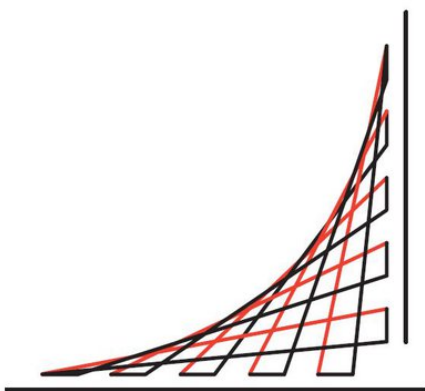


# Tarea 04

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## 1. Punto 2

### Punto 2

$A$  dice: “Soy escudero o  $B$  es un caballero”

$$\Gamma_0 = \{(a \equiv ((\neg a) \vee b)), a\}$$

$$\Gamma_1 = \{(a \equiv ((\neg a) \vee b)), (\neg a)\}$$

$\therefore$   $A$  es caballero y  $B$  es escudero

Con  $\Gamma_0$

0.  $(\exists \mathbf{v} \mid \mathbf{v} \text{ satisface } \Gamma_0)$
1.  $\mathbf{v}[(a \equiv ((\neg a) \vee b))] = \mathbf{T}$  Def.(p0)
2.  $\mathbf{v}[a] = \mathbf{T}$  Def.(p0)
3.  $\mathbf{v}[(\neg a) \vee b] = \mathbf{T}$  MT 2.23( $\equiv$ )(p2, p1)
4.  $\mathbf{v}[(\neg a)] = \mathbf{T}$  o  $\mathbf{v}[b] = \mathbf{T}$  MT 2.23 ( $\vee$ )(p3)
5.  $\mathbf{v}[b] = \mathbf{T}$  MT 2.23( $\vee$ )(p4, p2)

Con  $\Gamma_1$

0.  $(\exists \mathbf{v} \mid \mathbf{v} \text{ satisface } \Gamma_1)$
1.  $\mathbf{v}[(a \equiv ((\neg a) \vee b))] = \mathbf{T}$  Def.(p0)
2.  $\mathbf{v}[(\neg a)] = \mathbf{T}$  Def.(p0)
3.  $\mathbf{v}[(\neg a) \vee b] = \mathbf{F}$  MT 2.23( $\equiv$ )(p2, p1)
4.  $\mathbf{v}[(\neg a)] = \mathbf{F}$  y  $\mathbf{v}[b] = \mathbf{F}$  MT 2.23( $\vee$ )(p3)
5.  $\mathbf{v}[(\neg a)] = \mathbf{F}$  y  $\mathbf{v}[(\neg a)] = \mathbf{T}$  Contradicción (p4, p2)

## 2. Punto 11

### Punto 11

$B$  dijo: “ $A$  dijo que es escudero”

$C$  dijo: “No le crea a  $B$  porque está mintiendo”

$$\Gamma_0 = \{(b \equiv (a \equiv (\neg a))), (c \equiv (\neg b)), b\}$$

$$\Gamma_1 = \{(b \equiv (a \equiv (\neg a))), (c \equiv (\neg b)), (\neg b)\}$$

$\therefore$   $B$  es escudero y  $C$  es caballero

Con  $\Gamma_0$

0.  $(\exists \mathbf{v} \mid \mathbf{v} \text{ satisface } \Gamma_0)$
1.  $\mathbf{v}[(b \equiv (a \equiv (\neg a)))] = \mathbf{T}$  Def.(p0)
2.  $\mathbf{v}[b] = \mathbf{T}$  Def.(p0)
3.  $\mathbf{v}[(a \equiv (\neg a))] = \mathbf{F}$  MT 2.23 ( $\equiv$ )
4.  $\mathbf{v}[b] = \mathbf{F}$  MT 2.23( $\equiv$ )(p1)
5.  $\mathbf{v}[b] = \mathbf{T}$  y  $\mathbf{v}[b] = \mathbf{F}$  Contradicción (p4, p2)

Con  $\Gamma_1$

0.  $(\exists \mathbf{v} \mid \mathbf{v} \text{ satisface } \Gamma_0)$
1.  $\mathbf{v}[(b \equiv (a \equiv (\neg a)))] = \mathbf{T}$  Def.(p0)
2.  $\mathbf{v}[b] = \mathbf{T}$  Def.(p0)
3.  $\mathbf{v}[c] = \mathbf{T}$

### 3. Punto 12

Punto 12

$B$  dijo: “ $A$  dijo que hay al menos un caballero entre nosotros”

$C$  dijo: “ $B$  miente”

$\Gamma_0 = \{(b \equiv (a \equiv (a \vee b \vee c))), (c \equiv (\neg b)), b\}$

$\Gamma_1 = \{(b \equiv (a \equiv (a \vee b \vee c))), (c \equiv (\neg b)), (\neg b)\}$

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$\therefore$  No es posible determinar su naturaleza

Con  $\Gamma_0$

0.  $(\exists \mathbf{v} \mid \mathbf{v} \text{ satisface } \Gamma_0)$
1.  $\mathbf{v}[(b \equiv (a \equiv (a \vee b \vee c)))] = \mathbf{T}$  Def.(p0)
2.  $\mathbf{v}[(c \equiv (\neg b))] = \mathbf{T}$  Def.(p0)
3.  $\mathbf{v}[b] = \mathbf{T}$  Def.(p0)
4.  $\mathbf{v}[(\neg b)] = \mathbf{F}$  MT 2.23( $\neg$ )(p3)
5.  $\mathbf{v}[c] = \mathbf{F}$  MT 2.23( $\equiv$ )(p4,p2)

Con  $\Gamma_1$

0.  $(\exists \mathbf{v} \mid \mathbf{v} \text{ satisface } \Gamma_0)$
1.  $\mathbf{v}[(b \equiv (a \equiv (a \vee b \vee c)))] = \mathbf{T}$  Def.(p0)
2.  $\mathbf{v}[(c \equiv (\neg b))] = \mathbf{T}$  Def.(p0)
3.  $\mathbf{v}[(\neg b)] = \mathbf{T}$  Def.(p0)
4.  $\mathbf{v}[c] = \mathbf{T}$  MT 2.23( $\equiv$ )(p3, p2)

## 4. Punto 13

### Punto 13

A dice: “Todos nosotros somos escuderos”

B dice: “Exactamente uno de nosotros es caballero”

$$\begin{aligned}\Gamma_0 &= \{(a \equiv ((\neg a) \wedge (\neg b) \wedge (\neg c))), \\ &\quad (b \equiv (a \wedge (\neg b) \wedge (\neg c)) \vee ((\neg a) \wedge b \wedge (\neg c)) \vee ((\neg a) \wedge (\neg b) \wedge c)), ((\neg a) \wedge (\neg b))\} \\ \Gamma_1 &= \{(a \equiv ((\neg a) \wedge (\neg b) \wedge (\neg c))), \\ &\quad (b \equiv (a \wedge (\neg b) \wedge (\neg c)) \vee ((\neg a) \wedge b \wedge (\neg c)) \vee ((\neg a) \wedge (\neg b) \wedge c)), b\} \\ \Gamma_2 &= \{(a \equiv ((\neg a) \wedge (\neg b) \wedge (\neg c))), \\ &\quad (b \equiv (a \wedge (\neg b) \wedge (\neg c)) \vee ((\neg a) \wedge b \wedge (\neg c)) \vee ((\neg a) \wedge (\neg b) \wedge c)), (\neg b)\}\end{aligned}$$

∴ A es escudero, no se puede determinar la naturaleza de los demás

#### Con $\Gamma_0$

0.  $(\exists \mathbf{v} \mid \mathbf{v} \text{ satisface } \Gamma_0)$
1.  $\mathbf{v}[(a \equiv ((\neg a) \wedge (\neg b) \wedge (\neg c)))] = \mathbf{T}$  Def.(p0)
2.  $\mathbf{v}[(b \equiv (a \wedge (\neg b) \wedge (\neg c)) \vee ((\neg a) \wedge b \wedge (\neg c)) \vee ((\neg a) \wedge (\neg b) \wedge c))]$  Def.(p0)
3.  $\mathbf{v}[(\neg a) \wedge (\neg b)]$
4.  $\mathbf{v}[(\neg c)] = \mathbf{F}$  MT 2.23( $\equiv, \wedge$ )(p3, p1)

#### Con $\Gamma_1$

0.  $(\exists \mathbf{v} \mid \mathbf{v} \text{ satisface } \Gamma_1)$
1.  $\mathbf{v}[(a \equiv ((\neg a) \wedge (\neg b) \wedge (\neg c)))] = \mathbf{T}$  Def.(p0)
2.  $\mathbf{v}[(b \equiv (a \wedge (\neg b) \wedge (\neg c)) \vee ((\neg a) \wedge b \wedge (\neg c)) \vee ((\neg a) \wedge (\neg b) \wedge c))]$  Def.(p0)
3.  $\mathbf{v}[b] = \mathbf{T}$
4.  $\mathbf{v}[(\neg a) \wedge b \wedge (\neg c)] = \mathbf{F}$  MT 2.23( $\equiv, \wedge$ ) (p2)
5.  $\mathbf{v}[a] = \mathbf{F}$  MT 2.23( $\wedge, \neg$ )
6.  $\mathbf{v}[c] = \mathbf{F}$  MT 2.23( $\wedge, \neg$ )

#### Con $\Gamma_2$

0.  $(\exists \mathbf{v} \mid \mathbf{v} \text{ satisface } \Gamma_2)$
1.  $\mathbf{v}[(a \equiv ((\neg a) \wedge (\neg b) \wedge (\neg c)))] = \mathbf{T}$  Def.(p0)
2.  $\mathbf{v}[(b \equiv (a \wedge (\neg b) \wedge (\neg c)) \vee ((\neg a) \wedge b \wedge (\neg c)) \vee ((\neg a) \wedge (\neg b) \wedge c))]$  Def.(p0)
3.  $\mathbf{v}[(\neg b)] = \mathbf{T}$  Def.(p0)
4.  $\mathbf{v}[(a \wedge (\neg b) \wedge (\neg c))] = \mathbf{F}$  MT 2.23( $\neg, \vee$ )(p3, p2)
5.  $\mathbf{v}[(\neg b)] = \mathbf{F}$  MT 2.23( $\wedge$ )(4)
6.  $\mathbf{v}[(\neg b)] = \mathbf{F} \text{ y } \mathbf{v}[(\neg b)] = \mathbf{T}$  Contradicción (p5, p3)

## 5. Punto 14

### Punto 14

$A$  dice: “Todos somos escuderos”

$B$  dice: “Exactamente uno de nosotros es escudero”

$$\Gamma_0 = \{ (a \equiv ((\neg a) \wedge (\neg b) \wedge (\neg c))), \\ (b \equiv (((\neg a) \wedge b \wedge c) \vee (a \wedge (\neg b) \wedge c) \vee (a \wedge b \wedge (\neg c))))), (\neg a) \}$$

$$\Gamma_1 = \{ (a \equiv ((\neg a) \wedge (\neg b) \wedge (\neg c))), \\ (b \equiv (((\neg a) \wedge b \wedge c) \vee (a \wedge (\neg b) \wedge c) \vee (a \wedge b \wedge (\neg c))))), a \}$$

El ejercicio está mal planteado

#### Con $\Gamma_0$

0.  $(\exists \mathbf{v} \mid \mathbf{v} \text{ satisface } \Gamma_0)$
1.  $\mathbf{v}[(a \equiv ((\neg a) \wedge (\neg b) \wedge (\neg c)))] = \mathbf{T}$  Def.(p0)
2.  $\mathbf{v}[(b \equiv (((\neg a) \wedge b \wedge c) \vee (a \wedge (\neg b) \wedge c) \vee (a \wedge b \wedge (\neg c))))] = \mathbf{T}$  Def.(p0)
3.  $\mathbf{v}[(\neg a)] = \mathbf{T}$  Def.(p0)
4.  $\mathbf{v}[a] = \mathbf{F}$  MTT 2.23( $\neg$ )(p3)
5.  $\mathbf{v}[(\neg a)] = \mathbf{F}$  y  $\mathbf{v}[(\neg b)] = \mathbf{F}$  y  $\mathbf{v}[(\neg c)] = \mathbf{F}$  MT 2.23 ( $\equiv, \wedge$ )(p4, p1)
6.  $\mathbf{v}[(\neg a)] = \mathbf{F}$  y  $\mathbf{v}[(\neg a)] = \mathbf{T}$  Contradicción (p5, p3)

#### Con $\Gamma_1$

0.  $(\exists \mathbf{v} \mid \mathbf{v} \text{ satisface } \Gamma_0)$
1.  $\mathbf{v}[(a \equiv ((\neg a) \wedge (\neg b) \wedge (\neg c)))] = \mathbf{T}$  Def.(p0)
2.  $\mathbf{v}[(b \equiv (((\neg a) \wedge b \wedge c) \vee (a \wedge (\neg b) \wedge c) \vee (a \wedge b \wedge (\neg c))))] = \mathbf{T}$  Def.(p0)
3.  $\mathbf{v}[a] = \mathbf{T}$  Def.(p0)
4.  $\mathbf{v}[(\neg a)] = \mathbf{T}$  y  $\mathbf{v}[(\neg b)] = \mathbf{T}$  y  $\mathbf{v}[(\neg c)] = \mathbf{T}$  MT 2.23( $\equiv, \wedge$ )
5.  $\mathbf{v}[a] = \mathbf{F}$  MT 2.23( $\neg$ )(p4)
6.  $\mathbf{v}[a] = \mathbf{T}$  y  $\mathbf{v}[a] = \mathbf{F}$  (p5, p3)

## 6. Punto 18

El habitante  $A$  dice “Yo dije que si soy caballero entonces soy escudero, y si soy escudero entonces soy caballero”

## 7. Punto 19

El habitante  $A$  dice “Si  $B$  es caballero, entonces soy caballero”

El habitante  $B$  dice “Si soy caballero, entonces  $A$  es caballero”

## 8. Punto 23

### Punto 23

$C$  dijo: “A lo sumo uno de nosotros es caballero”

$$\Gamma_0 = \{ (c \equiv (a \wedge (\neg b) \wedge (\neg c)) \vee ((\neg a) \wedge b \wedge (\neg c)) \vee ((\neg a) \wedge (\neg b) \wedge c) \vee ((\neg a) \wedge (\neg b) \wedge (\neg c))), c \}$$

$$\Gamma_1 = \{ (c \equiv (a \wedge (\neg b) \wedge (\neg c)) \vee ((\neg a) \wedge b \wedge (\neg c)) \vee ((\neg a) \wedge (\neg b) \wedge c) \vee ((\neg a) \wedge (\neg b) \wedge (\neg c))), (\neg c) \}$$

$C$  es el único caballero, y por ende el único hombre lobo (tomando la suposición dada por el enunciado).

... Tomando lo que dijo  $C$  como  $\phi$ ...

#### Con $\Gamma_0$

0.  $(\exists \mathbf{v} \mid \mathbf{v} \text{ satisface } \Gamma_0)$
1.  $\mathbf{v}[(c \equiv \phi)] = \mathbf{T}$  Def.(p0)
2.  $\mathbf{v}[c] = \mathbf{T}$  Def(p0)
3.  $\mathbf{v}[(\neg a) \wedge (\neg b) \wedge c] = \mathbf{T}$  MT 2.23( $\equiv, \wedge$ )(p2, p1)

#### Con $\Gamma_1$

0.  $(\exists \mathbf{v} \mid \mathbf{v} \text{ satisface } \Gamma_0)$
1.  $\mathbf{v}[(c \equiv \phi)] = \mathbf{T}$  Def.(p0)
2.  $\mathbf{v}[(\neg c)] = \mathbf{T}$  Def(p0)
3.  $\mathbf{v}[(a \wedge (\neg b) \wedge (\neg c))] = \mathbf{F}$  MT 2.23( $\equiv, \wedge$ ) (p2, p1)
4.  $\mathbf{v}[(\neg c)] = \mathbf{F}$  MTT 2.23 ( $\wedge$ )(p3)
5.  $\mathbf{v}[(\neg c)] = \mathbf{F}$  y  $\mathbf{v}[(\neg c)] = \mathbf{T}$  Contradicción (p4, p2)