remind : like within...*)
 $z_{\frac{\alpha}{2}} \times \frac{\sigma}{\sqrt{n}}$
4. $\bar{x} \pm t_{\frac{\alpha}{2};v} \times \frac{s}{\sqrt{n}}$
5. $s^2 = \frac{\sum x^2 - (\sum x)^2/n}{n - 1}$
6. $(\bar{x}_1 - \bar{x}_2) \pm z_{\frac{\alpha}{2}} \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}$