

## Basic equations

$$U(n) = \sum_{i=1}^n \frac{C_i}{T_i} \leq n \cdot (2^{\frac{1}{n}} - 1)$$

$$\prod_{i=1}^n (\frac{C_i}{T_i} + 1) \leq 2$$

$$\forall i, Rwc_i = I_i + C_i$$

$$I_i = \sum_{k \in hp(i)} \lceil \frac{Rwc_k}{T_k} \rceil \cdot C_k$$

$$U(n) = \sum_{i=1}^n (\frac{C_i}{T_i}) \leq 1$$

$$L(0) = \sum_i (C_i)$$

$$L(m+1) = \sum_i (\lceil \frac{L(m)}{T_i} \rceil \cdot C_i)$$

$$h(t) = \sum_{i=1..N} \max(0, 1 + \lfloor \frac{t-D_i}{T_i} \rfloor) \cdot C_i$$

$$S = \bigcup_i (S_i), S_i = \{m \cdot T_i + D_i\}, m = 0, 1, \dots$$

## With blocking times

$$\forall 1 \leq i \leq N \quad \sum_{h: P_h > P_i} (\frac{C_h}{T_h}) + \frac{C_i + B_i}{T_i} \leq i \cdot (2^{\frac{1}{i}} - 1)$$

$$R_i(0) = C_i + B_i$$

$$R_i(m) = C_i + B_i + \sum_{h: P_h > P_i} \lceil \frac{R_i(m-1)}{T_h} \rceil C_h$$

## Servers

$$Rwc_i^a = C a_i + (T_s - C_s) \cdot (1 + \lceil \frac{C a_i}{C_s} \rceil)$$

$$U_p + U_s \leq (n+1) \cdot (2^{\frac{1}{n+1}} - 1)$$

$$U_p \leq n \cdot [(\frac{2}{U_s+1})^{\frac{1}{n}} - 1]$$

$$\prod_{i=1}^n (U_i + 1) \leq \frac{2}{U_s+1}$$

$$U_{lub}^{DS} = U_s + n \cdot [(\frac{U_s+2}{2U_s+1})^{\frac{1}{n}} - 1]$$

$$U_p^{SS} \leq n \cdot [(\frac{2}{U_s+1})^{\frac{1}{n}} - 1] ; \prod_{i=1}^n (U_i + 1) \leq \frac{2}{U_s+1}$$

$$d_k = \max(r_k, d_{k-1}) + \frac{C_k}{U_s}$$

If  $r_k + \frac{c_s}{U_s} < d_s^{actual}$ , then  $d_s^{actual}$  does not change.

Otherwise,  $d_s = r_k + T_s$  and  $c_s = Q_s$

If  $c_s = 0$ :  $d_s = d_s + T_s$  and  $c_s = Q_s$

## Non-preemption

$$L_i(0) = B_i + C_i$$

$$L_i(s) = B_i + \sum_{h: P_h \geq P_i} \lceil \frac{L_i(s-1)}{T_h} \rceil \cdot C_h$$

$$K_i = \lceil \frac{L_i}{T_i} \rceil$$

$$s_{i,k}^{(0)} = B_i + \sum_{h: P_h > P_i} C_h$$

$$s_{i,k}^{(l)} = B_i + (k-1) \cdot C_i + \sum_{h: P_h > P_i} \left( \left\lfloor \frac{s_{i,k}^{(l-1)}}{T_h} \right\rfloor + 1 \right) \cdot C_h$$

$$f_{i,k} = s_{i,k} + C_i$$

$$Rwc_i = \max_{k \in [1, K_i]} \{f_{i,k} - (k-1) \cdot T_i\}$$

## Overheads

$$\sigma = \frac{C_1^1 - C_1^0}{\lceil \frac{C_1^1}{T_{T_{ic}k}} \rceil} ; \delta = \frac{C_1^1 - C_1^0}{\lceil \frac{C_1^1}{T_2} \rceil}$$

## Release jitter

$$\forall i, Rwc_i = I_i + C_i, \text{ with } I_i = \sum_{k \in hp(i)} \lceil \frac{Rwc_k + J_k}{T_k} \rceil \cdot C_k$$

$$Rwc_i(0) = \left( \sum_{k \in hp(i)} C_k \right) + C_i$$

$$Rwc_i(m+1) = \left( \sum_{k \in hp(i)} \lceil \frac{Rwc_k(m) + J_k}{T_k} \rceil \cdot C_k \right) + C_i$$

## Multicore

$$C_i^S = \sum_{j=1}^{m_i} c_{i,j} ; U_i = \frac{C_i^S}{T_i}$$

$$\alpha_i = \frac{T_i}{D_i} ; V = \sum_i^n a_i$$

$$M_{lb} = \lceil \frac{V}{c} \rceil ; M_{ub} = \lceil \frac{2 \cdot V}{c} \rceil$$

$$M_{on} \geq \frac{4}{3} M_o$$

- NF/WF never use more than  $2 \cdot M0$  bins
- FF/BF never use more than  $(1.7 \cdot M0 + 1)$  bins
- FFD never uses more than  $(\frac{4}{3} M0 + 1)$  bins
- FFD never uses more than  $(\frac{11}{9} M0 + 4)$  bins
- Task sets with  $U \leq \frac{m+1}{2}$  are schedulable with  $m$  processors using FF + EDF scheduling.
- Task sets with  $U \leq m(2^{\frac{1}{2}} - 1)$  are schedulable with  $m$  processors using FF + RM scheduling.
- When each task has utilization  $u_i \leq \frac{m}{3m-2}$ , the task set is feasible by global RM scheduling if  $U \leq \frac{m^2}{3m-2}$ .