

TP2

1.4) $m = 0,1 \text{ kg}$ $V_A = 25 \text{ m/s}$
 $R = 4 \text{ m}$

a) $\omega = \frac{V}{R} = \frac{25}{4} = 6,25 \text{ m/s}$

b) $\alpha = \frac{d\omega}{dt} \Rightarrow \int_{\omega_0}^{\omega(t)} d\omega = \int_{t_0}^t \alpha dt$

$\Leftrightarrow \alpha(t - t_0) = \omega(t) - \omega_0$



$\omega(t) = \omega_0 + \alpha t = 6,25 + \alpha t$

$\omega(t) = \frac{d\theta}{dt} \Leftrightarrow \int_{\theta_0}^{\theta(t)} d\theta = \int_{t_0}^t \omega(t) dt \Leftrightarrow \int_{t_0}^t 6,25 + \alpha t = \theta(t) - \theta_0$

$\Leftrightarrow \theta(t) = \theta_0 + 6,25t + \frac{\alpha}{2} t^2$

$\theta(0,3) = \pi \text{ rad}$

$\pi = 6,25(0,3) + \frac{\alpha}{2} (0,3)^2 \Leftrightarrow \alpha = 28,1 \text{ rad/s}^2$

$\theta(t) = 6,25t + \frac{28,1}{2} t^2$

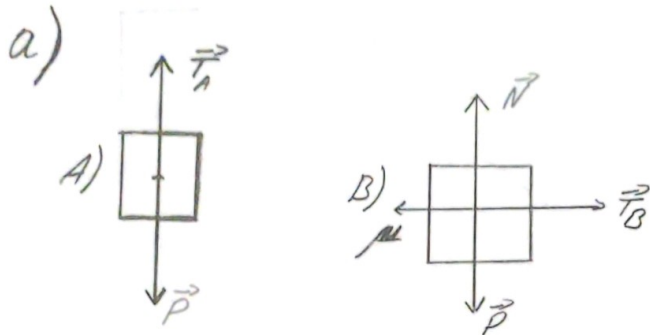
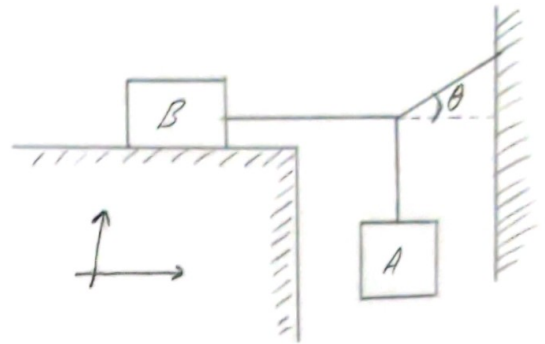
c) $F_c = m \times a_c$

$a_c(0,3) = \frac{v^2}{R} = \omega^2 R$

$\omega(0,3) = 6,25 + 28,1(0,3) = 14,68 \text{ rad/s}$

$F_c = (14,68)^2 \times 4 \times 0,1 = 86,2 \text{ N}$

2.1) $\mu = 0,25$
 $\theta = 30^\circ$



b) A)
$$\begin{cases} \text{nn} & \text{---} \\ \text{yy} & T_A - P_A = 0 \end{cases}$$

B)
$$\begin{cases} \text{nn} & T_B - F_a = 0 \\ \text{yy} & N - P = 0 \end{cases}$$

$$T_A = T \sin(\theta) \quad \text{e} \quad T_B = T \cos(\theta)$$

$$\begin{cases} T \cos(\theta) - \mu N_B g = 0 \\ T \sin(\theta) - N_A g = 0 \end{cases} \Leftrightarrow \begin{cases} T \cos(\theta) = \mu N_B g \\ T \sin(\theta) = N_A g \end{cases}$$

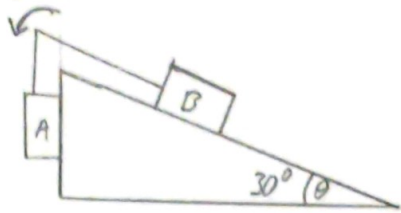
$$\Leftrightarrow \begin{cases} T \cos(\theta) = 0,25 N_B g \\ T \sin(\theta) = N_A g \end{cases}$$

$$\begin{aligned} \tan(\theta) &= \frac{N_A g}{N_B g \cdot 0,25} \\ &= \frac{N_A}{N_B \cdot 0,25} \end{aligned}$$

$$\Leftrightarrow \frac{1}{\sqrt{3}} = \frac{N_A}{N_B \cdot 0,25} \quad \Leftrightarrow \frac{0,25}{\sqrt{3}} = \frac{N_A}{N_B}$$

$$\Leftrightarrow \frac{N_A}{N_B} = 0,14$$

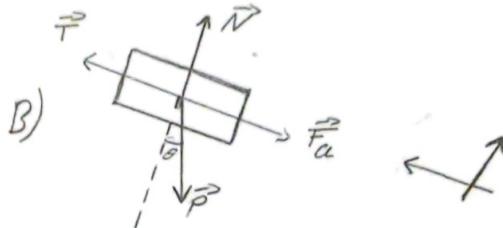
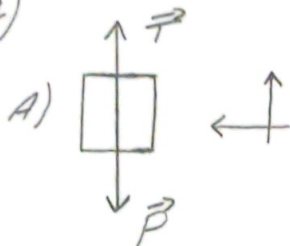
22)



$$M_A = 2 \text{ kg}$$

$$M_B = 1 \text{ kg}$$

a)



b)

A)

$$\begin{array}{l} \text{mm} \} \text{---} \\ \text{yy} \} T - P = -ma \end{array}$$

B)

$$\begin{array}{l} \text{xx} \} T - F_a - P \sin(\theta) = ma \\ \text{yy} \} N - P \cos(\theta) = 0 \end{array}$$

c)

AB)

$$\begin{cases} T - \mu M_B g - M_B g \sin(30) = M_B a \\ T - M_A g = -M_A a \end{cases} \quad \Leftrightarrow$$

$$\Leftrightarrow \begin{cases} T - (M_B (\mu g + g \frac{1}{2})) = M_B a \\ T = M_A (g - a) \end{cases} \quad \Leftrightarrow \begin{cases} T = M_B (\mu g + g \frac{1}{2} + a) \\ T = M_A (g - a) \end{cases}$$

$$\Leftrightarrow \begin{cases} T = (\mu 9.8 + 4.9 + 3) \\ T = 2(9.8 - 3) \end{cases} \quad \Leftrightarrow \begin{cases} 13.6 = \mu 9.8 + 7.9 \\ T = 13.6 \end{cases} \quad \Leftrightarrow$$

$$\Leftrightarrow \begin{cases} 5.7 = \mu 9.8 \\ T = 13.6 \end{cases} \quad \Leftrightarrow \begin{cases} \mu = 0.58 \\ T = 13.6 \end{cases}$$