

③  $m = 1.05$ ,  $b = 0.66$

$$\hat{y}_1 = 1.05(1) + 0.66$$

$$\text{Error}_1 = 2 - 1.71 = 0.29$$

$$= 1.71$$

$$\hat{y}_2 = 1.05(2) + 0.66$$

$$\text{Error}_2 = 3 - 2.76 = 0.24$$

$$= 2.76$$

Gradients:

$$\frac{\partial J}{\partial m} = \frac{2}{2} (1 \times 0.29 + 2 \times 0.24) = -1(0.29 + 0.48) = -0.77$$

$$\frac{\partial J}{\partial b} = -\frac{2}{2} (0.29 + 0.24) = -1(0.53) = -0.53$$

Update  $m$  &  $b$ :

$$m_{\text{new}} = 1.05 - 0.1(-0.77) = 1.05 + 0.077 = 1.127$$

$$b_{\text{new}} = 0.66 - 0.1(-0.53) = 0.66 + 0.053 = 0.713$$

$\hat{y}$  - predicted:

$$y_1 = 1.127(1) + 0.713 = 1.84$$

$$\text{Error}_1 = 2 - 1.84 = 0.16$$

$$y_2 = 1.127(2) + 0.713 = 2.967$$

$$\text{Error}_2 = 3 - 2.967 = 0.033$$





$$MSE = \frac{(0.16)^2 + (0.033)^2}{2}$$

$$= \underline{\underline{0.0133445}}$$