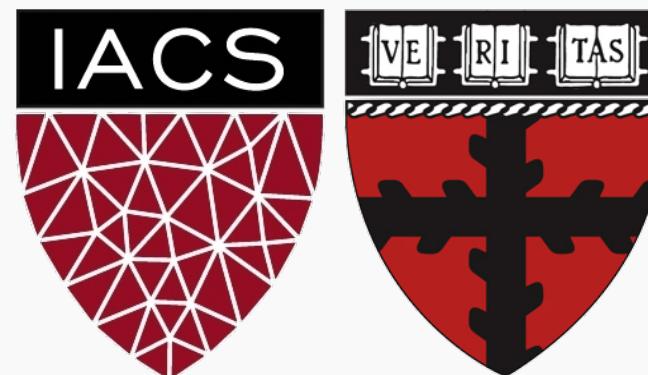


# Part A: Universal Approximators; Nodes and Layers

CS109A Introduction to Data Science  
Pavlos Protopapas, Kevin Rader and Chris Tanner



# Design Choices

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Activation function

Loss function

Output units

Architecture

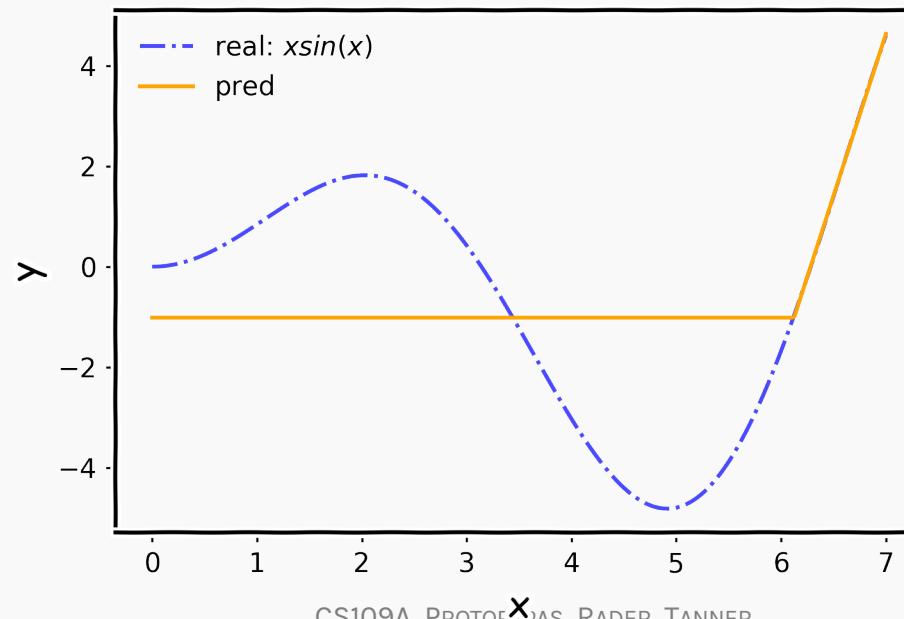
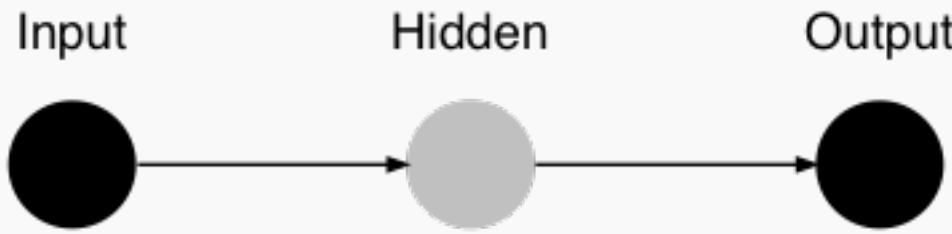
Optimizer



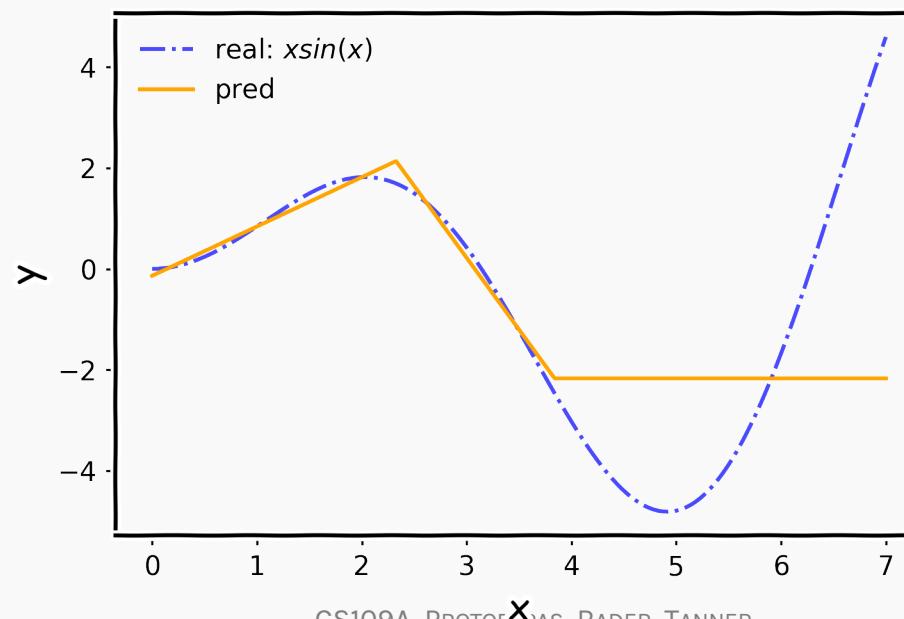
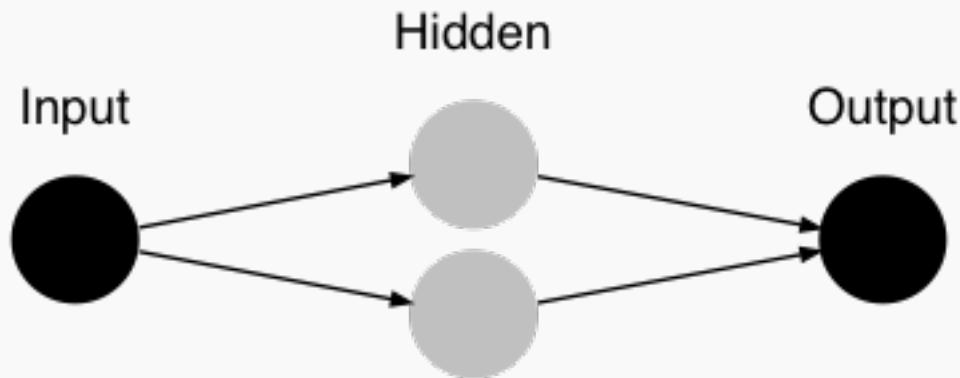


How to bully machine learning  
training

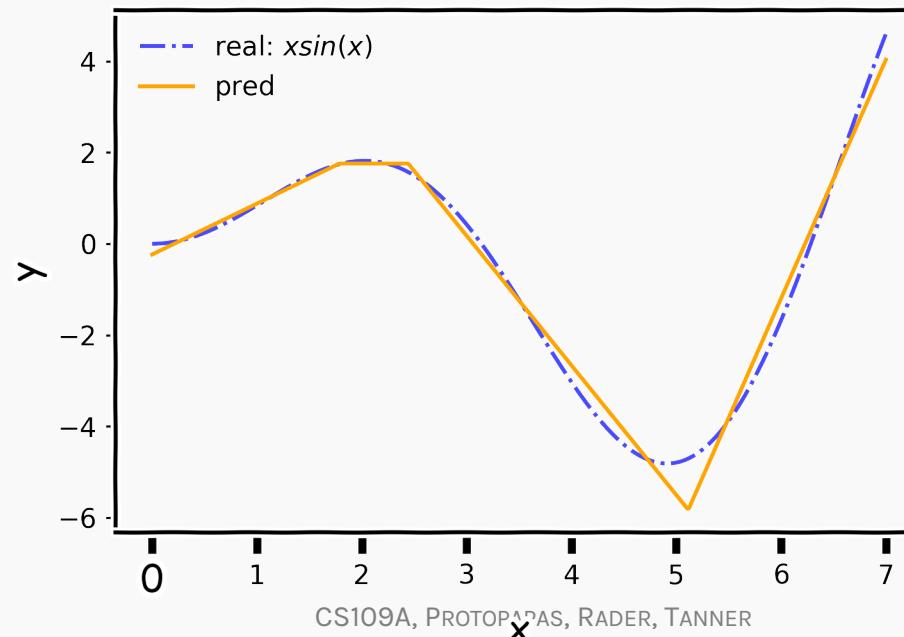
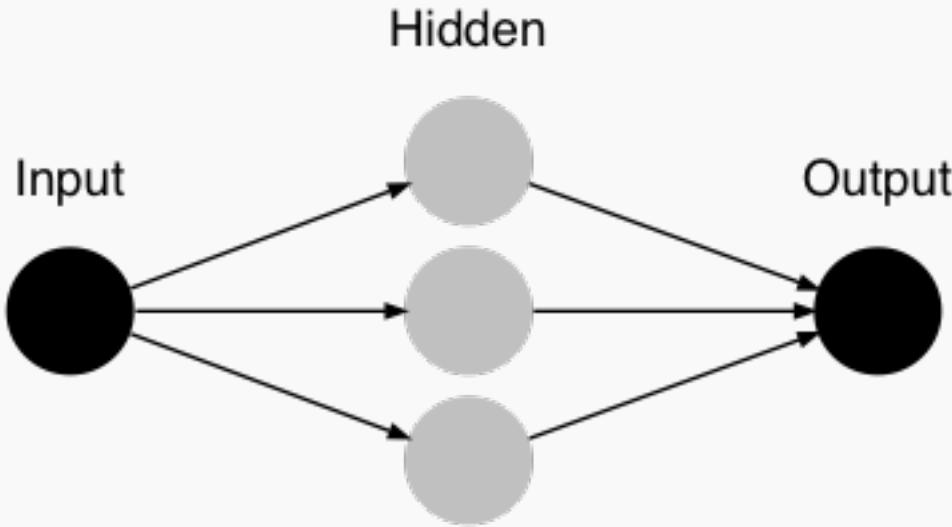
# Number of nodes



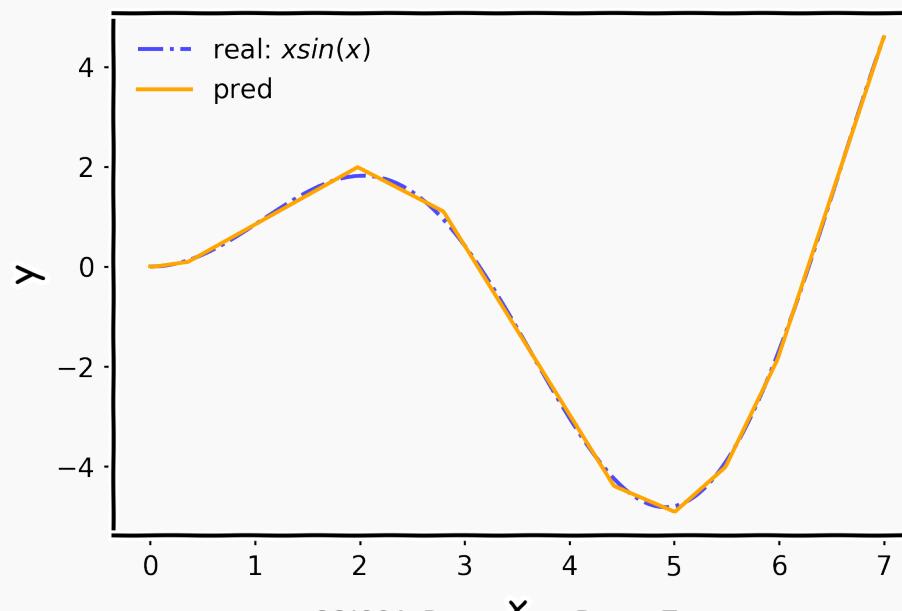
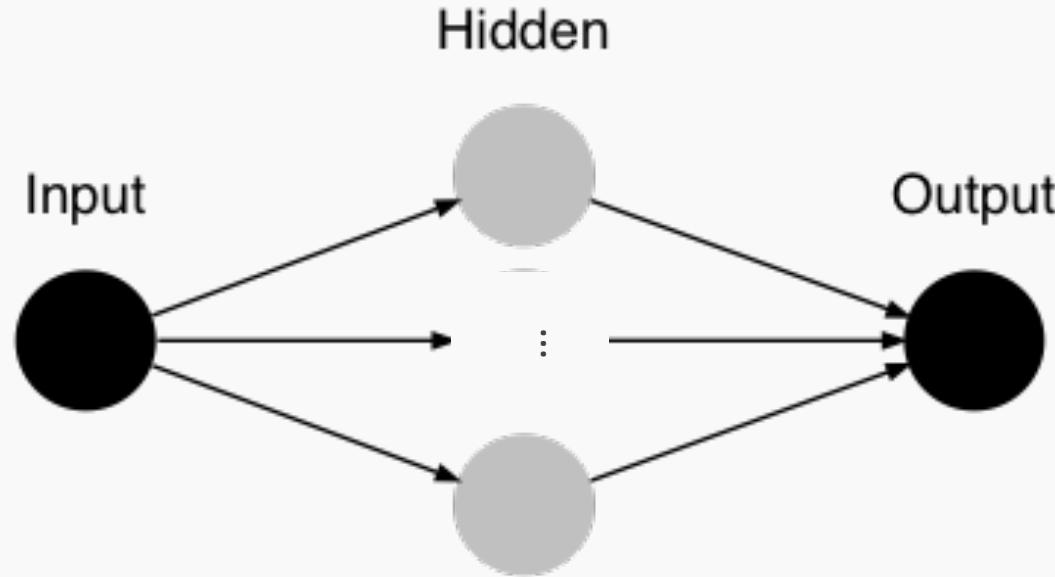
# Number of nodes



# Number of nodes

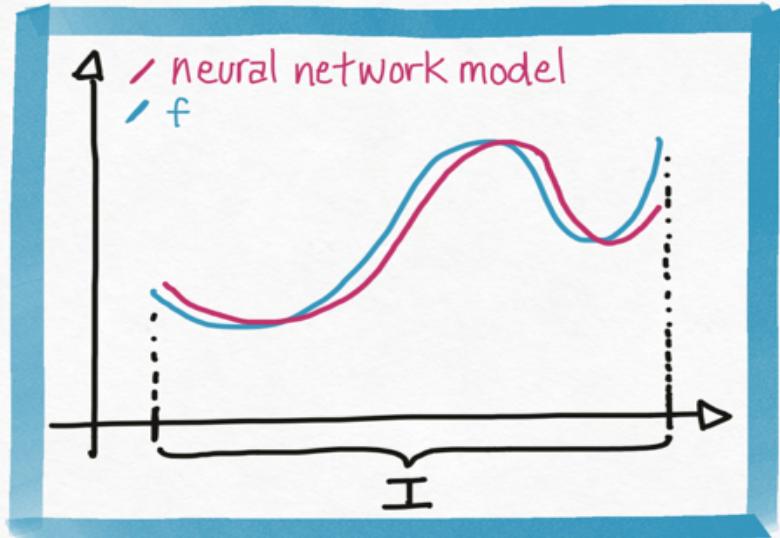


# Number of nodes





# Neural Networks as Universal Approximators



We have seen that neural networks can represent complex functions, but are there limitations on what a neural network can express?

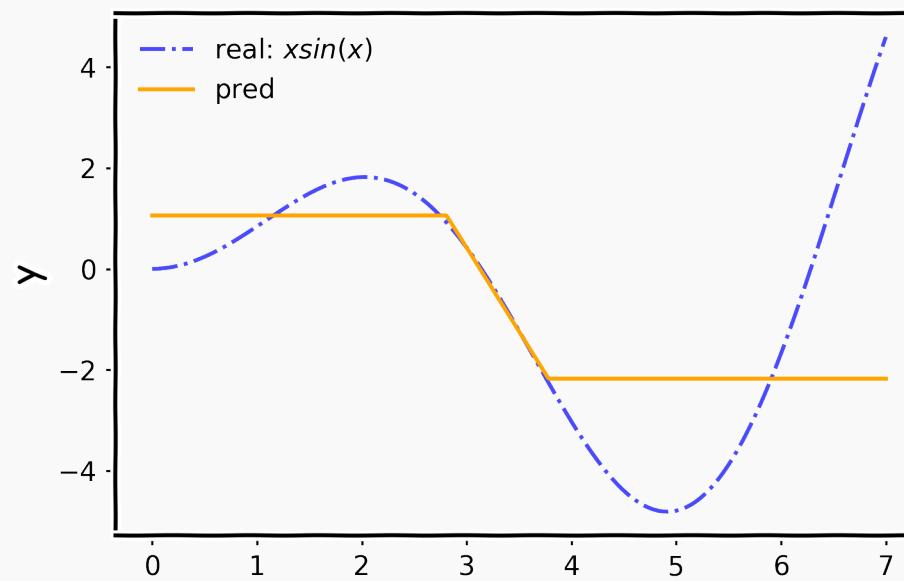
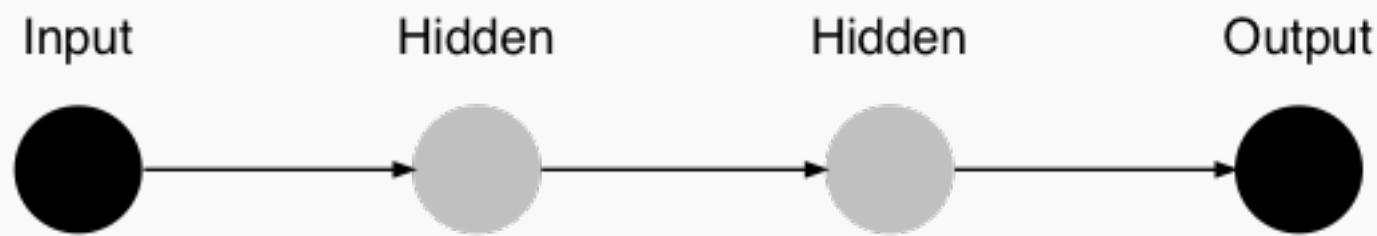
## Theorem:

For any continuous function  $f$  defined on a bounded domain, we can find a neural network that approximates  $f$  with an arbitrary degree of accuracy.

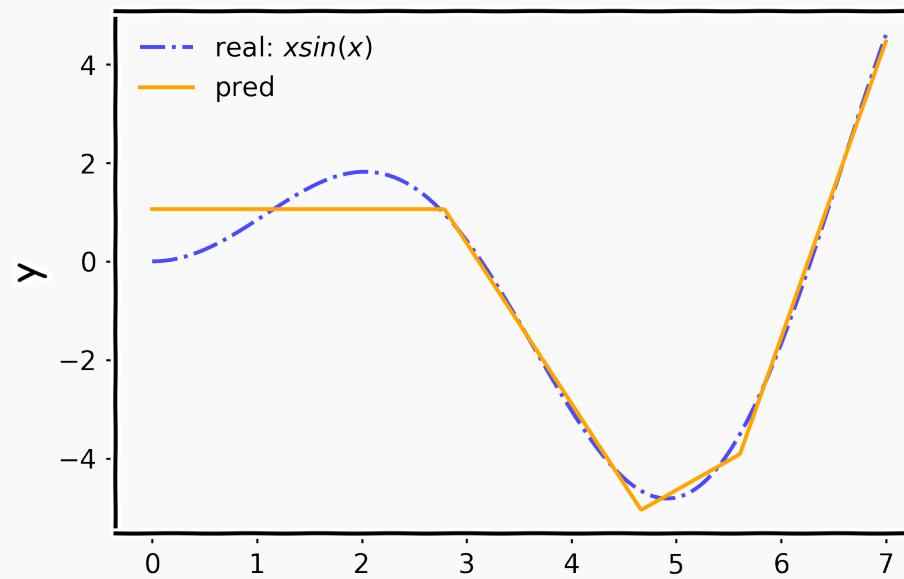
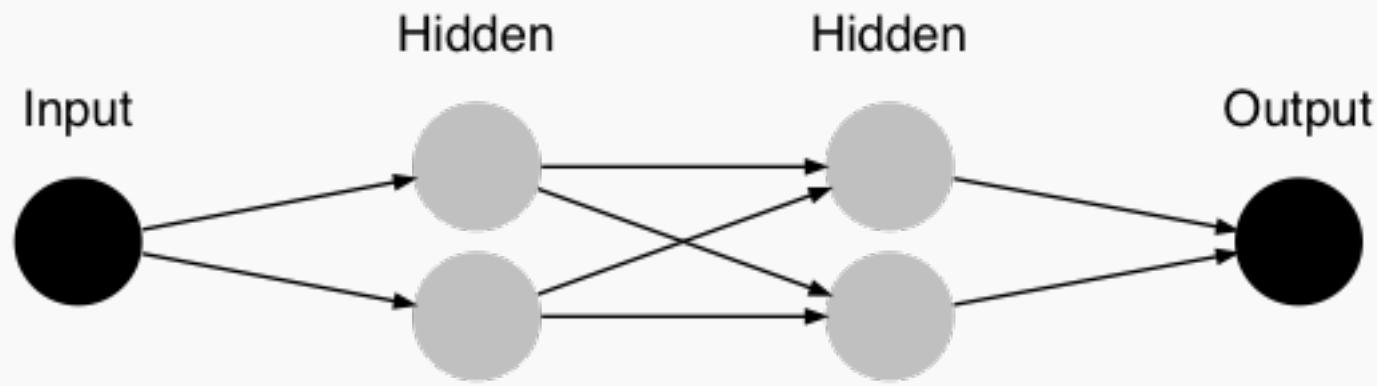
One hidden layer is enough to represent an approximation of any function to an arbitrary degree of accuracy.

So why deeper?

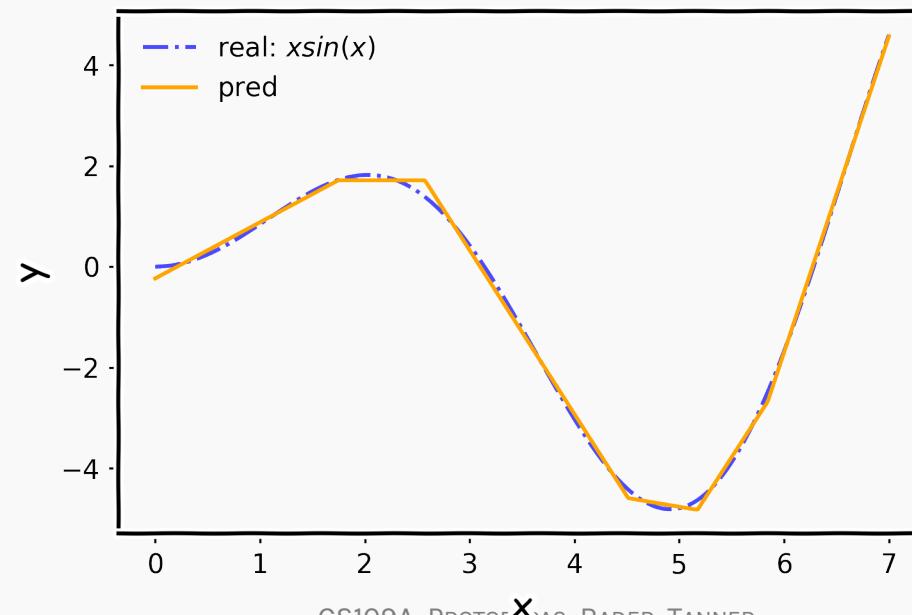
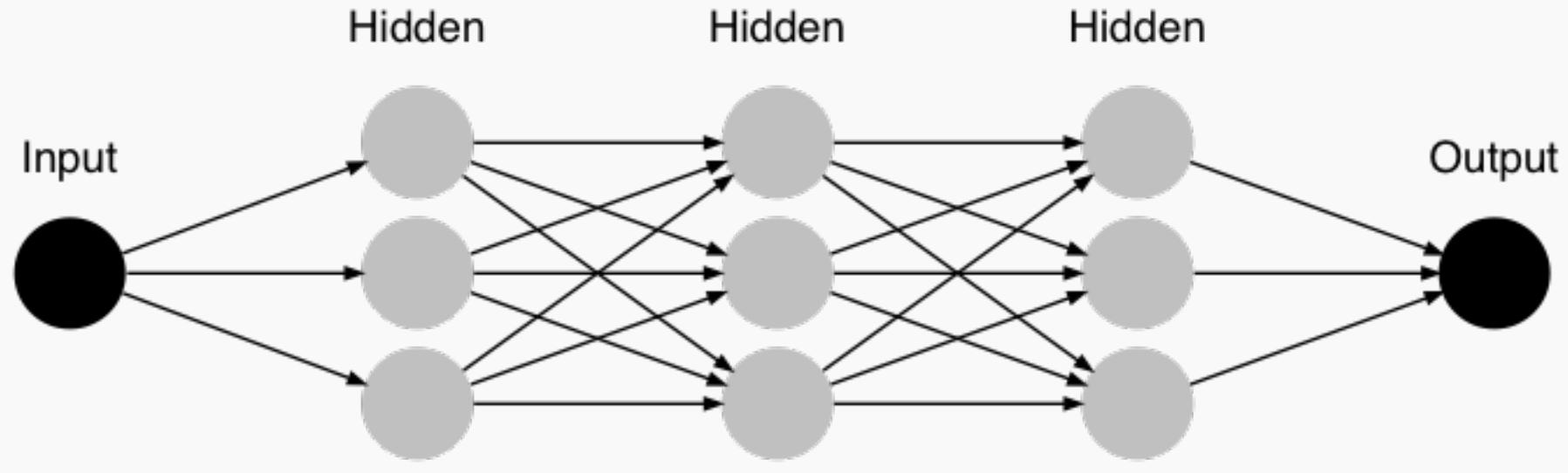
# Layers



# Layers

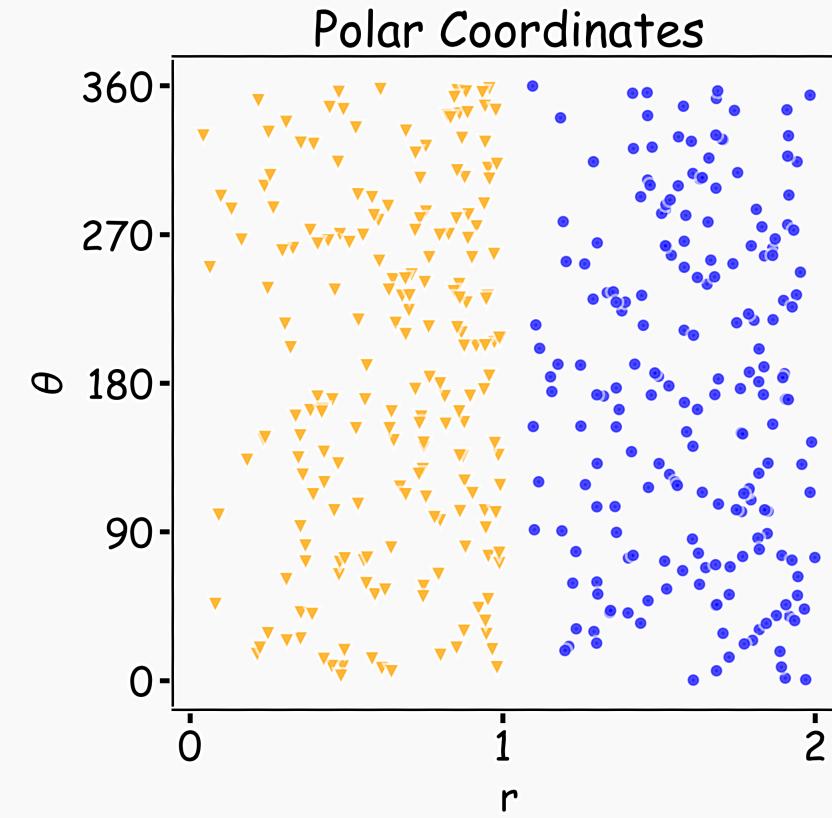
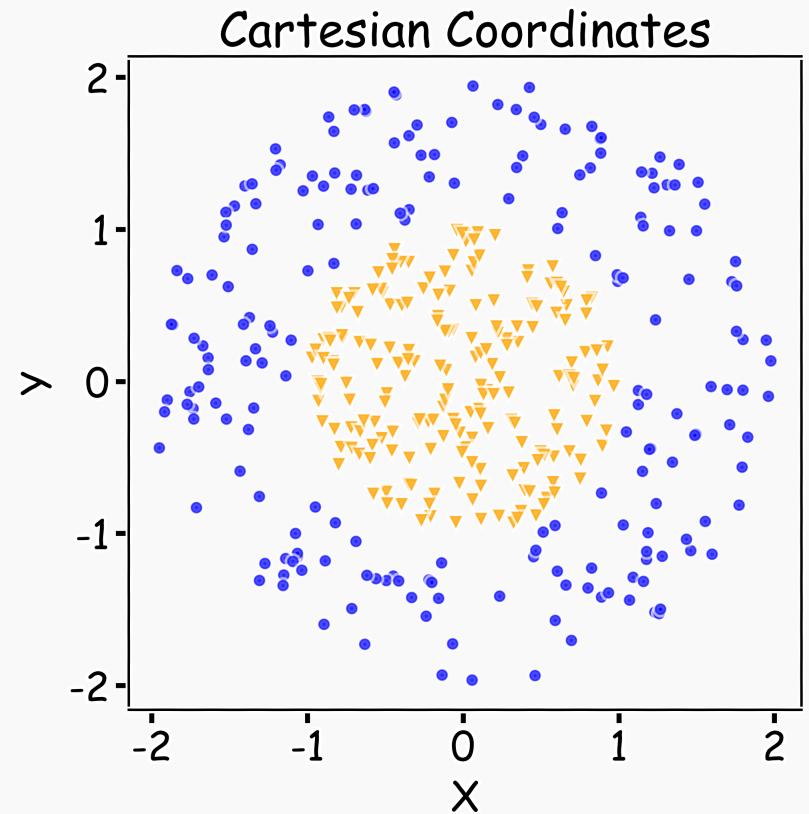


# Layers



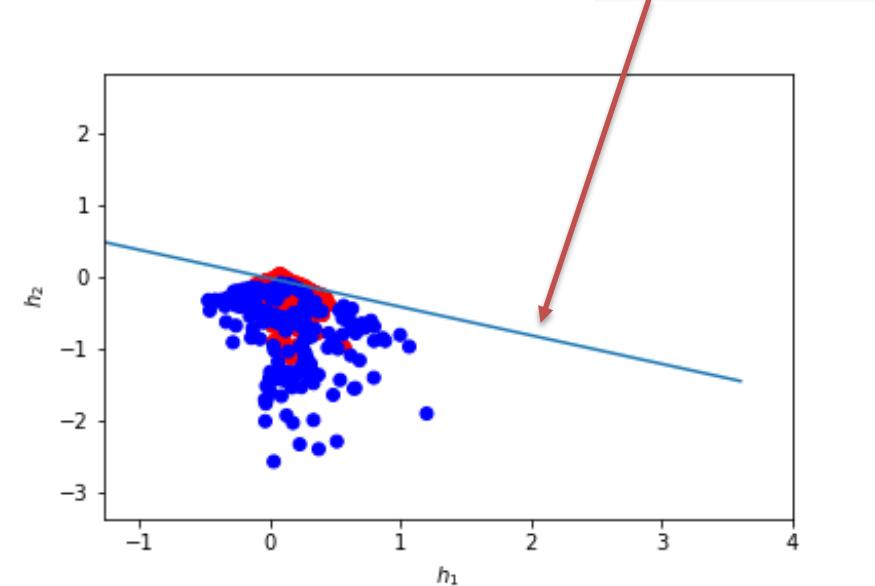
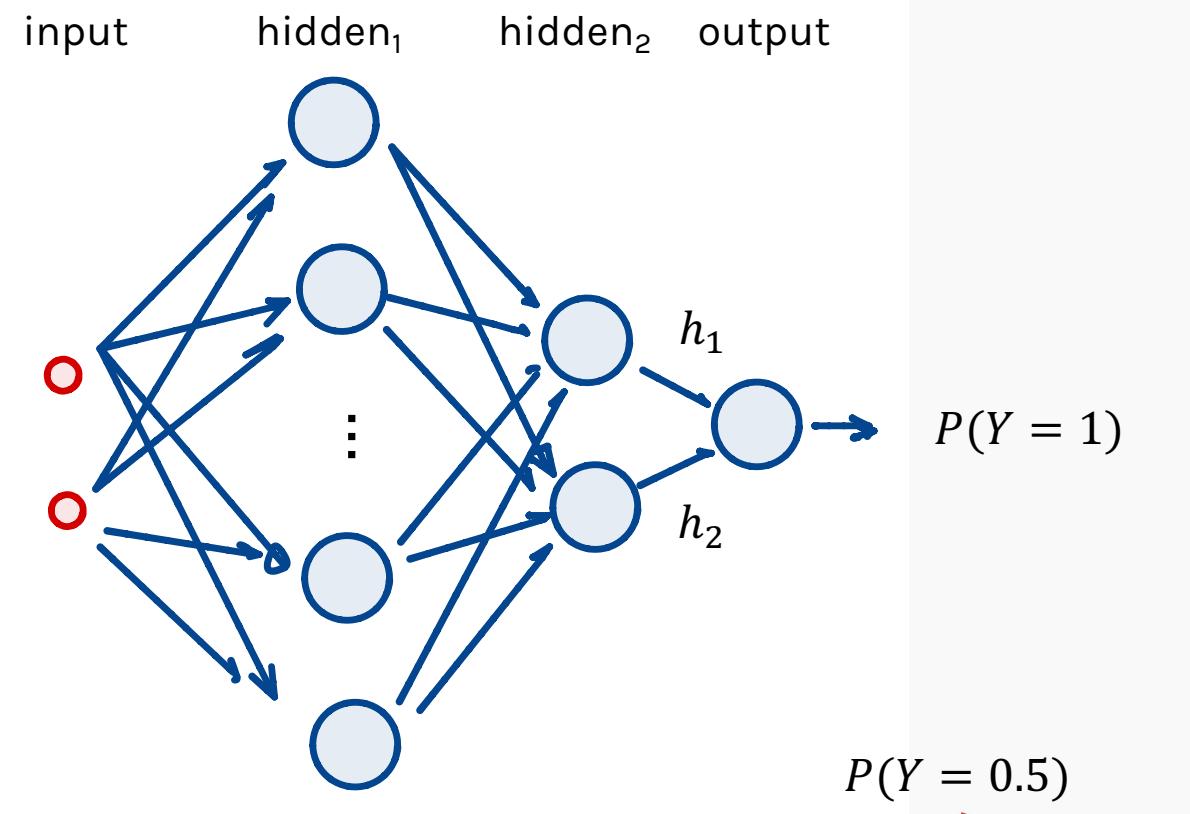
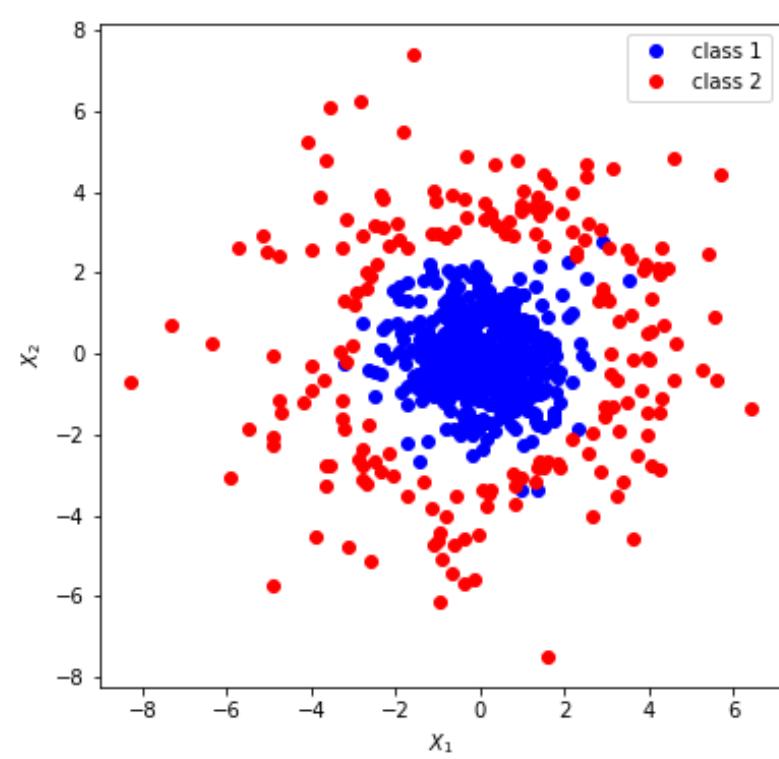
# Why layers?

Representation matters!

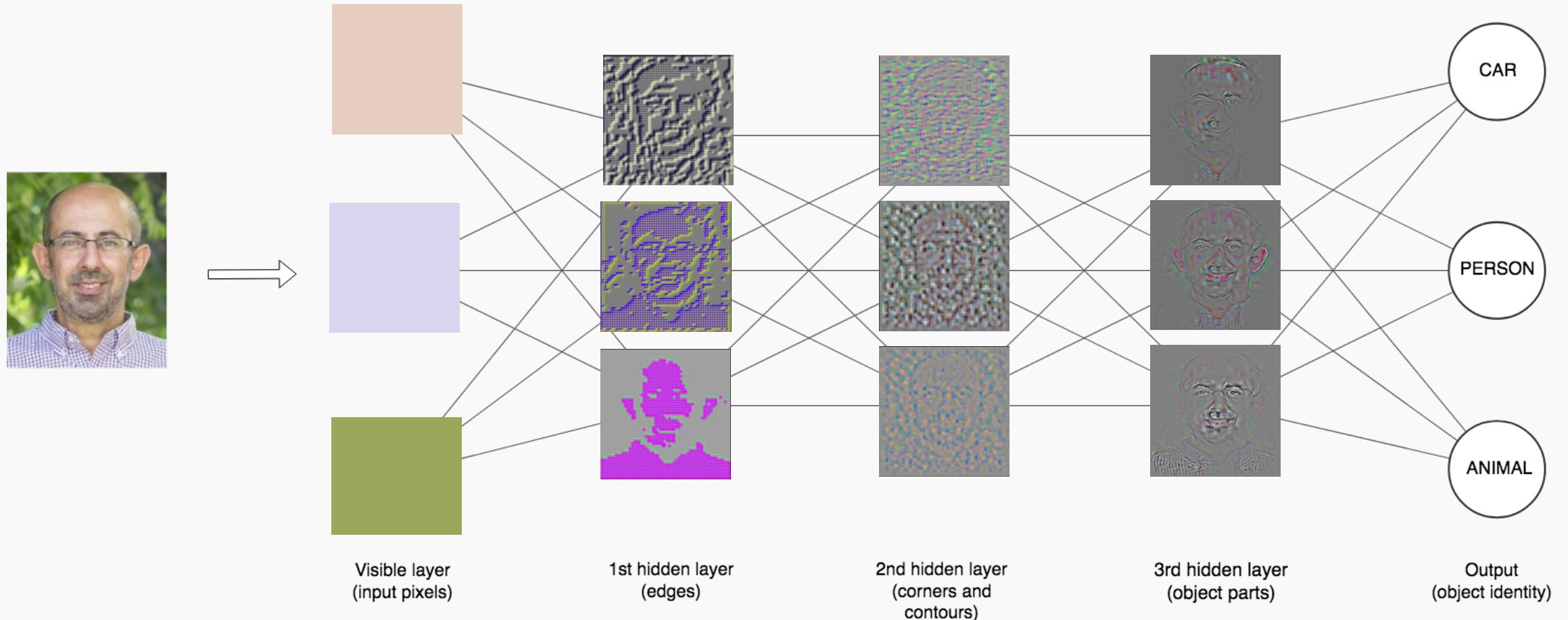


Neural networks can **learn useful representations** for the problem. This is another reason why they can be so powerful!

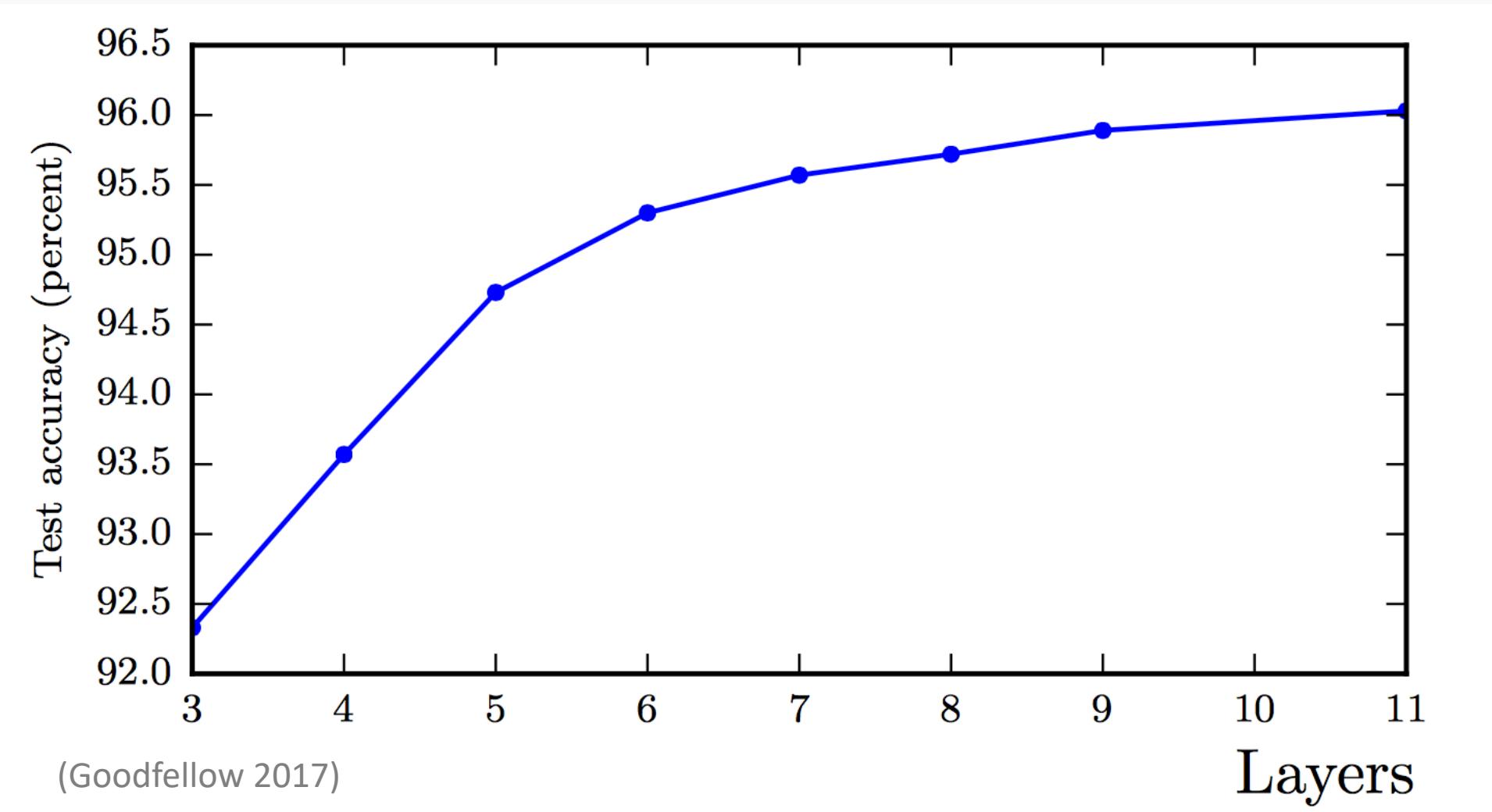




# Depth = Repeated Compositions

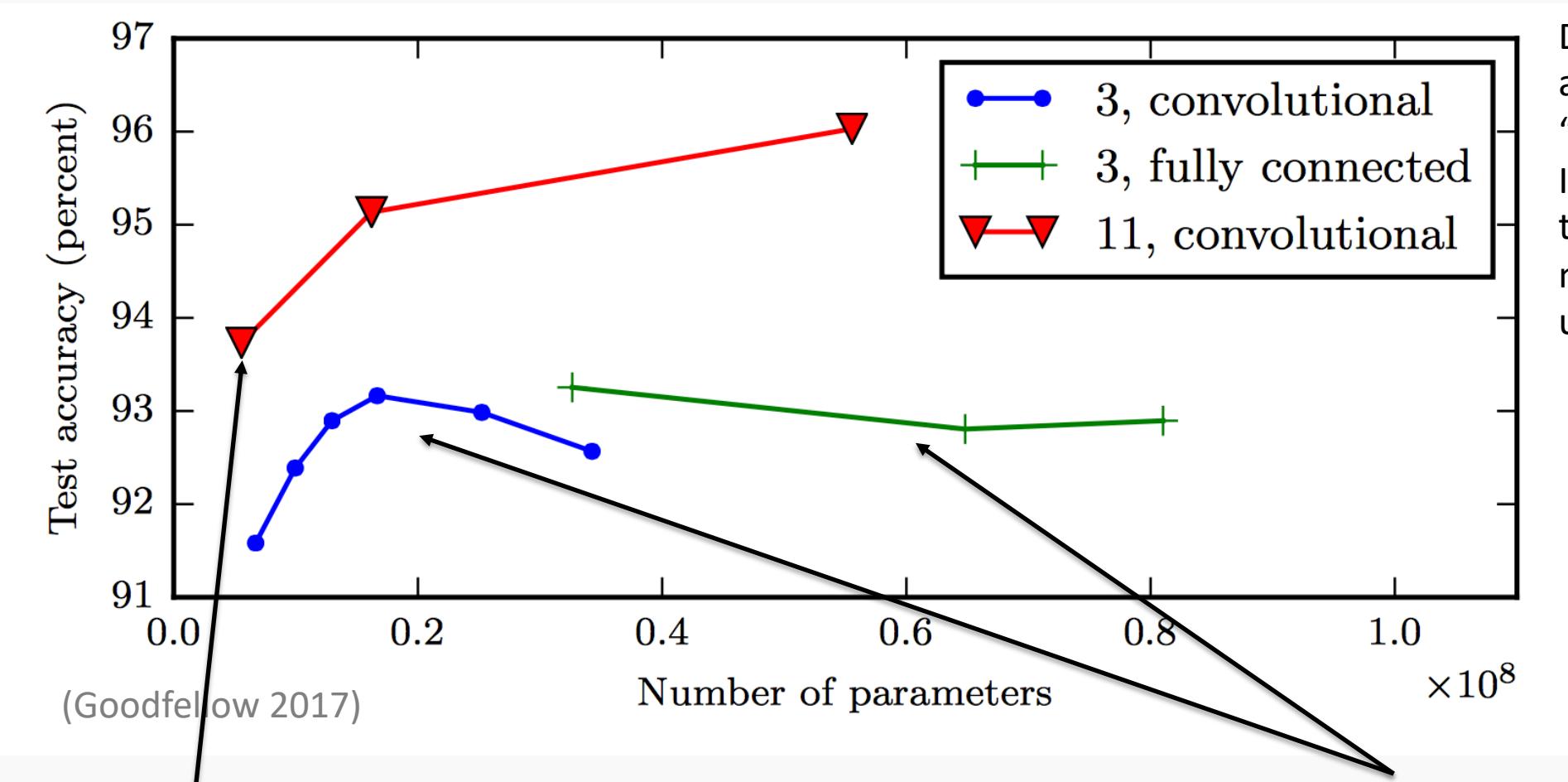


# Better Generalization with Depth



# Shallow Nets Overfit More

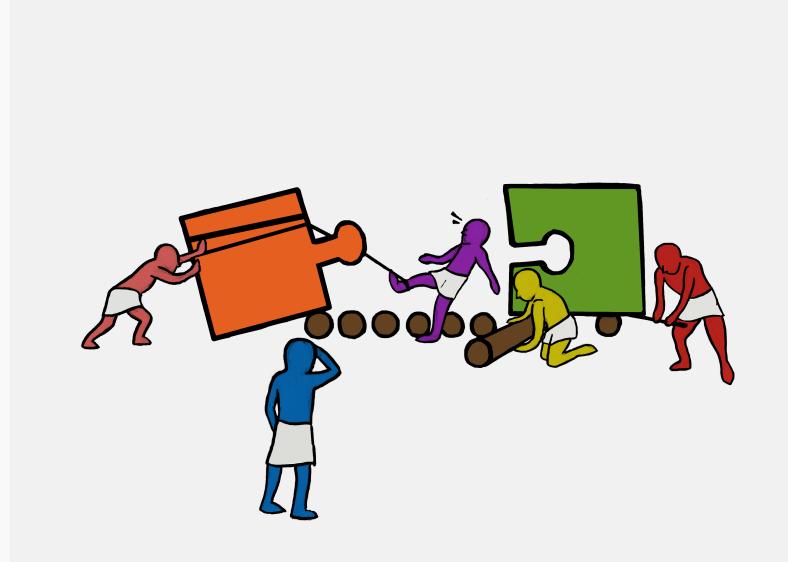
Depth helps, and it's not just because of more parameters



The **11-layer net** generalizes better on the test set when controlling for number of parameters.

The 3-layer nets perform worse on the test set, even with similar number of total parameters.

Don't worry about this word "convolutional". It's just a special type of neural network, often used for images.



## Classifier using Keras on Iris data

