

6.034

Boosting

Adaboost

Randall Davis

Learning

- Nearest neighbors, near misses, neural nets,...
 - Single approximations to the problem
- Boosting
 - Multiple methods
 - ... accumulated incrementally
 - ... moving us from weak classifiers to strength in numbers
 - Adaboost
 - Empirical performance

Meta-Learning

- The Value of Intuitive Explanations
 - Can you find a simple way to think about the issue?

Getting Started

- Binary classification problem?
- Weak classifier?
 - $\epsilon < 0.5$
- Why would/how could multiple not-so good elements add up to something better?

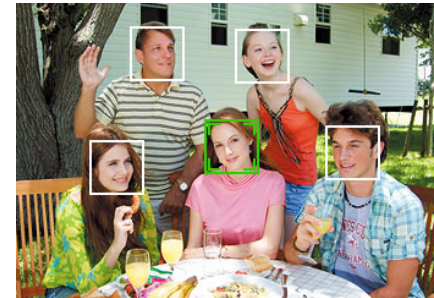
An Intuitive Image



- Informal football game
 - people you don't really know
 - but do know that they're not very good
- Can you still build a good team?
- How?
- Can you refine it over time?

More Realistic Problem

- Face detection



Refining the Intuition

- A set of weak binary classifiers:
 h_1, h_2, h_3, \dots
- Majority wins:
 $H(x) = \text{sign}(h_1(x) + h_2(x) + h_3(x))$
- Weighted majority wins
 $H(x) = \text{sign}(\alpha_1 h_1(x) + \alpha_2 h_2(x) + \alpha_3 h_3(x))$

Adaboost

- The ultimate excuse for a committee –
how a bunch of mediocre people can add up to smart
- Multiple rounds of classifier selection, with training instances re-weighted at each round *to emphasize the errors*
- Can be used to learn a (very!) good classifier
- Final classification based on weighted vote of multiple *weak classifiers*
 - weak: < 50% error over any distribution
 - (ie if you're better than a coin flip, you can be on the committee)

Adaboost, Formally

- given training set $(x_1, y_1), \dots, (x_m, y_m)$
- $y_i \in \{-1, +1\}$ correct label of instance $x_i \in X$
- for $t = 1, \dots, T$:
 - construct distribution D_t on $\{1, \dots, m\}$
 - find weak hypothesis (“rule of thumb”)

$$h_t : X \rightarrow \{-1, +1\}$$
 with small error ϵ_t on D_t :

$$\epsilon_t = \Pr_{D_t}[h_t(x_i) \neq y_i]$$

Adaboost, Formally

- constructing D_t :

- $D_1(i) = 1/m$
- given D_t and h_t :

$$D_{t+1}(i) = \frac{D_t(i)}{Z_t} \cdot \begin{cases} e^{-\alpha_t} & \text{if } y_i = h_t(x_i) \\ e^{\alpha_t} & \text{if } y_i \neq h_t(x_i) \end{cases}$$

$$= \frac{D_t(i)}{Z_t} \cdot \exp(-\alpha_t y_i h_t(x_i))$$

$$\alpha_t = \frac{1}{2} \ln \left(\frac{1 - \epsilon_t}{\epsilon_t} \right)$$

Vorpai Sword





Adaboost, Formally

- constructing D_t :

- $D_1(i) = 1/m$
- given D_t and h_t :

$$D_{t+1}(i) = \frac{D_t(i)}{Z_t} \cdot \begin{cases} e^{-\alpha_t} & \text{if } y_i = h_t(x_i) \\ e^{\alpha_t} & \text{if } y_i \neq h_t(x_i) \end{cases}$$

$$= \frac{D_t(i)}{Z_t} \cdot \exp(-\alpha_t y_i h_t(x_i))$$

$$\alpha_t = \frac{1}{2} \ln \left(\frac{1 - \epsilon_t}{\epsilon_t} \right)$$

Adaboost, Vorpally Decomposed

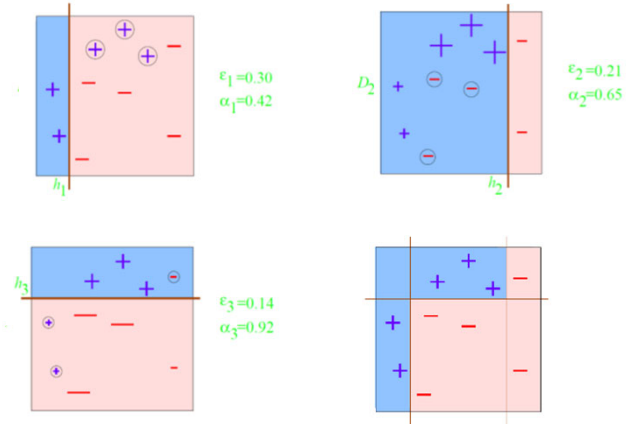
- constructing D_t :

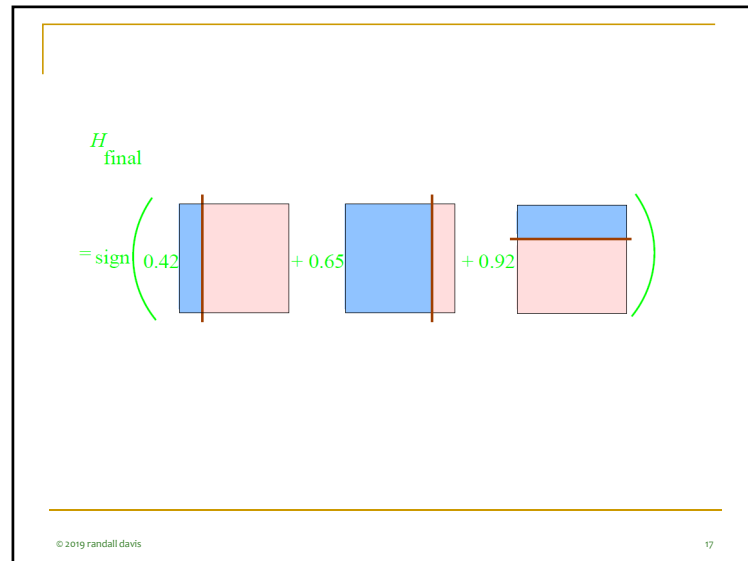
- $D_1(i) = 1/m$

What: Initialize the distribution by giving all points the same default weight.

Rationale: Don't know anything about the points yet, so $1/m$ is a plausible default.

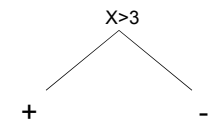
Copy of the slide on Canvas/Reference Material 11/2 lecture
Breakout rooms, 2-3 people per; reporter is alph. last name
Discuss the What/Rationale for the 2nd & 3rd arrows above
Everyone back in 4 minutes ready to report
Think it through. You may surprise yourselves.



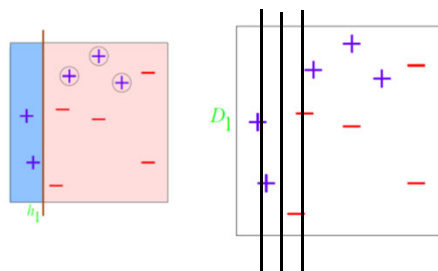


Whence the h_i 's?

- Most anywhere
- One easy answer: stumps
 - Single-level decision trees



Stumps



Generality of Adaboost

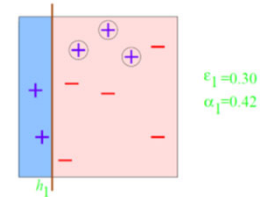
- What are the h_i ?

Taming The Math

■ Updating weights

- Turns out that for correct answers: $\sum D_i^t = 1/2$
Scale wts on correct answers *down* to 0.5
- For wrong answers: $\sum D_i^t = 1/2$
Scale wts on correct answers *up* to 0.5

Taming The Math



Original weights: 0.1
 Correct ans: 7, sums to 0.7
 Multiply by 5/7 to scale sum to .5; get new weights of $5/7 * 0.1 = 0.071$
 Incorrect ans: 3, sums to 0.3,
 Multiply by 5/3 to scale sum to .5; get new weights of $5/3 * 0.1 = 0.167$

Ada-Boost Summary

- Starting with a Training Set (initial weights $1/n$)
 - Weak learning algorithm returns a classifier
 - Reweight the examples
 - Weight on correct examples is decreased
 - Weight on errors is increased
- Final classifier is a weighted majority of Weak Classifiers
 - Classifiers with low error get larger weight

What's Good About Adaboost

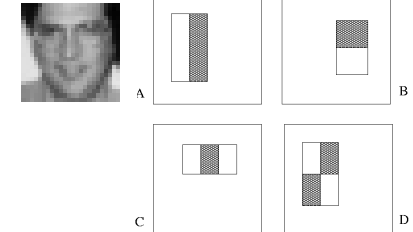
- Improves classification accuracy
- Can be used with many different classifiers
- Commonly used in many areas
- Simple to implement
- Not prone to overfitting
- Speed

An Early Application

■ Viola/Jones Face Detection

Image Features

"Rectangle filters"



Differences between sums of pixels in adjacent rectangles

$$h_i(x) = \begin{cases} +1 & \text{if } f_i(x) > q_i \\ -1 & \text{otherwise} \end{cases}$$

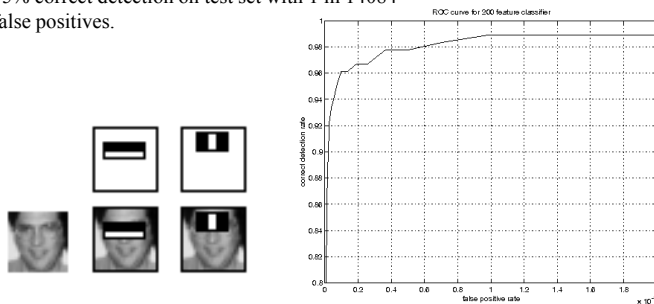
© 2019 randall davis

Viola and Jones, Robust object detection using a boosted cascade of simple features, CVPR 2001

Example Classifier for Face Detection

A classifier with 200 rectangle features was learned using AdaBoost

95% correct detection on test set with 1 in 14084 false positives.

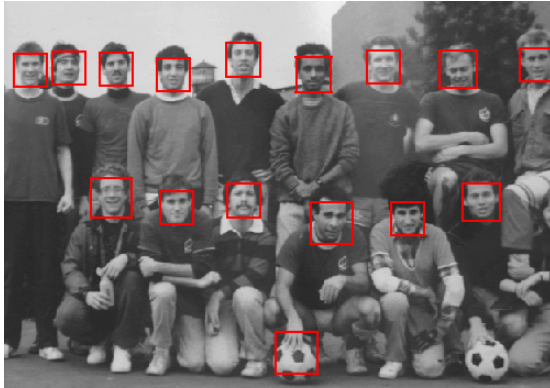


ROC curve for 200 feature classifier

© 2019 randall davis

Viola and Jones, Robust object detection using a boosted cascade of simple features, CVPR 2001





Gold Stars

- The wisdom of crowds
 - Of weighted crowds
 - Of crowds of weighted specialists with different specializations
 - Of crowds of perhaps only OK specialists
- Learn to wield your vorpal sword